

MODULE 3.1: CLASSIFICATION AND HIPOTHESIS TESTING

# CASE STUDY ACTIVITY TUTORIAL

**CASE STUDY 1 - CHALLENGER** 



# CASE STUDY ACTIVITY TUTORIAL

# **CASE STUDY 1 - CHALLENGER**

Faculty: David Gamarnik

In this document, we walk through some helpful tips to get you started with performing the analysis for the Challenger Case Study on your own. In this tutorial, we provide examples and some pseudo-code for the following programming environments: **R**, **Python**. We cover the following:

#### **Topics**

THE DATA	1
Accessing the Data	3
VISUALIZING THE DATA	3
LOGISTIC REGRESSION	

#### The Data

The entire data of observations is shown below. The data consists of three columns:

**Observation**: this is simply the count of the observation.

Y: this is the failure/success label for each observation. If there was a failure, Y=1. Else, Y=0.

X: this is the temperature (degrees Fahrenheit) at launch.

Copy the table below in to a csv (comma separate variable) file format. A sample is also separately made available with this document. It is titled "challenger-data.csv".

Observation	Y	Х
1	1	53
2	1	53
3	1	53
4	0	53
5	0	53
6	1	57
7	0	57
8	0	57
9	0	57
10	0	57
11	1	58
12	0	58
13	0	58

Observation	Υ	Х
61	0	70
62	0	70
63	0	70
64	0	70
65	0	70
66	0	70
67	0	70
68	0	70
69	0	70
70	0	70
71	0	72
72	0	72
73	0	72

		F.0
14	0	58
15	0	58
16	1	63
17	0	63
18	0	63
19	0	63
20	0	63
21	0	66
22	0	66
23	0	66
24	0	66
25	0	66
26	0	67
27	0	67
28	0	67
29	0	67
30	0	67
31	0	67
32	0	67
33	0	67
34	0	67
35	0	67
36	0	67
37	0	67
38	0	67
39	0	67
40	0	67
41	0	68
42	0	68
43	0	68
44	0	68
45	0	68
46	0	69
47	0	69
48	0	69
49	0	69
50	0	69
51	1	70
52	0	70
53	0	70
54	0	70
55	0	70
56	1	70
57	0	70
58	0	70
59		70
	0	
60	0	70

