

Figure 1: This is a caption for this figure.



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Thanks and recognition go to the following people for their contribution to this project. Professor Shiu-kai Chin for providing me with the opportunity and for his faith in me and my capabilities on this project. Eric Devendhorf at AFRL for making the ABD program happen. Mizra Tihic for making this happen, especially with respect to funding.

To properly acknowledge the contribution of others requires some description of the workflow. The actual work began as a collaboration between the subject matter expert from the United States Army and me, the author of this master thesis. The subject matter expert was Jesse Nathaniel Hall, a Captain [rank?] in the United States Army and also a graduate student in the iSchool (School of Information Science) at Syracuse University. Given the objective of demonstrating CSBD on the patrol base operation (or demonstrating its failure), we collaborated on the Systems Security Engineering (SSE) goals of the project. This work comprised a significant part of this research and is describe in the chapter on Systems Security Engineering. From thereon, the work was divided among the two of us with weekly updates and collaboration to resolve any potential conflicts. Jesse modeled the patrol base operations in Visio based on his interpretations of the patrol base operations in the Ranger Handbook [1]. A diagram of his work was included as a Visio file with this project. In addition, a squished version of this diagram was included in the chapter on the Patrol Base Operations. The result of this work was discussed in this context. On the other hand, I focused on the actual application of CSBD to the model as it was being developed. I continued to work on this aspect of the project after collaboration ceased.

In addition to the work done by Jesse and myself, another student worked with us on the project. This was YiHong Guo, an undergraduate student in the College of Engineering and Computer Science at Syracuse University. He helped us organize the original documentation of this work in LaTeX, a rather large project. (That documentation is separate from this master thesis.)

# Table Of Contents

A	bstra	ct																1
Li	st of	Figure	es															ix
Li	st of	Tables	3															x
Li	st of	Acron	yms															xi
1	Intr	oducti	on															1
	1.1	Motiva	ation															1
		1.1.1	Systems	Are Ev	erywher	re												1
	1.2	This N	Aaster Th	iesis												 •		1
2	Background												2					
	2.1	_	lete Medi	ation .														2
	2.2	_	l Method															2
	2.3		onal Prog															3
	2.4	Higher	Higher Order Logic (HOL) Interactive Theorem Prover															
	2.5	Other	Interactiv	ve Theo	rem Pro	overs												5
	2.6	How to	o Compil	e The Ir	ncluded	Files												5
3	Syst	ems S	ecurity	Engine	ering &	z Pat	rol	Ва	ase	. C	ne	rat	tioi	ıs				6
_	3.1		ystems Pe	_	_						_							6
	3.2	,	Systems Engineering										7					
	3.3		8 8										10					
	3.4		-									10						
	3.5	-	ns Securit	-	_													12
		3.5.1	Problem	ı														13
		3.5.2	Solution															15
		3.5.3	Trustwo															17
	3.6	Trustv	vorthiness	3														17
		3.6.1	Verificat	ion & D	)ocumei	ntatio	n.											18
			3.6.1.1	Verifica	ation .													18
			3.6.1.2	Forma	l Verific	ation												18
			3.6.1.3	Docum	nentatio	n												18
		3.6.2	Reprodu	icibility														18
		3.6.3	Account	ability.														18
		3.6.4	Assuran	ce Clain	ns													18

4 C	ertified	Security by Design (CSBD) & Access-Control Logic (ACL)
4.	1 Certif	ied Security by Design (CSBD)
	4.1.1	Formal Verification & Documentation
	4.1.2	Computer-aided Reasoning
		4.1.2.1 Higher Order Logic (HOL) Interactive Theorem Prover .
	4.1.3	The Principle of Complete Mediation
4.	2 Acces	s-Control Logic (ACL)
	4.2.1	ACL: A Command and Control (C2) Calculus
	4.2.2	Principals
	4.2.3	Propositional Variables, Requests, Authority, and Jurisdiction
	4.2.4	Well-formed Formulas
	4.2.5	Kripke Structure
	4.2.0	4.2.5.1 satisies
		4.2.5.1 satisfies
	4 O C	
	4.2.6	Inference Rules
	4.2.7	Complete mediation
4.	_	in HOL
	4.3.1	Complete Mediation
	4.3.2	satList
	1.75	
		se Operations
5.		ation
5.	O	er Handbook Description
5.		ling the Patrol Base Operations from the Ranger Handbook
5.	4 Overv	iew of The Hierarchy of Secure State Machines
5.	5 Hierai	chy of Secure State Machines
	5.5.1	Diagrammatic Description in Visio
	5.5.2	OMNI-Level
	5.5.3	Escape
	5.5.4	Top Level
	5.5.5	Horizontal Slice
	0.0.0	5.5.5.1 ssmPlanPB
		5.5.5.2 ssmMoveToORP
		5.5.5.3 ssmConductORP
		5.5.5.4 ssmMoveToPB
		5.5.5.5 ssmConductPB
	5.5.6	
	0.6.6	
		5.5.6.1 ssmSecureHalt
		5.5.6.2 ssmORPRecon
		5.5.6.3 ssmMoveToORP4L
		5.5.6.4 ssmFormRT
~	<b>.</b>	, N.C. 1 . N.C. 1 . 1
		ate Machine Model
6.		Machines
	6.1.1	Configuration
	6.1.2	Next-state Function
	6.1.3	Next-output Function
	6.1.4	Transition Commands

	6.2	Secure	State Machines
		6.2.1	State Machine Versus Secure State Machine
		6.2.2	Monitors
		6.2.3	Configuration
		6.2.4	Transition Types
			6.2.4.1 <i>exec</i>
			6.2.4.2 $trap$
			6.2.4.3 discard
		6.2.5	Authentication
		6.2.6	Authorization
	6.3		State Machines in HOL
	0.0	6.3.1	Parameterizable Secure State Machine
		6.3.2	Parameterization
		6.3.3	Configurations: five parts
		0.5.5	6.3.3.1 State Interpretation
			1
			v
			1
			6.3.3.4 State
		C 2 4	6.3.3.5 Output stream
		6.3.4	Configuration Interpretation
		6.3.5	Authentication
		6.3.6	Authorization
		6.3.7	Transition Definitions
7	Pat	rol Bas	se Operations as Secure State Machines 38
•	7.1		3: An Example from the Hierarchy
	1.1	7.1.1	Principals
		7.1.2	States
		7.1.3	Commands
		7.1.4	Next-State Function
		7.1.5	Next-Output Function
		7.1.6	Authentication
		7.1.7	Authorization
		7.1.7	Proved Theorems
		1.1.0	7.1.8.1 Platoon Leader Is Trusted on plCommands
	7.2	Othen	-
	1.2		
		7.2.1	ssmPlanPB: Non-sequential Transitions
		7.2.2	ssmConductORP: Principals Authorized for Subsets of Commands 39
8	Disc	cussion	$_{1}$
	8.1	Recap	
	8.2	1	n Accomplished
	8.3		Gaps, Lessons Learned, & Advice
	8.4	_	Verifiable Theories
	J. 1	8.4.1	Authentication: Roles and Cypto
		8.4.2	Soldier Theory
		8.4.3	Platoon Theory
		8.4.4	Squad And Fire Team Theories
		0.4.4	bquau mu me ream rucones 41

9	Fut	ure Wo	ork & In	nplications	<b>42</b>
	9.1	on T	he Patro	Base Operations	42
	9.2	on (	ther Non	a-automated Human-Centered Systems	42
	9.3			Systems	43
	9.4			ability	43
	9.5			mework of Systems Security Engineering	44
$\mathbf{A}_{\mathbf{J}}$	ppen	dices			45
$\mathbf{A}$	Acc	ess Co	ntrol Lo	gic Theories: Pretty-Printed Theories	46
В	Sec	ure Sta	ate Macl	nine & Patrol Base Operations: Pretty-Printed The	e-
	orie	S			69
$\mathbf{C}$	Sec			nine Theories: HOL Script Files	144
	C.1				144
	C.2	satList	t		149
D				chine Theories Applied to Patrol Base Operation	s:
		_	ot Files		151
	D.1	OMNI	Level .		151
	D.2	escape	eLevel .		152
	D.3	TopLe	vel		152
		D.3.1 D.3.2	0 1	Integrated Theory: Type Definitions ratedDef Theory: Authentication & Authorization Defini-	152
			tions .		154
		D.3.3	ssmPlan	PBIntegrated Theory: Theorems	155
	D.4	Horizo	ntal Slice		159
		D.4.1	ssmPlan	PB	159
				PlanPBType Theory: Type Definitions	159
			D.4.1.2	PlanPBDef Theory: Authentication & Authorization Def-	150
			D 440	initions	159
		D 4.0	D.4.1.3	ssmPlanPB Theory: Theorems	159
		D.4.2		eToORP	159
			D.4.2.1	MoveToORPType Theory: Type Definitions	159
			D.4.2.2	MoveToORPDef Theory: Authentication & Authorization Definitions	159
			D.4.2.3	ssmMoveToORP Theory: Theorems	159
		D.4.3		ductORP	159
		D.4.0	D.4.3.1	ConductORPType Theory: Type Definitions	159 $159$
			D.4.3.1 D.4.3.2	ConductORPDef Theory: Authentication & Authoriza-	109
			D.4.3.2	· · · · · · · · · · · · · · · · · · ·	150
			D 4 2 2	tion Definitions	159
		D 4.4	D.4.3.3	ssmConductORP Theory: Theorems	159
		D.4.4	ssmMov		159
			D.4.4.1	MoveToPBType Theory: Type Definitions	159
			D.4.4.2	MoveToPBDef Theory: Authentication & Authorization	4
			D 4 4 2	Definitions	159
		<b>5</b>	D.4.4.3	ssmMoveToPB Theory: Theorems	159
		D.4.5	ssmCone	ductPB	159

	D.4.5.2	ConductPBType Theory: Type Definitions	
	D.4.0.2	Definitions	159
	D.4.5.3	ssmConductPB Theory: Theorems	159
D 5 Vo			159
		reHalt	159 $159$
D.	D.5.1.1	SecureHaltType Theory: Type Definitions	159 $159$
	D.5.1.1 D.5.1.2	v - v	109
	D.5.1.2	SecureHaltDef Theory: Authentication & Authorization Definitions	150
	D = 1 9		159
D	D.5.1.3	ssmSecureHalt Theory: Theorems	159
D.		PRecon	159
	D.5.2.1	ORPReconType Theory: Type Definitions	159
	D.5.2.2	ORPReconDef Theory: Authentication & Authorization	
		Definitions	159
	D.5.2.3	ssmORPRecon Theory: Theorems	159
D.	5.3  ssmMov	eToORP4L	159
	D.5.3.1	MoveToORP4LType Theory: Type Definitions	159
	D.5.3.2	MoveToORP4LDef Theory: Authentication & Authoriza-	
		tion Definitions	159
	D.5.3.3	ssmMoveToORP4L Theory: Theorems	159
D.	5.4  ssmForm	nRT	159
	D.5.4.1	FormRTType Theory: Type Definitions	159
	D.5.4.2	FormRTDef Theory: Authentication & Authorization Def-	
		initions	159
	D.5.4.3	ssm Form RT Theory: Theorems	159
E Map of	f The File I	Folder Structure	160
Reference	S		161

# List of Figures

1	This is a caption for this figure	]
3.1	Systems security engineering in relation to systems engineering. (Image from NIST Special Publication 800-160: Systems Security Engineering Considerations for a Multidisciplinary Approach in the Engineering of	
3.2	Trustworthy Secure Systems.)	11 13
4.1	Kripke semantics. Image taken from Access Control, Security, and Trust: A Logical Approach[2]	24
4.2	The access-control logic (ACL) inference rules. Image taken from Access Control, Security, and Trust: A Logical Approach[2]	25
4.3	The Controls inference rule. Image taken from Access Control, Security, and Trust: A Logical Approach[2]	25
4.4	The Reps inference rule. Image taken from Access Control, Security, and Trust: A Logical Approach[2]	26
4.5	The Derived Speaks For inference rule. Image taken from Access Control, Security, and Trust: A Logical Approach[2]	26
4.6	The ACL formulas in HOL. Image taken from Access Control, Security, and Trust: A Logical Approach[2]	27
5.1	A diagram of the most abstract level in the hierarchy of secure state ma-	
	chines. Image generated by Jesse Nathaniel as part of the research involved in this master thesis. Shall I get his permission?	30
5.2	Diagrammatic description of patrol base operations as a hierarchy of secure state machines. (Generated by Jesse Nathaniel Hall.)	33

# List of Tables

# List of Acronyms

 $\mathbf{ACL}$  access-control logic.

 $\mathbf{CSBD}$  Certified Security by Design.

 $\mathbf{WFF}$  well-formed formula.

## Chapter 1

#### Introduction

#### 1.1 Motivation

#### 1.1.1 Systems Are Everywhere

#### 1.2 This Master Thesis

This master thesis describes a method for designing secure systems. The method is called Certified Security by Design (CSBD). CSBD has been successfully demonstrated on automated systems such as ... and .... But, until this research, it has not been demonstrated on non-automated, human-centered systems.

Systems span the range of fully automated to fully non-automated. This master thesis focuses on one end of this range: non-automated, human-centered systems.

• The first question addressed in this master thesis is whether CSBD could be successfully applied to non-automated, human-centered systems. This is the

primary objective. An example of a non-automated, human-centered system is the patrol base operations defined in the United States Army Ranger Handbook[1]. Patrol base operations exemplify a non-automated, human-centered system wherein security is critical to mission success. In this master thesis, the results of applying CSBD to patrol base operations is discussed.

- The patrol base operations are also an example of a predefined system. This means that this thesis also addresses the question of whether CSBD could be successfully applied to a pre-designed, non-automated, human-centered system. This is important because many such systems in use today are already designed and implemented. CSBD demonstrates that it can verify and document the security properties of current, in-use systems.
- These thesis describes a hierarchy of secure state machines (SSMs) used to model the patrol base operations. This approach demonstrates that formal methods can be applied to large scale and complicated systems. The hierarchy manages patrol base operations by successful levels of decreasing abstraction. Each level in the hierarchy consists of one or more SSMs. Each SSM is modularized and models one aspect of the patrol base operations at one level of abstraction. The levels and modules are connected together by an OMNI level, all-seeing, principal. Each module only needs to be aware of this OMNI level principal. They do not need to be aware of the details of any other module. With this divide-and-conquer approach, CSBD can be readily applied to large and complicated systems.
- The successful application of CSBD to patrol base operations also suggests its use in combining automation with human-centered systems. The approach employed by this master thesis involves describing the patrol base operations as a hierarchy of secure state machines. This hierarchy has the property that it is easy to demonstrate security properties of the system, which is the goal of CSBD. But, it also has the property that it describes the patrol base operations as a system that is amiable to automation. Such automations of pre-defined non-automated,

human-centered systems could include, for example, accountability systems for tracking supplies and personal.

In the not-so-distant future, the military, in particular, will most likely seek tracking and accountability systems for pre-existing, non-automated military operations. These systems, like all security-sensitive military systems, should be designed according to NIST 800-160 standards. These standards require the formal verification and documentation provided by CSBD and demonstrated in this thesis.

# Chapter 2

# Background

This section aims to provide some background on subjects discussed in this master thesis. These subjects are not directly addressed in other areas of this master thesis. Nevertheless, knowledge of them is either necessary or useful to understanding what follows.

#### 2.1 Complete Mediation

Complete mediation is discussed throughout this master thesis. It is described in this section so as to eliminate the need to repeatedly describe it in the ensuing chapters.

#### 2.2 Formal Methods

(Primary source for this section is [3])

Formal methods are aimed at improving the reliability and correctness of systems[4].

They are applied to all phases of systems engineering. Formal methods employ mathematics to verify desired aspects of a system. Mathematics adds a degree of rigor to the verification process that is amiable to automation.

The primary tools of formal methods are model checking and theorem proving. Model checking typically involves testing all possible states of a system for correctness. For large systems, model checking can be resource intensive. Theorem proving, on the other hand, employs a formal logic to verify that a system satisfies desired properties.

Theorem proving is usually applied to a system after it is modeled (referred to as specification). Theorem proving is typically partially or fully automated. Although, proofs by hand can also be employed.

This master thesis applies formal verification methods to prove the security properties of a system. It uses a formal logic based on modal propositional logic. The logic, called access-control logic (ACL), is implemented in the Higher Order Logic (HOL) Interactive theorem prover. Theorem proving is partially automated.

#### 2.3 Functional Programming

(Primary source for this section is [5])

Functional programing is a style of programming that uses functions to define program behavior. Functional programing is inherently different than procedural or object-oriented programming. These styles of program use procedures or objects and classes to define program behavior. c and Pascal are examples of procedural programming languages. c++ and Java are examples of object-oriented programming languages. Haskell and ML (meta language) are examples of functional programming languages. Functional programming languages are thought to be more pure. They have fewer side effects than procedural or object-oriented programming. They produce fewer

bugs. Functional programming languages are thus considered more reliable. This master thesis relies on the Higher Order Logic (HOL) Interactive theorem prover. HOL is implemented in the functional programming language polyML.

# 2.4 Higher Order Logic (HOL) Interactive Theorem Prover

The Higher Order Logic (HOL) Interactive theorem prover is a proof assistant. HOL has proved to be a very reliable theorem proving system. It is widely trusted in the interactive theorem proving community.

At its core, HOL implements a small set of axioms and a formal logic. All inferences and theorems must be derived from this small set of axioms using the formal logic. Reasoning logically with a small set of axioms contributes to the trustworthiness of the system. The user only has to trust the small set of axioms and the logic (in addition to HOL). Beyond the competence of the programmer, if it can't be proved in HOL then it can be proved.

HOL is a strongly-typed system. This means that data has a predefined type. As in all purely functional programming languages, the type of these data can not change. This adds to the reliability of HOL by preventing side-effect. HOL has several built-in data types. But, the user can also define her own data type. In addition to datatypes, the user can define her own set of axioms and definitions.

With user-defined types, axioms, and definitions, the user can describe a system in HOL and then use HOL's formal logic to prove properties of this system. This is the basis for theorem proving in formal methods.

This master thesis describes an access-control logic (ACL) that is implemented in HOL. Using this ACL, secure state machines (SSMs) are also described in HOL. With the ACL implemented in HOL, this thesis proves security properties of the SMMs. These proofs are considered formal verification of the security properties of the SSMs. As the patrol base operations are modeled as a hierarchy of SSMs, these proofs also provide formal verification of the security properties of the patrol base operations.

#### 2.5 Other Interactive Theorem Provers

#### 2.6 How to Compile The Included Files

## Chapter 3

# Systems Security Engineering & Patrol Base Operations

#### 3.1 The Systems Perspective

A system is a set of interacting and interdependent components that act as a whole to perform some behavior or function. Examples of systems include the human body, socio-political systems, and computer systems.

The patrol base operations satisfy this definition of a system. As a whole, the patrol base operations perform some function(s). This function is described in the Ranger Handbook [1] and discussed in chapter 5. The patrol base operations are comprised of interdependent and interacting components. In general these components are the individual soldiers. But, the way this master thesis defines the patrol base operations, the definition of a component varies.

This master thesis defines the patrol base operations as a system of systems. More specifically, this thesis models the patrol base operations as a hierarchy of secure state machines. Chapter 6 describes SSMs in general. Section 5.3 describes this model of the patrol base operations.

This model presents the patrol base operations as a hierarchy wherein each level of the hierarchy represents a decreasing level of abstraction. At the top and most abstract level, the components are phases of the patrol base operations. These phases commence in a sequential order to achieve the goal of the patrol base operations. Each lower level of the hierarchy is composed of less abstract phases. At each level, the components function sequentially (typically) to achieve the ultimate goal.

This system of systems also contains non-hierarchically defined components. For example, an escape-level component models situations wherein the patrol base operations are aborted. The escape level component is reachable from any component at any level of the hierarchy. Soldiers (as in a soldier model) also function within this system of systems in a non-hierarchical manner. However, the soldier module is not verified using the ACL because of time constraints. Nevertheless, a soldier module is discussed in the Discussions chapter 8 of this thesis.

In this way, the patrol base operations represent a system and are amiable to the systems engineering perspective.

#### 3.2 Systems Engineering

The recognized authoritative standard on systems engineering is ISO/IEC/IEEE 15288 [6]. This document is titled "Systems And Software Engineering–System Life Cycle Processing." A precursor to this standard is ISO/IEC TR 24748 1 [7] titled "Systems And Software Engineering–Life Cycle Management–Part 1: Guide for Life Cycle Management." These are the primary sources for this section.

Systems engineering is an interdisciplinary approach aimed at solving problems involved in the various phases of the life cycle of a system. ISO/IEC/IEEE 15288 and ISO/IEC TR 24748 1 define five major phases of the this life cycle: concept, development, production, utilization, support, and retirement.

This master thesis focuses on the Certified Security by Design (CSBD). The key premise of CSBD is that security should be built into the systems from the start, i.e., the design phase. This is the leading notion in systems engineering and its sub-discipline Systems Security Engineering. It is instructive to see how CSBD and its application to the patrol base operations fits into this framework described by the ISO standards.

Concept The concept phase describes stakeholders and the Concept of Operations (ConOps). Stakeholders are those who have a stake in the system. ConOps are defined in a variety of ways. Wikipedia defines ConOps as "...a document describing the characteristics of a proposed system from the viewpoint of an individual who will use that system [?]. U.S. Air Force Policy Directive 10-28 defines ConOps as "a high level concept whose purpose is to describe operational mission areas, enablers and effects necessary to achieve desired results/outcomes" [8]. ConOps are context specific.

The patrol base operations are already modeled and implemented. The mission areas, enablers, and effects to achieve the desired goal are already in place. The aim for this thesis is to maintain the structure of the patrol base operations and model it in a way that is amiable to verification and documentation of complete mediation.

It is also possible to look at this thesis as the modification of an already in-use systems. For example, an accountability system involving the patrol base operations may require a remodeling of the operations with few, if any, changes in the actual operations themselves. This is discussed in more detail in the Future Works & Implications Chapter in section 9.3.

CSBD in intended to by applied to this phase of the systems engineering process.

**Development** The development stage involves refinement of the ConOps and production of the productions. The development of the patrol base operations took place a long time ago. Regardless, the products for this master thesis are the verification and subsequent documentation of complete mediation.

In an accountability system, for example, the principle of complete mediation verified and documented would be embedded in the implementation of any procedures worked out at this phase of the system life-cycle.

The aim is to model the patrol base operations in a manner that is amiable to verifying specific security properties of the system. Specifically, the patrol base operations must satisfy the property of complete mediation.

But, this thesis does not aim to build a new system. Rather this thesis remodels an existing system. This is necessary because the goal of this thesis is to determine whether or not it is possible to verify the specific security properties on the subclass of systems that we are exploring. Most people would agree that testing a new method on a new system would be unwise. This is why this thesis did not do that.

This approach has the side-effect of also demonstrating CSBDs utility in the life-cycle phase of systems engineering. It follows readily from the news today that many systems are not designed with security in mind. Eliminating already-in-use systems and legacy systems may not always be practical or desirable. Nevertheless, security remains an important aspect of system performance. This, in part, justifies a re-look at (or remodeling of) of an already existing system.

There are additional benefits to systematically modeling the patrol base operations in a way that is amiable to formal verification. This type of thinking provides new insights

and suggests areas for improvement<sup>1</sup>. This is a known benefit. For example, Wikipedia [3] notes that "Sometimes, the motivation for proving the correctness of a system is not the obvious need for reassurance of the correctness of the system, but a desire to understand the system better." A greater understanding of a system applies to all phases of systems engineering.

#### 3.3 NIST Special Publication 800-160

One work in the field of Systems Security Engineering is such a critical component to the field of SSE that it warrants pointing out. The National Institute of Standards and Technology (NIST) defines its mission as such: "To promote U.S. innovation and industrial competitiveness by advancing measurement science, standards, and technology in ways that enhance economic security and improve our quality of life." [9]. As their name suggests, NIST develops standards for various industries of relevance to the nation.

The relevant standard for SSE is NIST Special Publication 800-160 Volumes 1 and 2. The title of volume 1 is "Systems Security Engineering Considerations for a Multidisciplinary Approach in the Engineering of Trustworthy Secure Systems." The title of volume 2 is "Systems Security Engineering Cyber Resiliency Considerations for the Engineering of Trustworthy Secure Systems." These, in particular volume 1, are the primary sources for the following two sections.

<sup>&</sup>lt;sup>1</sup>The subject matter expert who focused on the details of the patrol base operations also noted areas for improvement. He was not available to provide details at the writing of this master thesis.

#### 3.4 Systems Security Engineering

Systems security engineering (SSE) is a sub-discipline of systems engineering. Figure 3.1 shows SSE in relation to systems engineering and other sub-disciplines of SSE. This master thesis falls into one of the Security Specialties in this diagram.

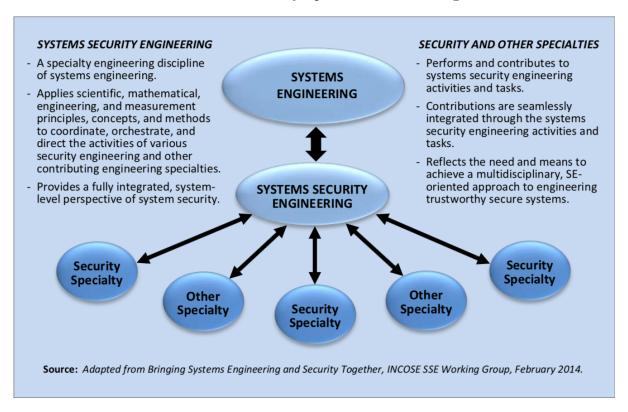


Figure 3.1: Systems security engineering in relation to systems engineering. (Image from NIST Special Publication 800-160: Systems Security Engineering Considerations for a Multidisciplinary Approach in the Engineering of Trustworthy Secure Systems.)

According to NIST Special Publication 800-160, "Systems security engineering focuses on the protection of stakeholder and system assets so as to exercise control over asset loss and the associated consequences." Three key concepts in SSE are stakeholder, asset, and unacceptable losses. In modeling the patrol base operations, this thesis first defines these key concepts.

**Stakeholder** The stakeholder controls the design of the system. The stakeholder defines what the system should do. The stakeholder also defines what the system should not do and what are unacceptable losses. The stakeholder for the patrol

base operations are ultimately the U.S. military. This was critical to the original design of the patrol base operations. But, this thesis has a different purpose, that of demonstrating specific security properties of the patrol base operations using CSBD. These security properties are that of complete mediation. For this master thesis, the stakeholders are everyone involved in this research.

**Asset** An asset is anything that is of value to the stakeholder. In the patrol base operations, this includes soldiers, equipment, and the mission.

Unacceptable losses Unacceptable losses are self-defining. Unacceptable losses for the patrol base operations are defined broadly as any event that would cause the patrol base operation as a whole to abort. These are: contact with the enemy, casualties, a change in mission from higher-up.

It is also a critical objective of SSE to identify and define the security goals of the stakeholder in a way that minimizes asset loss and avoids unacceptable losses. The security properties of the patrol base operations are already built-in to the design of the operations from the Ranger Handbook. These are undoubtedly the result of years of military expertise. Our goal is not to define the security features of the patrol base operations, but to describe them in manner amiable to verification of complete mediation. Identification of assets and unacceptable losses from the Ranger Handbook is sufficient to do this.

To cover the unacceptable losses, this master thesis models an escape-level secure state machine (SSM). If at any phase in the patrol base operations any authenticated principal (i.e., the platoon leader) reports an abortable event, the escape-level SSM will abort the patrol base operations. This includes casualties or unacceptable equipment failure. By creating one escape-level SSM, this thesis creates an modularized yet expandable treatement of unacceptable losses.

To further describe the model of the patrol base operations in the context of SSE, a few

#### 3.5 Systems Security Engineering Framework

NIST 800-160 describes the systems security engineering framework shown in figure 3.2 as "contexts within which systems security engineering activities are conducted." CSBD focuses primarily on demonstrating trustworthiness. Nevertheless, this master thesis also addressed other aspects of the framework.

