

$$\text{lin sup } A_n = \{x \in X : \mathcal{J}_x \text{ is infinitesimal}\};$$