

## Project 2

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## **Abstract**

Basic knowledge and application of AUCTeX, emacs, ML, and L<sup>A</sup>T<sub>E</sub>X. Beginning to work on natural language translation into ML code, as well as different ways of declaring and building functions. Work presented as relevant in the Exercise Chapters, with full source code included in the Appendices.

**Acknowledgements:** Professors Marvine Hamner, Shiu-Kai Chin, & Susan Older

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# Executive Summary

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Unable to complete parts of report. Partway solution to 5.3.4, problem 5.3.5 not attempted and 6.2.1 incomplete as well. Understand I am falling behind, not sure how to correct but will try some changes in the coming week. Many thanks to Prof. Hamner, and my apologies for missing the posting of the Report Example the first time. This and all subsequent reports should be formatted completely to spec, please call me out if that is not the case. Have used <https://www.overleaf.com> to help mitigate lack of time for classwork. Due to my inability to install software on my work computer, and time spent at work, I do not believe I could complete the required amount of school material without a web-based solution such as this. I especially like the error reports upon compilation, and extensive in-house documentation provided by Overleaf. If a class subscription is available I would highly recommend it for future sessions.

## Exercise 4.6.3

---

### 2.1 Problem Statement

1. In ML, define functions (and test them on examples) corresponding to each function below. For each of the functions, you will define two ML functions,
  - (a) the first using `fn` and `val` to define and name the function, and
  - (b) the other using `fun` to define and name the function.
    - i. A function that takes a 3-tuple of integers  $(x;y;z)$  as input and returns the value corresponding to the sum  $x+y+z$ .
    - ii. A function that takes two integer inputs  $x$  and  $y$  (where  $x$  is supplied first followed by  $y$ ) and returns the boolean value corresponding to  $x \leq y$ .
    - iii. A function that takes two strings  $s1$  and  $s2$  (where  $s1$  is supplied first followed by  $s2$ ) and concatenates them, where  $^{\wedge}$  denotes string concatenation. For example, `"Hi" ^ " there"` results in the string `"Hi there"`.
    - iv. A function that takes two lists  $list1$  and  $list2$  (where  $list1$  comes first) and appends them, where  $@$  denotes list append. For example `[true,false] @ [false, false, false]` results in the list `[true,false,false,false,false]`.
    - v. A function that takes a pair of integers  $(x;y)$  and returns the larger of the two values. You note that the conditional statement `if condition then a else b` returns `a` if `condition` is true, otherwise it returns `b`.
2. Make sure you use pattern matching. For example, suppose the function is  $lx:(ly:2x+y)$ . We would define in ML 1. `val funEx1 = (fn x => (fn y => 2*x + y))`, and 2. `fun funEx2 x y = 2*x + y` As a naming convention, use the names `funA1`, `funA2`, `funB1`, `funB2`, etc.

### 2.2 Relevant Code

```
(*** A ***)
val funA1 = (fn x => (fn y => (fn z => x + y + z)));
fun funA2 x y z = x + y + z;
(***) B (***)
val funB1 = (fn y => (fn x => x < y));
fun funB2 x y = x < y;
(***) C (***)
val funC1 = (fn a => (fn b => a ^ b));
fun funC2 a b = a ^ b;
(***) D (***)
val funD1 = (fn x => (fn y => x @ y));
fun funD2 x y = x @ y;
(***) E (***)
val funE1 = (fn a => (fn b => if a > b then a else b));
fun funE2 a b = if a > b then a else b;
```

## 2.3 Test Cases

```
(*** A ***)
funA1 1 1 1;
funA2 1 1 1;
(***) B (***)
funB1 1 2;
funB2 1 2;
(***) C (***)
funC1 "hi" " you";
funC2 "hi" " you";
(***) D (***)
funD1 [1] [2];
funD2 [1] [2];
(***) E (***)
funE1 7 8;
funE2 7 8;
```

## 2.4 Execution Transcripts

```
# val it = 3: int
> val it = 3: int
> # val it = false: bool
> val it = true: bool
> # val it = "hi you": string
> val it = "hi you": string
> # val it = [1, 2]: int list
> val it = [1, 2]: int list
> # val it = 8: int
> val it = 8: int
```

# Exercise 4.6.4

---

## 3.1 Problem Statement

1. In ML, define a function `listSquares` that when applied to the empty list of integers returns the empty list, and when applied to a non-empty list of integers returns a list where each element is squared. For example, `listSquares [2,3,4]` returns `[4,9,16]`.
2. Define the function using a `let` expression in ML.