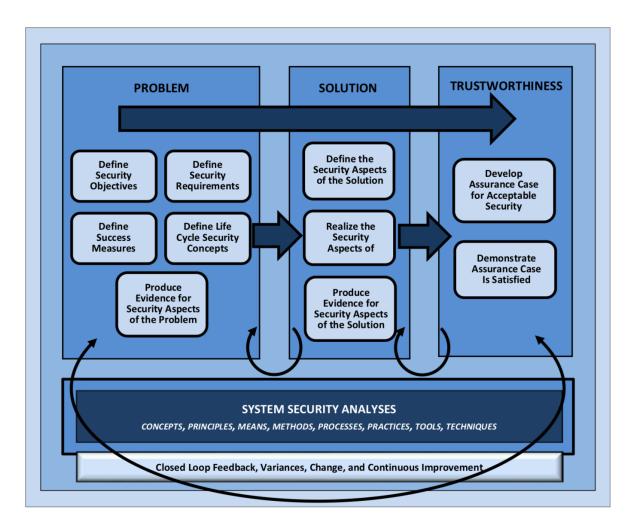


Figure 3.2: Systems security engineering Framework. (Image from NIST Special Publication 800-160: Systems Security Engineering Considerations for a Multidisciplinary Approach in the Engineering of Trustworthy Secure Systems.)

The problem and solution phases for the patrol base operations take a different

approach in the context of this master thesis. It is not our goal to outline the potential security threats and then to find solutions for them. This was, hopefully, already done when the patrol base operations were originally defined. Nonetheless, it is necessary to identify the problem and solution within the patrol base operations in order to verify their security properties.

#### 3.5.1 Problem

The security objective from the perspective of this master thesis is to ensure complete mediation of all actions. Complete mediation requires that we identify objects to be accessed, the accessors, the means of authenticating the accessors, and the a policy for authentication.

The objects to be accessed varies at each level of abstraction. At the top and most abstract level, the objects are the transitions. That is, control over the transitions between phases (or states) of the patrol base operations are to be protected. Objects are defined similarly for each module and at each level for the entire hierarchy of the model. These are deducible from the descriptions of each module (or SSM) in their appropriate section (see section 5.5.2 to start). For the sake of brevity, this section only discusses the top level to illustrate the key concepts.

The accessors are the leaders designated at each level of abstraction. The best way to negotiate access to objects is by the principle of least privilege. This principle assigns privilege to only those who are deemed necessary and to no others. At the top level, the platoon leader (and only the platoon leader) is designated as the accessor. This means that only the platoon leader can issue commands to move-on to the next phase (or state) in the patrol base operations. Some of the other modules have more than one accessor. These accessors are typically assigned privileges to specific objects within the module. The rights of each accessor are determined by the policy.

In the real patrol base operations, soldiers recognize each other by face. Thus, it is sufficient to just authenticate the platoon leader at each level without requiring any passwords or other means of authentication<sup>2</sup>.

Policy is determined for each module and at each level of the patrol base operations model. The model includes not only "who" is authorized to do what, but also what preconditions are necessary prior to authorization. This is more complicated than authentication.

At the top level, there are only two requirements for the patrol base operations to move to the next phase of the operations: (1) the previous phase is complete, and (2) the platoon leader issues the command to move to the next phase. This creates a potential conflict between the goal of modularizing each component and creating a hierarchy wherein each level of the hierarchy expands upon the one above it. In general, If the top level requires some signal from the lower level that it is complete, then these two levels are not independent.

To solve this problem, an OMNI level module is created. The OMNI level module is thought of as all-knowing. This module relays information from all modules as needed. With this construct, the top level does not need to "know" if the lower level module is complete. It only needs to know that the OMNI level says that it is complete. The OMNI level is given the authority to determine when any module is complete.

With this solution in mind, the top level policy looks like this.

if OMNI-Level says the previous phase is complete<sup>3</sup>, and

Platoon Leader says move to the next phase

then Platoon Leader has the authority to move to the next phase

<sup>&</sup>lt;sup>2</sup>The author and subject matter expert discussed authentication in the context of an accountability system wherein passwords or chips were required for authentication. But, we did not implement such authentication techniques in this project.

#### 3.5.2 Solution

The simplest solution to this problem is to model the patrol base operations as a hierarchy of secure state machines (SSM). The hierarchy simplifies the design of the solution by creating decreasing levels of abstraction with multiple modules at each level. This allows for focus on one level and one module at time. This essentially amounts to a system of systems approach. Furthermore, this allows for greater separation of work. After one level of the hierarchy is complete, CSBD is applied to that level while the next level of the hierarchy is being designed.

SSMs are readily defined with complete mediation embedded into their design. SSMs are discussed in detail in Chapter 6. In fact, a parameterizable model of an SSM<sup>4</sup> was already designed and implemented in HOL prior to the start of this project. The constraints of this project suggested Improvements<sup>5</sup> to this parameterizable SSM<sup>6</sup>.

The most useful property of the SSM is that complete mediation is made a condition for transitions among states. That is, to transition from one state to another the accessor (requestor) must be properly authenticated and authorized. Authentication and authorization are described above in the description of the problem. For example, at the top level, transition commands in an SSM look like this.

if Platoon Leader's identity is authenticated, and
Platoon Leader says move to the next phase, and
Platoon Leader has the authority to move to the next phase
then move to the next phase.

 $<sup>^4</sup>$ This SSM was modeled and implemented in HOL by Professor Shiu-kai Chin and used with his permission.

<sup>&</sup>lt;sup>5</sup>Because these improvements were significant, the original author (Professor Shiu-kai Chin) made them.

<sup>&</sup>lt;sup>6</sup>Much to the chagrin of the author, a significant portion of the SSMs had to be redone with the new parameterizable SSM.

The first line ensures authentication of the Platoon Leader. The second line is a request from the Platoon Leader to access the object (i.e., move to the next phase). The third line is the output of a policy as described in the section above and shown in the box above.

Note that this is an "if and only if" conditional. This means that if the Platoon Leader is authenticated, authorized on, and issues the command then the command is executed. It also means the converse. If the command is executed, then the Platoon Leader is authenticated, authorized on, and issues the command to do so.

#### 3.5.3 Trustworthiness

There are two requirement for trustworthiness relevant to this master thesis: (1)

Defining trustworthiness for the purposes of this master thesis, and (2) demonstrating that trustworthiness is achieved. The former is easy for this model. This master thesis focuses on the trustworthiness aspect of SSE. Therefore, this master thesis elaborates on trustworthiness in the following sections.

#### 3.6 Trustworthiness

This master thesis defines trustworthiness in the context of complete mediation<sup>7</sup>. Therefore, a measure of trustworthiness is weather or not the patrol base operations satisfy the properties of complete mediation. There are two aspects to this: (1) building complete mediation into the model of the patrol base operations, and (2) demonstrating that this is indeed the fact.

<sup>&</sup>lt;sup>7</sup>Note that there are certainly other measures of trustworthiness in any system. Nonetheless, the focus of this thesis is to demonstrate CSBD as a viable method for one aspect of the systems security engineering process. The author does not aim to claim that the patrol base operations are deemed trustworthy solely because they satisfy the property of complete mediation. CSBD is one piece of the larger puzzle.

#### 3.6.1 Verification & Documentation

#### 3.6.1.1 Verification

#### 3.6.1.2 Formal Verification

#### 3.6.1.3 Documentation

A common idiom of science and engineering is "if you didn't document it then it didn't happen." There is some leeway in engineering because the presence of a system is indicative that "you did it." However, this hides the important details regarding the security of the system. Maybe "you did it" but "did you do it right?" This is where documentation is important.

"'systems security engineering provides a sufficient base of evidence that supports claims that the desired level of trustworthiness has been achieved..."

#### 3.6.2 Reproducibility

#### 3.6.3 Accountability

Internet Hall of Fame Inductee Vint Cerf commented on the importance of accountability in SSE at a recorded conference in 2016. The conference titled "Exploring the Dimensions of Trustworthiness: Challenges and Opportunities" was presented by NIST.

#### 3.6.4 Assurance Claims

## Chapter 4

Certified Security by Design (CSBD)

&

Access-Control Logic (ACL)

#### 4.1 Certified Security by Design (CSBD)

In 1970 The Rand Corporation published a report[10] for the Office of The Director of Defense Research And Engineering. This report titled, Security Controls For Computer Systems, noted that "Providing satisfactory security controls in a computer system is in itself a system design problem." NIST 800-160 also highlights the importance of incorporating security into the design phase of the system engineering process. CSBD focuses on the design phase of systems engineering, applying formal methods to verify that a system satisfies the principle of complete mediation.

More specifically, CSBD is a method for formally verifying and documenting the security properties of a systems. It focuses on designing systems that satisfy the principle of complete mediation. It uses an access-control logic (ACL) to reason about

access to security sensitive objects of a system. It uses computer-aided reasoning such as the Higher Order Logic (HOL) Interactive theorem prover to formally verify and document these security properties. The outcomes of CSBD applied to a system conform to the guidelines set fourth in NIST 800-160 [verify and discuss this.]

In addition to providing formal proofs that demonstrate satisfiability of complete mediation, CDBD is reproducible. This means that third parties can also verify the formal proofs. This touches on the heart of formal verification of satisfiability: "don't just take my word for it, prove it for yourself."

#### 4.1.1 Formal Verification & Documentation

#### 4.1.2 Computer-aided Reasoning

4.1.2.1 Higher Order Logic (HOL) Interactive Theorem Prover

#### 4.1.3 The Principle of Complete Mediation

#### 4.2 Access-Control Logic (ACL)

#### 4.2.1 ACL: A Command and Control (C2) Calculus

This section discusses the access-control logic in sufficient detail to understand the research reported in this master thesis. The material is adapted from *Access Control*, *Security, and Trust: A Logical Approach*[2]. For more indepth coverage of the ACL, read the text. Any references to "the text" in this section refer to the aforementioned text book.

ACL is a logic for reasoning about access to object. In the jargon of the day it is a command and control (C2) calculus<sup>1</sup>.

#### 4.2.2 Principals

Principals should be thought of as actors in the access-control logic. Principals can make statements or requests. They can be assigned privileges or authority over objects or actions. The text defines allowable principals using the identifier **Princ**:

#### Princ ::= PName / Princ & Princ / Princ | Princ

This is a recursive definition. **PName** refers to the name of a principal (i.e., Jane, PlatoonLeader, sensor1). **Princ & Princ** is read "Princ with Princ" or "Princ and Princ" (i.e., Principal1 with Principal2). **Princ** | **Princ** is read as "Princ quoting Princ" (i.e., Principal1 quoting Principal2).

# 4.2.3 Propositional Variables, Requests, Authority, and Jurisdiction

To reason about access-control and trust, the ACL uses propositional variables, requests, authority, and jurisdiction to make statements.

Propositions in logic are assertions that are either true or false. For example, "I am reading this master thesis" is a proposition because either you are or you are not reading this. Propositional variables are just place holders for propositions. For example, "I am reading something", where the propositional variable "something" is what you are reading.

<sup>&</sup>lt;sup>1</sup>command and control being self-evident and calculus being a method for reasoning

Principals can make requests. In the ACL, principals make requests using the says operator. Requests have the form P says  $\varphi$ , where P represents some principal and  $\varphi$  represents some assertion. For example, PlatoonLeader says platoonHalt. In this example, the Platoon Leader is issuing a command (or request) for the platoon to halt.

Principals can have authority over assertions. In the ACL, authority is conveyed using the *controls* operator. Statements of authority have the form P controls  $\varphi$ , where P represents some principal and  $\varphi$  represents some assertion. For example, PlatoonLeader controls platoonHalt. This example states that the Platoon Leader has the authority to issue the command (or request) for the platoon to halt.

Principals can also have jurisdiction over assertions. Both authority and jurisdiction use the *controls* operator. Statements of jurisdiction have the same form as statements of authority. Statements of authority are typically defined in an organization's policy. Statements of jurisdiction are statements that are readily believed given the context. For example, *PresidentOfUS controls (PlatoonLeader controls platoonHalt)*. In this example, the President of the United States, per the U.S. Constitution, has jurisdiction over the authority invested in the Platoon Leader. In particular, the President of the United States has the jurisdiction to give the Platoon Leader the authority to command her platoon to halt.

In addition, principals can speak for other principals. Principals do this using the *speaks* for operator. The ACL represents the *speaks* for operator with the symbol  $\Rightarrow$ . These types of statements have the form  $P \Rightarrow Q$ , where both P and Q are principals. For example,  $PlatoonLeader \Rightarrow PresidentOfUS$ . This example states that the Platoon Leader speaks for the President of the United States.

#### 4.2.4 Well-formed Formulas

Well-formed formulas (WFFs) are valid statements in the ACL. All statements must be a WFF. The text book defines the set of WFFs using the identifier **Form**:

Form ::= PropVar / ¬ Form / (Form 
$$\vee$$
 Form) / (Form  $\wedge$  Form) / (Form  $\supset$  Form) / (Form  $\equiv$  Form) / (Princ  $\Rightarrow$  Princ) / (Princ says Princ) / (Princ controls Form)

This is a recursive definition.  $\operatorname{PropVar}$  is a propositional variable. The symbols  $\neg$ ,  $\vee$ ,  $\wedge$ ,  $\subset$ , and  $\equiv$  are the standard set and logical symbols. They represent "not", "or", "and", "subset", and "equivalence", respectively. This master thesis primarily reasons with statements (WFFs) of the form  $\operatorname{Princ\ says\ Princ\ }$  and  $\operatorname{Princ\ }$  controls  $\operatorname{Form\ }$ .

#### 4.2.5 Kripke Structure

A Kripke structure deals with three things: worlds, propositions, and principals. The worlds can be thought of as possible states or configurations of some system. Propositions are just statements that are either true or false. And, principals are just actors. A Kripke structure  $\mathcal{M} = \langle W, I, J \rangle$  is defined as a three-tuple consisting of a set

of worlds W, a function I that maps propositions to worlds, and a functions J that maps principals to relations on worlds. A more formal definition is definition 2.1 in the text:

- W is a nonempty set, whose elements are called worlds.
- $I: \mathbf{PropVar} \to \mathcal{P}(W)$  is an interpretation function that maps each propositional variable to a set of worlds.
- $J: \mathbf{PName} \to \mathcal{P}((W \times W) \text{ is a function that maps each principal name to a relation on worlds.}$

$$\mathcal{E}_{\mathcal{M}}\llbracket p \rrbracket \ = \ I(p)$$

$$\mathcal{E}_{\mathcal{M}}\llbracket \neg \varphi \rrbracket \ = \ W - \mathcal{E}_{\mathcal{M}}\llbracket \varphi \rrbracket$$

$$\mathcal{E}_{\mathcal{M}}\llbracket \varphi_1 \wedge \varphi_2 \rrbracket \ = \ \mathcal{E}_{\mathcal{M}}\llbracket \varphi_1 \rrbracket \cap \mathcal{E}_{\mathcal{M}}\llbracket \varphi_2 \rrbracket$$

$$\mathcal{E}_{\mathcal{M}}\llbracket \varphi_1 \vee \varphi_2 \rrbracket \ = \ \mathcal{E}_{\mathcal{M}}\llbracket \varphi_1 \rrbracket \cup \mathcal{E}_{\mathcal{M}}\llbracket \varphi_2 \rrbracket$$

$$\mathcal{E}_{\mathcal{M}}\llbracket \varphi_1 \supset \varphi_2 \rrbracket \ = \ (W - \mathcal{E}_{\mathcal{M}}\llbracket \varphi_1 \rrbracket) \cup \mathcal{E}_{\mathcal{M}}\llbracket \varphi_2 \rrbracket$$

$$\mathcal{E}_{\mathcal{M}}\llbracket \varphi_1 \equiv \varphi_2 \rrbracket \ = \ \mathcal{E}_{\mathcal{M}}\llbracket \varphi_1 \supset \varphi_2 \rrbracket \cap \mathcal{E}_{\mathcal{M}}\llbracket \varphi_2 \supset \varphi_1 \rrbracket$$

$$\mathcal{E}_{\mathcal{M}}\llbracket P \Rightarrow Q \rrbracket \ = \ \begin{cases} W, & \text{if } \hat{J}(Q) \subseteq \hat{J}(P) \\ \emptyset, & \text{otherwise} \end{cases}$$

$$\mathcal{E}_{\mathcal{M}}\llbracket P \text{ says } \varphi \rrbracket \ = \ \{ w | \hat{J}(P)(w) \subseteq \mathcal{E}_{\mathcal{M}}\llbracket \varphi \rrbracket \}$$

$$\mathcal{E}_{\mathcal{M}}\llbracket P \text{ controls } \varphi \rrbracket \ = \ \mathcal{E}_{\mathcal{M}}\llbracket (P \text{ says } \varphi) \supset \varphi \rrbracket$$

$$\mathcal{E}_{\mathcal{M}}\llbracket P \text{ reps } Q \text{ on } \varphi \rrbracket \ = \ \mathcal{E}_{\mathcal{M}}\llbracket (P \mid Q \text{ says } \varphi) \supset Q \text{ says } \varphi \rrbracket$$

Figure 4.1: Kripke semantics. Image taken from  $Access\ Control,\ Security,\ and\ Trust:\ A\ Logical\ Approach[2]$ 

#### **4.2.5.1** satisies

#### 4.2.5.2 soundness

#### 4.2.6 Inference Rules

The inference rules for the access-control logic (ACL) are shown in figure 4.2. All the inference rules are sound. Details of proofs of soundness can be found in *Access Control*, *Security, and Trust: A Logical Approach*[2].

#### 4.2.7 Complete mediation

Fundamental to this work is the concept of complete mediation (discussed in section 4.1.3). In the ACL, this means that each principal must be authenticated and authorized on each request. ACL does this primarily by the *Controls* inference rule in

$$P \operatorname{controls} \varphi \stackrel{\operatorname{def}}{=} (P \operatorname{says} \varphi) \supset \varphi \qquad P \operatorname{reps} Q \operatorname{on} \varphi \stackrel{\operatorname{def}}{=} P \mid Q \operatorname{says} \varphi \supset Q \operatorname{says} \varphi$$

$$Modus \operatorname{Ponens} \stackrel{\varphi}{=} \varphi \supset \varphi' \qquad Says \qquad \frac{\varphi}{P \operatorname{says} \varphi} \qquad Controls \qquad \frac{P \operatorname{controls} \varphi}{\varphi} \qquad P \operatorname{says} \varphi$$

$$Derived \operatorname{Speaks} \operatorname{For} \qquad \frac{P \Rightarrow Q \quad P \operatorname{says} \varphi}{Q \operatorname{says} \varphi} \qquad \operatorname{Reps} \qquad \frac{Q \operatorname{controls} \varphi}{\varphi} \qquad P \operatorname{reps} Q \operatorname{on} \varphi \qquad P \mid Q \operatorname{says} \varphi$$

$$\& \operatorname{Says} (1) \qquad \frac{P \& Q \operatorname{says} \varphi}{P \operatorname{says} \varphi \land Q \operatorname{says} \varphi} \qquad \& \operatorname{Says} (2) \qquad \frac{P \operatorname{says} \varphi \land Q \operatorname{says} \varphi}{P \& Q \operatorname{says} \varphi}$$

$$Quoting (1) \qquad \frac{P \mid Q \operatorname{says} \varphi}{P \operatorname{says} Q \operatorname{says} \varphi} \qquad Quoting (2) \qquad \frac{P \operatorname{says} Q \operatorname{says} \varphi}{P \mid Q \operatorname{says} \varphi}$$

$$Idempotency \ of \Rightarrow \qquad \frac{P \Rightarrow P}{P \Rightarrow P} \qquad Monotonicity \ of \Rightarrow \qquad \frac{P' \Rightarrow P \quad Q' \Rightarrow Q}{P' \mid Q' \Rightarrow P \mid Q}$$

Figure 4.2: The ACL inference rules. Image taken from Access Control, Security, and Trust: A Logical Approach[2]

figure 4.2 and shown again here in figure 4.3.

$$\begin{array}{ccc} Controls & \frac{P \text{ controls } \varphi & P \text{ says } \varphi}{\varphi} \end{array}$$

Figure 4.3: The Controls inference rule. Image taken from  $Access\ Control$ , Security, and Trust:  $A\ Logical\ Approach[2]$ 

ACL refers to the left statement as an authorization<sup>2</sup>. The principal P controls (is authorized on) some action  $\varphi$ . ACL refers to the right statement in this inference rule as a request <sup>3</sup>. The principal P requests some action  $\varphi$ . The conjunction of the authorization and the request of P on  $\varphi$  results in the action  $\varphi$ . That is, if P controls  $\varphi$  and P says  $\varphi$  then  $\varphi$  is true.

The *Controls* rule is sufficient for basic authorization involving one principal and some action. It is the only rule applied in this master thesis. But, there are more complicated rules that allow for additional authentication and authorization schemes.

The Reps (shown in figure 4.4) rule also demonstrates complete mediation. It follows a

<sup>&</sup>lt;sup>2</sup>or a *control* in the C2 calculus

<sup>&</sup>lt;sup>3</sup>or a *command* in the C2 calculus

$$Reps \quad \frac{Q \; \text{controls} \; \varphi \quad P \; \text{reps} \; Q \; \text{on} \; \varphi \quad P \; | \; Q \; \text{says} \; \varphi}{\varphi}$$

Figure 4.4: The Reps inference rule. Image taken from Access Control, Security, and Trust:  $A \ Logical \ Approach[2]$ 

similar logic. But, this rule has two principals, in this case P and Q. The idea is that Q controls (is authorized on) some action  $\varphi$ . And also, P represents Q on that action. In the ACL, this means that P Reps Q on  $\varphi$ . Thus, P says  $\varphi$  is irrelevant because P does not have authority on  $\varphi$ . But,  $P \mid Q$  says  $\varphi$  (short for, P says Q says  $\varphi$ ) is relevant because P represents Q and Q has authority. Spelled out, the rule follows as such: if Q controls  $\varphi$  and P reps Q on  $\varphi$  and  $P \mid Q$  on  $\varphi$  then  $\varphi$  is true.

The *Reps* rule represents a principal acting in a role. For example, soldier G.I. Jane may be acting as the Platoon Leader. In this situation, it is the Platoon Leader (Q) who is granted authority over the action  $\varphi$ . But, it is G.I.Jane (P) acting in the role of Platoon Leader who (Q) is actually issuing the command  $\varphi$ .

Figure 4.5: The *Derived Speaks For* inference rule. Image taken from *Access Control*, *Security*, and *Trust: A Logical Approach*[2]

The Derived Speaks For rule also allows for variation in authentication and authorization. This rule is shown in figure 4.5. This also uses two principals and deals mainly with the concept of jurisdiction and authentication. In this case, the principal P is "speaking for" the principal Q. Again, the symbol  $\Rightarrow$  means "speaks for." Thus, if  $P \Rightarrow Q$  and P says  $\varphi$  then we believe that Q says  $\varphi$ .

The most common use of the *Derived Speaks For* rule is in jurisdictional case. For example, the United States Army has jurisdiction over who serves in the role of Platoon Leader. The U.S. Army may, in turn, issue i.d. cards with a soldier's photo (or in the

future chips) that say, for example, soldier G.I.Jane is who the she says she is. If we believe the i.d. card is genuine and it belongs to G.I.Jane, then the i.d. card speaks for G.I.Jane. So, if the i.d. card says issue G.I.Jane her equipment, then it follows that G.I. Jane says to issue her the equipment. It is somewhat more complicated, because the U.S. Army has jurisdiction over who gets what equipment. The i.d. card is not saying that G.I.Jane has control over her equipment. It only says that she is asking for the equipment.

The *Derived Speaks For* rule is critical to authentication, whereas the *Controls* and *Reps* rules are critical for authentication.

#### 4.3 ACL in HOL

The equivalence of the ACL formulas implemented in HOL are shown in figure 4.6.

Access-Control Logic Formula	HOL Syntax
$\langle jump \rangle$	prop jump
$\neg \langle jump \rangle$	notf (prop jump)
$\langle run \rangle \wedge \langle jump \rangle$	prop run andf prop jump
$\langle run \rangle \vee \langle stop \rangle$	prop run orf prop stop
$\langle run \rangle \supset \langle jump \rangle$	prop run impf prop jump
$\langle walk \rangle \equiv \langle stop \rangle$	prop walk eqf prop stop
$Alice \text{ says } \langle jump \rangle$	Name Alice says prop jump
$Alice \& Bob $ says $\langle stop \rangle$	Name Alice meet Name Bob says prop stop
$Bob \mid Carol \text{ says } \langle run \rangle$	Name Bob quoting Name Carol says prop run
$Bob$ controls $\langle walk \rangle$	Name Bob controls prop walk
$Bob$ reps $Alice$ on $\langle jump \rangle$	reps (Name Bob) (Name Alice) (prop jump)
$Carol \Rightarrow Bob$	Name Carol speaks_for Name Bob

Figure 4.6: The ACL formulas in HOL. Image taken from  $Access\ Control,\ Security,\ and\ Trust:\ A\ Logical\ Approach[2]$ 

Using this syntax, an ACL request of the form P says  $\varphi$  would have the form  $Name\ P\ says\ prop\ \varphi$ 

- 4.3.1 Complete Mediation
- 4.3.2 satList

## Patrol Base Operations

#### 5.1 Motivation

### 5.2 Ranger Handbook Description

# 5.3 Modeling the Patrol Base Operations from the Ranger Handbook

Modeling a system requires the knowledge of an expert on the system. This is necessary because only someone who is familiar with the system, especially with regards to security, can detail its nuances. For this reason, a subject matter expert from the United States Army (Jesse Nathaniel Hall) is employed to develop a model of the patrol base operations.

The model of the patrol base operations needs to be amiable to complete mediation and verification using an access-control logic (section 4.2). This is necessary to prove

security properties of the patrol base operations. To do this, the patrol base operations are abstracted from the Ranger Manual and modeled in Visio<sup>1</sup>. The result of doing this is a hierarchy of secure state machines (SSMs). (SSMs are described in section 6.2.)

# 5.4 Overview of The Hierarchy of Secure State Machines

Each level of the hierarchy of SSMs represents a level of abstraction of the patrol base operations. The most abstract level of the hierarchy is the top level SSM. A diagram of this most abstract level is shown in figure 5.1.

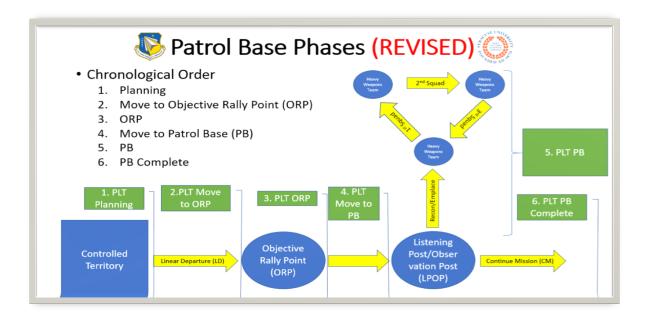


Figure 5.1: A diagram of the most abstract level in the hierarchy of secure state machines. Image generated by Jesse Nathaniel as part of the research involved in this master thesis. Shall I get his permission?

The diagram describes a chronological order of abstract phases (modeled as states) of

<sup>&</sup>lt;sup>1</sup>This work began as a collaboration between Jesse Nathaniel Hall and the author. Once the hierarchy of secure state machines was decided upon, the abstraction of the Ranger Handbook was done by Jesse Nathaniel Hall with only structural consultation with the author. Concurrently, the author focused on proving the properties of complete mediation in the ACL using HOL. Thus, there was a great deal of separation of work. Jesse's work is described here because it is necessary to put the entire system into context for this master thesis. This means that Jesse's work provided the model of the system for which the principle of complete mediation was proved, verified and documented.

the patrol base operations. The operations begin with the planning phase (1). Next, they move to the objective rally point (ORP) (2). At the ORP, operations commence (3). When these are complete, the patrol base operations move to the actual patrol base (4). At the patrol base, operations proceed (5). Finally, the patrol base operations are complete (6). These are the six states in the top level SSM.