75         0         72           76         0         73           77         0         73           78         0         73           79         0         73           80         0         73           81         1         75           82         1         75           83         0         75           84         0         75           85         0         75           86         0         75           87         0         75           88         0         75           89         0         75           90         0         75           91         0         76           92         0         76           93         0         76           94         0         76           95         0         76           96         0         76           97         0         76           98         0         76           99         0         76           99         0         76	74	0	72
77         0         73           78         0         73           79         0         73           80         0         73           81         1         75           82         1         75           83         0         75           84         0         75           85         0         75           86         0         75           87         0         75           88         0         75           89         0         75           89         0         75           90         0         75           91         0         76           92         0         76           93         0         76           94         0         76           95         0         76           96         0         76           97         0         76           98         0         76           99         0         76           99         0         76           100         0         78	75	0	72
78         0         73           79         0         73           80         0         73           81         1         75           82         1         75           83         0         75           84         0         75           85         0         75           86         0         75           87         0         75           89         0         75           90         0         75           91         0         76           92         0         76           93         0         76           94         0         76           95         0         76           96         0         76           97         0         76           98         0         76           99         0         76           99         0         76           99         0         76           100         0         78           102         0         78           103         0         78	76	0	73
79         0         73           80         0         73           81         1         75           82         1         75           83         0         75           84         0         75           85         0         75           86         0         75           87         0         75           88         0         75           89         0         75           90         0         75           91         0         76           92         0         76           93         0         76           94         0         76           95         0         76           96         0         76           97         0         76           98         0         76           99         0         76           98         0         76           99         0         76           100         0         78           102         0         78           103         0         78	77	0	73
80       0       73         81       1       75         82       1       75         83       0       75         84       0       75         85       0       75         86       0       75         87       0       75         88       0       75         89       0       75         90       0       75         91       0       76         92       0       76         93       0       76         94       0       76         95       0       76         96       0       76         97       0       76         98       0       76         99       0       76         99       0       76         90       0       76         98       0       76         99       0       76         98       0       76         99       0       76         100       0       78         102       0       78         <	78	0	73
81       1       75         82       1       75         83       0       75         84       0       75         85       0       75         86       0       75         87       0       75         88       0       75         89       0       75         90       0       75         91       0       76         92       0       76         93       0       76         94       0       76         95       0       76         96       0       76         97       0       76         98       0       76         99       0       76         99       0       76         100       0       76         101       0       78         102       0       78         103       0       78         104       0       78         105       0       78         106       0       79         107       0       79	79	0	73
82       1       75         83       0       75         84       0       75         85       0       75         86       0       75         87       0       75         88       0       75         89       0       75         90       0       75         91       0       76         92       0       76         93       0       76         94       0       76         95       0       76         96       0       76         97       0       76         98       0       76         99       0       76         99       0       76         100       0       76         101       0       78         102       0       78         103       0       78         104       0       78         105       0       78         106       0       79         107       0       79         108       0       79	80	0	73
83       0       75         84       0       75         85       0       75         86       0       75         87       0       75         88       0       75         89       0       75         90       0       75         91       0       76         92       0       76         93       0       76         94       0       76         95       0       76         96       0       76         97       0       76         98       0       76         99       0       76         99       0       76         99       0       76         99       0       76         98       0       76         98       0       76         99       0       76         98       0       76         98       0       76         99       0       76         100       0       78         102       0       78         <	81	1	75
84       0       75         85       0       75         86       0       75         87       0       75         88       0       75         89       0       75         90       0       75         91       0       76         92       0       76         93       0       76         94       0       76         95       0       76         96       0       76         97       0       76         98       0       76         99       0       76         99       0       76         99       0       76         99       0       76         99       0       76         100       0       78         102       0       78         103       0       78         104       0       78         105       0       78         106       0       79         107       0       79         108       0       79	82	1	75
85       0       75         86       0       75         87       0       75         88       0       75         89       0       75         90       0       75         91       0       76         92       0       76         93       0       76         94       0       76         95       0       76         96       0       76         98       0       76         99       0       76         99       0       76         99       0       76         99       0       76         99       0       76         99       0       76         99       0       76         100       0       78         102       0       78         103       0       78         104       0       78         105       0       78         106       0       79         107       0       79         108       0       79	83	0	75
86       0       75         87       0       75         88       0       75         89       0       75         90       0       75         91       0       76         92       0       76         93       0       76         94       0       76         95       0       76         96       0       76         98       0       76         99       0       76         99       0       76         99       0       76         99       0       76         99       0       76         99       0       76         99       0       76         99       0       76         99       0       76         100       0       78         102       0       78         103       0       78         104       0       78         105       0       79         106       0       79         109       0       79	84	0	75
87       0       75         88       0       75         89       0       75         90       0       75         91       0       76         92       0       76         93       0       76         94       0       76         95       0       76         96       0       76         97       0       76         98       0       76         99       0       76         99       0       76         99       0       76         100       0       76         98       0       76         99       0       76         99       0       76         100       0       78         101       0       78         102       0       78         103       0       78         104       0       78         105       0       79         107       0       79         108       0       79         110       0       79	85	0	75
88       0       75         89       0       75         90       0       75         91       0       76         92       0       76         93       0       76         94       0       76         95       0       76         96       0       76         98       0       76         99       0       76         99       0       76         99       0       76         100       0       76         101       0       78         102       0       78         103       0       78         104       0       78         105       0       78         106       0       79         107       0       79         108       0       79         110       0       79         111       0       80         112       0       80         113       0       80         114       0       80         115       0       80	86	0	75
89       0       75         90       0       75         91       0       76         92       0       76         93       0       76         94       0       76         95       0       76         96       0       76         98       0       76         99       0       76         99       0       76         100       0       76         101       0       78         102       0       78         103       0       78         104       0       78         105       0       78         106       0       79         107       0       79         108       0       79         110       0       79         111       0       80         112       0       80         113       0       80         114       0       80         115       0       81         117       0       81         119       0       81	87	0	75