## 3.2 Relevant Code

```
fun listSquares arr =  
  let  
    fun sqr x = x * x  
    fun arq [] = [] | arq (x::xs) = sqr x :: arq xs  
    in  
      arq arr  
    end;
```

## 3.3 Test Cases

```
listSquares [1,2];  
listSquares [3,4];
```



# Exercise 5.3.4

---

## 4.1 Problem Statement

1. Define a function `Filter` in ML, whose behavior is identical to `filter`. Note: you cannot use `filter` in the definition of `Filter`. However, you can adapt the definition of `filter` and use it in your definition. Show test cases of your function returning the expected results by comparing the outputs of both `Filter` and `filter`.
2. Your example should include the case  $\lambda x.x < 5$  on `[4, 6]`

## 4.2 Relevant Code

```
fun filt a b = map a b; (* THIS RETURNS THE BOOLS NEEDED *)
fun Filtr proc1 arr =
  let
    val out = []
    fun retr proc2 (z::zs) = if proc2 z then z::out else out :: retr proc2 zs
  in
    retr proc1 arr
  end;
```

## 4.3 Test Cases

```
Filtr (fn x => x < 5) [1,4,6];
```

## 4.4 Execution Transcripts

```
-----
HOL-4 [Kananaskis 13 (stdknl, built Thu Jan 16 23:56:17 2020)]

For introductory HOL help, type: help "hol";
To exit type <Control>-D
-----

> fun filt a b = map a b;
val filt = fn: ('a -> 'b) -> 'a list -> 'b list
> filt (fn x => x < 5) [1,4,6];
val it = [true, true, false]: bool list
> filter (fn x => x < 5) [1,4,6];
val it = [1, 4]: int list
> fun Filtr proc arr =
  let
    fun t# # ru proc arr = map proc arr;
    # fun retr (x::xs) (z::zs) = if x then z :: retr xs zs
  in
    # poly: : error: retr (else expectedtru pro but inc arr) was arr
  end;found
poly: : error: Expression expected but in was found
# #
Static Errors
> fun Filtr proc arr =
  let# t
    fun t# # ru proc arr = map proc arr;
    val# out = []
    fun re# tr (x::xs) (z::zs) = if x then z @ out else out :: retr xs zs
```

```

in
# #      retr (tru proc arr) arr
end;
# poly: : warning: Matches are not exhaustive.
Found near
  fun retr (x :: xs) (... :: ...) = if x then z @ out else out :: ... ..
val Filtr = fn: ('a list list -> bool) -> 'a list list list -> 'a list list
> Filtr (fn x => x < 5) [1,4,6];
poly: : error: Type error in function application.
  Function: Filtr :
    ('a list list -> bool) -> 'a list list list -> 'a list list
  Argument: (fn x => x < 5) : int -> bool
  Reason:
    Can't unify int (*In Basis*) with 'a list list (*In Basis*)
    (Different type constructors)
Found near Filtr (fn x => x < 5) [1, 4, 6]
poly: : error: Type error in function application.
  Function: Filtr (fn x => x < 5) : 'a list list list -> 'a list list
  Argument: [1, 4, 6] : int list
  Reason:
    Can't unify int (*In Basis*) with 'a list list (*In Basis*)
    (Different type constructors)
Found near Filtr (fn x => x < 5) [1, 4, 6]
Static Errors
> Filtr [1,4,6] (fn x => x < 5);
poly: : error: Type error in function application.
  Function: Filtr :
    ('a list list -> bool) -> 'a list list list -> 'a list list
  Argument: [1, 4, 6] : int list
  Reason: Can't unify int list to 'a list list -> bool (Incompatible types)
Found near Filtr [1, 4, 6] (fn x => x < 5)
poly: : error: Type error in function application.
  Function: Filtr [1, 4, 6] : 'a list list list -> 'a list list
  Argument: (fn x => x < 5) : int -> bool
  Reason: Can't unify 'a list list list to int -> bool (Incompatible types)
Found near Filtr [1, 4, 6] (fn x => x < 5)
Static Errors
> fun Filtr proc arr =
le# t
  fun t# ru proc arr = map proc arr;
  val# out = []
  #   fun retr (x::xs) (z::zs) = if x then [z] @ out else out :: retr xs zs
in
  # #   retr (tru proc arr) arr
end;#
poly: : warning: Matches are not exhaustive.
Found near
  fun retr (x :: xs) (... :: ...) = if x then [...] @ out else out :: ... ..
val Filtr = fn: ('a list -> bool) -> 'a list list -> 'a list list
> Filtr (fn x => x < 5) [1,4,6];
poly: : error: Type error in function application.
  Function: Filtr : ('a list -> bool) -> 'a list list -> 'a list list
  Argument: (fn x => x < 5) : int -> bool
  Reason:
    Can't unify int (*In Basis*) with 'a list (*In Basis*)
    (Different type constructors)
Found near Filtr (fn x => x < 5) [1, 4, 6]
poly: : error: Type error in function application.
  Function: Filtr (fn x => x < 5) : 'a list list -> 'a list list
  Argument: [1, 4, 6] : int list
  Reason:
    Can't unify int (*In Basis*) with 'a list (*In Basis*)
    (Different type constructors)
Found near Filtr (fn x => x < 5) [1, 4, 6]
Static Errors
> 1::[2,4];
val it = [1, 2, 4]: int list
> fun Filtr proc arr =
le# t
  fun t# ru proc arr = map proc arr;
  val# out = []
  fun r# etr (x::xs) (z::zs) = if x then z::out else out :: retr xs zs
in
  # #   retr (tru proc arr) arr
end;#
poly: : warning: Matches are not exhaustive.
Found near
  fun retr (x :: xs) (... :: ...) = if x then z :: out else out :: ... ..
val Filtr = fn: ('a list -> bool) -> 'a list list -> 'a list list

