

Ejercicios de Límite

Cálculo

<http://synergy.vision/>

Contenido

$$1. \lim_{x \rightarrow 2} \frac{x^2 + 6}{x^2 - 3}$$

$$2. \lim_{y \rightarrow 0} \left[\frac{y^2 - 2y + 2}{y - 4} + 1 \right]$$

$$3. \lim_{x \rightarrow \sqrt{2}} \frac{x^2 - 2}{x^4 + x + 1}$$

$$4. \lim_{x \rightarrow 1} \sqrt{\frac{2x^2 + 2}{8x^2 + 1}}$$

$$5. \lim_{x \rightarrow 3} \frac{x^2 - 9}{x - 3}$$

$$6. \lim_{y \rightarrow -5} \frac{y^2 - 25}{y + 5}$$

$$7. \lim_{h \rightarrow 2} \frac{h - 2}{h^2 - 4}$$

$$8. \lim_{x \rightarrow 2} \frac{x^3 - 8}{x - 2}$$

$$9. \lim_{y \rightarrow -3} \frac{y^3 + 27}{y + 3}$$

$$10. \lim_{x \rightarrow 4} \frac{x^2 + 4x - 32}{x - 4}$$

$$11. \lim_{x \rightarrow -1} \frac{\frac{1}{2}x^2 - \frac{5}{2}x - 3}{x + 1}$$

$$12. \lim_{x \rightarrow -2} \frac{\frac{1}{x+1} + 1}{x + 2}$$

$$13. \lim_{x \rightarrow \frac{1}{2}} \frac{8x^3 - 1}{6x^2 - 5x + 1}$$

$$14. \lim_{x \rightarrow 2} \frac{x^4 - 16}{x - 2}$$

$$15. \lim_{x \rightarrow 8} \frac{16 - x^{4/3}}{4 - x^{2/3}}$$

$$16. \lim_{x \rightarrow 2} \frac{\sqrt{x^2 + 5} - 3}{x^2 - 2x}$$

$$17. \lim_{x \rightarrow 9} \frac{x^2 - 81}{\sqrt{x} - 3}$$

18. $\lim_{x \rightarrow 0} \frac{x}{\sqrt{x+2} - \sqrt{2}}$
19. $\lim_{y \rightarrow 0} \frac{\sqrt{y+3} - \sqrt{3}}{y}$
20. $\lim_{x \rightarrow 1} \frac{\sqrt{x+3} - 2}{x-1}$
21. $\lim_{y \rightarrow 5} \frac{\sqrt{y-1} - 2}{y+5}$
22. $\lim_{h \rightarrow 0} \frac{\sqrt{1+h^2} - 1}{h}$
23. $\lim_{x \rightarrow 7} \frac{2 - \sqrt{x-3}}{x^2 - 49}$
24. $\lim_{x \rightarrow 1} \frac{x^2 - \sqrt{x}}{\sqrt{x} - 1}$
25. $\lim_{x \rightarrow 0} \frac{\sqrt{1+x} - \sqrt{1-x}}{\sqrt[3]{1+x} - \sqrt[3]{1-x}}$
26. $\lim_{x \rightarrow 8} \frac{x-8}{\sqrt[3]{x}-2}$
27. $\lim_{x \rightarrow 0} \frac{\sqrt[3]{x^2+1} - 1}{x^2}$
28. $\lim_{x \rightarrow 0} \frac{\sqrt[3]{1+x} - \sqrt[3]{1-x}}{x}$
29. $\lim_{x \rightarrow 1} \frac{\sqrt{x} - 1}{\sqrt[3]{x} - 1}$
30. $\lim_{x \rightarrow 64} \frac{\sqrt{x} - 8}{\sqrt[3]{x} - 4}$
31. $\lim_{x \rightarrow 1} \frac{\sqrt[3]{x} - 1}{\sqrt[4]{x} - 1}$
32. $\lim_{x \rightarrow 1} \frac{\sqrt[n]{x} - 1}{\sqrt[m]{x} - 1}$
33. $\lim_{x \rightarrow 2} \frac{\sqrt{6-x} - 2}{\sqrt{3-x} - 1}$
34. $\lim_{x \rightarrow a} \frac{x^3 - a^3}{x^2 - ax - x + a}$

$$35. \lim_{x \rightarrow 1} \frac{\sqrt{ax+b} - \sqrt{bx+a}}{\sqrt{cx+d} - \sqrt{dx+c}}$$