90       0       75         91       0       76         92       0       76         93       0       76         94       0       76         95       0       76         96       0       76         97       0       76         98       0       76         99       0       76         100       0       76         101       0       78         102       0       78         103       0       78         104       0       78         105       0       78         106       0       79         107       0       79         108       0       79         109       0       79         110       0       79         111       0       80         112       0       80         113       0       80         114       0       80         115       0       81         117       0       81         119       0       81	88	0	75
91       0       76         92       0       76         93       0       76         94       0       76         95       0       76         96       0       76         97       0       76         98       0       76         99       0       76         100       0       76         101       0       78         102       0       78         103       0       78         104       0       78         105       0       78         106       0       79         107       0       79         108       0       79         109       0       79         110       0       79         111       0       80         112       0       80         113       0       80         114       0       80         115       0       81         117       0       81         119       0       81	89	0	75
92       0       76         93       0       76         94       0       76         95       0       76         96       0       76         97       0       76         98       0       76         99       0       76         100       0       76         101       0       78         102       0       78         103       0       78         104       0       78         105       0       78         106       0       79         107       0       79         108       0       79         109       0       79         110       0       79         111       0       80         112       0       80         113       0       80         114       0       80         115       0       80         116       0       81         117       0       81         119       0       81	90	0	75
93       0       76         94       0       76         95       0       76         96       0       76         97       0       76         98       0       76         99       0       76         100       0       76         101       0       78         102       0       78         103       0       78         104       0       78         105       0       78         106       0       79         107       0       79         108       0       79         109       0       79         110       0       79         111       0       80         112       0       80         113       0       80         114       0       80         115       0       80         116       0       81         117       0       81         119       0       81	91	0	76
94       0       76         95       0       76         96       0       76         97       0       76         98       0       76         99       0       76         100       0       76         101       0       78         102       0       78         103       0       78         104       0       78         105       0       78         106       0       79         107       0       79         108       0       79         109       0       79         110       0       79         111       0       80         112       0       80         113       0       80         114       0       80         115       0       80         116       0       81         117       0       81         119       0       81	92	0	76
95       0       76         96       0       76         97       0       76         98       0       76         99       0       76         100       0       76         101       0       78         102       0       78         103       0       78         104       0       78         105       0       78         106       0       79         107       0       79         108       0       79         109       0       79         110       0       79         111       0       80         112       0       80         113       0       80         114       0       80         115       0       80         116       0       81         117       0       81         119       0       81	93	0	76
96       0       76         97       0       76         98       0       76         99       0       76         100       0       76         101       0       78         102       0       78         103       0       78         104       0       78         105       0       78         106       0       79         107       0       79         108       0       79         109       0       79         110       0       79         111       0       80         112       0       80         113       0       80         114       0       80         115       0       81         117       0       81         118       0       81         119       0       81	94	0	76
97       0       76         98       0       76         99       0       76         100       0       76         101       0       78         102       0       78         103       0       78         104       0       78         105       0       78         106       0       79         107       0       79         108       0       79         109       0       79         110       0       79         111       0       80         112       0       80         113       0       80         114       0       80         115       0       81         117       0       81         118       0       81         119       0       81	95	0	76
98       0       76         99       0       76         100       0       76         101       0       78         102       0       78         103       0       78         104       0       78         105       0       78         106       0       79         107       0       79         108       0       79         109       0       79         110       0       79         111       0       80         112       0       80         113       0       80         114       0       80         115       0       80         116       0       81         117       0       81         119       0       81	96	0	76
99       0       76         100       0       76         101       0       78         102       0       78         103       0       78         104       0       78         105       0       78         106       0       79         107       0       79         108       0       79         109       0       79         110       0       79         111       0       80         112       0       80         113       0       80         114       0       80         115       0       80         116       0       81         117       0       81         119       0       81	97	0	76
100       0       76         101       0       78         102       0       78         103       0       78         104       0       78         105       0       78         106       0       79         107       0       79         108       0       79         109       0       79         110       0       79         111       0       80         112       0       80         113       0       80         114       0       80         115       0       80         116       0       81         117       0       81         119       0       81		0	76
101     0     78       102     0     78       103     0     78       104     0     78       105     0     78       106     0     79       107     0     79       108     0     79       109     0     79       110     0     79       111     0     80       112     0     80       113     0     80       114     0     80       115     0     80       116     0     81       117     0     81       119     0     81	99	0	
102     0     78       103     0     78       104     0     78       105     0     78       106     0     79       107     0     79       108     0     79       109     0     79       110     0     79       111     0     80       112     0     80       113     0     80       114     0     80       115     0     80       116     0     81       117     0     81       119     0     81	100	0	76
103     0     78       104     0     78       105     0     78       106     0     79       107     0     79       108     0     79       109     0     79       110     0     79       111     0     80       112     0     80       113     0     80       114     0     80       115     0     80       116     0     81       117     0     81       118     0     81       119     0     81		0	
104     0     78       105     0     78       106     0     79       107     0     79       108     0     79       109     0     79       110     0     79       111     0     80       112     0     80       113     0     80       114     0     80       115     0     80       116     0     81       117     0     81       118     0     81       119     0     81		0	
105     0     78       106     0     79       107     0     79       108     0     79       109     0     79       110     0     79       111     0     80       112     0     80       113     0     80       114     0     80       115     0     80       116     0     81       117     0     81       118     0     81       119     0     81			
106     0     79       107     0     79       108     0     79       109     0     79       110     0     79       111     0     80       112     0     80       113     0     80       114     0     80       115     0     80       116     0     81       117     0     81       118     0     81       119     0     81		0	
107     0     79       108     0     79       109     0     79       110     0     79       111     0     80       112     0     80       113     0     80       114     0     80       115     0     80       116     0     81       117     0     81       118     0     81       119     0     81		0	
108     0     79       109     0     79       110     0     79       111     0     80       112     0     80       113     0     80       114     0     80       115     0     80       116     0     81       117     0     81       118     0     81       119     0     81			
109     0     79       110     0     79       111     0     80       112     0     80       113     0     80       114     0     80       115     0     80       116     0     81       117     0     81       118     0     81       119     0     81	107	0	
110     0     79       111     0     80       112     0     80       113     0     80       114     0     80       115     0     80       116     0     81       117     0     81       118     0     81       119     0     81			
111     0     80       112     0     80       113     0     80       114     0     80       115     0     80       116     0     81       117     0     81       118     0     81       119     0     81		0	
112     0     80       113     0     80       114     0     80       115     0     80       116     0     81       117     0     81       118     0     81       119     0     81		0	79
113     0     80       114     0     80       115     0     80       116     0     81       117     0     81       118     0     81       119     0     81		0	80
114     0     80       115     0     80       116     0     81       117     0     81       118     0     81       119     0     81			
115     0     80       116     0     81       117     0     81       118     0     81       119     0     81			
116     0     81       117     0     81       118     0     81       119     0     81			
117     0     81       118     0     81       119     0     81			
118     0     81       119     0     81			
<b>119</b> 0 81			
<b>120</b> 0 81			
	120	0	81

