

$$\limsup A_n := \bigcap_{n \geq 1} \left(\bigcup_{k \geq 0} A_{n+k} \right) \quad , \quad \liminf A_n := \bigcup_{n \geq 1} \left(\bigcap_{k \geq 0} A_{n+k} \right) \quad .$$