```

---

```

> Filtr (fn x => x < 5) [1,4,6];
poly: : error: Type error in function application.
Function: Filtr : ('a list -> bool) -> 'a list list -> 'a list list
Argument: (fn x => x < 5) : int -> bool
Reason:
  Can't unify int (*In Basis*) with 'a list (*In Basis*)
  (Different type constructors)
Found near Filtr (fn x => x < 5) [1, 4, 6]
poly: : error: Type error in function application.
Function: Filtr (fn x => x < 5) : 'a list list -> 'a list list
Argument: [1, 4, 6] : int list
Reason:
  Can't unify int (*In Basis*) with 'a list (*In Basis*)
  (Different type constructors)
Found near Filtr (fn x => x < 5) [1, 4, 6]
Static Errors
> ^[[Cfun Filtr proc1 arr =
lpoly: : error: et
      val unknown characterout = [] "\^[

      fun re# tr proc2# (z::# zs) = if proc2 z then z::out else out :: retr proc2 zs
    in
      #      retr # proc1 arr
    end;#
poly: : error: ] expected but ; was found
Static Errors
> fun Filtr proc1 arr =
let
  val # out = []#
  fun re# tr proc2 (z::zs) = if proc2 z then z::out else out :: retr proc2 zs
in
  #      retr # proc1 arr
end;#
poly: : warning: Matches are not exhaustive.
Found near
  fun retr proc2 (... :: ...) = if proc2 z then z :: out else out :: ... ...
val Filtr = fn: ('a list -> bool) -> 'a list list -> 'a list list
> Filtr (fn x => x < 5) [1,4,6];
poly: : error: Type error in function application.
Function: Filtr : ('a list -> bool) -> 'a list list -> 'a list list
Argument: (fn x => x < 5) : int -> bool
Reason:
  Can't unify int (*In Basis*) with 'a list (*In Basis*)
  (Different type constructors)
Found near Filtr (fn x => x < 5) [1, 4, 6]
poly: : error: Type error in function application.
Function: Filtr (fn x => x < 5) : 'a list list -> 'a list list
Argument: [1, 4, 6] : int list
Reason:
  Can't unify int (*In Basis*) with 'a list (*In Basis*)
  (Different type constructors)
Found near Filtr (fn x => x < 5) [1, 4, 6]
Static Errors
> (fn x => x < 5) 1;
val it = true: bool
> %

```

# Exercise 5.3.5

---

## 5.1 Problem Statement

1. Define an ML function `addPairsGreaterThan n list`, whose behavior is defined as follows:
  - (a) given an integer `n`, and
  - (b) given a list of pairs of integers `list`,
  - (c) `addPairsGreaterThan n list` will return a list of integers where each element is the sum of integer pairs in `list` where both elements of the pairs are greater than `n`.
2. An example session is shown below.

```
addPairsGreaterThan 0 [(0,1),(2,0),(2,3),(4,5)];  
> val it = [5, 9] : int list
```

Hint: the logical operators for negation, conjunction, and disjunction ML are `not`, `andalso`, and `orelse`.

