Ejercicios de Integrales

Cálculo

http://synergy.vision/

Contenido



Use la Parte 1 del Teorema Fundamental del Cálculo para encontrar la derivada de la función.

1.
$$g(x) = \int_{1}^{x} \frac{1}{t^3 + 1} dt$$

2.
$$g(x) = \int_{1}^{x} (2+t^4)^5 dt$$

3.
$$g(s) = \int_5^s (t - t^2)^8 dt$$

4.
$$g(r) = \int_0^r \sqrt{x^2 + 4} dx$$

5.
$$F(x) = \int_{x}^{\pi} \sqrt{1 + \sec t} dt$$

$$\left[\int_{x}^{\pi}\sqrt{1+\sec}tdt=-\int_{\pi}^{x}\sqrt{1+\sec}tdt\right]$$

6.
$$G(x) = \int_{1}^{x} \cos \sqrt{t} dt$$

7.
$$h(x) = \int_{2}^{1/x} \sin^4 t dt$$

8.
$$h(x) = \int_{1}^{\sqrt{x}} \frac{z^2}{z^4 + 1} dz$$

9.
$$y = \int_0^{tanx} \sqrt{t + \sqrt{t}} dt$$

10.
$$y = \int_0^{x^4} \cos^2 \theta d\theta$$

$$11. \ y = \int_{1-3x}^{1} \frac{u^3}{1+u^2} du$$

12.
$$y = \int_{sin x}^{1} \sqrt{1 + t^2} dt$$

$$13. \int_{-1}^{2} (x^3 - 2x) dx$$

14.
$$\int_{-1}^{1} x^{100} dx$$

15.
$$\int_{1}^{4} (5 - 2t + 3t^2) dt$$

16.
$$\int_0^1 (1 + \frac{1}{2}u^4 - \frac{2}{5}u^9)$$



17.
$$\int_{1}^{9} \sqrt{x} dx$$

18.
$$\int_{1}^{8} x^{-2/3} dx$$

19.
$$\int_{\pi/6}^{\pi} \sin\!\theta d\theta$$

20.
$$\int_{-5}^{5} \pi dx$$

21.
$$\int_0^1 (u+2)(u-3)du$$

22.
$$\int_0^4 (4-t)\sqrt{t}dt$$

23.
$$\int_{1}^{9} \frac{x-1}{\sqrt{x}} dx$$

24.
$$\int_0^2 (y-1)(2y+1)$$

$$25. \int_0^{\pi/4} \sec^2 t dt$$

26.
$$\int_0^{\pi/4} \sec\theta \quad \tan\theta \quad d\theta$$

27.
$$\int_{1}^{2} (1+2y)^2 dy$$

$$28. \int_{1}^{2} \frac{s^4 + 1}{s^2} ds$$

29.
$$\int_{1}^{2} \frac{v^5 + 3v^6}{v^4} dv$$

30.
$$\int_{1}^{18} \sqrt{\frac{3}{z}} dz$$

31.
$$\int_0^\pi f(x)dx \quad \text{donde} \quad f(x) = \begin{cases} \sin x & \text{si} \quad 0 \leq & x < \pi/2 \\ \cos x & \text{si} \quad \pi/2 \leq & x \leq \pi \end{cases}$$

32.
$$\int_{-2}^{2} f(x) dx$$
 donde $f(x) = \begin{cases} 2 & \text{si } -2 \leq x \leq 0 \\ 4 - x^2 & \text{si } 0 < x \leq 2 \end{cases}$

¿Qué está mal con la ecuación?

33.
$$\int_{-2}^{1} x^{-4} dx = \frac{x^{-3}}{-3} \Big|_{-2}^{1} = -\frac{3}{8}$$



34.
$$\int_{-1}^{2} \frac{4}{x^3} dx = -\frac{2}{x^2} \Big|_{-1}^{2} = \frac{3}{2}$$

35.
$$\int_{\pi/3}^{\pi} \sec \theta \tan \theta d\theta = \sec \theta \Big|_{\pi/3}^{\pi} = -3$$

36.
$$\int_0^{\pi} \sec^2 x dx = \tan x \Big|_0^{\pi} = 0$$

Use un gráfico para dar una estimación aproximada del área de la región que se encuentra debajo de la curva dada. Luego encuentra el área exacta.

