数据结构第二次作业

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1 实现 List

1.1 作业题目

未排序的顺序数组、已排序的顺序数组、未排序的单循环链表和已排序的单循环链表为了简化问题,这些数据结构都仅仅存储 int 类型,并且实现了如下抽象对象类型

```
// ListInterface.java 线性表接口
package sylxjtu;

interface List{
  boolean search(int x);  // 查询值为 x 的元素是否存在
  boolean insert(int x);  // 插入值为 x 的元素
  int delete(int x);  // 删除下标为 x 的元素
  int successor(int x);  // 获得该线性表中值为 x 的元素直接后继元素
  int predecessor(int x);  // 获得该线性表中值为 x 的元素的直接前驱元素
  int minimum();  // 获得该线性表的最小元素
  int maximum();  // 获得该线性表的最大元素
  int kthElement(int k);  // 获得线性表中第 k 大元素,参数为指定的 k 值的大小
}
```

1.2 程序实现

包括数据结构实现和测试代码,完整代码详见 Github 代码仓库 1

无序数组

```
// UnsortedArray.java 未排序数组实现线性表
package sylxjtu;

public class UnsortedArray implements sylxjtu.List{
  int[] data = new int[1];
  int capacity = 1;
  int size = 0;
```

 $^{^{1} \}rm https://github.com/sylxjtu/datastructure-homework/tree/master/homework2/src$

```
void extend(){
  int[] tmp = new int[capacity * 2];
  System.arraycopy(data, 0, tmp, 0, capacity);
  capacity *= 2;
  data = tmp;
}
int find(int x){
  for(int i = 0; i < size; i++){</pre>
    if(data[i] == x) return i;
  return -1;
@Override
public boolean search(int x){
  if(find(x) != -1) return true;
  return false;
}
@Override
public boolean insert(int x){
  if(size == capacity) extend();
  data[size++] = x;
  return true;
}
@Override
public int delete(int x){
  assert x >= 0 && x < size : "Invalid Index";</pre>
  int ret = data[x];
  for (int i = x; i < size - 1; i++) {</pre>
```

```
data[i] = data[i + 1];
  }
  size--;
  return ret;
@Override
public int successor(int x){
  int ind = find(x);
  assert ind >= 0 && ind < size - 1 : "No successor";</pre>
  return data[ind + 1];
@Override
public int predecessor(int x){
  int ind = find(x);
  assert ind > 0 && ind < size : "No predecessor";</pre>
 return data[ind - 1];
}
@Override
public int minimum(){
  assert size > 0 : "List is empty";
  int ret = data[0];
  for (int i = 1; i < size; i++) {</pre>
    ret = data[i] < ret ? data[i] : ret;</pre>
  }
  return ret;
}
@Override
public int maximum(){
  assert size > 0 : "List is empty";
```

```
int ret = data[0];
  for (int i = 1; i < size; i++) {</pre>
    ret = data[i] > ret ? data[i] : ret;
  }
  return ret;
}
@Override
public int kthElement(int k){
  assert k > 0 && k <= size : "Invalid k";</pre>
  int[] tmp = data.clone();
  return ArrayUtil.findKthElement(tmp, 0, size, k - 1);
}
public static void main(String[] args) {
  UnsortedArray a = new UnsortedArray();
  a.insert(1);
  a.insert(3);
  a.insert(2);
  assert a.search(1);
  assert !a.search(4);
  assert a.delete(0) == 1;
  assert !a.search(1);
  a.insert(1);
  assert a.size == 3;
  assert a.successor(2) == 1;
  assert a.predecessor(2) == 3;
  assert a.minimum() == 1;
  assert a.maximum() == 3;