## 5.2 Relevant Code

## 5.3 Test Cases

## 5.4 Execution Transcripts

## Exercise 6.2.1

---

### 6.1 Problem Statement and Results

1. In the following problems, enable HOL's Show types capability and disable Unicode so only ASCII characters are displayed.

- (a) Enter the HOL equivalent of  $P(x) \rightarrow Q(y)$ . Show what HOL returns. What are the types of  $x$ ,  $y$ ,  $P$ , and  $Q$ ?

```
> 'P x ==> Q y';
<<HOL message: inventing new type variable names: 'a, 'b>>
val it = \P x ==> Q y": term
```

- (b) Consider again  $P(x) \rightarrow Q(y)$ . Suppose we wish to constrain  $x$  to HOL type `:num` and  $y$  to HOL type `:bool`. Re-enter your expression corresponding to  $P(x) \rightarrow Q(y)$  and show that the types of  $x$ ,  $y$ ,  $P$ , and  $Q$  are appropriately typed.

```
> 'P x:num ==> Q y:bool';
Type inference failure: unable to infer a type for the application of
$==> :bool -> bool -> bool
roughly on line 6, characters 2-5
to
(P :x -> num) (x :x)
on line 6, characters 2-4
which has type
:num
unification failure message: Attempt to unify different type operators: min$bool and num$num
```

- (c) Enter the HOL equivalent of  $\exists x y. P(x) \rightarrow Q(y)$ , without explicitly specifying types. What do you get and why?
- (d) Enter the HOL equivalent of  $\exists (x : \text{num}). R(x : a)$ . What happens and why?
- (e) Enter the HOL equivalent of  $\exists x. P(x) \rightarrow Q(x) = \exists x. P(x) \rightarrow Q(x)$
- (f) Enter the HOL equivalent of the English sentence, All people are mortal, where  $P(x)$  represents  $x$  is a person and  $M(x)$  represents  $x$  is mortal.
- (g) Enter the HOL equivalent of the English sentence, Some people are funny, where  $\text{Funny}(x)$  denotes  $x$  is funny.

## Source Code for 4.6.3

---

```
(*****)  
(* Exercise 4.6.3 *)  
(* Author: Michael Hrishenko *)  
(* Date: 20JAN2020 *)  
(*****)  
(fn x => (fn y => 2*x + y))1 2; (* EXAMPLE *)  
(*** A ***)  
val funA1 = (fn x => (fn y => (fn z => x + y + z)));  
fun funA2 x y z = x + y + z;  
(*** B ***)  
val funB1 = (fn y => (fn x => x < y));  
fun funB2 x y = x < y;  
(*** C ***)  
val funC1 = (fn a => (fn b => a ^ b));  
fun funC2 a b = a ^ b;  
(*** D ***)  
val funD1 = (fn x => (fn y => x @ y));  
fun funD2 x y = x @ y;  
(*** E ***)  
val funE1 = (fn a => (fn b => if a > b then a else b));  
fun funE2 a b = if a > b then a else b;
```

## Source Code for 4.6.4

---

```
(*****)  
(* Exercise 4.6.4 *)  
(* Author: Michael Hrishenko *)  
(* Date: 20JAN2020 *)  
(*****)  
fun listSquares arr =  
  let  
    fun sqr x = x * x  
    fun arq [] = [] | arq (x::xs) = sqr x :: arq xs  
  in  
    arq arr  
  end;  
  
fun sqr [] = [] | sqr (x::xs) = (x * x) :: sqr xs;
```

## Source Code for 5.3.4

---

```
(*****)  
(* Exercise 5.3.4 *)  
(* Author: Michael Hrishenko *)  
(* Date: 20JAN2020 *)  
(*****)  
fun flt a b = map a b; (* THIS RETURNS THE BOOLS NEEDED *)  
fun Filtr proc1 arr =  
  let  
    val out = []  
    fun retr proc2 (z::zs) = if proc2 z then z::out else out :: retr proc2 zs  
  in  
    retr proc1 arr  
end;
```



## Source Code for 5.3.5

---

## Source Code for 6.2.1

---