37.
$$y = \sqrt[3]{x}, \quad 0 \le x \le 27$$

38.
$$y = x^{-4}, \quad 1 \le x \le 6$$

39.
$$y = \sin x$$
, $0 \le x \le \pi$

40.
$$y = \sec^2 x$$
, $0 \le x \le \pi/3$

41.
$$\int_{1}^{9} \frac{1}{2x} dx$$

42.
$$\int_0^1 10^x dx$$

43.
$$\int_{1/2}^{\sqrt{3/2}} \frac{6}{\sqrt{1-t^2}} dt$$

44.
$$\int_0^1 \frac{4}{t^2+1} dt$$

45.
$$\int_{-1}^{1} e^{u+1} du$$

46.
$$\int_{1}^{2} \frac{4+u^{2}}{u^{3}} du$$



Verificar por diferenciación que la fórmula es correcta.

1.
$$\int \frac{1}{x^2 \sqrt{1+x^2}} dx = -\frac{\sqrt{1+x^2}}{x} + C$$

2.
$$\int \cos^2 x dx = \frac{1}{2}x + \frac{1}{4}\sin 2x + C$$

3.
$$\int \cos^3 x dx = \sin x - \frac{1}{3} \sin^3 x + C$$

4.
$$\int \frac{x}{\sqrt{a+bx}} dx = \frac{2}{3b^2} (bx - 2a)\sqrt{a+bx} + C$$

Encuentra la integral general indefinida.

5.
$$\int (x^2 + x^{-2})dx$$

6.
$$\int (\sqrt{x^3} + \sqrt[3]{x^2}) dx$$

7.
$$\int (x^4 - \frac{1}{2}x^3 + \frac{1}{4}x - 2)dx$$

8.
$$\int (y^3 + 1.8y^2 - 2.4y)dy$$

9.
$$\int (u+4)(2u+1)du$$

10.
$$\int v(v^2+2)^2 dv$$

$$11. \int \frac{x^3 - 2\sqrt{x}}{x} dx$$

12.
$$\int \left(u^2 + 1 + \frac{1}{u^2}\right) du$$

13.
$$\int (\theta - \csc\theta \cot\theta) d\theta$$

$$14. \int \sec t (\sec t + \tan t) dt$$

15.
$$\int (1 + \tan^2 \alpha) d\alpha$$

$$16. \int \frac{\sin 2x}{\sin x} dx$$

17.
$$\int_{-3}^{3} (x^2 - 3) dx$$



18.
$$\int_{1}^{2} (4x^3 - 3x^2 + 2x) dx$$

19.
$$\int_{-2}^{0} (\frac{1}{2}t^4 + \frac{1}{4}t^3 - t)dt$$

20.
$$\int_0^3 (1+6w^2-10w^4)dw$$

21.
$$\int_0^2 (2x-3)(4x^2+1)dx$$

22.
$$\int_{-1}^{1} t(1-t)^2 dt$$

$$23. \int_0^{\pi} (4\sin\theta - 3\cos\theta)d\theta$$

24.
$$\int_{1}^{2} \left(\frac{1}{x^2} - \frac{4}{x^3} \right) dx$$

$$25. \int_{1}^{4} \left(\frac{4+6u}{\sqrt{u}} \right) du$$

26.
$$\int_{1}^{2} \left(x + \frac{1}{x}\right)^{2} dx$$

27.
$$\int_{1}^{2} \sqrt{\frac{5}{x}} dx$$

28.
$$\int_{1}^{9} \frac{3x-2}{\sqrt{x}} dx$$

29.
$$\int_{1}^{4} \sqrt{t}(1+t)dt$$

$$30. \int_{\pi/4}^{\pi/3} \csc^2 \theta d\theta$$

31.
$$\int_0^{\pi/4} \frac{1 + \cos^2 \theta}{\cos^2 \theta} d\theta$$

32.
$$\int_0^{\pi/3} \frac{\sin \theta + \sin \theta \tan^2 \theta}{\sec^2 \theta} d\theta$$