  assert a.kthElement(2) == 2;
  try {
    assert false;
  } catch (AssertionError e) {
```

```
System.out.println("Test passed");
      return;
    throw new Error("Please enable assertions");
}
有序数组
// SortedArray.java 排序数组实现线性表
package sylxjtu;
public class SortedArray implements sylxjtu.List{
  int[] data = new int[1];
 int capacity = 1;
  int size = 0;
 void extend(){
    int[] tmp = new int[capacity * 2];
    System.arraycopy(data, 0, tmp, 0, capacity);
    capacity *= 2;
   data = tmp;
  int find(int x){
    int l = 0, r = size, mid = (r + l) / 2;
   while(x != data[mid] \&\& l < r - 1){
     if(data[mid] < x) l = mid;</pre>
     else r = mid;
     mid = (r + l) / 2;
   }
    return x == data[mid] ? mid : -1;
```

```
@Override
public boolean search(int x){
  if(find(x) != -1) return true;
  return false;
}
@Override
public boolean insert(int x){
  if(size == capacity) extend();
  if(size == 0 \mid \mid x >= data[size - 1]) {
    data[size] = x;
  } else if(x <= data[0]) {</pre>
    for(int i = size; i > 0; i--){
      data[i] = data[i - 1];
    }
    data[0] = x;
  } else {
    for(int i = 0; i < size - 1; i++){</pre>
      if(data[i] < x && x <= data[i + 1]){</pre>
        for(int j = size; j > i + 1; j--){
          data[j] = data[j - 1];
        data[i + 1] = x;
        break;
    }
  }
  size++;
  return true;
@Override
public int delete(int x){
```

```
assert x >= 0 && x < size : "Invalid Index";</pre>
  int ret = data[x];
  for (int i = x; i < size - 1; i++) {</pre>
    data[i] = data[i + 1];
  }
  size--;
  return ret;
@Override
public int successor(int x){
  int ind = find(x);
  assert ind >= 0 && ind < size - 1 : "No successor";</pre>
 return data[ind + 1];
}
@Override
public int predecessor(int x){
  int ind = find(x);
  assert ind > 0 && ind < size : "No predecessor";</pre>
  return data[ind - 1];
}
@Override
public int minimum(){
  assert size > 0 : "List is empty";
  return data[0];
}
@Override
public int maximum(){
  assert size > 0 : "List is empty";
  return data[size - 1];
```

```
}
  @Override
 public int kthElement(int k){
    assert k > 0 && k <= size : "Invalid k";</pre>
   return data[k - 1];
  }
 public static void main(String[] args) {
    SortedArray a = new SortedArray();
    a.insert(1);
    a.insert(3);
   a.insert(2);
    assert a.search(1);
    assert !a.search(4);
    assert a.delete(0) == 1;
    assert !a.search(1);
    a.insert(1);
    assert a.size == 3;
    assert a.successor(2) == 3;
    assert a.predecessor(2) == 1;
    assert a.minimum() == 1;
    assert a.maximum() == 3;
    assert a.kthElement(2) == 2;
    try {
     assert false;
   } catch (AssertionError e) {
     System.out.println("Test passed");
      return;
    throw new Error("Please enable assertions");
}
```