36. Si $f(x) = \frac{1}{x}$, $x \neq 0$, probar que

$$\lim_{h \rightarrow 0} \frac{g(x+h) - g(x)}{h} = -\frac{1}{x^2}$$

37. Si $f(x) = \sqrt{x}$, $x > 0$, probar que

$$\lim_{h \rightarrow 0} \frac{f(x+h) - f(x)}{h} = \frac{1}{2\sqrt{x}}$$

$$38. \lim_{x \rightarrow 2^+} \frac{\sqrt{x-2}}{2x-1}$$

$$39. \lim_{x \rightarrow 4^+} \frac{x-4}{\sqrt{x^2-16}}$$

$$40. \lim_{x \rightarrow 2^-} [x]$$

$$41. \lim_{x \rightarrow 2^+} [x]$$

$$42. \lim_{x \rightarrow -2^-} [x]$$

$$43. \lim_{x \rightarrow -2^+} [x]$$

$$44. \lim_{x \rightarrow 5/2} [x]$$

$$45. \lim_{x \rightarrow 2^-} (x - [x])$$

$$46. \lim_{x \rightarrow 2^+} (x - [x])$$

$$47. \lim_{x \rightarrow 3^-} [x^2 + x + 1]$$

$$48. \lim_{x \rightarrow 3^+} [x^2 + x + 1]$$

$$49. \lim_{x \rightarrow 3^-} [[x] + [4-x]]$$

$$50. \lim_{x \rightarrow 3^+} [[x] + [4-x]]$$

$$51. \lim_{x \rightarrow 4^+} \frac{x-4}{|x-4|}$$

$$52. \lim_{x \rightarrow 1^+} \frac{\sqrt{x+4} - \sqrt{4x+1}}{\sqrt{x-1}}$$

$$53. \lim_{x \rightarrow a^+} \frac{\sqrt{4-x^2} + 2 - x}{\sqrt{4-x^3/2} + \sqrt{2x-x^2}}$$

$$54. \lim_{x \rightarrow a^+} \frac{x\sqrt{x} - a\sqrt{a}}{\sqrt[3]{x} - \sqrt[3]{a}}$$

$$55. \text{ Si } h(x) = \begin{cases} 2x + 1 & \text{si } x \leq 2 \\ x^2 + 1 & \text{si } x > 2 \end{cases}$$

Hallar:

$$a. \lim_{x \rightarrow 2^-} h(x)$$

$$b. \lim_{x \rightarrow 2^+} h(x)$$

$$c. \lim_{x \rightarrow 2} h(x)$$

$$56. \text{ Si } f(x) = \begin{cases} x^3, & \text{si } x \leq 2 \\ x^2 + 4, & \text{si } x > 2 \end{cases}$$

Hallar:

$$a. \lim_{x \rightarrow 2^-} f(x)$$

$$b. \lim_{x \rightarrow 2^+} f(x)$$

$$c. \lim_{x \rightarrow 2} f(x)$$

$$57. \text{ Si } f(x) = \begin{cases} -4 & \text{si } x < -2 \\ \frac{x^3}{2} & \text{si } -2 \leq x < 2 \\ x - 1 & \text{si } x \geq 2 \end{cases}$$

Hallar:

$$a. \lim_{x \rightarrow -2} f(x)$$

$$b. \lim_{x \rightarrow 2} f(x)$$