33.
$$\int_{1}^{64} \frac{1+\sqrt[3]{x}}{\sqrt{x}} dx$$

34.
$$\int_{1}^{8} \frac{x-1}{\sqrt[3]{x^2}} dx$$

35.
$$\int_0^1 (\sqrt[4]{x^5} + \sqrt[5]{x^4}) dx$$



36.
$$\int_0^1 (1+x^2)^3 dx$$

37.
$$\int_{2}^{5} |x-3| dx$$

38.
$$\int_0^2 |2x-1| dx$$

39.
$$\int_{-1}^{2} (x-2|x|)dx$$

40.
$$\int_0^{3\pi/2} |\sin x| dx$$

41.
$$\int (\sin x + \sin hx) dx$$

42.
$$\int_{-10}^{10} \frac{2e^x}{\sinh x + \cosh x} dx$$

43.
$$\int \left(x^2 + 1 + \frac{1}{x^2 + 1}\right) dx$$

44.
$$\int_{1}^{2} \frac{(x-1)^{3}}{x^{2}} dx$$

45.
$$\int_0^{1/\sqrt{3}} \frac{t^2 - 1}{t^4 - 1} dt$$

Evalúa la integral haciendo la sustitución dada.

1.
$$\int \sin \pi x dx, \quad u = \pi x$$

2.
$$\int x^3 (2+x^4)^5 dx, \quad u=2+x^4$$

3.
$$\int x^2 \sqrt{x^3 + 1} dx$$
, $u = x^3 + 1$

4.
$$\int \frac{dt}{(1-6t)^4}, \quad u = 1 - 6t$$

5.
$$\int \cos^3 \theta \sin \theta d\theta, \quad u = \cos \theta$$

6.
$$\int \frac{\sec^2(1/x)}{x^2} dx$$
, $u = 1/x$

Evaluar la integral indefinida.

7.
$$\int x \sin(x^2) dx$$

$$8. \int x^2 \cos(x^3) dx$$



9.
$$\int (1-2x)^9 dx$$

10.
$$\int (3t+2)^{2.4} dt$$

11.
$$\int (x+1)\sqrt{2x+x^2}dx$$

12.
$$\int \sec^2 2\theta d\theta$$

13.
$$\int \sec 3t \tan 3t dt$$

$$14. \int u\sqrt{1-u^2}du$$

$$15. \int \frac{a+bx^2}{\sqrt{3ax+bx^3}} dx$$

$$16. \int \frac{\sin \sqrt{x}}{\sqrt{x}} dx$$

17.
$$\int \sec^2 \theta \tan^3 \theta d\theta$$

18.
$$\int \cos^4 \theta \sin \theta d\theta$$

19.
$$\int (x^2 + 1)(x^3 + 3x)^4 dx$$

20.
$$\int \sqrt{x} \sin(1+x^{3/2}) dx$$

$$21. \int \frac{\cos x}{\sin^2 x} dx$$

$$22. \int \frac{\cos(\pi/x)}{x^2} dx$$

23.
$$\int \frac{z^2}{\sqrt[3]{1+z^3}} dz$$

$$24. \int \frac{dt}{\cos^2 t \sqrt{1 + \tan t}}$$

$$25. \int \sqrt{\cot x} \csc^2 x dx$$

26.
$$\int \sin t \sec^2(\cos t) dt$$

27.
$$\int \sec^3 x \tan x dx$$



$$28. \int x^2 \sqrt{2+x} dx$$

29.
$$\int x(2x+5)^8 dx$$

30.
$$\int x^3 \sqrt{x^2 + 1} dx$$

Evalúa la integral indefinida. Ilustre y compruebe que su respuesta es razonable graficando tanto la función como su antiderivada (tomar C=0).

31.
$$\int x(x^2-1)^3 dx$$

32.
$$\int \tan^2 \theta \sec^2 \theta d\theta$$

33.
$$\int \sin^3 x \cos x dx$$

$$34. \int \sin x \cos^4 x dx$$

Evaluar la integral definida.