无序链表

```
// UnsortedLinkedList.java 未排序链表实现线性表
package sylxjtu;
public class UnsortedLinkedList implements sylxjtu.List{
 Node head;
 Node tail;
  int size = 0;
 Node find(int x){
    if(size == 0) return null;
    if(head.value == x) return head;
   Node cur = head.next;
    while(cur.value != x && cur != head){
     cur = cur.next;
    if(cur == head) return null;
    else return cur;
  }
 @Override
 public boolean search(int x){
    if(find(x) != null) return true;
    return false;
  }
  @Override
  public boolean insert(int x){
    if(size == 0){
     head = tail = new Node(x);
     head.next = head;
    } else {
     tail.next = new Node(head, x);
```

```
tail = tail.next;
  size++;
  return true;
@Override
public int delete(int x){
  assert x >= 0 && x < size : "Invalid Index";</pre>
  Node cur = head;
  for(int i = 0; i < x; i++){</pre>
    cur = cur.next;
  int ret = cur.value;
  if(x == 0) head = tail.next = head.next;
  else {
    cur = head;
    for(int i = 0; i < x - 1; i++){</pre>
      cur = cur.next;
    cur.next = cur.next.next;
  }
  size--;
  return ret;
@Override
public int successor(int x){
  Node ind = find(x);
  assert ind != null && ind != tail : "No successor";
```

```
return ind.next.value;
}
@Override
public int predecessor(int x){
  Node ind = find(x);
  assert ind != null && ind != head : "No predecessor";
  Node cur = ind.next;
  while(cur.next != ind){
    cur = cur.next;
  return cur.value;
@Override
public int minimum(){
  int ret = head.value;
  for(Node cur = head.next; cur != head; cur = cur.next){
    ret = cur.next.value < ret ? cur.next.value : ret;</pre>
  }
  return ret;
@Override
public int maximum(){
  int ret = head.value;
  for(Node cur = head.next; cur != head; cur = cur.next){
    ret = cur.next.value > ret ? cur.next.value : ret;
  }
  return ret;
@Override
```

```
public int kthElement(int k){
  assert k > 0 && k <= size : "Invalid k";</pre>
  int[] arr = new int[size];
  Node cur = head;
  for(int i = 0; i < size; i++, cur = cur.next){</pre>
    arr[i] = cur.value;
  return ArrayUtil.findKthElement(arr, 0, size, k - 1);
public static void main(String[] args) {
  UnsortedLinkedList a = new UnsortedLinkedList();
  a.insert(1);
  a.insert(3);
  a.insert(2);
  assert a.search(1);
  assert !a.search(4);
  assert a.delete(0) == 1;
  assert !a.search(1);
  a.insert(1);
  assert a.size == 3;
  assert a.successor(2) == 1;
  assert a.predecessor(2) == 3;
  assert a.minimum() == 1;
  assert a.maximum() == 3;
  assert a.kthElement(2) == 2;
  try {
    assert false;
  } catch (AssertionError e) {
    System.out.println("Test passed");
    return;
  throw new Error("Please enable assertions");
```

```
}
有序链表
// SortedLinkedList.java 排序链表实现线性表
package sylxjtu;
public class SortedLinkedList implements sylxjtu.List{
 Node head;
 Node tail;
 int size = 0;
 void print(){
   Node cur = head;
   for (int i = 0; i < size; i++) {</pre>
     System.out.print(cur.value + " ");
     cur = cur.next;
   System.out.println();
 Node find(int x){
    if(size == 0) return null;
    if(head.value == x) return head;
   Node cur = head.next;
   while(cur.value != x && cur != head){
     cur = cur.next;
    if(cur == head) return null;
   else return cur;
 @Override
```

```
public boolean search(int x){
  if(find(x) != null) return true;
  return false;
@Override
public boolean insert(int x){
  if(size == 0){
   head = tail = new Node(x);
   head.next = head;
 } else {
   if(head.value > x){
      tail.next = new Node(head, x);
      head = tail.next;
   } else {
      for(Node cur = head; ; cur = cur.next){
        if(cur.next.value > x || cur == tail){
          cur.next = new Node(cur.next, x);
          if(cur.next.next == head) tail = tail.next;
          size++;
          return true;
       }
      }
   }
  }
  size++;
  return true;
@Override
public int delete(int x){
  assert x >= 0 && x < size : "Invalid Index";</pre>
```

```
Node cur = head;
  for(int i = 0; i < x; i++){</pre>
   cur = cur.next;
  int ret = cur.value;
  if(x == 0) {
   head = tail.next = head.next;
 } else {
   cur = head;
   for(int i = 0; i < x - 1; i++){
     cur = cur.next;
   cur.next = cur.next.next;
 }
 size--;
 return ret;
}
@Override
public int successor(int x){
 Node ind = find(x);
 assert ind != null && ind != tail : "No successor";
 return ind.next.value;
}
@Override
public int predecessor(int x){
  Node ind = find(x);
 assert ind != null && ind != head : "No predecessor";
 Node cur = ind.next;
 while(cur.next != ind){
```

```
cur = cur.next;
  return cur.value;
@Override
public int minimum(){
  return head.value;
@Override
public int maximum(){
  return tail.value;
@Override
public int kthElement(int k){
  Node cur = head;
  for(int i = 0; i < k - 1; i++, cur = cur.next)
  return cur.value;
public static void main(String[] args) {
  SortedLinkedList a = new SortedLinkedList();
  a.insert(1);
  a.insert(3);
  a.insert(2);
  assert a.search(1);
  assert !a.search(4);
  assert a.delete(0) == 1;
  assert !a.search(1);
  a.insert(1);
```

```
assert a.size == 3;
assert a.successor(2) == 3;
assert a.predecessor(2) == 1;
assert a.minimum() == 1;
assert a.maximum() == 3;
assert a.kthElement(2) == 2;
try {
   assert false;
} catch (AssertionError e) {
   System.out.println("Test passed");
   return;
}
throw new Error("Please enable assertions");
}
```