The next level of abstraction in the hierarchy of SSMs represents a horizontal slice through the patrol base operations. This is the second level of the hierarchical description of the patrol base operations. It is referred to as the sub-level. In this documentation, SSMs at this level are referred to as the sub-level, sublevel, or sub-level SSMs. This slice describes the patrol base operations at a lower level of abstraction. It expands each of the states in the top level (except for the last state PB Complete). For example, the planning phase (1) in figure 5.1 is expanded into an SSM of its own. This is called ssmPlanPB. It consists of several states (see section 5.5.5.1) which detail activities conducted during the planning phase of the patrol base operations. Each state in the top level (except for PB Complete) has it's own SSM (see the next section).

At yet another lower level of abstraction is the sub-sub (3rd) level. In this documentation, SSMs at this level are referred to as the sub-sub-level, subsublevel, or subsubLevel SSMs. This level expands upon the states in the sub level (one level above) in the same manner that the sub level expands upon the states in the top level SSM. In this manner, each level is a lower level of abstraction than the level above it.

A vertical slice through the diagram is also modeled. This slice models the patrol base operations from the top level down to the most detailed level (level 8). This vertical slice consists of a series of SSMs. Each SSM expands upon only one state in the level above it. This differs from the horizontal slice which expands upon all states in the level above it. Expanding upon only one state focuses on a vertical slice through all 8 states of the hierarchy of SSMs.

The vertical slice begins at the top level SSM. Next, it expands upon one state at this level, the move to ORP state (2). This results in a sub level SSM named ssmMoveToORP. The vertical slice progresses in this manner, by expanding one state at each level into a new SSM. From ssmMoveToORP, the state secure halt is expanded to ssmSecureHalt. From within this SSM, the state ORP Recon is expanded into ssmORPRecon. From within this SSM, the state Move to ORP 4L (fourth level move to ORP state) is expanded into ssmMoveToORP4L. Finally, from within this SSM, the state Form RT is expanded into ssmFormRT.

The vertical slice spans the all eight levels. However, not all levels are represented with an SSM. The last SSM in the vertical slice, ssmFormRT, is actually at the 5th level of the hierarchy. This SSM, consists of three states. These three states reside at the 7th level because ssmFormRT does not have states at the 6th level (it skips the 6th level). Furthermore, the 7th level states are not expanded into an SSM because each of these 7th level states expand into only one state at the 8th level.

In addition to the horizontal and vertical slices, an escape level is also modeled. Actions in the escape level are reachable from any phase of the patrol base operations. These actions are the unacceptable circumstances that require the patrol base operations to abort. For example, if the patrol base contacts the enemy in any phase of the operations, then the command *react to combat* is issued. The patrol base operations are subsequently aborted.

Excluding the escape level, there are eight levels of the hierarchy of SSMs.

Note that, the purpose of this master thesis is to demonstrate that the properties of complete mediation could be applied and verified on a non-automated, human-centered systems. Thus, it is sufficient to demonstrate this on a horizontal and vertical slice of the patrol base operations.

#### 5.5 Hierarchy of Secure State Machines



Figure 5.2: Diagrammatic description of patrol base operations as a hierarchy of secure state machines. (Generated by Jesse Nathaniel Hall.)

#### 5.5.1 Diagrammatic Description in Visio

The enormity of the hierarchy of SSMs is evident in figure 5.2. This is a squashed version of the Visio diagram for the hierarchy of SSMs. The diagram is included as a Visio file with the files for this project (LaTeX/figures/diagram.vis).

The straight, colored lines that span the diagram in figure 5.2 delineate levels of the hierarchy of SSMs. The top lines are obscured by the size of this squashed version of the diagram. The most visible bright yellow line delineates the sub-sub-sub (4th) level of the hierarchy, for example.

The small, colored dots in figure 5.2 represent states (phases) of the patrol base operations. The red dots are an exception. The labels for these states are not readable in this diagram. The dots are color coded. The colors correspond to the level of those states. For example, the dots at the top level (level below the red dots) are all dark blue.

In figure 5.2, the red dots at the top of the diagram represent the escape level SSM.

But, they do not represent states in the SSM. This is because the escape level SSM is accessible by all phases of the patrol base operations. This means that if can not be ascribed to any one level of the hierarchy.

The dots representing states are connected to each other by lines. These lines represent allowable transitions from one state to another. The escape level is again an exception. If no line connects one state to another then no transition is allowed.

The red dots representing the escape level SSM are best thought of as multiple copies of a floating SSM. The escape level SSM acts as a sub-SSM for all SSMs in the hierarchy. During patrol base operations, abortion of the patrol base operations can occur at any action from any state at any level. This means that any state at any level can be terminated by the escape level SSM. Drawing lines from all states to the escape level SSM and drawing really long lines clutters the diagram. Therefore, only lines at the top level are drawn and the red dots are duplicated.

The lines in the diagram are annotated by SSM requests. (Annotations are visible in the original Visio diagram, but not in this squashed version.) For example, a line connecting the top level state PLAN\_PB is annotated with the request *PlatoonLeader says crossLD*. crossLD is an abbreviation for "cross the line of discrimination" and it is the command to transition to the MOVE\_TO\_ORP state. Lines are not annotated beyond the sub level.

Details of each level follow in the next section.

5.5.2 OMNI-Level 5.5.3 Escape 5.5.4 Top Level 5.5.5 Horizontal Slice 5.5.5.1 ssmPlanPB 5.5.5.2 ssmMoveToORP 5.5.5.3 ssmConductORP 5.5.5.4 ssmMoveToPB 5.5.5.5 ssmConductPB 5.5.6 Vertical Slice 5.5.6.1 ssmSecureHalt 5.5.6.2 ssmORPRecon 5.5.6.3 ssmMoveToORP4L

5.5.6.4 ssmFormRT

## Secure State Machine Model

6.1	State	$M_{20}$	hinos
(). I	State	IVIAC	mmes

- 6.1.1 Configuration
- 6.1.2 Next-state Function
- 6.1.3 Next-output Function
- 6.1.4 Transition Commands
- 6.2 Secure State Machines
- 6.2.1 State Machine Versus Secure State Machine
- 6.2.2 Monitors

# Patrol Base Operations as Secure State Machines

- 7.1 ssmPB: An Example from the Hierarchy
- 7.1.1 Principals
- **7.1.2** States
- 7.1.3 Commands
- 7.1.4 Next-State Function
- 7.1.5 Next-Output Function
- 7.1.6 Authentication

### Discussion

- 8.1 Recap
- 8.2 Mission Accomplished
- 8.3 Stop-Gaps, Lessons Learned, & Advice
- 8.4 Other Verifiable Theories

There were other modules and complexities in the patrol base operations that were discussed during the course of the work. However, because of time constraints they were no verified in the ACL and HOL.

#### 8.4.1 Authentication: Roles and Cypto

This master thesis discussed authentication as a visual confirmation among the soldiers. For example, most often, most soldiers in a platoon know who their platoon leader is and do not require a password. But, this is not always the case. One example where it may not be readily obvious is when the platoon leader has been incapacitated and can no longer function in that role. The military has a clearly defined succession hierarchy and soldier are (or should be) aware of this. But, computers aren't as smart as soldiers...unless they are designed to be so. In this case, the concept of soldiers acting in roles is useful.

The idea behind defining the platoon leader as the authorized principal in, for example, the top level SSM allows for the system to work regardless of who the platoon leader is. Nevertheless, it is the soldier acting in the role of the platoon leader who is actually authorized. This can also be represented in the SSM model. In fact, a parametrizable SSM is already designed and implemented in HOL to do this.

In this model, the reps rule from figure 4.2 does this.

#### 8.4.2 Soldier Theory

#### 8.4.3 Platoon Theory

#### 8.4.4 Squad And Fire Team Theories

## Future Work & Implications

### 9.1 ...on The Patrol Base Operations

# 9.2 ...on Other Non-automated Human-Centered Systems

Emergency Management systems require human communications. As with most systems of communication, the communicators need to work with the confidence that they are receiving instructions from the right source with the right authority. A remodeling of the system with complete mediation in mind. From the work in this thesis, the system could simply be modeled in a way that highlights communication avenues and applies CSBD to verify complete mediation.

On perhaps a smaller scale, but no less significant, are non-automated, human-centered school drills such as fire drills and active shooter drills. Clearly, a systems engineering approach could be used to model these drills. The systems security engineering aspect

would cover things such as verifying that safety zones are assigned and reasonably accessible, "what to do if" scenarios problems are discussed and solved, and who to trust under what circumstances are solved. Complete mediation would be intertwined within this system design. For example, when should students leave their classrooms after lock-down? Who says so? How do you know if that person is trust worthy? If its the teacher or a police officer, then authentication is typically a matter of visual recognition as it is with authentication in the patrol base operations. Regardless of how these are decided, these things should be decided during the design phase of the drill and the concepts of complete mediation should be built-in to the design.

#### 9.3 Accountability Systems

### 9.4 Further Applicability

Thinking about complete mediation should accompany any system design, big or small. For example, parents often sends their child(ren) to school with instructions to come home safely. But, what does that mean. By thinking about complete mediation, the parents should ask some important questions. Many of these questions and answers involve concepts of complete mediation. Does the bus driver have the authority to drive you home on the bus? How do you recognize this bus from the wrong bus? Does a stranger have the authority to pick your child(ren) up from school? If so, under what circumstances? An emergency? How do you know that this stranger really is a friend of your parents? A key word? A note from your mom?

# 9.5 The Bigger Framework of Systems Security Engineering

The span of manmade systems.

# Appendices

# Appendix A

Access Control Logic Theories: Pretty-Printed Theories

### Contents

1	aclfoundation Theory	3
	aclfoundation Theory 1.1 Datatypes	3
	1.2 Definitions	3
	1.3 Theorems	4
<b>2</b>	aclsemantics Theory	6
	aclsemantics Theory 2.1 Definitions	
	2.2 Theorems	8
3	aclrules Theory	10
	aclrules Theory 3.1 Definitions	11
	3.2 Theorems	11
4	aclDrules Theory	17
	4.1 Theorems	17

#### 1 aclfoundation Theory

Built: 25 February 2018

Parent Theories: indexedLists, patternMatches

#### 1.1 Datatypes

```
Form =
    TT
  | FF
  | prop 'aavar
  | notf (('aavar, 'apn, 'il, 'sl) Form)
  | (andf) (('aavar, 'apn, 'il, 'sl) Form)
           (('aavar, 'apn, 'il, 'sl) Form)
  | (orf) (('aavar, 'apn, 'il, 'sl) Form)
          (('aavar, 'apn, 'il, 'sl) Form)
  | (impf) (('aavar, 'apn, 'il, 'sl) Form)
           (('aavar, 'apn, 'il, 'sl) Form)
  | (eqf) (('aavar, 'apn, 'il, 'sl) Form)
          (('aavar, 'apn, 'il, 'sl) Form)
  | (says) ('apn Princ) (('aavar, 'apn, 'il, 'sl) Form)
  | (speaks_for) ('apn Princ) ('apn Princ)
  | (controls) ('apn Princ) (('aavar, 'apn, 'il, 'sl) Form)
  | reps ('apn Princ) ('apn Princ)
         (('aavar, 'apn, 'il, 'sl) Form)
  | (domi) (('apn, 'il) IntLevel) (('apn, 'il) IntLevel)
  | (eqi) (('apn, 'il) IntLevel) (('apn, 'il) IntLevel)
  | (doms) (('apn, 'sl) SecLevel) (('apn, 'sl) SecLevel)
  | (eqs) (('apn, 'sl) SecLevel) (('apn, 'sl) SecLevel)
  | (eqn) num num
  | (lte) num num
  | (lt) num num
Kripke =
    KS ('aavar -> 'aaworld -> bool)
       ('apn -> 'aaworld -> 'aaworld -> bool) ('apn -> 'il)
       ('apn -> 'sl)
Princ =
   Name 'apn
  | (meet) ('apn Princ) ('apn Princ)
  | (quoting) ('apn Princ) ('apn Princ);
IntLevel = iLab 'il | il 'apn ;
SecLevel = sLab 'sl | sl 'apn
```

#### 1.2 Definitions

```
[imapKS_def]
  \vdash \forall \mathit{Intp} \ \mathit{Jfn} \ \mathit{ilmap} \ \mathit{slmap}.
        imapKS (KS Intp Jfn ilmap slmap) = ilmap
[intpKS_def]
  \vdash \ \forall \mathit{Intp} \ \mathit{Jfn} \ \mathit{ilmap} \ \mathit{slmap}.
        intpKS (KS Intp Jfn ilmap slmap) = Intp
[jKS_def]
 \vdash \forall Intp \ Jfn \ ilmap \ slmap. jKS (KS Intp \ Jfn \ ilmap \ slmap) = Jfn
[01_def]
 ⊢ 01 = PO one_weakorder
[one_weakorder_def]
 \vdash \forall x \ y. \ \text{one\_weakorder} \ x \ y \iff \mathtt{T}
[po_TY_DEF]
 \vdash \exists \mathit{rep}. TYPE_DEFINITION WeakOrder \mathit{rep}
[po_tybij]
 \vdash (\forall a. PO (repPO a) = a) \land
     \forall r. WeakOrder r \iff (repPO (PO r) = r)
[prod_PO_def]
  \vdash \forall PO_1 \ PO_2.
        prod_PO PO_1 PO_2 = PO (RPROD (repPO PO_1) (repPO PO_2))
[smapKS_def]
  \vdash \forall Intp \ Jfn \ ilmap \ slmap.
        smapKS (KS Intp Jfn ilmap slmap) = slmap
[Subset_PO_def]
 \vdash Subset_P0 = P0 (\subseteq)
1.3 Theorems
[abs_po11]
  \vdash \forall r \ r'.
        \texttt{WeakOrder} \ r \ \Rightarrow \ \texttt{WeakOrder} \ r' \ \Rightarrow \ \texttt{((PO} \ r \ \texttt{=} \ \texttt{PO} \ r') \ \Longleftrightarrow \ (r \ \texttt{=} \ r'))
[absPO_fn_onto]
 \vdash \ \forall \, a . \ \exists \, r . \ (a = \texttt{PO} \ r) \ \land \ \texttt{WeakOrder} \ r
```

```
[antisym_prod_antisym]
 \vdash \forall r \ s.
       antisymmetric r \wedge \text{antisymmetric } s \Rightarrow
       antisymmetric (RPROD r s)
[EQ_WeakOrder]
 ⊢ WeakOrder (=)
[KS_bij]
 \vdash \forall M. M = KS \text{ (intpKS } M) \text{ (jKS } M) \text{ (imapKS } M) \text{ (smapKS } M)
[one_weakorder_WO]
 ⊢ WeakOrder one_weakorder
[onto_po]
 \vdash \ \forall \, r. WeakOrder r \iff \exists \, a. r = repPO a
[po_bij]
 \vdash (\forall a. PO (repPO a) = a) \land
    \forall r. WeakOrder r \iff (repPO (PO r) = r)
[PO_repPO]
 \vdash \forall a. \ PO \ (repPO \ a) = a
[refl_prod_refl]
 \vdash \ \forall \, r \ s. reflexive r \ \land reflexive s \ \Rightarrow reflexive (RPROD r \ s)
[repPO_iPO_partial_order]
 \vdash (\forall x. repPO iPO x x) \land
     (\forall x \ y. \ \texttt{repPO} \ iPO \ x \ y \ \land \ \texttt{repPO} \ iPO \ y \ x \ \Rightarrow \ (x = y)) \ \land
    \forall x \ y \ z. repPO iPO \ x \ y \ \land repPO iPO \ y \ z \Rightarrow repPO iPO \ x \ z
[repP0_01]
 ⊢ repPO 01 = one_weakorder
[repPO_prod_PO]
 \vdash \forall po_1 po_2.
       repPO (prod_PO po_1 po_2) = RPROD (repPO po_1) (repPO po_2)
[repPO_Subset_PO]
 \vdash repPO Subset_PO = (\subseteq)
[RPROD_THM]
 \vdash \forall r \ s \ a \ b.
       RPROD r s a b \iff r (FST a) (FST b) \wedge s (SND a) (SND b)
```

```
[SUBSET\_WO] \\ \vdash WeakOrder (\subseteq) \\ [trans\_prod\_trans] \\ \vdash \forall r \ s. \ transitive \ r \land transitive \ s \Rightarrow transitive \ (RPROD \ r \ s) \\ [WeakOrder\_Exists] \\ \vdash \exists R. \ WeakOrder \ R \\ [WO\_prod\_WO] \\ \vdash \forall r \ s. \ WeakOrder \ r \land WeakOrder \ s \Rightarrow WeakOrder \ (RPROD \ r \ s) \\ [WO\_repPO] \\ \vdash \forall r. \ WeakOrder \ r \iff (repPO \ (PO \ r) = r) \\
```

#### 2 aclsemantics Theory

Built: 25 February 2018

Parent Theories: aclfoundation

#### 2.1 Definitions

```
[Efn_def]
 \vdash (\forall Oi \ Os \ M. Efn Oi \ Os \ M TT = \mathcal{U}(:,v)) \land
     (\forall Oi \ Os \ M. \ Efn \ Oi \ Os \ M \ FF = \{\}) \land
     (\forall~Oi~Os~M~p. Efn Oi~Os~M (prop p) = intpKS M~p) \land
     (\forall Oi \ Os \ M \ f.
         Efn Oi\ Os\ M (notf f) = \mathcal{U}(:'v) DIFF Efn Oi\ Os\ M f) \land
     (\forall Oi \ Os \ M \ f_1 \ f_2.
         Efn Oi Os M (f_1 and f_2) =
         Efn Oi Os M f_1 \cap Efn Oi Os M f_2) \wedge
     (\forall Oi \ Os \ M \ f_1 \ f_2.
         Efn Oi Os M (f_1 orf f_2) =
         Efn Oi Os M f_1 \cup Efn Oi Os M f_2) \wedge
     (\forall Oi \ Os \ M \ f_1 \ f_2.
         Efn Oi Os M (f_1 \text{ impf } f_2) =
         \mathcal{U}(:, v) DIFF Efn Oi\ Os\ M\ f_1\ \cup Efn Oi\ Os\ M\ f_2)\ \wedge
     (\forall Oi \ Os \ M \ f_1 \ f_2.
         Efn Oi Os M (f_1 eqf f_2) =
         (\mathcal{U}(:\,\,{}^{\backprime}\mathtt{v}) DIFF Efn Oi\ Os\ M\ f_1\ \cup Efn Oi\ Os\ M\ f_2) \cap
         (\mathcal{U}(:, v) DIFF Efn Oi\ Os\ M\ f_2\ \cup Efn Oi\ Os\ M\ f_1)) \wedge
     (\forall Oi \ Os \ M \ P \ f.
         Efn Oi\ Os\ M\ (P\ says\ f) =
         \{w \mid \text{Jext (jKS } M) \mid P \mid w \subseteq \text{Efn } Oi \mid Os \mid M \mid f\} \}) \land 
     (\forall Oi \ Os \ M \ P \ Q.
         Efn Oi\ Os\ M (P speaks_for Q) =
```

```
if Jext (jKS M) Q RSUBSET Jext (jKS M) P then \mathcal{U}(:'v)
         else { }) \ \
     (\forall Oi \ Os \ M \ P \ f.
         Efn Oi\ Os\ M (P controls f) =
         \mathcal{U}(: `v) DIFF \{w \mid \text{Jext (jKS } M) \mid P \mid w \subseteq \text{Efn } Oi \mid Os \mid M \mid f\} \cup \mathcal{U}(: `v)
         Efn Oi Os M f) \land
     (\forall Oi \ Os \ M \ P \ Q \ f.
         Efn Oi\ Os\ M (reps P\ Q\ f) =
         \mathcal{U}(:,v) DIFF
         \{w \mid \text{Jext (jKS } M) \mid (P \text{ quoting } Q) \mid w \subseteq \text{Efn } Oi \mid Os \mid M \mid f\} \cup G
         \{w \mid \text{Jext (jKS } M) \mid Q \mid w \subseteq \text{Efn } Oi \mid Os \mid M \mid f\} \}
     (\forall Oi \ Os \ M \ intl_1 \ intl_2.
         Efn Oi \ Os \ M \ (intl_1 \ domi \ intl_2) =
         if repPO Oi (Lifn M intl_2) (Lifn M intl_1) then \mathcal{U}(:,v)
         else { }) \ \
     (\forall Oi \ Os \ M \ intl_2 \ intl_1.
         Efn Oi \ Os \ M \ (intl_2 \ eqi \ intl_1) =
         (if repPO Oi (Lifn M intl_2) (Lifn M intl_1) then \mathcal{U}(:,v)
          else { }) ∩
         if repPO Oi (Lifn M intl_1) (Lifn M intl_2) then \mathcal{U}(:,v)
         else { }) \
     (\forall Oi \ Os \ M \ secl_1 \ secl_2.
         Efn Oi Os M (secl_1 doms secl_2) =
         if repPO Os (Lsfn M secl_2) (Lsfn M secl_1) then \mathcal{U}(:,v)
         else { }) \ \
     (\forall Oi \ Os \ M \ secl_2 \ secl_1.
         Efn Oi\ Os\ M\ (secl_2\ eqs\ secl_1) =
         (if repPO Os (Lsfn M secl_2) (Lsfn M secl_1) then \mathcal{U}(:,v)
          else { }) ∩
         if repPO Os (Lsfn M secl_1) (Lsfn M secl_2) then \mathcal{U}(:,v)
         else { }) \ \
     (\forall Oi \ Os \ M \ numExp_1 \ numExp_2.
         Efn Oi\ Os\ M\ (numExp_1\ eqn\ numExp_2) =
         if numExp_1 = numExp_2 then \mathcal{U}(:,v) else \{\}) \land
     (\forall Oi \ Os \ M \ numExp_1 \ numExp_2.
         Efn Oi\ Os\ M\ (numExp_1\ lte\ numExp_2) =
         if numExp_1 \leq numExp_2 then \mathcal{U}(:'v) else \{\}) \land
     \forall Oi \ Os \ M \ numExp_1 \ numExp_2.
       Efn Oi Os M (numExp_1 lt numExp_2) =
       if numExp_1 < numExp_2 then \mathcal{U}(:,v) else \{\}
[Jext_def]
 \vdash (\forall J \ s. Jext J (Name s) = J \ s) \land
     (\forall J P_1 P_2.
         Jext J (P_1 meet P_2) = Jext J P_1 RUNION Jext J P_2) \wedge
     \forall J \ P_1 \ P_2. Jext J \ (P_1 \ \text{quoting} \ P_2) = Jext J \ P_2 O Jext J \ P_1
[Lifn_def]
 \vdash (\forall M \ l. Lifn M (iLab l) = l) \land
    \forall M \ name. Lifn M (il name) = imapKS M name
```

```
[Lsfn_def]
 \vdash (\forall M \ l. Lsfn M (sLab l) = l) \land
    \forall\,M name. Lsfn M (sl name) = smapKS M name
2.2
       Theorems
[andf_def]
 \vdash \ \forall \ Oi \ Os \ M \ f_1 \ f_2.
       Efn Oi Os M (f_1 and f_2) = Efn Oi Os M f_1 \cap Efn Oi Os M f_2
[controls_def]
 \vdash \forall Oi \ Os \ M \ P \ f.
       Efn Oi \ Os \ M \ (P \ controls \ f) =
       \mathcal{U}(:"v) DIFF \{w \mid \text{Jext (jKS } M) \mid P \mid w \subseteq \text{Efn } Oi \mid Os \mid M \mid f\} \cup \mathcal{U}(:"v)
       Efn Oi Os M f
[controls_says]
 \vdash \forall M \ P \ f.
       Efn Oi\ Os\ M (P controls f) = Efn Oi\ Os\ M (P says f impf f)
[domi_def]
 \vdash \ \forall \ Oi \ Os \ M \ intl_1 \ intl_2.
       Efn Oi Os M (intl_1 domi intl_2) =
       if repPO Oi (Lifn M intl_2) (Lifn M intl_1) then \mathcal{U}(:'v)
       else { }
[doms_def]
 \vdash \ \forall \ Oi \ Os \ M \ secl_1 \ secl_2.
       Efn Oi \ Os \ M \ (secl_1 \ doms \ secl_2) =
       if repPO Os (Lsfn M secl_2) (Lsfn M secl_1) then \mathcal{U}(:,v)
       else { }
[eqf_def]
 \vdash \ \forall \ Oi \ Os \ M \ f_1 \ f_2.
       Efn Oi Os M (f_1 eqf f_2) =
       (\mathcal{U}(:, v) DIFF Efn Oi\ Os\ M\ f_2\ \cup Efn Oi\ Os\ M\ f_1)
[eqf_impf]
 \vdash \ \forall M \ f_1 \ f_2.
       Efn Oi Os M (f_1 eqf f_2) =
       Efn Oi Os M ((f_1 impf f_2) andf (f_2 impf f_1))
```

```
[eqi_def]
 \vdash \ \forall \ Oi \ \ Os \ \ M \ \ intl_2 \ \ intl_1 \, .
       Efn Oi\ Os\ M (intl_2 eqi intl_1) =
       (if repPO Oi (Lifn M intl_2) (Lifn M intl_1) then \mathcal{U}(:,v)
        else { }) ∩
       if repPO Oi (Lifn M intl_1) (Lifn M intl_2) then \mathcal{U}(:,v)
       else { }
[eqi_domi]
 \vdash \ \forall M \ intL_1 \ intL_2.
       Efn Oi \ Os \ M \ (intL_1 \ eqi \ intL_2) =
       Efn Oi Os M (intL_2 domi intL_1 and intL_1 domi intL_2)
eqn_def
 \vdash \ \forall \ Oi \ Os \ M \ numExp_1 \ numExp_2.
       Efn Oi\ Os\ M (numExp_1 eqn numExp_2) =
       if numExp_1 = numExp_2 then \mathcal{U}(:,v) else \{\}
[eqs_def]
 \vdash \forall Oi \ Os \ M \ secl_2 \ secl_1.
       Efn Oi \ Os \ M \ (secl_2 \ eqs \ secl_1) =
       (if repPO Os (Lsfn M secl_2) (Lsfn M secl_1) then \mathcal{U}(:,v)
        else { }) ∩
       if repPO Os (Lsfn M secl_1) (Lsfn M secl_2) then \mathcal{U}(:,v)
       else { }
[eqs_doms]
 \vdash \forall M \ secL_1 \ secL_2.
       Efn Oi\ Os\ M\ (secL_1\ eqs\ secL_2) =
       Efn Oi Os M (secL_2 doms secL_1 and secL_1 doms secL_2)
[FF_def]
 \vdash \forall Oi \ Os \ M. Efn Oi \ Os \ M FF = {}
[impf_def]
 \vdash \ \forall \ Oi \ Os \ M \ f_1 \ f_2.
       Efn Oi \ Os \ M \ (f_1 \ \text{impf} \ f_2) =
       \mathcal{U}(:, v) DIFF Efn Oi Os M f_1 \cup Efn Oi Os M f_2
[lt_def]
 \vdash \ \forall \ Oi \ Os \ M \ numExp_1 \ numExp_2.
       Efn Oi\ Os\ M\ (numExp_1\ lt\ numExp_2) =
       if numExp_1 < numExp_2 then \mathcal{U}(:,v) else \{\}
[lte_def]
 \vdash \forall Oi \ Os \ M \ numExp_1 \ numExp_2.
       Efn Oi\ Os\ M (numExp_1 lte numExp_2) =
       if numExp_1 \leq numExp_2 then \mathcal{U}(: `v) else \{\}
```

```
[meet_def]
 \vdash \forall J \ P_1 \ P_2. Jext J \ (P_1 \ \text{meet} \ P_2) = Jext J \ P_1 RUNION Jext J \ P_2
[name_def]
 \vdash \forall J \ s. \ \texttt{Jext} \ J \ (\texttt{Name} \ s) = J \ s
[notf_def]
 \vdash \forall Oi \ Os \ M \ f. Efn Oi \ Os \ M (notf f) = \mathcal{U}(:'v) DIFF Efn Oi \ Os \ M \ f
[orf_def]
 \vdash \forall Oi \ Os \ M \ f_1 \ f_2.
        Efn Oi Os M (f_1 orf f_2) = Efn Oi Os M f_1 \cup Efn Oi Os M f_2
[prop_def]
 \vdash \ \forall \ Oi \ Os \ M \ p. Efn Oi \ Os \ M (prop p) = intpKS M p
[quoting_def]
 \vdash \forall J \ P_1 \ P_2. Jext J (P_1 quoting P_2) = Jext J P_2 O Jext J P_1
[reps_def]
  \vdash \ \forall \ Oi \ Os \ M \ P \ Q \ f.
        Efn Oi\ Os\ M (reps P\ Q\ f) =
        \mathcal{U}(:,v) DIFF
        \{w \mid \mathsf{Jext} \ (\mathsf{jKS} \ M) \ (P \ \mathsf{quoting} \ Q) \ w \subseteq \mathsf{Efn} \ \mathit{Oi} \ \mathit{Os} \ M \ f\} \ \cup
        \{w \mid \text{Jext (jKS } M) \mid Q \mid w \subseteq \text{Efn } Oi \mid Os \mid M \mid f\}
[says_def]
 \vdash \forall Oi \ Os \ M \ P \ f.
        Efn Oi \ Os \ M \ (P \ \text{says} \ f) =
        \{w \mid \text{Jext (jKS } M) \mid P \mid w \subseteq \text{Efn } Oi \mid Os \mid M \mid f\}
[speaks_for_def]
  \vdash \forall Oi \ Os \ M \ P \ Q.
        Efn Oi\ Os\ M (P speaks_for Q) =
        if Jext (jKS M) Q RSUBSET Jext (jKS M) P then \mathcal{U}(:'v)
[TT_def]
 \vdash \ \forall \ Oi \ Os \ M . Efn Oi \ Os \ M TT = \mathcal{U}(: `v)
```