35.
$$\int_0^1 \cos(\pi t/2) dt$$

36.
$$\int_0^1 (3t-1)^{50} dt$$

37.
$$\int_0^1 \sqrt[3]{1+7x} dx$$

38.
$$\int_0^{\sqrt{\pi}} x \cos(x^2) dx$$

39.
$$\int_0^{\pi} \sec^2(t/4) dt$$

40.
$$\int_{1/6}^{1/2} \csc \pi t \cot \pi t dt$$

41.
$$\int_{-\pi/4}^{\pi/4} (x^3 + x^4 \tan x) dx$$

42.
$$\int_0^{\pi/2} \cos x \sin(\sin x) dx$$

43.
$$\int_0^{13} \frac{dx}{\sqrt[3]{(1+2x)^2}}$$

44.
$$\int_0^a x\sqrt{a^2-x^2}dx$$



45.
$$\int_0^a x\sqrt{x^2+a^2}dx \quad (a>0)$$

46.
$$\int_{-\pi/3}^{\pi/3} x^4 \sin x dx$$

47.
$$\int_{1}^{2} x \sqrt{x-1} dx$$

48.
$$\int_0^4 \frac{x}{\sqrt{1+2x}} dx$$

49.
$$\int_{1/2}^{1} \frac{\cos(x^{-2})}{x^3} dx$$

50.
$$\int_0^{T/2} \sin(2\pi t/T - \alpha) dt$$

51.
$$\int_0^1 \frac{dx}{(1+\sqrt{x})^4}$$

$$52. \int \frac{dx}{5-3x}$$

$$53. \int e^x \sin(e^x) dx$$

$$54. \int \frac{(\ln x)^2}{x} dx$$

$$55. \int \frac{dx}{ax+b} (a \neq 0)$$

$$56. \int e^{\tan x} \sec^2 x dx$$

$$57. \int e^{\cos t} \sin t dt$$

$$58. \int e^{\tan x} \sec^2 x dx$$

59.
$$\int \frac{\tan^{-1} x}{1 + x^2} dx$$

60.
$$\int \frac{1+x}{1+x^2} dx$$

$$\mathbf{61.} \int \frac{\sin(\ln x)}{x} dx$$

62.
$$\int \frac{\sin 2x}{1 + \cos^2 x} dx$$



$$63. \int \frac{\sin 2x}{1 + \cos 2x} dx$$

$$64. \int \frac{\sin x}{1 + \cos^2 x} dx$$

$$65. \int \cot x dx$$

$$66. \int \frac{\sin x}{1 + \cos^2 x} dx$$

$$67. \int_{e}^{e4} \frac{dx}{x\sqrt{\ln x}}$$

68.
$$\int_0^1 xe^{-x^2} dx$$

69.
$$\int_0^1 \frac{e^z + 1}{e^z + z} dz$$

70.
$$\int_0^{1/2} \frac{\sin^{-1}}{\sqrt{1-x^2}} dx$$

71.
$$\int_{1}^{2} (8x^3 + 3x^2) dx$$

72.
$$\int_0^T (x^4 - 8x + 7) dx$$

73.
$$\int_0^1 (1-x^9)dx$$

74.
$$\int_0^1 (\sqrt[4]{u} + 1)^2 du$$

75.
$$\int_0^1 y(y^2+1)^5 dy$$

76.
$$\int_0^2 y^2 \sqrt{1+y^3} dy$$

77.
$$\int_{1}^{5} \frac{dt}{(t-4)^2}$$

78.
$$\int_0^1 \sin(3\pi t) dt$$

79.
$$\int_0^1 v^2 \cos(v^3) dv$$

80.
$$\int_{-1}^{1} \frac{\sin x}{1 + x^2} dx$$



81.
$$\int_{-\pi/4}^{\pi/4} \frac{t^4 \tan t}{2 + \cos t} dt$$

82.
$$\int \frac{x+2}{\sqrt{x^2+4x}} dx$$

83.
$$\int \sin \pi t \cos \pi t dt$$

84.
$$\int \sin x \cos(\cos x) dx$$

85.
$$\int_0^{\pi/8} \sec 2\theta \tan 2\theta d\theta$$

86.
$$\int_0^{\pi/4} (1 + \tan t)^3 \sec^2 t dt$$

87.
$$\int_0^3 |x^2 - 4| dx$$

88.
$$\int_0^4 |\sqrt{x} - 1| dx$$

Encuentra la derivada de la función.

89.
$$F(x) = \int_0^x \frac{t^2}{1+t^3} dt$$

90.
$$F(x) = \int_{x}^{1} \sqrt{t + \sin t} dt$$

91.
$$g(x) = \int_0^{x^4} \cos(t^2) dt$$

92.
$$g(x) = \int_{1}^{\sin x} \frac{1 - t^2}{1 + t^4} dt$$

93.
$$y = \int_{\sqrt{x}}^{x} \frac{\cos \theta}{\theta} d\theta$$

94.
$$y = \int_{2x}^{3x+1} \sin(t^4) dt$$



$$1. \int \frac{\sqrt[5]{x^3} + \sqrt[6]{x}}{\sqrt{x}} dx.$$

$$2. \int \frac{dx}{\sqrt{x-1} + \sqrt{x+1}}.$$

3.
$$\int \frac{e^x + e^{2x} + e^{3x}}{e^{4x}} dx$$
.