1.3 程序运行结果与时间统计

运行结果 所有程序均通过测试

1.4 算法分析

数据结构	无序数组	有序数组	无序链表	有序链表
search	O(n)	$O(\log n)$	O(n)	O(n)
insert	O(1)	O(n)	O(1)	O(n)
delete	O(n)	O(n)	O(n)	O(n)
successor	O(1)	O(1)	O(1)	O(1)
predecessor	O(1)	O(1)	O(1)	O(1)
minimum	O(n)	O(1)	O(n)	O(1)
maximum	O(n)	O(1)	O(n)	O(1)
kthElement	O(n)	O(1)	O(n)	O(k)

2 创建布尔表达式计算器

2.1 题目描述

本题是要计算如下的布尔表达式: (T|T)&F&(F|T) 其中 T 表示 True, F 表示 False。表达式可以包含如下运算符: ! 表示 not, & 表示 and, | 表示 or, 允许使用括号。

为了执行表达式的运算,要考虑运算符的优先级: not 的优先级最高, or 的优先级最低。计算器要产生 V 或 F,表达最终表达式计算的结果。 对输入的表达式的要求如下:

- 1. 一个表达式不超过 100 个符号,符号间可以用任意个空格分开,或者根本没有空格,所以表达式总的长度也就是字符的个数,它是未知的。
- 2. 要能处理表达式中出现括号不匹配、运算符缺少运算操作数等常见的输入错误。

2.2 问题分析

表达式文法为

$$expr \to and expr|expr \\ \to and expr \tag{1}$$

$$and expr \rightarrow not expr \& expr \\ \rightarrow not expr \tag{2}$$

$$notexpr \to !notexpr \\ \to atom$$
 (3)

$$\begin{array}{l} atom \rightarrow T \\ \rightarrow F \\ \rightarrow (expr) \end{array} \tag{4}$$

规约为 LL(1) 文法为

$$expr \rightarrow andexpr \ rexpr$$
 (5)

$$rexpr \to |expr \\ \to \epsilon \tag{6}$$

$$andexpr \rightarrow notexpr \ randexpr$$
 (7)

$$randexpr \rightarrow \&andexpr \\ \rightarrow \epsilon$$
 (8)

$$notexpr \to !notexpr \\ \to atom$$
 (9)

$$atom \to T$$

$$\to F$$

$$\to (expr)$$
(10)