#### 3 aclrules Theory

Built: 25 February 2018

Parent Theories: aclsemantics

#### 3.1 Definitions

```
[sat_def]
 \vdash \forall M \ Oi \ Os \ f. \ (M,Oi,Os) \ \text{sat} \ f \iff (\text{Efn} \ Oi \ Os \ M \ f = \mathcal{U}(:'world))
3.2
       Theorems
[And_Says]
 \vdash \forall M \ Oi \ Os \ P \ Q \ f.
       (M,Oi,Os) sat P meet Q says f eqf P says f and Q says f
[And_Says_Eq]
 \vdash (M, Oi, Os) sat P meet Q says f \iff
     (M,Oi,Os) sat P says f and Q says f
[and_says_lemma]
 \vdash \forall M \ Oi \ Os \ P \ Q \ f.
       (M,Oi,Os) sat P meet Q says f impf P says f and f says f
[Controls_Eq]
 \vdash \forall M \ Oi \ Os \ P \ f.
       (M,Oi,Os) sat P controls f\iff (M,Oi,Os) sat P says f impf f
[DIFF_UNIV_SUBSET]
 \vdash (\mathcal{U}(:'a) DIFF s \cup t = \mathcal{U}(:'a)) \iff s \subseteq t
[domi_antisymmetric]
 \vdash \ \forall M \ Oi \ Os \ l_1 \ l_2.
       (M,Oi,Os) sat l_1 domi l_2 \Rightarrow
       (M, Oi, Os) sat l_2 domi l_1 \Rightarrow
       (M,Oi,Os) sat l_1 eqi l_2
[domi_reflexive]
 \vdash \ \forall \, M \ Oi \ Os \ l. \ (M,Oi,Os) \ {\it sat} \ l \ {\it domi} \ l
[domi_transitive]
 \vdash \ \forall M \ Oi \ Os \ l_1 \ l_2 \ l_3.
       (M, Oi, Os) sat l_1 domi l_2 \Rightarrow
       (M, Oi, Os) sat l_2 domi l_3 \Rightarrow
       (M,Oi,Os) sat l_1 domi l_3
[doms_antisymmetric]
 \vdash \ \forall M \ Oi \ Os \ l_1 \ l_2.
       (M,Oi,Os) sat l_1 doms l_2 \Rightarrow
       (M,Oi,Os) sat l_2 doms l_1 \Rightarrow
       (M,Oi,Os) sat l_1 eqs l_2
```

```
[doms_reflexive]
 \vdash \forall \, M \ Oi \ Os \ l. \ (M,Oi,Os) \ {\it sat} \ l \ {\it doms} \ l
[doms_transitive]
 \vdash \ \forall M \ Oi \ Os \ l_1 \ l_2 \ l_3.
        (M, Oi, Os) sat l_1 doms l_2 \Rightarrow
        (M,Oi,Os) sat l_2 doms l_3 \Rightarrow
        (M, Oi, Os) sat l_1 doms l_3
[eqf_and_impf]
 \vdash \ \forall M \ Oi \ Os \ f_1 \ f_2.
        (M,Oi,Os) sat f_1 eqf f_2 \iff
        (M,Oi,Os) sat (f_1 \text{ impf } f_2) and (f_2 \text{ impf } f_1)
[eqf_andf1]
 \vdash \ \forall \, M \ \ Oi \ \ Os \ f \ \ f' \ \ g \, .
        (M, Oi, Os) sat f \neq f' \Rightarrow
        (M,Oi,Os) sat f and g \Rightarrow
        (M, Oi, Os) sat f' and g
[eqf_andf2]
 \vdash \ \forall \, M \ \ Oi \ \ Os \ f \ \ f' \ \ g \, .
        (M,Oi,Os) sat f eqf f' \Rightarrow
        (M,Oi,Os) sat g and f \Rightarrow
        (M,Oi,Os) sat g and f'
eqf_controls
 \vdash \forall M \ Oi \ Os \ P \ f \ f'.
        (M,Oi,Os) sat f \neq f' \Rightarrow
        (M,Oi,Os) sat P controls f \Rightarrow
        (M, Oi, Os) sat P controls f'
[eqf_eq]
 \vdash (Efn Oi\ Os\ M\ (f_1\ \mathsf{eqf}\ f_2) = \mathcal{U}(:\ \mathsf{'b})) \iff
     (Efn Oi Os M f_1 = Efn Oi Os M f_2)
[eqf_eqf1]
 \vdash \ \forall M \ Oi \ Os \ f \ f' \ g.
        (M,Oi,Os) sat f eqf f' \Rightarrow
        (M, Oi, Os) sat f \neq g \Rightarrow
        (M,Oi,Os) sat f' eqf g
[eqf_eqf2]
 \vdash \ \forall \, M \ \ Oi \ \ Os \ f \ f' \ g \, .
        (M,Oi,Os) sat f \neq f' \Rightarrow
        (M,Oi,Os) sat g eqf f \Rightarrow
        (M,Oi,Os) sat g eqf f'
```

```
[eqf_impf1]
 \vdash \forall M \ Oi \ Os \ f \ f' \ g.
       (M,Oi,Os) sat f eqf f' \Rightarrow
       (M,Oi,Os) sat f impf g \Rightarrow
       (M,Oi,Os) sat f' impf g
[eqf_impf2]
 \vdash \forall M \ Oi \ Os \ f \ f' \ g.
       (M,Oi,Os) sat f eqf f' \Rightarrow
       (M,Oi,Os) sat g impf f \Rightarrow
       (M,Oi,Os) sat g impf f'
[eqf_notf]
 \vdash \forall M \ Oi \ Os \ f \ f'.
       (M,Oi,Os) sat f \neq f' \Rightarrow
       (M,Oi,Os) sat notf f \Rightarrow
       (M,Oi,Os) sat notf f'
[eqf_orf1]
 \vdash \ \forall M \ Oi \ Os \ f \ f' \ g.
       (M,Oi,Os) sat f eqf f' \Rightarrow
       (M,Oi,Os) sat f orf g \Rightarrow
       (M,Oi,Os) sat f' orf g
[eqf_orf2]
 \vdash \forall M \ Oi \ Os \ f \ f' \ g.
       (M,Oi,Os) sat f eqf f' \Rightarrow
       (M,Oi,Os) sat g orf f \Rightarrow
       (M,Oi,Os) sat g orf f'
[eqf_reps]
 \vdash \forall M \ Oi \ Os \ P \ Q \ f \ f'.
       (M,Oi,Os) sat f eqf f' \Rightarrow
       (M,Oi,Os) sat reps P Q f \Rightarrow
       (M,Oi,Os) sat reps P Q f'
[eqf_sat]
 \vdash \forall M \ Oi \ Os \ f_1 \ f_2.
       (M,Oi,Os) sat f_1 eqf f_2 \Rightarrow
       ((M,Oi,Os) \text{ sat } f_1 \iff (M,Oi,Os) \text{ sat } f_2)
[eqf_says]
 \vdash \forall M \ Oi \ Os \ P \ f \ f'.
       (M,Oi,Os) sat f eqf f' \Rightarrow
       (M,Oi,Os) sat P says f \Rightarrow
       (M,Oi,Os) sat P says f'
```

```
[eqi_Eq]
 \vdash \forall M \ Oi \ Os \ l_1 \ l_2.
        (M,Oi,Os) sat l_1 eqi l_2 \iff
        (M,Oi,Os) sat l_2 domi l_1 andf l_1 domi l_2
[eqs_Eq]
 \vdash \ \forall M \ Oi \ Os \ l_1 \ l_2.
        (M,Oi,Os) sat l_1 eqs l_2 \iff
        (M,Oi,Os) sat l_2 doms l_1 and l_1 doms l_2
[Idemp_Speaks_For]
 \vdash \ \forall M \ Oi \ Os \ P. (M,Oi,Os) sat P speaks_for P
[Image_cmp]
 \vdash \forall R_1 \ R_2 \ R_3 \ u. (R_1 \ \mathsf{O} \ R_2) u \subseteq R_3 \iff R_2 \ u \subseteq \{y \mid R_1 \ y \subseteq R_3\}
[Image_SUBSET]
 \vdash \ \forall \, R_1 \ R_2 \,. \ R_2 \ \text{RSUBSET} \ R_1 \ \Rightarrow \ \forall \, w \,. \ R_2 \ w \ \subseteq \ R_1 \ w
[Image_UNION]
 \vdash \forall R_1 R_2 w. (R_1 RUNION R_2) w = R_1 w \cup R_2 w
[INTER_EQ_UNIV]
 \vdash (s \cap t = \mathcal{U}(:'a)) \iff (s = \mathcal{U}(:'a)) \land (t = \mathcal{U}(:'a))
[Modus_Ponens]
 \vdash \ \forall M \ Oi \ Os \ f_1 \ f_2.
        (M, Oi, Os) sat f_1 \Rightarrow
        (M, Oi, Os) sat f_1 impf f_2 \Rightarrow
        (M,Oi,Os) sat f_2
[Mono_speaks_for]
 \vdash \ \forall M \ Oi \ Os \ P \ P' \ Q \ Q'.
        (M,Oi,Os) sat P speaks_for P' \Rightarrow (M,Oi,Os) sat Q speaks_for Q' \Rightarrow
        (M,Oi,Os) sat P quoting Q speaks_for P' quoting Q'
[MP_Says]
 \vdash \forall M \ Oi \ Os \ P \ f_1 \ f_2.
        (M, Oi, Os) sat
        P says (f_1 \text{ impf } f_2) impf P says f_1 impf P says f_2
Quoting
 \vdash \forall M \ Oi \ Os \ P \ Q \ f.
        (M,Oi,Os) sat P quoting Q says f eqf P says Q says f
```

```
[Quoting_Eq]
 \vdash \ \forall M \ Oi \ Os \ P \ Q \ f.
        (M, Oi, Os) sat P quoting Q says f \iff
       (M,Oi,Os) sat P says Q says f
[reps_def_lemma]
 \vdash \ \forall M \ Oi \ Os \ P \ Q \ f.
       Efn Oi\ Os\ M (reps P\ Q\ f) =
       Efn Oi Os M (P quoting Q says f impf Q says f)
[Reps_Eq]
 \vdash \forall M \ Oi \ Os \ P \ Q \ f.
        (M,Oi,Os) sat reps P Q f \iff
       (M,Oi,Os) sat P quoting Q says f impf Q says f
[sat_allworld]
 \vdash \ \forall \ M \ f. \ (M,Oi,Os) \ {\sf sat} \ f \iff \forall \ w. \ w \in {\sf Efn} \ Oi \ Os \ M \ f
[sat_andf_eq_and_sat]
 \vdash (M, Oi, Os) sat f_1 and f_2 \iff
     (M,Oi,Os) sat f_1 \wedge (M,Oi,Os) sat f_2
sat_TT
 \vdash (M, Oi, Os) sat TT
[Says]
 \vdash \ \forall M \ Oi \ Os \ P \ f. \ (M,Oi,Os) \ {\tt sat} \ f \ \Rightarrow \ (M,Oi,Os) \ {\tt sat} \ P \ {\tt says} \ f
[says_and_lemma]
 \vdash \ \forall \, M \ Oi \ Os \ P \ Q \ f \, .
       (M,Oi,Os) sat P says f and f says f impf P meet f says f
[Speaks_For]
 \vdash \forall M \ Oi \ Os \ P \ Q \ f.
        (M,Oi,Os) sat P speaks_for Q impf P says f impf Q says f
[speaks_for_SUBSET]
 \vdash \forall R_3 \ R_2 \ R_1.
       R_2 RSUBSET R_1 \Rightarrow \forall w. \{w \mid R_1 \mid w \subseteq R_3\} \subseteq \{w \mid R_2 \mid w \subseteq R_3\}
[SUBSET_Image_SUBSET]
 \vdash \ \forall R_1 \ R_2 \ R_3.
       (\forall w_1. R_2 w_1 \subseteq R_1 w_1) \Rightarrow
       \forall w. \{w \mid R_1 \ w \subseteq R_3\} \subseteq \{w \mid R_2 \ w \subseteq R_3\}
```

```
Trans_Speaks_For
  \vdash \forall M \ Oi \ Os \ P \ Q \ R.
           (M,Oi,Os) sat P speaks_for Q \Rightarrow
           (M, Oi, Os) sat Q speaks_for R \Rightarrow
           (M,Oi,Os) sat P speaks_for R
[UNIV_DIFF_SUBSET]
  \vdash \forall R_1 \ R_2. \ R_1 \subseteq R_2 \Rightarrow (\mathcal{U}(:\ 'a)\ \mathtt{DIFF}\ R_1 \cup R_2 = \mathcal{U}(:\ 'a))
[world_and]
  \vdash \forall M \ Oi \ Os \ f_1 \ f_2 \ w.
           w \in \mathsf{Efn}\ \mathit{Oi}\ \mathit{Os}\ \mathit{M}\ (\mathit{f}_1\ \mathsf{andf}\ \mathit{f}_2) \iff
           w \in \text{Efn } Oi \ Os \ M \ f_1 \ \land \ w \in \text{Efn } Oi \ Os \ M \ f_2
[world_eq]
  \vdash \ \forall M \ Oi \ Os \ f_1 \ f_2 \ w.
           w \in \text{Efn } Oi \ Os \ M \ (f_1 \ \text{eqf} \ f_2) \iff
           (w \in \mathsf{Efn}\ \mathit{Oi}\ \mathit{Os}\ \mathit{M}\ \mathit{f}_1 \iff w \in \mathsf{Efn}\ \mathit{Oi}\ \mathit{Os}\ \mathit{M}\ \mathit{f}_2)
world_eqn
  \vdash \forall M \ Oi \ Os \ n_1 \ n_2 \ w. \ w \in \texttt{Efn} \ Oi \ Os \ m \ (n_1 \ \texttt{eqn} \ n_2) \iff (n_1 \ \texttt{=} \ n_2)
[world_F]
  \vdash \ \forall \, M \ Oi \ Os \ w \, . \ w \, \notin \, \mathtt{Efn} \ Oi \ Os \ M \ \mathtt{FF}
world_imp
  \vdash \forall M \ Oi \ Os \ f_1 \ f_2 \ w.
           w \in \text{Efn } Oi \ Os \ M \ (f_1 \ \text{impf} \ f_2) \iff
           w \in \texttt{Efn} \ Oi \ Os \ M \ f_1 \ \Rightarrow \ w \in \texttt{Efn} \ Oi \ Os \ M \ f_2
[world_lt]
  \vdash \ orall \ \mathit{M} \ \mathit{Oi} \ \mathit{Os} \ \mathit{n}_1 \ \mathit{n}_2 \ \mathit{w} . \ \mathit{w} \in \mathsf{Efn} \ \mathit{Oi} \ \mathit{Os} \ \mathit{m} \ (\mathit{n}_1 \ \mathsf{lt} \ \mathit{n}_2) \iff \mathit{n}_1 < \mathit{n}_2
[world_lte]
  \vdash \ orall \ \mathit{M} \ \mathit{Oi} \ \mathit{Os} \ \mathit{n}_1 \ \mathit{n}_2 \ \mathit{w} . \ \mathit{w} \ \in \ \mathsf{Efn} \ \mathit{Oi} \ \mathit{Os} \ \mathit{m} \ (\mathit{n}_1 \ \mathsf{lte} \ \mathit{n}_2) \ \Longleftrightarrow \ \mathit{n}_1 \ \leq \ \mathit{n}_2
[world_not]
  [world_or]
  \vdash \forall M \ f_1 \ f_2 \ w.
           w \in \mathsf{Efn} \ \mathit{Oi} \ \mathit{Os} \ \mathit{M} \ (\mathit{f}_1 \ \mathsf{orf} \ \mathit{f}_2) \iff
           w \in \mathtt{Efn}\ Oi\ Os\ M\ f_1\ \lor\ w \in \mathtt{Efn}\ Oi\ Os\ M\ f_2
[world_says]
  \vdash \ \forall M \ Oi \ Os \ P \ f \ w.
           w \in \text{Efn } Oi \ Os \ M \ (P \ \text{says} \ f) \iff
           \forall v. v \in \text{Jext (jKS } M) \ P \ w \Rightarrow v \in \text{Efn } Oi \ Os \ M \ f
world_T
  \vdash \forall M \ Oi \ Os \ w. \ w \in \texttt{Efn} \ Oi \ Os \ M \ \texttt{TT}
```

# 4 aclDrules Theory

Built: 25 February 2018

Parent Theories: aclrules

#### 4.1 Theorems

```
[Conjunction]
 \vdash \ \forall M \ Oi \ Os \ f_1 \ f_2.
       (M,Oi,Os) sat f_1 \Rightarrow
       (M,Oi,Os) sat f_2 \Rightarrow
       (M, Oi, Os) sat f_1 and f_2
[Controls]
 \vdash \ \forall M \ Oi \ Os \ P \ f.
       (M,Oi,Os) sat P says f \Rightarrow
       (M, Oi, Os) sat P controls f \Rightarrow
       (M,Oi,Os) sat f
[Derived_Controls]
 \vdash \forall M \ Oi \ Os \ P \ Q \ f.
       (M,Oi,Os) sat P speaks_for Q \Rightarrow
       (M,Oi,Os) sat Q controls f \Rightarrow
       (M,Oi,Os) sat P controls f
[Derived_Speaks_For]
 \vdash \ \forall M \ Oi \ Os \ P \ Q \ f.
       (M,Oi,Os) sat P speaks_for Q \Rightarrow
       (M,Oi,Os) sat P says f \Rightarrow
       (M,Oi,Os) sat Q says f
[Disjunction1]
 \vdash \forall M \ Oi \ Os \ f_1 \ f_2. \ (M,Oi,Os) \ sat \ f_1 \Rightarrow (M,Oi,Os) \ sat \ f_1 \ orf \ f_2
[Disjunction2]
 \vdash \forall M \ Oi \ Os \ f_1 \ f_2. (M,Oi,Os) sat f_2 \Rightarrow (M,Oi,Os) sat f_1 orf f_2
[Disjunctive_Syllogism]
 \vdash \ \forall M \ Oi \ Os \ f_1 \ f_2.
       (M,Oi,Os) sat f_1 orf f_2 \Rightarrow
       (M,Oi,Os) sat notf f_1 \Rightarrow
       (M,Oi,Os) sat f_2
[Double_Negation]
 \vdash \forall M \ Oi \ Os \ f. \ (M,Oi,Os) \ \text{sat notf (notf } f) \Rightarrow (M,Oi,Os) \ \text{sat } f
```

```
[eqn_eqn]
 \vdash (M, Oi, Os) sat c_1 eqn n_1 \Rightarrow
     (M,Oi,Os) sat c_2 eqn n_2 \Rightarrow
     (M,Oi,Os) sat n_1 eqn n_2 \Rightarrow
     (M, Oi, Os) sat c_1 eqn c_2
[eqn_lt]
 \vdash (M, Oi, Os) sat c_1 eqn n_1 \Rightarrow
     (M,Oi,Os) sat c_2 eqn n_2 \Rightarrow
     (M,Oi,Os) sat n_1 lt n_2 \Rightarrow
     (M, Oi, Os) sat c_1 lt c_2
[eqn_lte]
 \vdash (M, Oi, Os) sat c_1 eqn n_1 \Rightarrow
     (M,Oi,Os) sat c_2 eqn n_2 \Rightarrow
     (M,Oi,Os) sat n_1 lte n_2 \Rightarrow
     (M,Oi,Os) sat c_1 lte c_2
[Hypothetical_Syllogism]
 \vdash \ \forall M \ Oi \ Os \ f_1 \ f_2 \ f_3.
        (M, Oi, Os) sat f_1 impf f_2 \Rightarrow
        (M,Oi,Os) sat f_2 impf f_3 \Rightarrow
        (M, Oi, Os) sat f_1 impf f_3
[il_domi]
 \vdash \ \forall \, M \ \ Oi \ \ Os \ \ P \ \ Q \ \ l_1 \ \ l_2 \, .
        (M, Oi, Os) sat il P eqi l_1 \Rightarrow
        (M, Oi, Os) sat il Q eqi l_2 \Rightarrow
        (M,Oi,Os) sat l_2 domi l_1 \Rightarrow
        (M,Oi,Os) sat il Q domi il P
[INTER_EQ_UNIV]
 \vdash \forall s_1 \ s_2. \ (s_1 \cap s_2 = \mathcal{U}(:'a)) \iff (s_1 = \mathcal{U}(:'a)) \land (s_2 = \mathcal{U}(:'a))
[Modus_Tollens]
 \vdash \ \forall M \ Oi \ Os \ f_1 \ f_2.
        (M,Oi,Os) sat f_1 impf f_2 \Rightarrow
        (M,Oi,Os) sat notf f_2 \Rightarrow
        (M, Oi, Os) sat notf f_1
[Rep_Controls_Eq]
 \vdash \forall M \ Oi \ Os \ A \ B \ f.
        (M,Oi,Os) sat reps A B f \iff
        (M, Oi, Os) sat A controls B says f
```

```
[Rep_Says]
 \vdash \ \forall M \ Oi \ Os \ P \ Q \ f.
        (M,Oi,Os) sat reps P Q f \Rightarrow
        (M,Oi,Os) sat P quoting Q says f \Rightarrow
        (M,Oi,Os) sat Q says f
[Reps]
 \vdash \ \forall \, M \ \ Oi \ \ Os \ \ P \ \ Q \ \ f \, .
        (M,Oi,Os) sat reps P Q f \Rightarrow
        (M,Oi,Os) sat P quoting Q says f \Rightarrow
        (M,Oi,Os) sat Q controls f \Rightarrow
        (M, Oi, Os) sat f
[Says_Simplification1]
 \vdash \ \forall M \ Oi \ Os \ P \ f_1 \ f_2.
        (M,Oi,Os) sat P says (f_1 \text{ andf } f_2) \Rightarrow (M,Oi,Os) sat P says f_1
[Says_Simplification2]
 \vdash \forall M \ Oi \ Os \ P \ f_1 \ f_2.
        (M,Oi,Os) sat P says (f_1 \text{ andf } f_2) \Rightarrow (M,Oi,Os) sat P says f_2
[Simplification1]
 \vdash \ \forall \ M \ Oi \ Os \ f_1 \ f_2. (M,Oi,Os) sat f_1 andf f_2 \Rightarrow (M,Oi,Os) sat f_1
[Simplification2]
 \vdash \forall \, M \;\; Oi \;\; Os \;\; f_1 \;\; f_2 . (M, Oi, Os) sat f_1 andf f_2 \;\Rightarrow\; (M, Oi, Os) sat f_2
[sl_doms]
 \vdash \ \forall \, M \ \ Oi \ \ Os \ \ P \ \ Q \ \ l_1 \ \ l_2 \, .
        (M, Oi, Os) sat sl P eqs l_1 \Rightarrow
        (M,Oi,Os) sat sl Q eqs l_2 \Rightarrow
        (M,Oi,Os) sat l_2 doms l_1 \Rightarrow
        (M,Oi,Os) sat sl Q doms sl P
```

# $\mathbf{Index}$

aclDrules Theory, 17	absPO_fn_onto, 4
Theorems, 17	antisym_prod_antisym, 5
Conjunction, 17	EQ_WeakOrder, 5
Controls, 17	KS_bij, 5
Derived_Controls, 17	one_weakorder_WO, 5
Derived_Speaks_For, 17	onto_po, 5
Disjunction1, 17	po_bij, 5
Disjunction2, 17	PO_repPO, 5
Disjunctive_Syllogism, 17	refl_prod_refl, 5
Double_Negation, 17	repPO_iPO_partial_order, 5
eqn_eqn, 18	$repPO_O1, 5$
eqn.lt, 18	repPO_prod_PO, 5
eqn.lte, 18	repPO_Subset_PO, 5
Hypothetical_Syllogism, 18	RPROD_THM, 5
il_domi, 18	SUBSET_WO, 6
INTER_EQ_UNIV, 18	$trans\_prod\_trans, 6$
Modus_Tollens, 18	WeakOrder_Exists, 6
Rep_Controls_Eq, 18	$WO_{prod}WO, 6$
$Rep\_Says, 19$	WO_repPO, 6
Reps, $19$	aclrules Theory, 10
Says_Simplification1, 19	Definitions, 11
Says_Simplification2, 19	$sat_def, 11$
Simplification 1, 19	Theorems, 11
Simplification 2, 19	And_Says, 11
$sl\_doms, 19$	And_Says_Eq, 11
aclfoundation Theory, 3	and_says_lemma, 11
Datatypes, 3	Controls_Eq, 11
Definitions, 3	DIFF_UNIV_SUBSET, 11
$imapKS\_def, 4$	$domi_antisymmetric, 11$
$intpKS_{-}def, 4$	domi_reflexive, 11
$jKS_{-}def, 4$	$domi_{-}transitive, 11$
$O1_def, 4$	$doms\_antisymmetric, 11$
one_weakorder_def, $4$	$doms\_reflexive, 12$
$po_TY_DEF, 4$	$doms\_transitive, 12$
$po_tybij$ , 4	$eqf\_and\_impf, 12$
$prod\_PO\_def, 4$	$eqf\_andf1, 12$
$smapKS_def, 4$	$eqf\_andf2, 12$
Subset_PO_def, $4$	$eqf\_controls, 12$
Theorems, 4	$eqf_eq, 12$
$abs\_po11, 4$	$eqf\_eqf1, 12$

eqf_eqf2, 12	$world_{-}T$ , 16
eqf_impf1, 13	aclsemantics Theory, 6
eqf_impf2, 13	Definitions, 6
eqf_notf, 13	$Efn_{-}def, 6$
eqf_orf1, 13	$Jext_def, 7$
$eqf_{orf2}$ , 13	Lifn_def, 7
eqf_reps, 13	$Lsfn_{-}def, 8$
$eqf_sat, 13$	Theorems, 8
eqf_says, 13	$andf_{-}def, 8$
eqi_Eq, 14	controls_def, 8
eqs_Eq, 14	controls_says, 8
Idemp_Speaks_For, 14	domi_def, 8
Image_cmp, 14	$doms\_def, 8$
Image_SUBSET, 14	$eqf_{-}def, 8$
Image_UNION, 14	$eqf\_impf, 8$
INTER_EQ_UNIV, 14	$eqi_def, 9$
Modus_Ponens, 14	$eqi\_domi, 9$
Mono_speaks_for, 14	$eqn_def, 9$
MP_Says, 14	$eqs_def, 9$
Quoting, 14	$eqs\_doms, 9$
Quoting_Eq, 15	$FF_{-}def, 9$
reps_def_lemma, 15	$impf_{-}def, 9$
Reps_Eq, 15	$lt_def, 9$
sat_allworld, 15	$lte\_def, 9$
sat_andf_eq_and_sat, 15	meet_def, 10
sat_TT, 15	$name\_def, 10$
Says, 15	$notf_{-}def, 10$
says_and_lemma, 15	orf_def, 10
Speaks_For, 15	prop_def, 10
speaks_for_SUBSET, 15	quoting_def, 10
SUBSET_Image_SUBSET, 15	reps_def, 10
Trans_Speaks_For, 16	says_def, 10
UNIV_DIFF_SUBSET, 16	speaks_for_def, 10
world_and, 16	$TT_{-}def, 10$
world_eq, 16	
world_eqn, 16	
world_F, 16	
world_imp, 16	
world_lt, 16	
world_lte, 16	
world_not, 16	
world_or, 16	
world_says, 16	