4.
$$\int \frac{a^x}{b^x} dx.$$

5.
$$\int tg^2xdx$$
.

6.
$$\int \frac{dx}{a^2 + x^2}$$
.

$$7. \int \frac{dx}{\sqrt{a^2 - x^2}}.$$

8.
$$\int \frac{dx}{1 + senx}.$$

9.
$$\int \frac{8x^2 + 6x + 4}{x + 1} dx$$
.

$$10. \int \frac{1}{\sqrt{2x-x^2}} dx.$$

11.
$$\int e^x \operatorname{sen} e^x dx$$
.

12.
$$\int xe^{-x^2}dx$$
.

13.
$$\int \frac{logx}{x} dx.$$

14.
$$\int \frac{e^x dx}{e^{2x} + 2e^x + 1}.$$

$$15. \int e^{x^2} e^x dx.$$

$$16. \int \frac{xdx}{\sqrt{1-x^4}}.$$

17.
$$\int \frac{e\sqrt{x}}{\sqrt{x}} dx.$$

18.
$$\int x\sqrt{1-x^2}dx$$
.



- 19. $\int log(\cos x)tgxdx$.
- 20. $\int \frac{\log(\log x)}{x \log x} dx.$
- 21. $\int x^2 e^x dx.$
- **22.** $\int x^3 e^{x^2} dx$.
- 23. $\int e^{ax} senbxdx$.
- 24. $\int x^2 senx dx$.
- **25.** $\int (\log x)^3 dx.$
- 26. $\int \frac{\log(\log x)}{x} dx.$
- 27. $\int sec^3x dx$.
- **28.** $\int \cos(\log x) dx.$
- **29.** $\int \sqrt{x} log x dx.$
- 30. $\int x(\log x)^2 dx.$
- $31. \int \frac{dx}{\sqrt{1-x^2}}.$
- $32. \int \frac{dx}{\sqrt{1+x^2}}.$
- $33. \int \frac{dx}{\sqrt{x^2 1}}.$
- **34.** $\int \frac{dx}{x\sqrt{x^2-1}}$.
- $35. \int \frac{dx}{x\sqrt{1-x^2}}.$
- $36. \int \frac{dx}{x\sqrt{1+x^2}}.$
- **37.** $\int x^2 \sqrt{1-x^2} dx$.



$$38. \int \sqrt{1-x^2} dx.$$

39.
$$\int \sqrt{1+x^2} dx$$
.

40.
$$\int \sqrt{x^2 - 1} dx$$
.

$$41. \int \frac{dx}{1+\sqrt{x+1}}.$$

42.
$$\int \frac{dx}{1+e^x}$$
.

$$43. \int \frac{dx}{\sqrt{x} + \sqrt[3]{x}}.$$

$$44. \int \frac{dx}{\sqrt{1+e^x}}.$$

$$45. \int \frac{dx}{2 + tgx}.$$

$$46. \int \frac{dx}{\sqrt{\sqrt{x+1}}}.$$

47.
$$\int \frac{4^x + 1}{2^x + 1} dx.$$

48.
$$\int e\sqrt{x}dx$$
.

$$49. \int \frac{\sqrt{1-x}}{1-\sqrt{x}} dx.$$

50.
$$\int \sqrt{\frac{x-1}{x+1}} \cdot \frac{1}{x^2} dx$$
.

$$51. \int \frac{2x^2 + 7x - 1}{x^3 + x^2 - x - 1} dx.$$

52.
$$\int \frac{2x+1}{x^3-3x^2+3x-1} dx.$$

53.
$$\int \frac{x^3 + 7x^2 - 5x + 5}{(x-1)^2(x+1)^3} dx.$$

54.
$$\int \frac{2x^2 + x + 1}{(x+3)(x-1)^2} dx.$$

55.
$$\int \frac{x+4}{x^2+1} dx$$
.