之后可以通过递归下降法求解

2.3 程序实现

```
// BoolEquationEvaluate.java 布尔表达式求值
package sylxjtu;
import java.util.Scanner;
public class BoolEquationEvaluate {
   String s;
   int cur;
   BoolEquationEvaluate(String str){
      s = str + "$";
   }
   public boolean eval() {
      boolean ret = expr();
      if(s.charAt(cur) != '$') {
        System.err.println("Error: Unexpected " + s.charAt(cur) + " at position " + cur);
        System.err.println(s);
      for (int i = 0; i < cur; i++) {</pre>
```

```
System.err.print(" ");
    System.err.println("^");
    throw new Error("Invalid expression");
  }
  return ret;
void gonext(){
  do {
    cur++;
  } while(s.charAt(cur) == ' ');
boolean expr(){
  return andexpr() | rexpr();
boolean rexpr(){
  if(s.charAt(cur) == '|') {
    gonext();
    return expr();
  } else {
    return false;
  }
boolean andexpr(){
  return notexpr() & randexpr();
boolean randexpr(){
  if(s.charAt(cur) == '&') {
    gonext();
    return andexpr();
  } else {
    return true;
  }
```

```
boolean notexpr(){
  if(s.charAt(cur) == '!') {
    gonext();
   return !notexpr();
 } else {
    return atom();
  }
}
boolean atom(){
  if(s.charAt(cur) == 'T') {
    gonext();
    return true;
  } else if(s.charAt(cur) == 'F') {
   gonext();
    return false;
  } else if(s.charAt(cur) == '(') {
    gonext();
    boolean ret = expr();
    if(s.charAt(cur) != ')'){
      System.err.println("Error: Missing right branket at position " + cur);
      System.err.println(s);
      for (int i = 0; i < cur; i++) {</pre>
        System.err.print(" ");
      System.err.println("^");
      throw new Error("Invalid expression");
    }
    gonext();
    return ret;
  } else {
   System.err.println("Error: Unexpected " + s.charAt(cur) + " at position " + cur);
    System.err.println(s);
```

```
for (int i = 0; i < cur; i++) {</pre>
        System.err.print(" ");
      System.err.println("^");
      throw new Error("Invalid expression");
    }
  }
  public static void main(String[] args) {
    Scanner scanner = new Scanner(System.in);
    while (scanner.hasNextLine()) {
      String line = scanner.nextLine();
      try {
        BoolEquationEvaluate x = new BoolEquationEvaluate(line);
        System.out.println(x.eval() ? 'V' : 'F');
      } catch (Error e) {}
      System.out.println();
    }
    scanner.close();
}
```

2.4 程序运行结果与时间统计

运行结果 通过 POJ2109 测试

时间统计 POJ2109 测试, 10 组表达式, 用时 279ms

2.5 算法分析

根据递归下降法,每次扫描一个符号,故复杂度为O(N)(N)为符号数)

3 队列实现基数排序

3.1 题目描述

利用队列实现对某一个数据序列的排序(采用基数排序),其中对数据序列的数据(第 1 和第 2 条进行说明)和队列的存储方式(第 3 条进行说明)有如下的要求:

1. 当数据序列是整数类型的数据的时候,数据序列中每个数据的位数不要求等宽,比如:

```
1, 21, 12, 322, 44, 123, 2312, 765, 56
```

2. 当数据序列是字符串类型的数据的时候,数据序列中每个字符串都是等宽的,比如:

```
"abc", "bde", "fad", "abd", "bef", "fdd", "abe"
```

3. 要求重新构建队列的存储表示方法: 使其能够将 n 个队列顺序映射到 一个数组 listArray 中,每个队列都表示成内存中的一个循环队列

3.2 问题分析

首先确定排序的顺序,对于整数排序的顺序是按数的大小升序,对于字符串排序的顺序是字典序升序按照要求 3,通过一个循环数组实现队列的操作

3.3 程序实现

整数队列接口

```
// QueueInt.java 整形队列接口
package sylxjtu;
interface QueueInt {
  boolean empty();
  Pair front();
  void pop();
  void push(Pair elem);
}
```