# Appendix B

Secure State Machine & Patrol Base Operations: Pretty-Printed Theories

# Contents

1	$\mathbf{OM}$	NIType Theory	3
	1.1	Datatypes	3
	1.2	Theorems	3
<b>2</b>	ssm	11 Theory	4
	2.1	Datatypes	4
	2.2	Definitions	
	2.3	Theorems	
3	ssm	Theory	11
	3.1	·	11
	3.2		12
	3.3		13
4	satL	List Theory	21
_	4.1	·	21
	4.2		21
5	ssm	PB Theory	21
•	5.1	·	21
	5.2		22
6	PBT	TypeIntegrated Theory	26
•	6.1		<b>2</b> 6
	6.2		27
7	PRI	IntegratedDef Theory	28
•	7.1	· ·	28
	7.2		28
8	ssm	ConductORP Theory	33
_	8.1	Definitions	
	8.2	Theorems	
^	Con	aductORPType Theory	38
9			
	9.1		38
	9.2	Theorems	39
10			39
			40
	10.2	Theorems	40

11	ConductPBType Theory	45
	11.1 Datatypes	45
	11.2 Theorems	45
12	ssmMoveToORP Theory	46
	12.1 Definitions	46
	12.2 Theorems	46
13	MoveToORPType Theory	<b>5</b> 1
	13.1 Datatypes	51
	13.2 Theorems	51
14	ssmMoveToPB Theory	<b>52</b>
	14.1 Definitions	52
	14.2 Theorems	52
15	MoveToPBType Theory	<b>56</b>
	15.1 Datatypes	56
	15.2 Theorems	56
16	ssmPlanPB Theory	57
	16.1 Theorems	57
17	PlanPBType Theory	67
	17.1 Datatypes	67
	17.2 Theorems	

# 1 OMNIType Theory

**Built:** 13 May 2018

Parent Theories: indexedLists, patternMatches

#### 1.1 Datatypes

```
command = ESCc escCommand | SLc 'slCommand
escCommand = returnToBase | changeMission | resupply
               | reactToContact
escOutput = ReturnToBase | ChangeMission | Resupply
             | ReactToContact
escState = RTB | CM | RESUPPLY | RTC
output = ESCo escOutput | SLo 'slOutput
principal = SR 'stateRole
state = ESCs escState | SLs 'slState
1.2
       Theorems
[command_distinct_clauses]
 \vdash \ \forall \ a' \ a. ESCc a \neq \operatorname{SLc} \ a'
[command_one_one]
 \vdash (\forall a \ a'. (ESCc a = ESCc \ a') \iff (a = a')) \land
    \forall a \ a'. (SLc a = SLc \ a') \iff (a = a')
[escCommand_distinct_clauses]
 \vdash returnToBase \neq changeMission \land returnToBase \neq resupply \land
    returnToBase \neq reactToContact \land changeMission \neq resupply \land
    \texttt{changeMission} \neq \texttt{reactToContact} \ \land \ \texttt{resupply} \neq \texttt{reactToContact}
[escOutput_distinct_clauses]
 \vdash ReturnToBase \neq ChangeMission \land ReturnToBase \neq Resupply \land
    \texttt{ReturnToBase} \neq \texttt{ReactToContact} \ \land \ \texttt{ChangeMission} \neq \texttt{Resupply} \ \land
    \texttt{ChangeMission} \neq \texttt{ReactToContact} \ \land \ \texttt{Resupply} \neq \texttt{ReactToContact}
[escState_distinct_clauses]
 \vdash RTB \neq CM \land RTB \neq RESUPPLY \land RTB \neq RTC \land CM \neq RESUPPLY \land
    \mathtt{CM} \neq \mathtt{RTC} \wedge \mathtt{RESUPPLY} \neq \mathtt{RTC}
```

```
[output_distinct_clauses]
\vdash \forall a' \ a. \ ESCo \ a \neq SLo \ a'
[output_one_one]
\vdash (\forall a \ a'. \ (ESCo \ a = ESCo \ a') \iff (a = a')) \land \\ \forall a \ a'. \ (SLo \ a = SLo \ a') \iff (a = a')
[principal_one_one]
\vdash \forall a \ a'. \ (SR \ a = SR \ a') \iff (a = a')
[state_distinct_clauses]
\vdash \forall a' \ a. \ ESCs \ a \neq SLs \ a'
[state_one_one]
\vdash (\forall a \ a'. \ (ESCs \ a = ESCs \ a') \iff (a = a')) \land \\ \forall a \ a'. \ (SLs \ a = SLs \ a') \iff (a = a')
```

## 2 ssm11 Theory

**Built:** 13 May 2018

Parent Theories: satList

#### 2.1 Datatypes

```
configuration =
    CFG (('command order, 'principal, 'd, 'e) Form -> bool)
        ('state -> ('command order, 'principal, 'd, 'e) Form)
        (('command order, 'principal, 'd, 'e) Form list)
        (('command order, 'principal, 'd, 'e) Form list) 'state
        ('output list)

order = SOME 'command | NONE

trType = discard 'command | trap 'command | exec 'command
```

#### 2.2 Definitions

```
\begin{array}{l} [\mathsf{TR\_def}] \\ \vdash \mathsf{TR} = \\ (\lambda \, a_0 \ a_1 \ a_2 \ a_3 \, . \\ \forall \, \mathit{TR'} \, . \\ (\forall \, a_0 \ a_1 \ a_2 \ a_3 \, . \\ (\exists \, \mathit{authenticationTest} \, P \, \mathit{NS} \, \mathit{M} \, \mathit{Oi} \, \mathit{Os} \, \mathit{Out} \, s \\ securityContext \, \, \mathit{stateInterp} \, \mathit{cmd} \, \mathit{ins} \, \mathit{outs} \, . \\ (a_0 = (M, \mathit{Oi}, \mathit{Os})) \, \land \, (a_1 = \mathsf{exec} \, \mathit{cmd}) \, \land \\ (a_2 = (a_2 \ a_3 \ a_3 \ a_3 \ a_4 \ a_5)) \, \land \, (a_4 \ a_5) \, \land \, (a_5) \, a_5 \, a
```

SSM11 THEORY Theorems

```
{\tt CFG} authentication Test stateInterp
                     securityContext (P says prop (SOME cmd)::ins) s
                     outs) \land
                  (a_3 =
                   CFG authentication Test stateInterp
                     securityContext ins (NS s (exec cmd))
                     (Out \ s \ (exec \ cmd)::outs)) \land
                  authenticationTest (P says prop (SOME cmd)) \land
                  CFGInterpret (M, Oi, Os)
                    (CFG authentication Test stateInterp
                        securityContext (P says prop (SOME cmd)::ins)
                        s outs)) \vee
              (\exists authenticationTest\ P\ NS\ M\ Oi\ Os\ Out\ s
                   security Context\ state Interp\ cmd\ ins\ outs .
                  (a_0 = (M, Oi, Os)) \land (a_1 = trap \ cmd) \land
                   {\tt CFG} authentication Test stateInterp
                     securityContext (P says prop (SOME cmd)::ins) s
                     outs) \land
                  (a_3 =
                   CFG authentication Test stateInterp
                     securityContext ins (NS s (trap cmd))
                     (Out \ s \ (trap \ cmd) :: outs)) \land
                  authenticationTest (P says prop (SOME cmd)) \land
                  CFGInterpret (M, Oi, Os)
                    (CFG authenticationTest\ stateInterp
                        securityContext (P says prop (SOME cmd)::ins)
                        s outs)) \vee
              (\exists authentication Test\ NS\ M\ Oi\ Os\ Out\ s\ security Context
                   stateInterp\ cmd\ x\ ins\ outs.
                  (a_0 = (M, Oi, Os)) \land (a_1 = discard \ cmd) \land
                  (a_2 =
                   CFG authentication Test stateInterp
                     securityContext (x::ins) s outs) \land
                  (a_3 =
                   {\tt CFG} authentication Test stateInterp
                     securityContext\ ins\ (NS\ s\ ({\tt discard}\ cmd))
                     (Out \ s \ (discard \ cmd)::outs)) \land
                  \neg authentication Test x) \Rightarrow
              TR' a_0 a_1 a_2 a_3) \Rightarrow
          TR' a_0 a_1 a_2 a_3)
      Theorems
[CFGInterpret_def]
 \vdash CFGInterpret (M, Oi, Os)
       (CFG \ authentication Test \ stateInterp \ security Context
```

(input::ins) state  $outputStream) \iff$ 

2.3

SSM11 THEORY Theorems

```
(M,Oi,Os) satList securityContext \land (M,Oi,Os) sat input \land
     (M,Oi,Os) sat stateInterp state
[CFGInterpret_ind]
 \vdash \ \forall P.
       (\forall M \ Oi \ Os \ authentication Test \ stateInterp \ security Context
             input ins state outputStream.
            P (M, Oi, Os)
               (CFG \ authentication Test \ stateInterp \ security Context
                   (input::ins) state outputStream)) <math>\land
       (\forall v_{15} \ v_{10} \ v_{11} \ v_{12} \ v_{13} \ v_{14}.
            P \ v_{15} \ (CFG \ v_{10} \ v_{11} \ v_{12} \ [] \ v_{13} \ v_{14})) \ \Rightarrow
       \forall v \ v_1 \ v_2 \ v_3. P \ (v, v_1, v_2) \ v_3
[configuration_one_one]
 \vdash \forall a_0 \ a_1 \ a_2 \ a_3 \ a_4 \ a_5 \ a_0' \ a_1' \ a_2' \ a_3' \ a_4' \ a_5'.
       (CFG a_0 a_1 a_2 a_3 a_4 a_5 = CFG a_0' a_1' a_2' a_3' a_4' a_5') \iff
       (a_0 = a_0') \wedge (a_1 = a_1') \wedge (a_2 = a_2') \wedge (a_3 = a_3') \wedge
       (a_4 = a_4') \wedge (a_5 = a_5')
[order_distinct_clauses]
 \vdash \ \forall \, a. SOME a \neq \mathtt{NONE}
[order_one_one]
 \vdash \forall a \ a'. (SOME a = \text{SOME } a') \iff (a = a')
[TR_cases]
 \vdash \forall a_0 \ a_1 \ a_2 \ a_3.
       TR a_0 a_1 a_2 a_3 \iff
       (\exists authenticationTest\ P\ NS\ M\ Oi\ Os\ Out\ s\ securityContext
             stateInterp cmd ins outs.
            (a_0 = (M, Oi, Os)) \land (a_1 = exec \ cmd) \land
            (a_2 =
             {\tt CFG} \ \ authentication Test \ \ state Interp \ \ security Context
                (P says prop (SOME cmd)::ins) s outs) \land
            (a_3 =
             {\tt CFG} authentication Test state Interp security Context ins
                (NS s (exec cmd)) (Out s (exec cmd)::outs)) \land
            authenticationTest (P says prop (SOME cmd)) \land
           CFGInterpret (M, Oi, Os)
               (CFG \ authentication Test \ stateInterp \ security Context
                   (P says prop (SOME cmd)::ins) s outs)) \lor
       (\exists authenticationTest\ P\ NS\ M\ Oi\ Os\ Out\ s\ securityContext
             stateInterp cmd ins outs.
            (a_0 = (M, Oi, Os)) \land (a_1 = trap \ cmd) \land
            (a_2 =
             {\tt CFG} authentication Test state Interp security Context
                (P says prop (SOME cmd)::ins) s outs) \land
```

Theorems SSM11 THEORY

```
{\tt CFG} authentication Test state Interp security Context ins
              (NS s (trap cmd)) (Out s (trap cmd)::outs)) \wedge
          authenticationTest (P says prop (SOME cmd)) \land
          CFGInterpret (M, Oi, Os)
             (CFG \ authentication Test \ stateInterp \ security Context
                (P \text{ says prop (SOME } cmd)::ins) \ s \ outs)) \ \lor
      \exists authenticationTest NS M Oi Os Out s securityContext
          stateInterp\ cmd\ x\ ins\ outs.
         (a_0 = (M, Oi, Os)) \land (a_1 = discard \ cmd) \land
         (a_2 =
          {\tt CFG} authentication Test state Interp security Context
             (x::ins) s outs) \wedge
         (a_3 =
          {\tt CFG} authentication Test state Interp security Context ins
             (NS \ s \ (discard \ cmd)) (Out \ s \ (discard \ cmd)::outs)) \land
         \neg authentication Test x
[TR_discard_cmd_rule]
 \vdash TR (M, Oi, Os) (discard cmd)
       (CFG authenticationTest stateInterp securityContext
          (x::ins) s outs)
       (\mathtt{CFG}\ authenticationTest\ stateInterp\ securityContext\ ins
          (NS \ s \ (discard \ cmd)) \ (Out \ s \ (discard \ cmd)::outs)) \iff
    \neg authenticationTest x
[TR_EQ_rules_thm]
 \vdash (TR (M, Oi, Os) (exec cmd)
        (CFG authentication Test stateInterp securityContext
            (P says prop (SOME cmd)::ins) s outs)
        (\mathtt{CFG}\ authenticationTest\ stateInterp\ securityContext\ ins
           (NS \ s \ (exec \ cmd)) \ (Out \ s \ (exec \ cmd)::outs)) \iff
     authenticationTest (P says prop (SOME cmd)) \land
     CFGInterpret (M, Oi, Os)
        (CFG authentication Test stateInterp securityContext
            (P says prop (SOME cmd)::ins) s outs)) \land
    (TR (M, Oi, Os) (trap cmd)
        (CFG \ authentication Test \ stateInterp \ security Context
            (P says prop (SOME cmd)::ins) s outs)
        (\mathtt{CFG}\ authentication Test\ stateInterp\ security Context\ ins
            (NS \ s \ (trap \ cmd)) \ (Out \ s \ (trap \ cmd)::outs)) \iff
     authenticationTest (P says prop (SOME cmd)) \land
     CFGInterpret (M, Oi, Os)
        (CFG \ authentication Test \ stateInterp \ security Context
            (P says prop (SOME cmd)::ins) s outs)) \land
    (TR (M,Oi,Os) (discard cmd)
        ({\tt CFG}\ \ authentication Test\ \ state Interp\ \ security Context
            (x::ins) s outs)
        (CFG authenticationTest stateInterp securityContext ins
```

SSM11 THEORY Theorems

```
(NS \ s \ (discard \ cmd)) \ (Out \ s \ (discard \ cmd)::outs)) \iff
     \neg authentication Test x)
[TR_exec_cmd_rule]
 \vdash \ \forall \ authenticationTest \ \ securityContext \ \ stateInterp \ \ P \ \ cmd \ \ ins \ \ s
       (\forall M \ Oi \ Os.
          CFGInterpret (M, Oi, Os)
             (CFG \ authentication Test \ stateInterp \ security Context
                 (P \text{ says prop (SOME } cmd)::ins) \ s \ outs) \Rightarrow
           (M,Oi,Os) sat prop (SOME cmd)) \Rightarrow
      \forall NS \ Out \ M \ Oi \ Os.
         TR (M, Oi, Os) (exec cmd)
            (CFG authenticationTest stateInterp securityContext
                (P says prop (SOME cmd)::ins) s outs)
            (\mathtt{CFG}\ authentication\ Test\ stateInterp\ security\ Context\ ins
                (NS \ s \ (exec \ cmd)) \ (Out \ s \ (exec \ cmd)::outs)) \iff
         authenticationTest (P says prop (SOME cmd)) \land
         CFGInterpret (M, Oi, Os)
            (CFG \ authentication Test \ stateInterp \ security Context
                (P \text{ says prop } (SOME \ cmd) :: ins) \ s \ outs) \ \land
         (M, Oi, Os) sat prop (SOME cmd)
[TR_ind]
 \vdash \forall TR'.
       (\forall authentication Test P NS M Oi Os Out s security Context
            stateInterp cmd ins outs.
           authenticationTest (P says prop (SOME cmd)) \land
          CFGInterpret (M, Oi, Os)
             (CFG \ authentication Test \ stateInterp \ security Context
                 (P \text{ says prop (SOME } cmd)::ins) \ s \ outs) \Rightarrow
           TR' (M, Oi, Os) (exec cmd)
             (CFG \ authentication Test \ stateInterp \ security Context
                 (P says prop (SOME cmd)::ins) s outs)
             ({\tt CFG}\ authentication Test\ state Interp\ security Context
                 ins \ (NS \ s \ (exec \ cmd)) \ (Out \ s \ (exec \ cmd)::outs))) \ \land
       (\forall authentication Test\ P\ NS\ M\ Oi\ Os\ Out\ s\ security Context
            stateInterp cmd ins outs.
           authenticationTest (P says prop (SOME cmd)) \land
          CFGInterpret (M, Oi, Os)
             (CFG authenticationTest stateInterp securityContext
                 (P \text{ says prop (SOME } cmd)::ins) \ s \ outs) \Rightarrow
           TR' (M, Oi, Os) (trap cmd)
             (CFG \ authentication Test \ stateInterp \ security Context
                 (P says prop (SOME cmd)::ins) s outs)
             (\mathtt{CFG}\ authenticationTest\ stateInterp\ securityContext)
                 ins \ (NS \ s \ (trap \ cmd)) \ (Out \ s \ (trap \ cmd)::outs))) \ \land
       (\forall\, authentication Test\ NS\ M\ Oi\ Os\ Out\ s\ security Context
            stateInterp\ cmd\ x\ ins\ outs.
```

Theorems SSM11 THEORY

```
\neg authentication Test \ x \Rightarrow
           TR' (M, Oi, Os) (discard cmd)
              (\mathtt{CFG}\ authentication\ Test\ stateInterp\ security\ Context
                  (x::ins) s outs)
              (CFG \ authentication Test \ stateInterp \ security Context
                 ins (NS \ s \ (discard \ cmd))
                  (Out \ s \ (discard \ cmd)::outs))) \Rightarrow
       \forall a_0 \ a_1 \ a_2 \ a_3. TR a_0 \ a_1 \ a_2 \ a_3 \Rightarrow TR' \ a_0 \ a_1 \ a_2 \ a_3
[TR_rules]
 \vdash (\forall authenticationTest\ P\ NS\ M\ Oi\ Os\ Out\ s\ securityContext
         stateInterp cmd ins outs.
        authenticationTest (P says prop (SOME cmd)) \land
        CFGInterpret (M, Oi, Os)
           (\mathtt{CFG}\ authentication\ Test\ stateInterp\ securityContext
               (P \text{ says prop } (SOME \ cmd) :: ins) \ s \ outs) \Rightarrow
        TR (M, Oi, Os) (exec cmd)
           (CFG authenticationTest stateInterp securityContext
               (P \text{ says prop } (SOME \ cmd)::ins) \ s \ outs)
           (CFG \ authentication Test \ stateInterp \ security Context \ ins
               (NS \ s \ (exec \ cmd)) \ (Out \ s \ (exec \ cmd)::outs))) \ \land
     (\forall authenticationTest\ P\ NS\ M\ Oi\ Os\ Out\ s\ securityContext
          stateInterp cmd ins outs.
        authenticationTest (P says prop (SOME cmd)) \land
        CFGInterpret (M, Oi, Os)
           (CFG \ authentication Test \ stateInterp \ security Context
               (P \text{ says prop (SOME } cmd)::ins) \ s \ outs) \Rightarrow
        TR (M, Oi, Os) (trap cmd)
           (CFG authenticationTest stateInterp securityContext
               (P says prop (SOME cmd)::ins) s outs)
           (CFG\ authentication Test\ state Interp\ security Context\ ins
               (NS s (trap cmd)) (Out s (trap cmd)::outs))) \land
    \forall authenticationTest \ NS \ M \ Oi \ Os \ Out \ s \ securityContext
        stateInterp\ cmd\ x\ ins\ outs.
       \neg authenticationTest \ x \Rightarrow
       TR (M, Oi, Os) (discard cmd)
          (\mathtt{CFG}\ authentication\ Test\ stateInterp\ securityContext
              (x::ins) s outs)
          (CFG \ authentication Test \ state Interp \ security Context \ ins
              (NS \ s \ (discard \ cmd)) \ (Out \ s \ (discard \ cmd)::outs))
[TR_strongind]
 \vdash \forall TR'.
       (\forall authentication Test\ P\ NS\ M\ Oi\ Os\ Out\ s\ security Context
            stateInterp cmd ins outs.
           authenticationTest (P says prop (SOME cmd)) \land
           CFGInterpret (M, Oi, Os)
              (CFG \ authentication Test \ stateInterp \ security Context
                  (P \text{ says prop } (SOME \ cmd)::ins) \ s \ outs) \Rightarrow
```

SSM11 THEORY Theorems

```
TR' (M, Oi, Os) (exec cmd)
             (CFG \ authentication Test \ stateInterp \ security Context
                 (P says prop (SOME cmd)::ins) s outs)
             (CFG authenticationTest stateInterp securityContext
                 ins (NS s (exec cmd)) (Out s (exec cmd)::outs))) \land
       (\forall authentication Test\ P\ NS\ M\ Oi\ Os\ Out\ s\ security Context
            stateInterp cmd ins outs.
           authenticationTest (P says prop (SOME cmd)) \land
          CFGInterpret (M, Oi, Os)
             (CFG \ authentication Test \ stateInterp \ security Context
                 (P \text{ says prop (SOME } cmd)::ins) \ s \ outs) \Rightarrow
           TR' (M, Oi, Os) (trap cmd)
             (CFG authenticationTest stateInterp securityContext
                 (P says prop (SOME cmd)::ins) s outs)
             ({\tt CFG}\ authentication Test\ state Interp\ security Context
                 ins (NS s (trap cmd)) (Out s (trap cmd)::outs))) \land
       (\forall authentication Test\ NS\ M\ Oi\ Os\ Out\ s\ security Context
            stateInterp\ cmd\ x\ ins\ outs.
           \neg authentication Test \ x \Rightarrow
           TR' (M, Oi, Os) (discard cmd)
             (CFG \ authentication Test \ stateInterp \ security Context
                 (x::ins) s outs)
             (CFG \ authentication Test \ stateInterp \ security Context
                 ins (NS \ s \ (discard \ cmd))
                 (Out \ s \ (discard \ cmd)::outs))) \Rightarrow
      \forall a_0 \ a_1 \ a_2 \ a_3. TR a_0 \ a_1 \ a_2 \ a_3 \Rightarrow TR' \ a_0 \ a_1 \ a_2 \ a_3
[TR_trap_cmd_rule]
 \vdash \ \forall \ authenticationTest \ \ stateInterp \ \ securityContext \ \ P \ \ cmd \ \ ins \ \ s
        outs.
       (\forall M \ Oi \ Os.
          CFGInterpret (M, Oi, Os)
             (CFG authenticationTest stateInterp securityContext
                 (P \text{ says prop } (SOME \ cmd) :: ins) \ s \ outs) \Rightarrow
           (M,Oi,Os) sat prop NONE) \Rightarrow
      \forall NS \ Out \ M \ Oi \ Os.
         TR (M, Oi, Os) (trap cmd)
            (\mathtt{CFG}\ authentication} \mathit{Test}\ stateInterp\ securityContext
                (P says prop (SOME cmd)::ins) s outs)
            (CFG\ authentication Test\ state Interp\ security Context\ ins
                (NS \ s \ (trap \ cmd)) \ (Out \ s \ (trap \ cmd)::outs)) \iff
         authenticationTest (P says prop (SOME cmd)) \land
         CFGInterpret (M, Oi, Os)
            (CFG authenticationTest stateInterp securityContext
                (P says prop (SOME cmd)::ins) s outs) \land
         (M, Oi, Os) sat prop NONE
[TRrule0]
 \vdash TR (M, Oi, Os) (exec cmd)
       (CFG authentication Test stateInterp security Context
```

```
(P says prop (SOME cmd)::ins) s outs)
       (CFG \ authentication Test \ stateInterp \ security Context \ ins
          (NS \ s \ (exec \ cmd)) \ (Out \ s \ (exec \ cmd)::outs)) \iff
    authenticationTest (P says prop (SOME cmd)) \land
    CFGInterpret (M, Oi, Os)
       (CFG \ authentication Test \ stateInterp \ security Context
          (P says prop (SOME cmd)::ins) s outs)
[TRrule1]
 \vdash TR (M, Oi, Os) (trap cmd)
       (CFG \ authentication Test \ stateInterp \ security Context
          (P says prop (SOME cmd)::ins) s outs)
       (\mathtt{CFG}\ authenticationTest\ stateInterp\ securityContext\ ins
          (NS \ s \ (trap \ cmd)) \ (Out \ s \ (trap \ cmd)::outs)) \iff
    authenticationTest (P says prop (SOME cmd)) \land
    CFGInterpret (M, Oi, Os)
       (\mathtt{CFG}\ authentication\ Test\ stateInterp\ security\ Context
          (P \text{ says prop } (SOME \ cmd) :: ins) \ s \ outs)
[trType_distinct_clauses]
 \vdash (\forall a' \ a. \ discard \ a \neq trap \ a') \land (\forall a' \ a. \ discard \ a \neq exec \ a') \land
    \forall a' \ a. \ \mathsf{trap} \ a \neq \mathsf{exec} \ a'
[trType_one_one]
 \vdash (\forall a \ a'. (discard a =  discard a') \iff (a = a')) \land
    (\forall a \ a'. \ (\text{trap} \ a = \text{trap} \ a') \iff (a = a')) \land
    \forall a \ a'. (exec a = \text{exec } a') \iff (a = a')
3
     ssm Theory
Built: 13 May 2018
Parent Theories: satList
3.1
       Datatypes
configuration =
     CFG (('command option, 'principal, 'd, 'e) Form -> bool)
          ('state ->
           ('command option, 'principal, 'd, 'e) Form list ->
           ('command option, 'principal, 'd, 'e) Form list)
          (('command option, 'principal, 'd, 'e) Form list ->
           ('command option, 'principal, 'd, 'e) Form list)
          (('command option, 'principal, 'd, 'e) Form list list)
```

