

$$\bigcup E_x = \bigcup_{r>0} C(x,r) = \mathbb{R}^2 \setminus \{x\}$$