56.
$$\int \frac{x^3 + x + 2}{x^4 + 2x^2 + 1} dx.$$

$$57. \int \frac{3x^2 + 3x + 1}{x^3 + 2x^2 + 2x + 1} dx.$$

58.
$$\int \frac{dx}{x^4 + 1}$$
.

$$59. \int \frac{2x}{(x^2 + x + 1)^3} dx.$$

60.
$$\int \frac{3x}{(x^2+x+1)^3} dx.$$

61.
$$\int \frac{\operatorname{arctg } \mathbf{x}}{1+x^2} dx.$$

62.
$$\int \frac{x \arctan x}{(1+x^2)^3}$$
.

$$63. \int \log \sqrt{1+x^2} dx.$$

$$64. \int x \log \sqrt{1+x^2} dx.$$

65.
$$\int \frac{x^2-1}{x^2+1} \cdot \frac{1}{\sqrt{1+x^4}} dx$$
.

66.
$$\int \operatorname{arcsen} \sqrt{x} dx$$
.

67.
$$\int \frac{x}{1 + senx} dx.$$

68.
$$\int e^{senx} \cdot \frac{x\cos^3 x - senx}{\cos^2 x} dx.$$

69.
$$\int \sqrt{tgx} dx.$$

70.
$$\int \frac{dx}{x^6 + 1}$$
.

71.
$$\int \log(a^2 + x^2) dx$$
.

72.
$$\int \frac{1 + \cos x}{\sin^2 x} dx.$$

73.
$$\int \frac{x+1}{\sqrt{4-x^2}} dx$$
.



74.
$$\int x \operatorname{arctg} x dx$$
.

75.
$$\int sen^3x dx$$
.

$$76. \int \frac{sen^3x}{cos^2x} dx.$$

77.
$$\int x^2 \operatorname{arctg} x dx$$
.

78.
$$\int \frac{xdx}{\sqrt{x^2 - 2x + 2}}$$
.

79.
$$\int sec^3x \quad tg \quad x \quad dx$$
.

80.
$$\int x tg^2 x dx$$
.

81.
$$\int \frac{dx}{(a^2 + x^2)^2}$$

82.
$$\int \sqrt{1 - senx dx}.$$

83.
$$\int \operatorname{arctg} \sqrt{x} dx$$
.

84.
$$\int sen\sqrt{x+1}dx.$$

85.
$$\int \frac{\sqrt{x^3 - 2}}{x} dx$$
.

86.
$$\int log(x + \sqrt{x^2 - 1}) dx$$
.

87.
$$\int log(x+\sqrt{x})dx.$$

88.
$$\int \frac{dx}{x - x^{3/5}}$$
.

89.
$$\int \frac{dx}{1 + senx}.$$

90.
$$\int \frac{dx}{3 + 5senx}.$$

Evaluar la integral utilizando la integración por partes con las elecciones indicadas de u y dv.

1.
$$\int x \ln x dx$$
; $u = \ln x$, $dv = x dx$



2.
$$\int \theta \sec^2 \theta d\theta$$
; $u = \theta$, $dv = \sec^2 \theta d\theta$

- $3. \int x \cos 5x dx$
- 4. $\int xe^{-x}dx$
- 5. $\int re^{r/2}dr$
- 6. $\int t \sin 2t dt$
- 7. $\int x^2 \sin \pi x dx$
- 8. $\int x^2 \cos mx dx$
- $9. \int \ln(2x+1)dx$
- $10. \int \sin^{-1} x dx$
- 11. $\int arc \tan 4t dt$
- $12. \int p^5 \ln p dp$
- **13.** $\int (\ln x^2) dx$
- 14. $\int t^3 e^t dt$
- **15.** $\int e^{2\theta} \sin 3\theta d\theta$
- $16. \int e^{\theta} \cos 2\theta d\theta$
- 17. $\int y \sinh y dy$
- 18. $\int y \cosh ay dy$
- 19. $\int_0^{\pi} t \sin 3t dt$
- **20.** $\int_0^1 (x^2+1)e^{-x}dx$



21.
$$\int_{1}^{2} \frac{\ln x}{x^2} dx$$

$$22. \int_{1}^{4} \sqrt{t} \ln t dt$$

23.
$$\int_0^1 \frac{y}{e^{2y}} dy$$

24.
$$\int_{\pi/4}^{\pi/2} x \csc^2 x dx$$

25.
$$\int_0^{1/2} \cos^{-1} x dx$$

26.
$$\int_0^1 x 5^x dx$$

27.
$$\int \cos x \ln(\sin x) dx$$

$$28. \int_{1}^{\sqrt{3}} \arctan(1/x) dx$$

$$29. \int \cos(\ln x) dx$$

30.
$$\int_0^1 \frac{r^3}{\sqrt{4+r^2}} dr$$

31.
$$\int_{1}^{2} x^{4} (\ln x)^{2} dx$$

32.
$$\int_0^t e^s \sin(t-s) ds$$

Primero realice una sustitución y luego use la integración por partes para evaluar la integral.