'state ('output list)

trType = discard 'cmdlist | trap 'cmdlist | exec 'cmdlist

SSM THEORY Definitions

#### 3.2 Definitions

```
[authenticationTest_def]
 \vdash \forall elementTest x.
       \verb|authenticationTest|| elementTest|| x \iff
       FOLDR (\lambda p \ q. \ p \land q) T (MAP elementTest \ x)
[commandList_def]
 \vdash \ \forall \, x \,. commandList x = MAP extractCommand x
[inputList_def]
 \vdash \ \forall \, xs. inputList xs = MAP extractInput xs
[propCommandList_def]
 \vdash \ \forall \, x. propCommandList x = MAP extractPropCommand x
[TR_def]
 \vdash TR =
    (\lambda \ a_0 \ a_1 \ a_2 \ a_3.
        \forall TR'.
           (\forall a_0 \ a_1 \ a_2 \ a_3.
               (\exists elementTest\ NS\ M\ Oi\ Os\ Out\ s\ context\ stateInterp\ x
                   (a_0 = (M, Oi, Os)) \land (a_1 = exec (inputList x)) \land
                   (a_2 =
                    CFG elementTest stateInterp context (x::ins) s
                       outs) \wedge
                   (a_3 =
                    {\tt CFG} elementTest stateInterp context ins
                       (NS \ s \ (exec \ (inputList \ x)))
                       (Out \ s (exec (inputList x))::outs)) \land
                  \verb|authenticationTest|| elementTest|| x \ \land
                  CFGInterpret (M, Oi, Os)
                     (CFG elementTest stateInterp context (x::ins) s
                         outs)) \
               (\exists elementTest\ NS\ M\ Oi\ Os\ Out\ s\ context\ stateInterp\ x
                   (a_0 = (M, Oi, Os)) \land (a_1 = trap (inputList x)) \land
                    CFG elementTest stateInterp context (x::ins) s
                       outs) \wedge
                   (a_3 =
                    {\tt CFG} \ elementTest \ stateInterp \ context \ ins
                       (NS \ s \ (trap \ (inputList \ x)))
                       (Out \ s \ (trap \ (inputList \ x))::outs)) \ \land
                  \verb|authenticationTest|| elementTest|| x \ \land
                  CFGInterpret (M, Oi, Os)
                     (CFG elementTest stateInterp context (x::ins) s
```

Theorems SSM THEORY

 $outs)) \lor$ 

```
(\exists elementTest\ NS\ M\ Oi\ Os\ Out\ s\ context\ stateInterp\ x
                     (a_0 = (M, Oi, Os)) \land (a_1 = discard (inputList x)) \land
                     (a_2 =
                      CFG elementTest stateInterp context (x::ins) s
                         outs) \land
                     (a_3 =
                      CFG elementTest stateInterp context ins
                         (NS \ s \ (discard \ (inputList \ x)))
                         (Out \ s (discard (inputList x))::outs)) \land
                     \negauthenticationTest elementTest x) \Rightarrow
                 TR' a_0 a_1 a_2 a_3) \Rightarrow
            TR' a_0 a_1 a_2 a_3)
3.3
        Theorems
[CFGInterpret_def]
 \vdash CFGInterpret (M, Oi, Os)
        (CFG elementTest stateInterp context (x::ins) state
            outStream) \iff
     (M,Oi,Os) satList context \ x \land (M,Oi,Os) satList x \land (M,Oi,Os)
     (M,Oi,Os) satList stateInterp state x
[CFGInterpret_ind]
 \vdash \forall P.
        (\forall M \ Oi \ Os \ elementTest \ stateInterp \ context \ x \ ins \ state
             outStream.
            P (M, Oi, Os)
               (CFG elementTest stateInterp context (x::ins) state
                   outStream)) \land
        (\forall v_{15} \ v_{10} \ v_{11} \ v_{12} \ v_{13} \ v_{14}.
            P \ v_{15} \ (\text{CFG} \ v_{10} \ v_{11} \ v_{12} \ [] \ v_{13} \ v_{14})) \ \Rightarrow
       \forall v \ v_1 \ v_2 \ v_3. P \ (v, v_1, v_2) \ v_3
[configuration_one_one]
 \vdash \forall a_0 \ a_1 \ a_2 \ a_3 \ a_4 \ a_5 \ a_0' \ a_1' \ a_2' \ a_3' \ a_4' \ a_5'.
        (CFG a_0 a_1 a_2 a_3 a_4 a_5 = CFG a_0' a_1' a_2' a_3' a_4' a_5') \iff
        (a_0 = a_0') \wedge (a_1 = a_1') \wedge (a_2 = a_2') \wedge (a_3 = a_3') \wedge
        (a_4 = a'_4) \wedge (a_5 = a'_5)
[extractCommand_def]
 \vdash extractCommand (P says prop (SOME cmd)) = cmd
[extractCommand_ind]
 \vdash \forall P'.
        (\forall P \ cmd. \ P' \ (P \ \text{says prop (SOME} \ cmd))) \ \land \ P' \ \text{TT} \ \land \ P' \ \text{FF} \ \land
        (\forall v_1. P' \text{ (prop } v_1)) \land (\forall v_3. P' \text{ (notf } v_3)) \land
```

SSM THEORY Theorems

```
(\forall v_6 \ v_7. \ P' \ (v_6 \ \text{andf} \ v_7)) \ \land \ (\forall v_{10} \ v_{11}. \ P' \ (v_{10} \ \text{orf} \ v_{11})) \ \land
           (\forall v_{14} \ v_{15}. \ P' \ (v_{14} \ \text{impf} \ v_{15})) \ \land
           (\forall v_{18} \ v_{19}. \ P' \ (v_{18} \ \text{eqf} \ v_{19})) \ \land \ (\forall v_{129}. \ P' \ (v_{129} \ \text{says} \ \text{TT})) \ \land
           (\forall v130. P' (v130 \text{ says FF})) \land
           (\forall v132. P' (v132 \text{ says prop NONE})) \land
           (\forall v133 v_{66}. P' (v133 says notf v_{66})) \wedge
           (\forall v134\ v_{69}\ v_{70}. P' (v134 says (v_{69} andf v_{70}))) \land
           (\forall v135 \ v_{73} \ v_{74}. \ P' \ (v135 \ \text{says} \ (v_{73} \ \text{orf} \ v_{74}))) \land
           (\forall v136 \ v_{77} \ v_{78}. \ P' \ (v136 \ \text{says} \ (v_{77} \ \text{impf} \ v_{78}))) \land
           (\forall v137 \ v_{81} \ v_{82}. \ P' \ (v137 \ \text{says} \ (v_{81} \ \text{eqf} \ v_{82}))) \ \land
           (\forall v138 \ v_{85} \ v_{86}. \ P' \ (v138 \ \text{says} \ v_{85} \ \text{says} \ v_{86})) \ \land
           (\forall v139 \ v_{89} \ v_{90}. \ P' \ (v139 \ \text{says} \ v_{89} \ \text{speaks\_for} \ v_{90})) \ \land
           (\forall v140 \ v_{93} \ v_{94}. \ P' \ (v140 \ \text{says} \ v_{93} \ \text{controls} \ v_{94})) \ \land
           (\forall v141 \ v_{98} \ v_{99} \ v100. \ P' \ (v141 \ {\tt says \ reps} \ v_{98} \ v_{99} \ v100)) \ \land
           (\forall v142 v103 v104. P' (v142 says v103 domi v104)) \land
           (\forall v143 \ v107 \ v108. \ P' \ (v143 \ \text{says} \ v107 \ \text{eqi} \ v108)) \ \land
           (\forall v144 \ v111 \ v112. \ P' \ (v144 \ \text{says} \ v111 \ \text{doms} \ v112)) \ \land
           (\forall v145 \ v115 \ v116. \ P' \ (v145 \ \text{says} \ v115 \ \text{eqs} \ v116)) \ \land
           (\forall v146 \ v119 \ v120. \ P' \ (v146 \ \text{says} \ v119 \ \text{eqn} \ v120)) \ \land
           (\forall v147 \ v123 \ v124. \ P' \ (v147 \ \text{says} \ v123 \ \text{lte} \ v124)) \ \land
           (\forall v148 \ v127 \ v128. \ P' \ (v148 \ \text{says} \ v127 \ \text{lt} \ v128)) \ \land
           (\forall v_{24} \ v_{25}. \ P' \ (v_{24} \ \text{speaks\_for} \ v_{25})) \ \land
           (\forall v_{28} \ v_{29}. P' (v_{28} controls v_{29})) \land
           (\forall v_{33} \ v_{34} \ v_{35}. \ P' \ (reps \ v_{33} \ v_{34} \ v_{35})) \ \land
           (\forall v_{38} \ v_{39}. \ P' \ (v_{38} \ \text{domi} \ v_{39})) \land
           (\forall v_{42} \ v_{43}. \ P' \ (v_{42} \ \text{eqi} \ v_{43})) \ \land
           (\forall v_{46} \ v_{47}. \ P' \ (v_{46} \ \text{doms} \ v_{47})) \ \land
           (\forall \, v_{50} \ v_{51}. P' (v_{50} eqs v_{51})) \wedge
           (\forall v_{54} \ v_{55}. \ P' \ (v_{54} \ \text{eqn} \ v_{55})) \ \land
           (\forall v_{58} \ v_{59}. \ P' \ (v_{58} \ \text{lte} \ v_{59})) \ \land
           (\forall v_{62} \ v_{63}. \ P' \ (v_{62} \ \text{lt} \ v_{63})) \Rightarrow
          \forall v. P' v
[extractInput_def]
  \vdash extractInput (P says prop x) = x
[extractInput_ind]
  \vdash \forall P'.
           (\forall P \ x. \ P' \ (P \ \text{says prop} \ x)) \ \land \ P' \ \text{TT} \ \land \ P' \ \text{FF} \ \land
           (\forall v_1.\ P'\ (\texttt{prop}\ v_1))\ \land\ (\forall v_3.\ P'\ (\texttt{notf}\ v_3))\ \land
           (\forall v_6 \ v_7. \ P' \ (v_6 \ \text{andf} \ v_7)) \land (\forall v_{10} \ v_{11}. \ P' \ (v_{10} \ \text{orf} \ v_{11})) \land
           (\forall v_{14} \ v_{15}. \ P' \ (v_{14} \ \text{impf} \ v_{15})) \ \land
           (\forall \, v_{18} \ v_{19}. P' (v_{18} eqf v_{19})) \land (\forall \, v129. P' (v129 says TT)) \land
           (\forall v130. P' (v130 \text{ says FF})) \land
           (\forall\,v131\ v_{66}. P' (v131 says notf v_{66})) \land
           (\forall\,v132\ v_{69}\ v_{70}. P' (v132\ \mathrm{says} (v_{69}\ \mathrm{andf}\ v_{70}))) \wedge
           (\forall v133 \ v_{73} \ v_{74}. \ P' \ (v133 \ \text{says} \ (v_{73} \ \text{orf} \ v_{74}))) \ \land
           (\forall v134 \ v_{77} \ v_{78}. \ P' \ (v134 \ \text{says} \ (v_{77} \ \text{impf} \ v_{78}))) \ \land
           (\forall v135 \ v_{81} \ v_{82}. \ P' \ (v135 \ \text{says} \ (v_{81} \ \text{eqf} \ v_{82}))) \land
```

Theorems SSM THEORY

```
(\forall\,v136\ v_{85}\ v_{86}. P' (v136\ \mathrm{says}\ v_{85}\ \mathrm{says}\ v_{86})) \wedge
          (\forall\,v137\ v_{89}\ v_{90}. P' (v137\ \mathrm{says}\ v_{89}\ \mathrm{speaks\_for}\ v_{90})) \land
          (\forall v138 \ v_{93} \ v_{94}. \ P' \ (v138 \ \text{says} \ v_{93} \ \text{controls} \ v_{94})) \ \land
          (\forall v139 \ v_{98} \ v_{99} \ v100. \ P' \ (v139 \ \text{says reps} \ v_{98} \ v_{99} \ v100)) \ \land
          (\forall \, v140 \ v103 \ v104 \,. \ P' \ (v140 \ {\tt says} \ v103 \ {\tt domi} \ v104)) \ \land
          (\forall\,v141\ v107\ v108. P' (v141\ \mathrm{says}\ v107\ \mathrm{eqi}\ v108)) \land
          ( \forall\,v142\ v111\ v112 . P' ( v142\ {\rm says}\ v111\ {\rm doms}\ v112 ) \land
          (\forall\,v143\ v115\ v116. P' (v143\ \mathrm{says}\ v115\ \mathrm{eqs}\ v116)) \land
          (\forall v144 v119 v120. P' (v144 says v119 eqn v120)) \wedge
          (\forall v145 \ v123 \ v124 . P' \ (v145 \ \text{says} \ v123 \ \text{lte} \ v124)) \land
          (\forall v146 \ v127 \ v128. \ P' \ (v146 \ \text{says} \ v127 \ \text{lt} \ v128)) \ \land
          (\forall v_{24} \ v_{25}. \ P' \ (v_{24} \ \text{speaks\_for} \ v_{25})) \land
          (\forall v_{28} \ v_{29}. P' (v_{28} controls v_{29})) \land
          (\forall v_{33} \ v_{34} \ v_{35}. \ P' \ (\text{reps} \ v_{33} \ v_{34} \ v_{35})) \ \land
          (\forall \, v_{38} \ v_{39}. P' (v_{38} domi v_{39})) \wedge
          (\forall v_{42} \ v_{43}. \ P' \ (v_{42} \ \text{eqi} \ v_{43})) \ \land
          (\forall v_{46} \ v_{47}. \ P' \ (v_{46} \ \text{doms} \ v_{47})) \land
          (\forall v_{50} \ v_{51}. \ P' \ (v_{50} \ \text{eqs} \ v_{51})) \ \land
          (\forall v_{54} \ v_{55}. \ P' \ (v_{54} \ \text{eqn} \ v_{55})) \ \land
          (\forall v_{58} \ v_{59}. \ P' \ (v_{58} \ \text{lte} \ v_{59})) \land
          (\forall v_{62} \ v_{63}. \ P' \ (v_{62} \ \text{lt} \ v_{63})) \Rightarrow
         \forall v. P' v
[extractPropCommand_def]
  \vdash extractPropCommand (P says prop (SOME cmd)) = prop (SOME cmd)
[extractPropCommand_ind]
  \vdash \forall P'.
          (\forall P \ cmd. \ P' \ (P \ \text{says prop (SOME} \ cmd))) \ \land \ P' \ \text{TT} \ \land \ P' \ \text{FF} \ \land
          (\forall v_{14} \ v_{15}. P' (v_{14} impf v_{15})) \land
          (\forall v_{18} \ v_{19}. \ P' \ (v_{18} \ \text{eqf} \ v_{19})) \ \land \ (\forall v_{129}. \ P' \ (v_{129} \ \text{says} \ \text{TT})) \ \land
          (\forall\,v130. P' (v130 says FF)) \land
          (\forall v132. P' (v132 says prop NONE)) \land
          (\forall v133 \ v_{66}. \ P' \ (v133 \ \text{says notf} \ v_{66})) \ \land
          (\forall v134 \ v_{69} \ v_{70}. \ P' \ (v134 \ \text{says} \ (v_{69} \ \text{andf} \ v_{70}))) \land
          (\forall v135 \ v_{73} \ v_{74}. \ P' \ (v135 \ \text{says} \ (v_{73} \ \text{orf} \ v_{74}))) \ \land
          (\forall\,v136\ v_{77}\ v_{78}.\ P' (v136\ \mathrm{says} (v_{77}\ \mathrm{impf}\ v_{78}))) \wedge
          (\forall v137 \ v_{81} \ v_{82}. \ P' \ (v137 \ \text{says} \ (v_{81} \ \text{eqf} \ v_{82}))) \ \land
          (\forall v138 \ v_{85} \ v_{86}. \ P' \ (v138 \ \text{says} \ v_{85} \ \text{says} \ v_{86})) \ \land
          (\forall v139 \ v_{89} \ v_{90}. \ P' \ (v139 \ \text{says} \ v_{89} \ \text{speaks\_for} \ v_{90})) \ \land
          (\forall v140 \ v_{93} \ v_{94}. P' (v140 says v_{93} controls v_{94})) \land
          (\forall v141 \ v_{98} \ v_{99} \ v100. \ P' \ (v141 \ \text{says reps} \ v_{98} \ v_{99} \ v100)) \ \land
          (\forall\,v142\ v103\ v104. P' (v142\ \mathrm{says}\ v103\ \mathrm{domi}\ v104)) \land
          (\forall\,v143\ v107\ v108. P' (v143\ \mathrm{says}\ v107\ \mathrm{eqi}\ v108)) \land
          (\forall v114 v111 v112. P' (v144 says v111 doms v112)) \land
          (\forall\,v145\ v115\ v116. P' (v145\ \mathrm{says}\ v115\ \mathrm{eqs}\ v116)) \land
          (\forall\,v146\ v119\ v120. P' (v146\ \mathrm{says}\ v119\ \mathrm{eqn}\ v120)) \wedge
```

SSM THEORY Theorems

```
(\forall v147 \ v123 \ v124. \ P' \ (v147 \ \text{says} \ v123 \ \text{lte} \ v124)) \ \land
        (\forall v148 \ v127 \ v128. P' (v148 \ \mathrm{says} \ v127 \ \mathrm{lt} \ v128)) \land
        (\forall v_{24} \ v_{25}. \ P' \ (v_{24} \ \text{speaks\_for} \ v_{25})) \ \land
        (\forall \, v_{28} \ v_{29}. P' (v_{28} controls v_{29})) \land
        (\forall v_{33} v_{34} v_{35}. P' (reps v_{33} v_{34} v_{35})) \wedge
        (\forall\,v_{38}\;\;v_{39}. P' (v_{38}\; domi v_{39})) \wedge
        (\forall v_{42} \ v_{43}. \ P' \ (v_{42} \ \text{eqi} \ v_{43})) \ \land
        (\forall v_{46} \ v_{47}. \ P' \ (v_{46} \ \text{doms} \ v_{47})) \ \land
        (\forall v_{50} \ v_{51}. \ P' \ (v_{50} \ \text{eqs} \ v_{51})) \ \land
        (\forall v_{54} \ v_{55}. \ P' \ (v_{54} \ \text{eqn} \ v_{55})) \ \land
        (\forall v_{58} \ v_{59}. P' (v_{58} lte v_{59})) \wedge
        (\forall v_{62} \ v_{63}. \ P' \ (v_{62} \ \text{lt} \ v_{63})) \Rightarrow
        \forall v. P'v
[TR_cases]
 \vdash \forall a_0 \ a_1 \ a_2 \ a_3.
        TR a_0 a_1 a_2 a_3 \iff
        (\exists elementTest\ NS\ M\ Oi\ Os\ Out\ s\ context\ stateInterp\ x\ ins
             (a_0 = (M, Oi, Os)) \land (a_1 = exec (inputList x)) \land
             (a_2 =
              CFG elementTest stateInterp context (x::ins) s outs) \land
             (a_3 =
              {\tt CFG} \ elementTest \ stateInterp \ context \ ins
                 (NS \ s \ (exec \ (inputList \ x)))
                 (Out \ s \ (exec \ (inputList \ x))::outs)) \land
            authenticationTest elementTest x \land
            CFGInterpret (M, Oi, Os)
                (CFG elementTest stateInterp context (x::ins) s
                    outs)) ∨
        (\exists elementTest\ NS\ M\ Oi\ Os\ Out\ s\ context\ stateInterp\ x\ ins
             (a_0 = (M, Oi, Os)) \land (a_1 = trap (inputList x)) \land
             (a_2 =
              CFG elementTest stateInterp context (x::ins) s outs) \land
             (a_3 =
              CFG elementTest stateInterp context ins
                 (NS \ s \ (trap \ (inputList \ x)))
                 (Out \ s \ (trap \ (inputList \ x))::outs)) \ \land
            authenticationTest elementTest x \land
            CFGInterpret (M, Oi, Os)
                (CFG elementTest stateInterp context (x::ins) s
                    outs)) \lor
        \exists elementTest NS M Oi Os Out s context stateInterp x ins
           (a_0 = (M, Oi, Os)) \land (a_1 = discard (inputList x)) \land
           (a_2 =
            CFG elementTest stateInterp context (x::ins) s outs) \land
           (a_3 =
```

Theorems SSM THEORY

```
CFG elementTest stateInterp context ins
            (NS \ s \ (discard \ (inputList \ x)))
            (Out \ s (discard (inputList x))::outs)) \land
         \negauthenticationTest elementTest x
[TR_discard_cmd_rule]
 \vdash TR (M, Oi, Os) (discard (inputList x))
      (CFG elementTest stateInterp context (x::ins) s outs)
      (CFG elementTest stateInterp context ins
          (NS \ s \ (discard \ (inputList \ x)))
          (Out \ s \ (discard \ (inputList \ x))::outs)) \iff
    \negauthenticationTest elementTest x
[TR_EQ_rules_thm]
 \vdash (TR (M, Oi, Os) (exec (inputList x))
       (CFG elementTest stateInterp context (x::ins) s outs)
        (CFG elementTest stateInterp context ins
           (NS \ s \ (exec \ (inputList \ x)))
           (Out \ s \ (exec \ (inputList \ x))::outs)) \iff
     authenticationTest elementTest \ x \ \land
     CFGInterpret (M, Oi, Os)
        (CFG elementTest stateInterp context (x::ins) s outs)) \land
    (TR (M, Oi, Os) (trap (inputList x))
       (CFG elementTest stateInterp context (x::ins) s outs)
        (CFG elementTest stateInterp context ins
           (NS \ s \ (trap \ (inputList \ x)))
           (Out \ s \ (trap \ (inputList \ x))::outs)) \iff
     \verb|authenticationTest|| elementTest|| x \ \land
     CFGInterpret (M, Oi, Os)
        (CFG elementTest stateInterp context (x::ins) s outs)) \land
    (TR (M, Oi, Os) (discard (inputList x))
       (CFG elementTest stateInterp context (x::ins) s outs)
        (CFG elementTest stateInterp context ins
           (NS \ s \ (discard \ (inputList \ x)))
           (Out \ s \ (discard \ (inputList \ x))::outs)) \iff
     \negauthenticationTest elementTest x)
[TR_exec_cmd_rule]
 \vdash \forall elementTest \ context \ stateInterp \ x \ ins \ s \ outs.
      (\forall M \ Oi \ Os.
         CFGInterpret (M, Oi, Os)
            (CFG elementTest stateInterp context (x::ins) s
                outs) \Rightarrow
          (M, Oi, Os) satList propCommandList x) \Rightarrow
      \forall NS \ Out \ M \ Oi \ Os.
        TR (M, Oi, Os) (exec (inputList x))
           (CFG elementTest stateInterp context (x::ins) s outs)
           (CFG elementTest stateInterp context ins
```

SSM THEORY Theorems

```
(NS \ s \ (exec \ (inputList \ x)))
               (Out \ s \ (exec \ (inputList \ x))::outs)) \iff
         authenticationTest elementTest \ x \ \land
         CFGInterpret (M, Oi, Os)
            (CFG elementTest stateInterp context (x::ins) s outs) \land
         (M,Oi,Os) satList propCommandList x
[TR_ind]
 \vdash \ \forall \ TR'.
       (\forall elementTest\ NS\ M\ Oi\ Os\ Out\ s\ context\ stateInterp\ x\ ins
            outs.
          \verb|authenticationTest|| elementTest|| x \ \land
          CFGInterpret (M, Oi, Os)
             (CFG elementTest stateInterp context (x::ins) s
                 outs) \Rightarrow
          TR' (M, Oi, Os) (exec (inputList x))
             (CFG elementTest stateInterp context (x::ins) s outs)
             (CFG elementTest stateInterp context ins
                (NS \ s \ (exec \ (inputList \ x)))
                (Out \ s \ (exec \ (inputList \ x))::outs))) \land
       (\forall elementTest\ NS\ M\ Oi\ Os\ Out\ s\ context\ stateInterp\ x\ ins
          authenticationTest elementTest x \land
          CFGInterpret (M, Oi, Os)
             (CFG elementTest stateInterp context (x::ins) s
                outs) \Rightarrow
          TR' (M, Oi, Os) (trap (inputList x))
             (CFG elementTest stateInterp context (x::ins) s outs)
             (CFG elementTest stateInterp context ins
                 (NS \ s \ (trap \ (inputList \ x)))
                (Out \ s \ (trap \ (inputList \ x))::outs))) \land
       (\forall elementTest\ NS\ M\ Oi\ Os\ Out\ s\ context\ stateInterp\ x\ ins
          \negauthenticationTest elementTest x \Rightarrow
          TR' (M, Oi, Os) (discard (inputList x))
             (CFG elementTest stateInterp context (x::ins) s outs)
             (CFG elementTest stateInterp context ins
                (NS \ s \ (discard \ (inputList \ x)))
                (Out \ s \ (discard \ (inputList \ x))::outs))) \Rightarrow
      \forall a_0 \ a_1 \ a_2 \ a_3. TR a_0 \ a_1 \ a_2 \ a_3 \Rightarrow TR' \ a_0 \ a_1 \ a_2 \ a_3
[TR_rules]
 \vdash (\forall elementTest NS M Oi Os Out s context stateInterp x ins
         outs.
        \verb|authenticationTest|| elementTest||x| \wedge
        CFGInterpret (M, Oi, Os)
          (CFG elementTest stateInterp context (x::ins) s outs) \Rightarrow
        TR (M, Oi, Os) (exec (inputList x))
          (CFG elementTest stateInterp context (x::ins) s outs)
```

Theorems SSM THEORY

```
(CFG elementTest stateInterp context ins
              (NS \ s \ (exec \ (inputList \ x)))
              (Out \ s \ (exec \ (inputList \ x))::outs))) \land
    (\forall elementTest\ NS\ M\ Oi\ Os\ Out\ s\ context\ stateInterp\ x\ ins
       \verb|authenticationTest|| elementTest|| x \ \land
       CFGInterpret (M, Oi, Os)
          (CFG elementTest\ stateInterp\ context\ (x::ins)\ s\ outs) \Rightarrow
       TR (M, Oi, Os) (trap (inputList x))
          (CFG elementTest stateInterp context (x::ins) s outs)
          (CFG elementTest stateInterp context ins
              (NS \ s \ (trap \ (inputList \ x)))
              (Out \ s \ (trap \ (inputList \ x))::outs))) \land
    \forall elementTest NS M Oi Os Out s context stateInterp x ins outs.
       \negauthenticationTest elementTest x \Rightarrow
      TR (M, Oi, Os) (discard (inputList x))
         (CFG elementTest stateInterp context (x::ins) s outs)
         (CFG elementTest stateInterp context ins
            (NS \ s \ (discard \ (inputList \ x)))
            (Out s (discard (inputList x))::outs))
[TR_strongind]
 \vdash \forall TR'.
       (\forall elementTest\ NS\ M\ Oi\ Os\ Out\ s\ context\ stateInterp\ x\ ins
           outs.
          authenticationTest elementTest x \land
          CFGInterpret (M, Oi, Os)
            (CFG elementTest stateInterp context (x::ins) s
                outs) \Rightarrow
          TR' (M, Oi, Os) (exec (inputList x))
            (CFG elementTest stateInterp context (x::ins) s outs)
            (CFG elementTest\ stateInterp\ context\ ins
                (NS \ s \ (exec \ (inputList \ x)))
                (Out \ s \ (exec \ (inputList \ x))::outs))) \land
       (\forall elementTest\ NS\ M\ Oi\ Os\ Out\ s\ context\ stateInterp\ x\ ins
          authenticationTest elementTest x \land
          CFGInterpret (M, Oi, Os)
            (CFG elementTest stateInterp context (x::ins) s
                outs) \Rightarrow
          TR' (M, Oi, Os) (trap (inputList x))
            (CFG elementTest stateInterp context (x::ins) s outs)
            (CFG elementTest\ stateInterp\ context\ ins
                (NS \ s \ (trap \ (inputList \ x)))
                (Out \ s \ (trap \ (inputList \ x))::outs))) \land
       (\forall elementTest\ NS\ M\ Oi\ Os\ Out\ s\ context\ stateInterp\ x\ ins
          \negauthenticationTest elementTest x \Rightarrow
          TR' (M, Oi, Os) (discard (inputList x))
```