## Accessing the Data

The data can be accessed from the csv file "challenger-data.csv" via the following function calls:

#### <u>In R</u>:

```
data = read.csv("challenger-data.csv")
```

#### In Python:

We will use the Pandas (and Numpy) libraries to help process the data in Python. Please ensure you have them installed before using the code below.

```
import pandas as pd
import numpy as np
data = pd.read csv("challenger-data.csv")
```

We now have the data readily accessible for further analysis.

# Visualizing the Data

Using our data structure, it is possible to plot the data on a graph. For instance, if we want to plot the frequency of failures at each temperature on a plot, we can do it in the following manner.

#### In R:

```
install.packages('plyr') # we need this package for computing frequency counts Library(plyr)

failures = subset(data, data$Y == 1) # subset of the data for just failures no\_failures = subset(data, data$Y == 0) # subset of the data for no failures

failures\_freq = count(failures, 'X') # count of failures, for each temperature no\_failures\_freq = count(no\_failures, 'X')# count of no failures, for each temperature

plot(no\_failures$X, integer(length(no\_failures$X)), ylim=c(-0.5, 3.5), col='blue', xlab='X:

Temperature', ylab='Number of Failures', pch=19) # plot the no failures first points(failures\_freq$X, failures\_freq$freq, col='red', pch=19) # add the failures
```

#### In Python:

We will be using the Matplotlib library for plotting. Pleas ensure it is installed before proceeding.

```
# subsetting data
failures = data.loc[(data.Y == 1)]
no_failures = data.loc[(data.Y == 0)]
# frequencies
```

```
failures_freq = failures.X.value_counts()#failures.groupby('X')

no_failures_freq = no_failures.X.value_counts()

# plotting

import matplotlib as mpl

from matplotlib import pyplot as plt

plt.scatter(failures_freq.index, failures_freq, c='red', s=40)

plt.scatter(no_failures_freq.index, np.zeros(len(no_failures_freq)), c='blue', s=40)

plt.xlabel('X: Temperature')

plt.ylabel('Number of Failures')

plt.show()
```

## Logistic Regression

We are now ready to use Logistic Regression.

#### In R,

```
model = glm(data\$Y \sim data\$X,family=binomial(link='logit'),data=data) # build the model summary(model) # summarize the model
```

#### In Python,

You will need to have the following libraries installed before proceeding:

```
patsy
statsmodels
from patsy import dmatrices
import statsmodels.discrete.discrete_model as sm

#get the data in correct format
y, X = dmatrices('Y ~ X', data, return_type = 'dataframe')

#build the model
logit = sm.Logit(y, X)
result = logit.fit()

# summarize the model
print result.summary()
```

We now have the model and the summaries should provide the coefficient, intercept, standard errors and p-values.