$$33. \int \sin \sqrt{x} dx$$

34.
$$\int_{1}^{4} e^{\sqrt{x}} dx$$

35.
$$\int_{\sqrt{\pi/2}}^{\sqrt{\pi}} \theta^3 \cos(\theta^2) d\theta$$

36.
$$\int x^5 e^{x^2} dx$$

37.
$$\int x \cos \pi x dx$$

38.
$$\int x^{3/2} \ln x dx$$



39.
$$\int (2x+3)e^x dx$$

40.
$$\int x^3 e^{x^2} dx$$

41.

a. Demuestre que:

$$\int \sin^2 x dx = \frac{x}{2} - \frac{\sin 2x}{4} + C$$

b. Use la parte (a) y la fórmula de reducción para evaluar $\int \sin^4 x dx$.

42.

a. Demuestre la fórmula de reducción

$$\int \cos^n x dx = \frac{1}{n} \cos^{n-1} x \sin x + \frac{n-1}{n} \int \cos^{n-2} x dx$$

- b. Use la parte (a) para evaluar $\int \cos^2 x dx$.
- c. Use las partes (a) y (b) para evaluar $\int \cos^4 x dx$.

43.

a. Demuestre que:

$$\int_0^{\pi/2} \sin^n x dx = \frac{n-1}{n} \int_0^{\pi/2} \sin^{n-2} x dx$$

Cuando $n \ge 2$ es un numero entero.

- b. Use la parte (a) para evaluar, $\int_0^{\pi/2} \sin^3 x dx$ y $\int_0^{\pi/2} \sin^5 dx$.
- c. Use la parte (a) para mostrar que, para las potencias impares del seno,

$$\int_0^{\pi/2} \sin^{2n+1} x dx = \frac{2.4.6....2n}{3.5.7....(2n+1)}$$

44. Demuestre que, incluso para las potencias del seno:

$$\int_0^{\pi/2} \sin^{2n} x dx = \frac{1 \cdot 3 \cdot 5 \cdot \dots \cdot (2n-1)}{2 \cdot 4 \cdot 6 \cdot \dots \cdot 2n} \frac{\pi}{2}$$

Use la integración por partes para probar la fórmula de reducción

45.
$$\int (\ln x)^n dx = x(\ln x)^n - n \int (\ln x)^{n-1} dx$$



46.
$$\int x^n e^x dx = x^n e^x - n \int x^{n-1} e^x dx$$

47.
$$\int (x^2 + a^2)^n dx = \frac{x(x^2 + a^2)^n}{2n+1} + \frac{2na^2}{2n+1} \int (x^2 + a^2)^{n-1} dx \quad (n \neq -\frac{1}{2})$$

48.
$$\int \sec^n x dx = \frac{\tan x \sec^{n-2} x}{n-1} + \frac{n-1}{n-1} \int \sec^{n-2} x dx \quad (n \neq 1)$$

- 49. Usa el ejercicio 45 para encontrar $\int (\ln x)^3 dx$.
- 50. Usa el ejercicio 46 para encontrar $\int x^4 e^x dx$.

Encuentra el área de la región delimitada por las curvas dadas.