SSM THEORY Theorems

```
(CFG elementTest stateInterp context (x::ins) s outs)
             (CFG elementTest stateInterp context ins
                 (NS \ s \ (discard \ (inputList \ x)))
                 (Out \ s \ (discard \ (inputList \ x))::outs))) \Rightarrow
      \forall a_0 \ a_1 \ a_2 \ a_3. TR a_0 \ a_1 \ a_2 \ a_3 \Rightarrow TR' \ a_0 \ a_1 \ a_2 \ a_3
[TR_trap_cmd_rule]
 \vdash \ \forall \ elementTest \ \ context \ \ stateInterp \ \ x \ \ ins \ \ s \ \ outs.
       (\forall M \ Oi \ Os.
          CFGInterpret (M, Oi, Os)
             (CFG elementTest stateInterp context (x::ins) s
                 outs) \Rightarrow
           (M,Oi,Os) sat prop NONE) \Rightarrow
      \forall NS \ Out \ M \ Oi \ Os.
         TR (M, Oi, Os) (trap (inputList x))
            (CFG elementTest stateInterp context (x::ins) s outs)
            (CFG elementTest stateInterp context ins
                (NS \ s \ (trap \ (inputList \ x)))
                (Out \ s \ (trap \ (inputList \ x))::outs)) \iff
         authenticationTest elementTest x \land
         CFGInterpret (M, Oi, Os)
            (CFG elementTest stateInterp context (x::ins) s outs) \land
         (M,Oi,Os) sat prop NONE
[TRrule0]
 \vdash TR (M, Oi, Os) (exec (inputList x))
       (CFG elementTest stateInterp context (x::ins) s outs)
       (CFG elementTest stateInterp context ins
           (NS \ s \ (exec \ (inputList \ x)))
           (Out \ s \ (exec \ (inputList \ x))::outs)) \iff
    \verb|authenticationTest|| elementTest|| x \ \land
    CFGInterpret (M, Oi, Os)
       (CFG elementTest stateInterp context (x::ins) s outs)
[TRrule1]
 \vdash TR (M, Oi, Os) (trap (inputList x))
       (CFG elementTest stateInterp context (x::ins) s outs)
       (CFG elementTest stateInterp context ins
           (NS \ s \ (trap \ (inputList \ x)))
           (Out \ s \ (trap \ (inputList \ x))::outs)) \iff
    authenticationTest elementTest x \land
    CFGInterpret (M, Oi, Os)
       (CFG elementTest stateInterp context (x::ins) s outs)
[trType_distinct_clauses]
 \vdash (\forall a' \ a. discard a \neq \text{trap } a') \land (\forall a' \ a. discard a \neq \text{exec } a') \land
    \forall a' \ a. \ \mathsf{trap} \ a \neq \mathsf{exec} \ a'
```

```
[trType_one_one] 
 \vdash (\forall a \ a') (\text{discard } a = \text{discard } a') \iff (a = a')) \land (\forall a \ a') (\text{trap } a = \text{trap } a') \iff (a = a')) \land \forall a \ a'. (\text{exec } a = \text{exec } a') \iff (a = a')
```

## 4 satList Theory

**Built:** 13 May 2018

Parent Theories: aclDrules

#### 4.1 Definitions

```
[satList_def]

\vdash \forall M \ Oi \ Os \ formList.

(M,Oi,Os) satList formList \iff

FOLDR (\lambda x \ y. \ x \land y) T (MAP (\lambda f. \ (M,Oi,Os) sat f) formList)

4.2 Theorems
```

```
 \begin{split} & [\mathtt{satList\_conj}] \\ & \vdash \forall \, l_1 \ l_2 \ M \ Oi \ Os. \\ & \quad (M,Oi,Os) \ \mathtt{satList} \ l_1 \ \land \ (M,Oi,Os) \ \mathtt{satList} \ l_2 \ \Longleftrightarrow \\ & \quad (M,Oi,Os) \ \mathtt{satList} \ (l_1 \ ++ \ l_2) \\ & [\mathtt{satList\_cons}] \\ & \vdash \forall \, h \ t \ M \ Oi \ Os. \\ & \quad (M,Oi,Os) \ \mathtt{satList} \ (h::t) \ \Longleftrightarrow \\ & \quad (M,Oi,Os) \ \mathtt{satList} \ (h::t) \ \Longleftrightarrow \\ & \quad (M,Oi,Os) \ \mathtt{satList} \ (l_1 \ ++ \ l_2) \\ & [\mathtt{satList\_nil}] \\ & \vdash \ (M,Oi,Os) \ \mathtt{satList} \ [] \end{aligned}
```

### 5 ssmPB Theory

**Built:** 13 May 2018

Parent Theories: PBType, ssm11, OMNIType

#### 5.1 Definitions

SSMPB THEORY Theorems

#### 5.2 Theorems

```
[authenticationTest_cmd_reject_lemma]
 \vdash \forall cmd. \neg authenticationTest (prop (SOME cmd))
authenticationTest_def
 \vdash (authenticationTest (Name PlatoonLeader says prop cmd) \iff
     T) \land (authenticationTest TT \iff F) \land
    (authenticationTest FF \iff F) \land
    (authenticationTest (prop v) \iff F) \land
    (authenticationTest (notf v_1) \iff F) \land
    (authenticationTest (v_2 andf v_3) \iff F) \wedge
    (authenticationTest (v_4 orf v_5) \iff F) \land
    (authenticationTest (v_6 impf v_7) \iff F) \land
    (authenticationTest (v_8 eqf v_9) \iff F) \land
    (authenticationTest (v_{10} says TT) \iff F) \wedge
    (authenticationTest (v_{10} says FF) \iff F) \wedge
    (authenticationTest (v133 meet v134 says prop v_{66}) \iff F) \land
    (authenticationTest (v135 quoting v136 says prop v_{66}) \iff F) \land
    (authenticationTest (v_{10} says notf v_{67}) \iff F) \land
    (authenticationTest (v_{10} says (v_{68} andf v_{69})) \iff F) \land
    (authenticationTest (v_{10} says (v_{70} orf v_{71})) \iff F) \land
    (authenticationTest (v_{10} says (v_{72} impf v_{73})) \iff F) \wedge
    (authenticationTest (v_{10} says (v_{74} eqf v_{75})) \iff F) \wedge
    (authenticationTest (v_{10} says v_{76} says v_{77}) \iff F) \land
    (authenticationTest (v_{10} says v_{78} speaks_for v_{79}) \iff F) \land
    (authenticationTest (v_{10} says v_{80} controls v_{81}) \iff F) \wedge
    (authenticationTest (v_{10} says reps v_{82} v_{83} v_{84}) \iff F) \land
    (authenticationTest (v_{10} says v_{85} domi v_{86}) \iff F) \land
    (authenticationTest (v_{10} says v_{87} eqi v_{88}) \iff F) \land
    (authenticationTest (v_{10} says v_{89} doms v_{90}) \iff F) \wedge
    (authenticationTest (v_{10} says v_{91} eqs v_{92}) \iff F) \wedge
    (authenticationTest (v_{10} says v_{93} eqn v_{94}) \iff F) \wedge
    (authenticationTest (v_{10} says v_{95} lte v_{96}) \iff F) \wedge
    (authenticationTest (v_{10} says v_{97} lt v_{98}) \iff F) \land
    (authenticationTest (v_{12} speaks_for v_{13}) \iff F) \wedge
    (authenticationTest (v_{14} controls v_{15}) \iff F) \wedge
    (authenticationTest (reps v_{16} v_{17} v_{18}) \iff F) \wedge
    (authenticationTest (v_{19} domi v_{20}) \iff F) \wedge
    (authenticationTest (v_{21} eqi v_{22}) \iff F) \land
    (authenticationTest (v_{23} doms v_{24}) \iff F) \wedge
    (authenticationTest (v_{25} eqs v_{26}) \iff F) \wedge
    (authenticationTest (v_{27} eqn v_{28}) \iff F) \wedge
    (authenticationTest (v_{29} lte v_{30}) \iff F) \land
    (authenticationTest (v_{31} lt v_{32}) \iff F)
authenticationTest_ind
 \vdash \forall P.
      (\forall cmd. P \text{ (Name PlatoonLeader says prop } cmd)) \land P \text{ TT } \land
```

Theorems SSMPB THEORY

```
P \text{ FF } \wedge (\forall v. P \text{ (prop } v)) \wedge (\forall v_1. P \text{ (notf } v_1)) \wedge
          (\forall v_2 \ v_3. \ P \ (v_2 \ \text{andf} \ v_3)) \ \land \ (\forall v_4 \ v_5. \ P \ (v_4 \ \text{orf} \ v_5)) \ \land
          (\forall v_6 \ v_7. \ P \ (v_6 \ \text{impf} \ v_7)) \ \land \ (\forall v_8 \ v_9. \ P \ (v_8 \ \text{eqf} \ v_9)) \ \land
          (\forall v_{10}. \ P \ (v_{10} \ \text{says TT})) \ \land \ (\forall v_{10}. \ P \ (v_{10} \ \text{says FF})) \ \land
          (\forall v133 \ v134 \ v_{66}. \ P \ (v133 \ \text{meet} \ v134 \ \text{says prop} \ v_{66})) \ \land
          (\forall\,v135\ v136\ v_{66}. P (v135 quoting v136 says prop v_{66})) \wedge
          (\forall v_{10} \ v_{67}. P (v_{10} says notf v_{67})) \land
          (\forall v_{10} \ v_{68} \ v_{69}. \ P \ (v_{10} \ \text{says} \ (v_{68} \ \text{andf} \ v_{69}))) \ \land
          (\forall v_{10} \ v_{70} \ v_{71}. \ P \ (v_{10} \ \text{says} \ (v_{70} \ \text{orf} \ v_{71}))) \land
          (\forall v_{10} \ v_{72} \ v_{73}. \ P \ (v_{10} \ \text{says} \ (v_{72} \ \text{impf} \ v_{73}))) \ \land
          (\forall v_{10} \ v_{74} \ v_{75}. \ P \ (v_{10} \ \text{says} \ (v_{74} \ \text{eqf} \ v_{75}))) \land
          (\forall v_{10} \ v_{76} \ v_{77}. \ P \ (v_{10} \ \text{says} \ v_{76} \ \text{says} \ v_{77})) \ \land
          (\forall\,v_{10}\,v_{78}\,v_{79}. P (v_{10} says v_{78} speaks_for v_{79})) \wedge
          (\forall v_{10} \ v_{80} \ v_{81}. \ P \ (v_{10} \ \text{says} \ v_{80} \ \text{controls} \ v_{81})) \ \land
          (\forall v_{10} \ v_{82} \ v_{83} \ v_{84}. P (v_{10} says reps v_{82} \ v_{83} \ v_{84})) \land
          (\forall v_{10} \ v_{85} \ v_{86}. \ P \ (v_{10} \ \text{says} \ v_{85} \ \text{domi} \ v_{86})) \ \land
          (\forall v_{10} \ v_{89} \ v_{90}. \ P \ (v_{10} \ {\tt says} \ v_{89} \ {\tt doms} \ v_{90})) \ \land
          (\forall \, v_{10} \ v_{91} \ v_{92}. P (v_{10} says v_{91} eqs v_{92})) \wedge
          (\forall v_{10} \ v_{93} \ v_{94}. \ P \ (v_{10} \ \text{says} \ v_{93} \ \text{eqn} \ v_{94})) \ \land
          (\forall v_{10} \ v_{95} \ v_{96}. P (v_{10} says v_{95} lte v_{96})) \land
          (\forall v_{10} \ v_{97} \ v_{98}. \ P \ (v_{10} \ \text{says} \ v_{97} \ \text{lt} \ v_{98})) \ \land
          (\forall v_{12} \ v_{13}. \ P \ (v_{12} \ \text{speaks\_for} \ v_{13})) \land
          (\forall v_{14} \ v_{15}. \ P \ (v_{14} \ \text{controls} \ v_{15})) \land
          (\forall v_{16} \ v_{17} \ v_{18}. \ P \ (\text{reps} \ v_{16} \ v_{17} \ v_{18})) \ \land
          (\forall v_{19} \ v_{20}. \ P \ (v_{19} \ \mathsf{domi} \ v_{20})) \ \land
          (\forall v_{21} \ v_{22}. \ P \ (v_{21} \ \text{eqi} \ v_{22})) \ \land
          (\forall v_{23} \ v_{24}. \ P \ (v_{23} \ \text{doms} \ v_{24})) \ \land
          (\forall v_{25} \ v_{26}. \ P \ (v_{25} \ \text{eqs} \ v_{26})) \ \land \ (\forall v_{27} \ v_{28}. \ P \ (v_{27} \ \text{eqn} \ v_{28})) \ \land
          (\forall v_{29} \ v_{30}. \ P \ (v_{29} \ \text{lte} \ v_{30})) \land (\forall v_{31} \ v_{32}. \ P \ (v_{31} \ \text{lt} \ v_{32})) \Rightarrow
         \forall v. P v
[PBNS_def]
  ⊢ (PBNS PLAN_PB (exec (SLc crossLD)) = MOVE_TO_ORP) ∧
      (PBNS PLAN_PB (exec (SLc incomplete)) = PLAN_PB) \(\lambda\)
      (PBNS MOVE_TO_ORP (exec (SLc conductORP)) = CONDUCT_ORP) \(\lambda\)
      (PBNS MOVE_TO_ORP (exec (SLc incomplete)) = MOVE_TO_ORP) \(\lambda\)
      (PBNS CONDUCT_ORP (exec (SLc moveToPB)) = MOVE_TO_PB) \(\lambda\)
      (PBNS CONDUCT_ORP (exec (SLc incomplete)) = CONDUCT_ORP) \(\lambda\)
      (PBNS MOVE_TO_PB (exec (SLc conductPB)) = CONDUCT_PB) \( \Lambda \)
      (PBNS MOVE_TO_PB (exec (SLc incomplete)) = MOVE_TO_PB) \(\lambda\)
      (PBNS CONDUCT_PB (exec (SLc completePB)) = COMPLETE_PB) \land
      (PBNS CONDUCT_PB (exec (SLc incomplete)) = CONDUCT_PB) \( \)
      (PBNS s (trap (SLc cmd)) = s) \land
      (PBNS s (discard (SLc cmd)) = s)
[PBNS_ind]
  \vdash \forall P.
          P PLAN_PB (exec (SLc crossLD)) \wedge
```

SSMPB THEORY Theorems

```
P PLAN_PB (exec (SLc incomplete)) \wedge
       P MOVE_TO_ORP (exec (SLc conductORP)) \wedge
      P MOVE_TO_ORP (exec (SLc incomplete)) \wedge
      P CONDUCT_ORP (exec (SLc moveToPB)) \wedge
      P CONDUCT_ORP (exec (SLc incomplete)) \wedge
      P MOVE_TO_PB (exec (SLc conductPB)) \wedge
       P MOVE_TO_PB (exec (SLc incomplete)) \wedge
       P CONDUCT_PB (exec (SLc completePB)) \wedge
      P CONDUCT_PB (exec (SLc incomplete)) \wedge
       (\forall s \ cmd. \ P \ s \ (trap \ (SLc \ cmd))) \land
       (\forall s \ v_6. \ P \ s \ (\texttt{discard} \ (\texttt{ESCc} \ v_6))) \ \land
       (\forall s \ v_9. \ P \ s \ (trap \ (ESCc \ v_9))) \land
       (\forall v_{12}. P PLAN_PB (exec (ESCc v_{12}))) \land
       P PLAN_PB (exec (SLc conductORP)) \wedge
       P PLAN_PB (exec (SLc moveToPB)) \wedge
       P PLAN_PB (exec (SLc conductPB)) \wedge
       P PLAN_PB (exec (SLc completePB)) \wedge
       (\forall v_{15}. \ P \ \texttt{MOVE\_TO\_ORP} \ (\texttt{exec} \ (\texttt{ESCc} \ v_{15}))) \ \land
       P MOVE_TO_ORP (exec (SLc crossLD)) \wedge
       P MOVE_TO_ORP (exec (SLc moveToPB)) \wedge
       P MOVE_TO_ORP (exec (SLc conductPB)) \wedge
       P MOVE_TO_ORP (exec (SLc completePB)) \wedge
       (\forall v_{18}. \ P \ \texttt{CONDUCT\_ORP} \ (\texttt{exec} \ (\texttt{ESCc} \ v_{18}))) \ \land
       P CONDUCT_ORP (exec (SLc crossLD)) \wedge
      P CONDUCT_ORP (exec (SLc conductORP)) \wedge
      P CONDUCT_ORP (exec (SLc conductPB)) \wedge
      P CONDUCT_ORP (exec (SLc completePB)) \wedge
       (\forall v_{21}. P \text{ MOVE\_TO\_PB (exec (ESCc } v_{21}))) \land
       P MOVE_TO_PB (exec (SLc crossLD)) \wedge
       P \text{ MOVE\_TO\_PB (exec (SLc conductORP))} \land
       P MOVE_TO_PB (exec (SLc moveToPB)) \land
       P MOVE_TO_PB (exec (SLc completePB)) \wedge
       (\forall v_{24}.\ P CONDUCT_PB (exec (ESCc v_{24}))) \land
       P CONDUCT_PB (exec (SLc crossLD)) \wedge
      P CONDUCT_PB (exec (SLc conductORP)) \wedge
       P CONDUCT_PB (exec (SLc moveToPB)) \wedge
       P CONDUCT_PB (exec (SLc conductPB)) \wedge
       (\forall v_{26}. \ P \ \texttt{COMPLETE\_PB} \ (\texttt{exec} \ v_{26})) \Rightarrow
      \forall v \ v_1 . \ P \ v \ v_1
[PBOut_def]
 ⊢ (PBOut PLAN_PB (exec (SLc crossLD)) = MoveToORP) ∧
    (PBOut PLAN_PB (exec (SLc incomplete)) = PlanPB) \(\lambda\)
    (PBOut MOVE_TO_ORP (exec (SLc conductORP)) = ConductORP) \( \)
    (PBOut MOVE_TO_ORP (exec (SLc incomplete)) = MoveToORP) \(\lambda\)
    (PBOut CONDUCT_ORP (exec (SLc moveToPB)) = MoveToPB) \(\lambda\)
    (PBOut CONDUCT_ORP (exec (SLc incomplete)) = ConductORP) \( \)
    (PBOut MOVE_TO_PB (exec (SLc conductPB)) = ConductPB) \(\lambda\)
```

Theorems SSMPB THEORY

```
(PBOut MOVE_TO_PB (exec (SLc incomplete)) = MoveToPB) \(\lambda\)
    (PBOut CONDUCT_PB (exec (SLc completePB)) = CompletePB) \(\lambda\)
    (PBOut CONDUCT_PB (exec (SLc incomplete)) = ConductPB) \land
    (PBOut s (trap (SLc cmd)) = unAuthorized) \land
    (PBOut s (discard (SLc cmd)) = unAuthenticated)
[PBOut_ind]
 \vdash \forall P.
       P PLAN_PB (exec (SLc crossLD)) \wedge
       P PLAN_PB (exec (SLc incomplete)) \wedge
       P MOVE_TO_ORP (exec (SLc conductORP)) \wedge
       P MOVE_TO_ORP (exec (SLc incomplete)) \wedge
       P CONDUCT_ORP (exec (SLc moveToPB)) \wedge
       P CONDUCT_ORP (exec (SLc incomplete)) \wedge
       P MOVE_TO_PB (exec (SLc conductPB)) \wedge
       P MOVE_TO_PB (exec (SLc incomplete)) \wedge
       P CONDUCT_PB (exec (SLc completePB)) \wedge
       P CONDUCT_PB (exec (SLc incomplete)) \wedge
       (\forall s \ cmd. \ P \ s \ (trap \ (SLc \ cmd))) \ \land
       (\forall s \ cmd. \ P \ s \ (discard \ (SLc \ cmd))) \ \land
       (\forall s \ v_6. \ P \ s \ (discard \ (ESCc \ v_6))) \ \land
       (\forall s \ v_9. \ P \ s \ (trap \ (ESCc \ v_9))) \ \land
       (\forall v_{12}. P PLAN_PB (exec (ESCc v_{12}))) \land
       P PLAN_PB (exec (SLc conductORP)) \wedge
       P PLAN_PB (exec (SLc moveToPB)) \wedge
       P PLAN_PB (exec (SLc conductPB)) \wedge
       P PLAN_PB (exec (SLc completePB)) \wedge
       (\forall v_{15}. \ P \ \texttt{MOVE\_TO\_ORP} \ (\texttt{exec} \ (\texttt{ESCc} \ v_{15}))) \ \land
       P MOVE_TO_ORP (exec (SLc crossLD)) \wedge
       P MOVE_TO_ORP (exec (SLc moveToPB)) \wedge
       P MOVE_TO_ORP (exec (SLc conductPB)) \land
       P MOVE_TO_ORP (exec (SLc completePB)) \wedge
       (\forall v_{18}. \ P \ \texttt{CONDUCT\_ORP} \ (\texttt{exec} \ (\texttt{ESCc} \ v_{18}))) \ \land
       P CONDUCT_ORP (exec (SLc crossLD)) \wedge
       P CONDUCT_ORP (exec (SLc conductORP)) \wedge
       P CONDUCT_ORP (exec (SLc conductPB)) \wedge
       P CONDUCT_ORP (exec (SLc completePB)) \wedge
       (\forall v_{21}.\ P MOVE_TO_PB (exec (ESCc v_{21}))) \land
       P MOVE_TO_PB (exec (SLc crossLD)) \wedge
       P MOVE_TO_PB (exec (SLc conductORP)) \wedge
       P MOVE_TO_PB (exec (SLc moveToPB)) \wedge
       P MOVE_TO_PB (exec (SLc completePB)) \wedge
       (\forall v_{24}. \ P \ \texttt{CONDUCT\_PB} \ (\texttt{exec} \ (\texttt{ESCc} \ v_{24}))) \ \land
       P CONDUCT_PB (exec (SLc crossLD)) \wedge
       P CONDUCT_PB (exec (SLc conductORP)) \wedge
       P CONDUCT_PB (exec (SLc moveToPB)) \wedge
       P CONDUCT_PB (exec (SLc conductPB)) \wedge
       (\forall v_{26}. \ P \ \texttt{COMPLETE\_PB} \ (\texttt{exec} \ v_{26})) \Rightarrow
       \forall v \ v_1 . \ P \ v \ v_1
```

```
[PlatoonLeader_exec_slCommand_justified_thm]
 \vdash \ \forall NS \ Out \ M \ Oi \ Os.
     TR (M, Oi, Os) (exec (SLc slCommand))
        (CFG authenticationTest ssmPBStateInterp
           (secContext slCommand)
           (Name PlatoonLeader says prop (SOME (SLc slCommand))::
                ins) s outs)
        (CFG authenticationTest ssmPBStateInterp
           (secContext slCommand) ins
           (NS \ s \ (exec \ (SLc \ slCommand)))
           (Out \ s \ (exec \ (SLc \ slCommand))::outs)) \iff
     authenticationTest
        (Name PlatoonLeader says prop (SOME (SLc slCommand))) \land
     CFGInterpret (M, Oi, Os)
        (CFG authenticationTest ssmPBStateInterp
           (secContext slCommand)
           (Name PlatoonLeader says prop (SOME (SLc slCommand))::
                ins) s outs) \wedge
      (M, Oi, Os) sat prop (SOME (SLc slCommand))
[PlatoonLeader_slCommand_lemma]
 \vdash CFGInterpret (M, Oi, Os)
      (CFG authenticationTest ssmPBStateInterp
         (secContext slCommand)
         (Name PlatoonLeader says prop (SOME (SLc slCommand))::
              ins) s outs) \Rightarrow
    (M, Oi, Os) sat prop (SOME (SLc slCommand))
```

# 6 PBTypeIntegrated Theory

**Built:** 13 May 2018

Parent Theories: OMNIType

## 6.1 Datatypes

```
| CONDUCT_PB | COMPLETE_PB
stateRole = PlatoonLeader | Omni
6.2
        Theorems
[omniCommand_distinct_clauses]
 \vdash ssmPlanPBComplete \neq ssmMoveToORPComplete \land
     {\tt ssmPlanPBComplete} \, \neq \, {\tt ssmConductORPComplete} \, \, \land \, \,
     {\tt ssmPlanPBComplete} \, \neq \, {\tt ssmMoveToPBComplete} \, \, \land \, \,
     {\tt ssmPlanPBComplete} \, \neq \, {\tt ssmConductPBComplete} \, \, \wedge \,
     ssmPlanPBComplete \neq invalidOmniCommand \land
     {\tt ssmMoveToORPComplete} \, \neq \, {\tt ssmConductORPComplete} \, \, \wedge \,
     {\tt ssmMoveToORPComplete} \, \neq \, {\tt ssmMoveToPBComplete} \, \, \wedge \,
     ssmMoveToORPComplete \neq ssmConductPBComplete \land
     ssmMoveToORPComplete \neq invalidOmniCommand \land
     {\tt ssmConductORPComplete} \, \neq \, {\tt ssmMoveToPBComplete} \, \, \wedge \,
     {\tt ssmConductORPComplete} \, \neq \, {\tt ssmConductPBComplete} \, \, \wedge \,
     {\tt ssmConductORPComplete} \neq {\tt invalidOmniCommand} \ \land \\
     {\tt ssmMoveToPBComplete} \, \neq \, {\tt ssmConductPBComplete} \, \, \land \, \,
     {\tt ssmMoveToPBComplete} \, \neq \, {\tt invalid0mniCommand} \, \, \land \, \,
     ssmConductPBComplete \neq invalidOmniCommand
[plCommand_distinct_clauses]
 \vdash crossLD \neq conductORP \land crossLD \neq moveToPB \land
     \texttt{crossLD} \neq \texttt{conductPB} \ \land \ \texttt{crossLD} \neq \texttt{completePB} \ \land
     \verb|crossLD| \neq \verb|incomplete| \land \verb|conductORP| \neq \verb|moveToPB| \land
     conductORP \neq conductPB \land conductORP \neq completePB \land
     \mathtt{conductORP} \, \neq \, \mathtt{incomplete} \, \, \land \, \, \mathtt{moveToPB} \, \neq \, \mathtt{conductPB} \, \, \land \, \,
     moveToPB \neq completePB \land moveToPB \neq incomplete \land
     conductPB \neq completePB \land conductPB \neq incomplete \land
     completePB \neq incomplete
[slCommand_distinct_clauses]
 \vdash \forall a' \ a. \ PL \ a \neq OMNI \ a'
[slCommand_one_one]
 \vdash (\forall a \ a'. (PL \ a = PL \ a') \iff (a = a')) \land
     \forall a \ a'. (OMNI a = OMNI \ a') \iff (a = a')
[slOutput_distinct_clauses]
 \vdash PlanPB \neq MoveToORP \land PlanPB \neq ConductORP \land
     {\tt PlanPB} \neq {\tt MoveToPB} \ \land \ {\tt PlanPB} \neq {\tt ConductPB} \ \land \\
     PlanPB \neq CompletePB \land PlanPB \neq unAuthenticated \land
     {\tt PlanPB} \, \neq \, {\tt unAuthorized} \, \wedge \, {\tt MoveToORP} \, \neq \, {\tt ConductORP} \, \wedge \,
```

 $\texttt{MoveToORP} \, \neq \, \texttt{MoveToPB} \, \wedge \, \texttt{MoveToORP} \, \neq \, \texttt{ConductPB} \, \wedge \,$ 