整数队列实现

```
// LoopArrayQueueString.java 循环数组实现字符串队列
package sylxjtu;
class LoopArrayQueueInt implements QueueInt{
  int capacity = 1;
 int size = 0;
 Pair[] arr;
 int fp, lp;
 LoopArrayQueueInt(){
    arr = new Pair[capacity];
  }
 void extend(){
   Pair[] tmp = new Pair[capacity * 2];
   System.arraycopy(arr, 0, tmp, 0, lp);
   System.arraycopy(arr, fp, tmp, fp + capacity, capacity - fp);
    fp += capacity;
   arr = tmp;
   capacity *= 2;
 @Override
 public boolean empty(){
    return size == 0;
  }
 @Override
 public Pair front(){
    return arr[fp];
 @Override
 public void pop(){
    assert size > 0 : "Queue is empty";
```

```
fp++;
   fp %= capacity;
   size--;
 @Override
  public void push(Pair elem){
    if(size == capacity) extend();
   arr[lp++] = elem;
   lp %= capacity;
   size++;
}
字符串队列接口
// QueueString.java 字符串队列接口
package sylxjtu;
interface QueueString {
  boolean empty();
 String front();
 void pop();
 void push(String elem);
}
字符串队列实现
// LoopArrayQueueString.java 循环数组实现字符串队列
package sylxjtu;
class LoopArrayQueueString implements QueueString{
  int capacity = 1;
  int size = 0;
  String[] arr;
  int fp, lp;
  LoopArrayQueueString(){
```

```
arr = new String[capacity];
void extend(){
  String[] tmp = new String[capacity * 2];
  System.arraycopy(arr, 0, tmp, 0, lp);
  System.arraycopy(arr, fp, tmp, fp + capacity, capacity - fp);
  fp += capacity;
  arr = tmp;
 capacity *= 2;
@Override
public boolean empty(){
  return size == 0;
}
@Override
public String front(){
  return arr[fp];
}
@Override
public void pop(){
  assert size > 0 : "Queue is empty";
  fp++;
 fp %= capacity;
 size--;
@Override
public void push(String elem){
  if(size == capacity) extend();
  arr[lp++] = elem;
```

```
lp %= capacity;
   size++;
}
整数基数排序
// IntegerRadixSort.java 正整数基数排序
// 考虑到模运算、除运算的速度,设置基数为 16,以便将其转化为位运算
// x % 16 -> x & 0xF
// x / 16 -> x >> 4
// StringRadixSort.java 字符串基数排序
package sylxjtu;
public class IntegerRadixSort {
  static void print(int[] arr){
   for(int i = 0; i < arr.length; i++){</pre>
     System.out.println(arr[i]);
   }
  }
  static void sort(int[] arr){
   LoopArrayQueueInt[] qarr = new LoopArrayQueueInt[16];
   Pair[] tarr = new Pair[arr.length];
   for (int i = 0; i < arr.length; i++) {</pre>
     tarr[i] = new Pair(arr[i], arr[i]);
   }
   for (int i = 0; i < qarr.length; i++) {</pre>
      qarr[i] = new LoopArrayQueueInt();
   }
    if(arr.length == 0) return;
   for(int l = 1; ; l++){
     boolean flag = false;
     for(int i = 0; i < arr.length; i++){</pre>
       if((tarr[i].curWeight & 0xF) != 0) flag = true;
```

```
qarr[(tarr[i].curWeight & 0xF)].push(tarr[i]);
        tarr[i].curWeight >>= 4;
      if(!flag) break;
      int j = 0;
      for(int i = 0; i < 16; i++){</pre>
        while(!qarr[i].empty()){
          tarr[j] = qarr[i].front();
          j++;
          qarr[i].pop();
        }
      }
    }
    for (int i = 0; i < arr.length; i++) {</pre>
     arr[i] = tarr[i].value;
    }
  }
 public static void main(String[] args) {
    int[] arr = {1, 21, 12, 322, 4, 123, 2312, 765, 56};
    print(arr);
    System.out.println("");
    sort(arr);
    print(arr);
  }
}
字符串基数排序
// StringRadixSort.java 字符串基数排序
package sylxjtu;
public class StringRadixSort {
  static void print(String[] arr){
    for(int i = 0; i < arr.length; i++){</pre>
      System.out.println(arr[i]);
```

```
}
  }
  static void sort(String[] arr){
    LoopArrayQueueString[] qarr = new LoopArrayQueueString[26];
    for (int i = 0; i < qarr.length; i++) {</pre>
      qarr[i] = new LoopArrayQueueString();
    }
    if(arr.length == 0) return;
    int len = arr[0].length();
    for(int l = len - 1; l >= 0; l--){
      for(int i = 0; i < arr.length; i++){</pre>
        qarr[arr[i].charAt(l) - 'a'].push(arr[i]);
      }
      int j = 0;
      for(int i = 0; i < 26; i++){</pre>
        while(!qarr[i].empty()){
          arr[j] = qarr[i].front();
          j++;
          qarr[i].pop();
        }
      }
    }
  public static void main(String[] args) {
    String[] arr = {"abc", "bde", "fad", "abd", "bef", "fdd", "abe"};
    print(arr);
    System.out.println("");
    sort(arr);
    print(arr);
}
```

3.4 程序运行结果

运行结果 通过两组样例测试

3.5 算法分析

复杂度分析 基数排序复杂度为 O(kN) ,其中 k 为最大数据长度,k 为数组大小