51.
$$y = xe^{-0.4x}$$
, $y = 0$, $x = 5$

52.
$$y = 5 \ln x$$
, $y = x \ln x$



Integrales trigonométricas

$$1. \int \sin^3 x \cos^2 x dx$$

$$2. \int \sin^6 x \cos^3 x dx$$

3.
$$\int -\pi/2^{3\pi/4} \sin^5 x \cos^3 x dx$$

4.
$$\int_0^{\pi/2} \cos^5 x dx$$

$$5. \int \cos^5 x \sin^4 x dx$$

6.
$$\int_{\sin^3(mx)dx}$$

$$7. \int_0^{\pi/2} \cos^2 \theta d\theta$$

8.
$$\int_0^{\pi/2} \sin^2(2\theta) d\theta$$

9.
$$\int_0^{\pi} \sin^4(3t) dt$$

10.
$$\int_0^{\pi} \cos^6 \theta d\theta$$

11.
$$\int (1+\cos\theta)^2 d\theta$$

$$12. \int x \cos^2 x dx$$

13.
$$\int_0^{\pi/4} \sin^4 x \cos^2 x dx$$

14.
$$\int_0^{\pi/2} \sin^2 x \cos^2 x dx$$

$$15. \int \sin^3 x \sqrt{\cos x} dx$$

16.
$$\int \cos \theta \cos^5(\sin \theta) d\theta$$

17.
$$\int \cos^2 x \tan^3 x dx$$

18.
$$\int \cot^5 \theta \sin^4 \theta d\theta$$



$$19. \int \frac{1 - \sin x}{\cos x} dx$$

$$20. \int \cos^2 x \sin 2x dx$$

21.
$$\int \sec^2 x \tan x dx$$

22.
$$\int_0^{\pi/2} \sec^4(t/2) dt$$

23.
$$\int \tan^2 x dx$$

24.
$$\int \tan^4 x dx$$

25.
$$\int \sec^6 t dt$$

26.
$$\int_0^{\pi/4} \sec^4 \theta \tan^4 \theta d\theta$$

27.
$$\int_0^{\pi/3} \tan^5 \sec^4 x dx$$

28.
$$\int \tan^3(2x) \sec^5(2x) dx$$

29.
$$\int \tan^3 \sec x dx$$

30.
$$\int_0^{\pi/3} \tan^5 x \sec^6 x dx$$

31.
$$\int \tan^5 x dx$$

32.
$$\int \tan^6(ay)dy$$

$$33. \int \frac{\tan^3 \theta}{\cos^4 \theta} d\theta$$

34.
$$\int \tan^2 x \sec x dx$$

35.
$$\int_{\pi/6}^{\pi/2} \cot^2 x dx$$

36.
$$\int_{\pi/4}^{\pi/2} \cot^3 x dx$$

$$37. \int \cot^3 \alpha \csc^3 \alpha d\alpha$$



38.
$$\int \csc^4 x \cot^5 x dx$$

39.
$$\int \csc x dx$$

40.
$$\int_{\pi/6}^{\pi/3} \csc^3 x dx$$

41.
$$\int \sin 5x \sin 2x dx$$

42.
$$\int \sin 3x \cos x dx$$

43.
$$\int \cos 7\theta \cos 5\theta d\theta$$

$$44. \int \frac{\cos x + \sin x}{\sin 2x} dx$$

$$45. \int \frac{1 - \tan^2 x}{\sec^2 x} dx$$

$$46. \int \frac{dx}{\cos x - 1}$$

47.
$$\int t \sec^2(t^2) \tan^4(t^2) dt$$

48. Si
$$\int_0^{\pi/4} \tan^6 x \sec x dx = I$$
 exprese el valor de $\int_0^{\pi/4} \tan^8 x \sec x dx$ en terminos de I .

Evalúa la integral indefinida. Ilustre y compruebe que su respuesta es razonable, graficando tanto el integrando como su antiderivada (tomando ${\cal C}=0$)

49.
$$\int \sin^5 x dx$$

$$50. \int \sin^4 x \cos^4 x dx$$

51.
$$\int \sin 3x \sin 6x dx$$

52.
$$\int \sec^4 \frac{x}{2} dx$$

Evaluar la integral usando la sustitución trigonométrica indicada. Dibuje y etiquete el triángulo rectángulo asociado.

1.
$$\int \frac{1}{x^2 \sqrt{x^2 - 9}} dx$$
; $x = 3 \sec \theta$

$$2. \int x^3 \sqrt{9 - x^2} dx; \quad x = 3\sin\theta$$



3.
$$\int \frac{x^3}{\sqrt{x^2+9}} dx$$
; $x = 3 \tan \theta$

4.
$$\int_0^{2\sqrt{3}} \frac{x^3}{\sqrt{16-x^2}} dx$$

$$5. \int_{\sqrt{2}}^{2} \frac{1}{t^3 \sqrt{t^2 - 1}} dt$$

6.
$$\int_0^2 x^3 \sqrt{x^2 + 4} dx$$

7.
$$\int \frac{1}{x^2\sqrt{25-x^2}} dx$$