 $MoveToORP \neq CompletePB \land MoveToORP \neq unAuthenticated \land$ 

 $slState = PLAN_PB \mid MOVE_TO_ORP \mid CONDUCT_ORP \mid MOVE_TO_PB$ 

```
MoveToORP \neq unAuthorized \land ConductORP \neq MoveToPB \land
          \texttt{ConductORP} \, \neq \, \texttt{ConductPB} \, \wedge \, \texttt{ConductORP} \, \neq \, \texttt{CompletePB} \, \wedge \,
          {\tt ConductORP} \neq {\tt unAuthenticated} \ \land \ {\tt ConductORP} \neq {\tt unAuthorized} \ \land
          \texttt{MoveToPB} \neq \texttt{ConductPB} \ \land \ \texttt{MoveToPB} \neq \texttt{CompletePB} \ \land \\
          	exttt{MoveToPB} 
eq 	exttt{unAuthenticated} \land 	exttt{MoveToPB} 
eq 	exttt{unAuthorized} \land
          {\tt ConductPB} \, \neq \, {\tt CompletePB} \, \wedge \, {\tt ConductPB} \, \neq \, {\tt unAuthenticated} \, \wedge \,
          {\tt ConductPB} \, \neq \, {\tt unAuthorized} \, \wedge \, {\tt CompletePB} \, \neq \, {\tt unAuthenticated} \, \wedge \,
          {\tt CompletePB} \neq {\tt unAuthorized} \ \land \ {\tt unAuthenticated} \ \neq \ {\tt unAuthorized}
[slState_distinct_clauses]
   \vdash PLAN_PB \neq MOVE_TO_ORP \land PLAN_PB \neq CONDUCT_ORP \land
          PLAN_PB \neq MOVE_TO_PB \wedge PLAN_PB \neq CONDUCT_PB \wedge
          {\tt PLAN\_PB} \ \neq \ {\tt COMPLETE\_PB} \ \land \ {\tt MOVE\_TO\_ORP} \ \neq \ {\tt CONDUCT\_ORP} \ \land \\
          \texttt{MOVE\_TO\_ORP} \ \neq \ \texttt{MOVE\_TO\_PB} \ \land \ \texttt{MOVE\_TO\_ORP} \ \neq \ \texttt{CONDUCT\_PB} \ \land \\
          MOVE_TO_ORP ≠ COMPLETE_PB ∧ CONDUCT_ORP ≠ MOVE_TO_PB ∧
          {\tt CONDUCT\_ORP} \ \neq \ {\tt CONDUCT\_PB} \ \land \ {\tt CONDUCT\_ORP} \ \neq \ {\tt COMPLETE\_PB} \ \land \\
          	exttt{MOVE\_TO\_PB} 
eq 	exttt{CONDUCT\_PB} 
ightharpoonup MOVE\_TO\_PB 
eq 	exttt{COMPLETE\_PB} 
eq 	exttt{COMPLET
          CONDUCT_PB \neq COMPLETE_PB
[stateRole_distinct_clauses]
   \vdash PlatoonLeader \neq Omni
             PBIntegratedDef Theory
Built: 13 May 2018
Parent Theories: PBTypeIntegrated, aclfoundation
                Definitions
7.1
[secAuthorization_def]
   \vdash \forall xs. secAuthorization xs = secHelper (getOmniCommand xs)
[secHelper_def]
   \vdash \forall cmd.
                secHelper \ cmd =
                [Name Omni controls prop (SOME (SLc (OMNI cmd)))]
7.2
                Theorems
[getOmniCommand_def]
   ├ (get0mniCommand [] = invalid0mniCommand) ∧
          (\forall xs \ cmd.
                   get0mniCommand
                         (Name Omni controls prop (SOME (SLc (OMNI cmd)))::xs) =
                   cmd) \wedge
           (\forall xs. \text{ getOmniCommand } (TT::xs) = \text{getOmniCommand } xs) \land
```

```
(\forall xs. \text{ getOmniCommand } (FF::xs) = \text{getOmniCommand } xs) \land
(\forall xs \ v_2. \ \text{getOmniCommand (prop } v_2::xs) = \text{getOmniCommand } xs) \land
(\forall xs \ v_3. \ \text{getOmniCommand (notf} \ v_3::xs) = \text{getOmniCommand} \ xs) \ \land
(\forall xs \ v_5 \ v_4.
   getOmniCommand (v_4 andf v_5::x_5) = getOmniCommand x_5) \land
(\forall xs \ v_7 \ v_6.
   getOmniCommand (v_6 orf v_7::x_8) = getOmniCommand x_8) \land
(\forall xs \ v_9 \ v_8.
   getOmniCommand (v_8 impf v_9::x_s) = getOmniCommand x_s) \land
(\forall xs \ v_{11} \ v_{10}.
   getOmniCommand (v_{10} eqf v_{11}::xs) = getOmniCommand xs) \land
(\forall xs \ v_{13} \ v_{12}.
   getOmniCommand (v_{12} says v_{13}::xs) = getOmniCommand xs) \land
(\forall xs \ v_{15} \ v_{14}.
   getOmniCommand (v_{14} speaks_for v_{15}::xs) =
   getOmniCommand xs) \land
(\forall xs \ v_{16}.
   getOmniCommand (v_{16} controls TT::xs) =
   getOmniCommand xs) \land
(\forall xs \ v_{16}.
   getOmniCommand (v_{16} controls FF::xs) =
   getOmniCommand xs) \land
(\forall xs \ v134.
   getOmniCommand (Name v134 controls prop NONE::xs) =
   get0mniCommand xs) \land
(\forall xs \ v144.
   get0mniCommand
      (Name PlatoonLeader controls prop (SOME v144)::xs) =
   getOmniCommand xs) \land
(\forall xs \ v146.
   get0mniCommand
      (Name Omni controls prop (SOME (ESCc v146))::xs) =
   getOmniCommand xs) \land
(\forall xs \ v150.
   get0mniCommand
      (Name Omni controls prop (SOME (SLc (PL v150)))::xs) =
   getOmniCommand xs) \land
(\forall xs \ v_{68} \ v136 \ v135.
   getOmniCommand (v135 meet v136 controls prop v_{68}::xs) =
   getOmniCommand xs) \wedge
(\forall xs \ v_{68} \ v_{138} \ v_{137}.
   getOmniCommand (v137 quoting v138 controls prop v_{68}::xs) =
   getOmniCommand xs) \land
(\forall xs \ v_{69} \ v_{16}.
   getOmniCommand (v_{16} controls notf v_{69}::xs) =
   getOmniCommand xs) \land
(\forall xs \ v_{71} \ v_{70} \ v_{16}.
   getOmniCommand (v_{16} controls (v_{70} andf v_{71})::xs) =
   getOmniCommand xs) \land
```

```
(\forall xs \ v_{73} \ v_{72} \ v_{16}.
    getOmniCommand (v_{16} controls (v_{72} orf v_{73})::xs) =
    getOmniCommand xs) \land
(\forall xs \ v_{75} \ v_{74} \ v_{16}.
    getOmniCommand (v_{16} controls (v_{74} impf v_{75})::xs) =
    getOmniCommand xs) \land
(\forall xs \ v_{77} \ v_{76} \ v_{16}.
    getOmniCommand (v_{16} controls (v_{76} eqf v_{77})::xs) =
    getOmniCommand xs) \land
(\forall xs \ v_{79} \ v_{78} \ v_{16}.
    getOmniCommand (v_{16} controls v_{78} says v_{79}::xs) =
    getOmniCommand xs) \wedge
(\forall xs \ v_{81} \ v_{80} \ v_{16}.
    getOmniCommand (v_{16} controls v_{80} speaks_for v_{81}::xs) =
    getOmniCommand xs) \land
(\forall xs \ v_{83} \ v_{82} \ v_{16}.
    getOmniCommand (v_{16} controls v_{82} controls v_{83}::xs) =
    getOmniCommand xs) \land
(\forall xs \ v_{86} \ v_{85} \ v_{84} \ v_{16}.
    getOmniCommand (v_{16} controls reps v_{84} v_{85} v_{86}::xs) =
    getOmniCommand xs) \land
(\forall xs \ v_{88} \ v_{87} \ v_{16}.
    getOmniCommand (v_{16} controls v_{87} domi v_{88}::xs) =
    getOmniCommand xs) \wedge
(\forall xs \ v_{90} \ v_{89} \ v_{16}.
    getOmniCommand (v_{16} controls v_{89} eqi v_{90}::xs) =
    getOmniCommand xs) \wedge
(\forall xs \ v_{92} \ v_{91} \ v_{16}.
    getOmniCommand (v_{16} controls v_{91} doms v_{92}::xs) =
    getOmniCommand xs) \land
(\forall xs \ v_{94} \ v_{93} \ v_{16}.
    getOmniCommand (v_{16} controls v_{93} eqs v_{94}::xs) =
    getOmniCommand xs) \land
(\forall xs \ v_{96} \ v_{95} \ v_{16}.
    getOmniCommand (v_{16} controls v_{95} eqn v_{96}::xs) =
    getOmniCommand xs) \land
(\forall xs \ v_{98} \ v_{97} \ v_{16}.
    getOmniCommand (v_{16} controls v_{97} lte v_{98}::xs) =
    getOmniCommand xs) \land
(\forall xs \ v_{99} \ v_{16} \ v_{100}).
    getOmniCommand (v_{16} controls v_{99} lt v100::xs) =
    getOmniCommand xs) \land
(\forall xs \ v_{20} \ v_{19} \ v_{18}.
    getOmniCommand (reps v_{18} v_{19} v_{20}::xs) =
    getOmniCommand xs) \land
(\forall xs \ v_{22} \ v_{21}.
    getOmniCommand (v_{21} domi v_{22}::xs) = getOmniCommand xs) \land
(\forall xs \ v_{24} \ v_{23}.
    getOmniCommand (v_{23} eqi v_{24}::xs) = getOmniCommand xs) \land
```

```
(\forall xs \ v_{26} \ v_{25}.
           getOmniCommand (v_{25} doms v_{26}::xs) = getOmniCommand xs) \land
      (\forall xs \ v_{28} \ v_{27}.
           \verb"getOmniCommand" (v_{27} \verb" eqs" v_{28}{::}xs) = \verb"getOmniCommand" xs) \ \land
      (\forall xs \ v_{30} \ v_{29}.
           getOmniCommand (v_{29} eqn v_{30}::xs) = getOmniCommand xs) \land
      (\forall xs \ v_{32} \ v_{31}.
           getOmniCommand (v_{31} lte v_{32}::xs) = getOmniCommand xs) \land
     \forall xs \ v_{34} \ v_{33}.
         getOmniCommand (v_{33} lt v_{34}::xs) = getOmniCommand xs
[getOmniCommand_ind]
  \vdash \forall P.
         P [] \land
         (\forall cmd xs.
                  (Name Omni controls prop (SOME (SLc (OMNI cmd)))::
                          xs)) \land (\forall xs. P xs \Rightarrow P (TT::xs)) \land
         (\forall xs. P xs \Rightarrow P (FF::xs)) \land
         (\forall v_2 \ xs. \ P \ xs \Rightarrow P \ (prop \ v_2::xs)) \land
         (\forall v_3 \ xs. \ P \ xs \Rightarrow P \ (\texttt{notf} \ v_3::xs)) \ \land
         (\forall v_4 \ v_5 \ xs. \ P \ xs \Rightarrow P \ (v_4 \ \text{andf} \ v_5::xs)) \ \land
         (\forall v_6 \ v_7 \ xs. \ P \ xs \Rightarrow P \ (v_6 \ \text{orf} \ v_7::xs)) \ \land
         (\forall v_8 \ v_9 \ xs. \ P \ xs \Rightarrow P \ (v_8 \ \text{impf} \ v_9::xs)) \land
         (\forall v_{10} \ v_{11} \ xs. \ P \ xs \Rightarrow P \ (v_{10} \ \mathsf{eqf} \ v_{11} :: xs)) \ \land
         (\forall v_{12} \ v_{13} \ xs. \ P \ xs \Rightarrow P \ (v_{12} \ \text{says} \ v_{13}::xs)) \ \land
         (\forall v_{14} \ v_{15} \ xs. \ P \ xs \Rightarrow P \ (v_{14} \ \text{speaks\_for} \ v_{15}::xs)) \land
         (\forall v_{16} \ xs. \ P \ xs \Rightarrow P \ (v_{16} \ \text{controls TT::} xs)) \ \land
         (\forall v_{16} \ xs. \ P \ xs \Rightarrow P \ (v_{16} \ \text{controls FF}::xs)) \land
         (\forall v134 \ xs. \ P \ xs \Rightarrow P \ (Name \ v134 \ controls \ prop \ NONE::xs)) \land
         (\forall v144 xs.
              P xs \Rightarrow
              P (Name PlatoonLeader controls prop (SOME v144)::xs)) \land
         (\forall v146 \ xs.
              P xs \Rightarrow
              P (Name Omni controls prop (SOME (ESCc v146))::xs)) \land
         (\forall v150 xs.
              P xs \Rightarrow
              P
                  (Name Omni controls prop (SOME (SLc (PL v150)))::
                          xs)) \wedge
         (\forall v135 \ v136 \ v_{68} \ xs.)
              P xs \Rightarrow P (v135 \text{ meet } v136 \text{ controls prop } v_{68}::xs)) \land
         (\forall v137 \ v138 \ v_{68} \ xs.
              P xs \Rightarrow P (v137 \text{ quoting } v138 \text{ controls prop } v_{68}::xs)) \land
         (\forall v_{16} \ v_{69} \ xs. \ P \ xs \Rightarrow P \ (v_{16} \ \text{controls notf} \ v_{69}::xs)) \land
         (\forall v_{16} \ v_{70} \ v_{71} \ xs.
              P xs \Rightarrow P (v_{16} \text{ controls } (v_{70} \text{ andf } v_{71})::xs)) \land
         (\forall v_{16} \ v_{72} \ v_{73} \ xs.
```

```
P xs \Rightarrow P (v_{16} \text{ controls } (v_{72} \text{ orf } v_{73})::xs)) \land
          (\forall v_{16} \ v_{74} \ v_{75} \ xs.
                P xs \Rightarrow P (v_{16} \text{ controls } (v_{74} \text{ impf } v_{75})::xs)) \land
          (\forall v_{16} \ v_{76} \ v_{77} \ xs.)
                P \ xs \Rightarrow P \ (v_{16} \ {\tt controls} \ (v_{76} \ {\tt eqf} \ v_{77})::xs)) \ \land
          (\forall v_{16} \ v_{78} \ v_{79} \ xs.
                P xs \Rightarrow P (v_{16} \text{ controls } v_{78} \text{ says } v_{79} :: xs)) \land
          (\forall v_{16} \ v_{80} \ v_{81} \ xs.
                P xs \Rightarrow P (v_{16} \text{ controls } v_{80} \text{ speaks\_for } v_{81} :: xs)) \land
          (\forall v_{16} \ v_{82} \ v_{83} \ xs.
                P xs \Rightarrow P (v_{16} \text{ controls } v_{82} \text{ controls } v_{83} :: xs)) \land
          (\forall v_{16} \ v_{84} \ v_{85} \ v_{86} \ xs.
                P \ xs \Rightarrow P \ (v_{16} \ {\tt controls} \ {\tt reps} \ v_{84} \ v_{85} \ v_{86}{\tt ::} xs)) \ \land
          (\forall v_{16} \ v_{87} \ v_{88} \ xs.
                P xs \Rightarrow P (v_{16} \text{ controls } v_{87} \text{ domi } v_{88}::xs)) \land
          (\forall v_{16} \ v_{89} \ v_{90} \ xs.
                P xs \Rightarrow P (v_{16} \text{ controls } v_{89} \text{ eqi } v_{90} :: xs)) \land
          (\forall v_{16} \ v_{91} \ v_{92} \ xs.
                P xs \Rightarrow P (v_{16} \text{ controls } v_{91} \text{ doms } v_{92} :: xs)) \land
          (\forall v_{16} \ v_{93} \ v_{94} \ xs.
                P \ xs \Rightarrow P \ (v_{16} \ \text{controls} \ v_{93} \ \text{eqs} \ v_{94}\!::\!xs)) \ \land
          (\forall v_{16} \ v_{95} \ v_{96} \ xs.
                P xs \Rightarrow P (v_{16} \text{ controls } v_{95} \text{ eqn } v_{96}::xs)) \land
          (\forall v_{16} \ v_{97} \ v_{98} \ xs.
                P xs \Rightarrow P (v_{16} \text{ controls } v_{97} \text{ lte } v_{98}::xs)) \land
          (\forall v_{16} \ v_{99} \ v_{100} \ xs.
                P \ xs \Rightarrow P \ (v_{16} \ {\tt controls} \ v_{99} \ {\tt lt} \ v100::xs)) \ \land
          (\forall v_{18} \ v_{19} \ v_{20} \ xs. \ P \ xs \Rightarrow P \ (\texttt{reps} \ v_{18} \ v_{19} \ v_{20} :: xs)) \ \land
          (\forall v_{21} \ v_{22} \ xs. \ P \ xs \Rightarrow P \ (v_{21} \ \text{domi} \ v_{22}\!::\!xs)) \ \land
          (\forall v_{23} \ v_{24} \ xs. \ P \ xs \Rightarrow P \ (v_{23} \ \text{eqi} \ v_{24}::xs)) \land
          (\forall v_{25} \ v_{26} \ xs. \ P \ xs \Rightarrow P \ (v_{25} \ \text{doms} \ v_{26}::xs)) \land
          (\forall v_{27} \ v_{28} \ xs. \ P \ xs \Rightarrow P \ (v_{27} \ \text{eqs} \ v_{28}::xs)) \land
          (\forall v_{29} \ v_{30} \ xs. \ P \ xs \Rightarrow P \ (v_{29} \ \text{eqn} \ v_{30}{::}xs)) \ \land
          (\forall v_{31} \ v_{32} \ xs. \ P \ xs \Rightarrow P \ (v_{31} \ \text{lte} \ v_{32} :: xs)) \ \land
          (\forall v_{33} \ v_{34} \ xs. \ P \ xs \Rightarrow P \ (v_{33} \ \text{lt} \ v_{34}\!:\!:\!xs)) \Rightarrow
          \forall v. P v
[secContext_def]
  \vdash (secContext PLAN_PB (x::xs) =
        [prop (SOME (SLc (OMNI ssmPlanPBComplete))) impf
          Name PlatoonLeader controls
          prop (SOME (SLc (PL crossLD)))]) \cap 
       (secContext MOVE_TO_ORP (x::xs) =
        [prop (SOME (SLc (OMNI ssmMoveToORPComplete))) impf
          Name PlatoonLeader controls
          prop (SOME (SLc (PL conductORP)))]) \cap \big|
       (secContext CONDUCT_ORP (x::xs) =
        [prop (SOME (SLc (OMNI ssmConductORPComplete))) impf
         Name PlatoonLeader controls
```

```
prop (SOME (SLc (PL moveToPB)))]) \capsum
    (secContext MOVE_TO_PB (x::xs) =
     [prop (SOME (SLc (OMNI ssmMoveToPBComplete))) impf
      Name PlatoonLeader controls
      prop (SOME (SLc (PL conductPB)))]) \capses
    (secContext CONDUCT_PB (x::xs) =
     [prop (SOME (SLc (OMNI ssmConductPBComplete))) impf
      Name PlatoonLeader controls
      prop (SOME (SLc (PL completePB)))])
[secContext_ind]
 \vdash \forall P.
       (\forall x \ xs. \ P \ \mathtt{PLAN\_PB} \ (x::xs)) \ \land
       (\forall x \ xs. \ P \ MOVE\_TO\_ORP \ (x::xs)) \land
       (\forall x \ xs. \ P \ \texttt{CONDUCT\_ORP} \ (x::xs)) \ \land
       (\forall x \ xs. \ P \ \texttt{MOVE\_TO\_PB} \ (x::xs)) \ \land
       (\forall x \ xs. \ P \ \texttt{CONDUCT\_PB} \ (x \colon : xs)) \ \land \ (\forall \, v_4 \ . \ P \ v_4 \ []) \ \land
       (\forall v_5 \ v_6. \ P \ COMPLETE\_PB \ (v_5::v_6)) \Rightarrow
      \forall v \ v_1 . \ P \ v \ v_1
     ssmConductORP Theory
Built: 13 May 2018
Parent Theories: ConductORPType, ssm11, OMNIType
8.1
       Definitions
[secContextConductORP_def]
 \vdash \forall plcmd psgcmd incomplete.
      {\tt secContextConductORP}\ plcmd\ psgcmd\ incomplete =
       [Name PlatoonLeader controls prop (SOME (SLc (PL plcmd)));
       Name PlatoonSergeant controls
       prop (SOME (SLc (PSG psgcmd)));
       Name PlatoonLeader says
       prop (SOME (SLc (PSG psgcmd))) impf prop NONE;
       Name PlatoonSergeant says
       prop (SOME (SLc (PL plcmd))) impf prop NONE]
[ssmConductORPStateInterp_def]
 \vdash \forall slState. ssmConductORPStateInterp slState = TT
8.2
       Theorems
[authTestConductORP_cmd_reject_lemma]
```

 $\vdash \forall cmd$ .  $\neg authTestConductORP$  (prop (SOME cmd))

```
[authTestConductORP_def]
 \vdash (authTestConductORP (Name PlatoonLeader says prop cmd) \iff
    (authTestConductORP (Name PlatoonSergeant says prop cmd) \iff
     T) \land (authTestConductORP TT \iff F) \land
    (authTestConductORP FF \iff F) \land
    (authTestConductORP (prop v) \iff F) \land
    (authTestConductORP (notf v_1) \iff F) \land
    (authTestConductORP (v_2 andf v_3) \iff F) \wedge
    (authTestConductORP (v_4 orf v_5) \iff F) \wedge
    (authTestConductORP (v_6 impf v_7) \iff F) \land
    (authTestConductORP (v_8 eqf v_9) \iff F) \land
    (authTestConductORP (v_{10} says TT) \iff F) \wedge
    (authTestConductORP (v_{10} says FF) \iff F) \wedge
    (authTestConductORP (v133 meet v134 says prop v_{66}) \iff F) \land
    (authTestConductORP (v135 quoting v136 says prop v_{66}) \iff F) \land
    (authTestConductORP (v_{10} says notf v_{67}) \iff F) \wedge
    (authTestConductORP (v_{10} says (v_{68} andf v_{69})) \iff F) \wedge
    (authTestConductORP (v_{10} says (v_{70} orf v_{71})) \iff F) \land
    (authTestConductORP (v_{10} says (v_{72} impf v_{73})) \iff F) \wedge
    (authTestConductORP (v_{10} says (v_{74} eqf v_{75})) \iff F) \wedge
    (authTestConductORP (v_{10} says v_{76} says v_{77}) \iff F) \wedge
    (authTestConductORP (v_{10} says v_{78} speaks_for v_{79}) \iff F) \wedge
    (authTestConductORP (v_{10} says v_{80} controls v_{81}) \iff F) \wedge
    (authTestConductORP (v_{10} says reps v_{82} v_{83} v_{84}) \iff F) \land
    (authTestConductORP (v_{10} says v_{85} domi v_{86}) \iff F) \wedge
    (authTestConductORP (v_{10} says v_{87} eqi v_{88}) \iff F) \wedge
    (authTestConductORP (v_{10} says v_{89} doms v_{90}) \iff F) \wedge
    (authTestConductORP (v_{10} says v_{91} eqs v_{92}) \iff F) \land
    (authTestConductORP (v_{10} says v_{93} eqn v_{94}) \iff F) \wedge
    (authTestConductORP (v_{10} says v_{95} lte v_{96}) \iff F) \wedge
    (authTestConductORP (v_{10} says v_{97} lt v_{98}) \iff F) \wedge
    (authTestConductORP (v_{12} speaks_for v_{13}) \iff F) \wedge
    (authTestConductORP (v_{14} controls v_{15}) \iff F) \wedge
    (authTestConductORP (reps v_{16} v_{17} v_{18}) \iff F) \wedge
    (authTestConductORP (v_{19} domi v_{20}) \iff F) \land
    (authTestConductORP (v_{21} eqi v_{22}) \iff F) \wedge
    (authTestConductORP (v_{23} doms v_{24}) \iff F) \wedge
    (authTestConductORP (v_{25} eqs v_{26}) \iff F) \wedge
    (authTestConductORP (v_{27} eqn v_{28}) \iff F) \wedge
    (authTestConductORP (v_{29} lte v_{30}) \iff F) \wedge
    (authTestConductORP (v_{31} lt v_{32}) \iff F)
[authTestConductORP_ind]
 \vdash \forall P.
       (\forall \, cmd \, . \, P \, (\texttt{Name PlatoonLeader says prop} \, \, cmd)) \, \land \,
       (\forall \, cmd \, . \, P \, \, ({\tt Name \, PlatoonSergeant \, says \, prop \, } \, cmd)) \, \wedge \, P \, \, {\tt TT} \, \, \wedge \,
       P FF \land (\forall v. P (prop v)) \land (\forall v_1. P (notf v_1)) \land
       (\forall v_2 \ v_3. \ P \ (v_2 \ \text{andf} \ v_3)) \land (\forall v_4 \ v_5. \ P \ (v_4 \ \text{orf} \ v_5)) \land
```

```
(\forall v_6 \ v_7. \ P \ (v_6 \ \text{impf} \ v_7)) \land (\forall v_8 \ v_9. \ P \ (v_8 \ \text{eqf} \ v_9)) \land
          (\forall v_{10}. P (v_{10} \text{ says TT})) \land (\forall v_{10}. P (v_{10} \text{ says FF})) \land
          (\forall v133 \ v134 \ v_{66}. \ P \ (v133 \ \text{meet} \ v134 \ \text{says prop} \ v_{66})) \ \land
          (\forall v135 \ v136 \ v_{66}. \ P \ (v135 \ {
m quoting} \ v136 \ {
m says} \ {
m prop} \ v_{66})) \ \land
          (\forall v_{10} \ v_{67}. P (v_{10} says notf v_{67})) \land
          (\forall\,v_{10}\,v_{68}\,v_{69}. P (v_{10} says (v_{68} andf v_{69}))) \wedge
          (\forall v_{10} \ v_{70} \ v_{71}. \ P \ (v_{10} \ \text{says} \ (v_{70} \ \text{orf} \ v_{71}))) \land
          (\forall v_{10} \ v_{72} \ v_{73}. \ P \ (v_{10} \ \text{says} \ (v_{72} \ \text{impf} \ v_{73}))) \land
          (\forall v_{10} \ v_{74} \ v_{75}. \ P \ (v_{10} \ \text{says} \ (v_{74} \ \text{eqf} \ v_{75}))) \land
          (\forall v_{10} \ v_{76} \ v_{77}. \ P \ (v_{10} \ \text{says} \ v_{76} \ \text{says} \ v_{77})) \ \land
          (\forall v_{10} \ v_{78} \ v_{79}. \ P \ (v_{10} \ \text{says} \ v_{78} \ \text{speaks\_for} \ v_{79})) \ \land
          (\forall v_{10} \ v_{80} \ v_{81}. \ P \ (v_{10} \ \text{says} \ v_{80} \ \text{controls} \ v_{81})) \ \land
          (\forall v_{10} \ v_{82} \ v_{83} \ v_{84}. \ P \ (v_{10} \ \text{says reps} \ v_{82} \ v_{83} \ v_{84})) \land
          (\forall v_{10} \ v_{85} \ v_{86}. P (v_{10} says v_{85} domi v_{86})) \land
          (\forall v_{10} \ v_{87} \ v_{88}. P (v_{10} says v_{87} eqi v_{88})) \land
          (\forall v_{10} \ v_{89} \ v_{90}. \ P \ (v_{10} \ \text{says} \ v_{89} \ \text{doms} \ v_{90})) \ \land
          (\forall v_{10} \ v_{91} \ v_{92}. \ P \ (v_{10} \ \text{says} \ v_{91} \ \text{eqs} \ v_{92})) \ \land
          (\forall v_{10} \ v_{93} \ v_{94}. P (v_{10} says v_{93} eqn v_{94})) \land
          (\forall v_{10} \ v_{95} \ v_{96}. \ P \ (v_{10} \ \text{says} \ v_{95} \ \text{lte} \ v_{96})) \ \land
          (\forall v_{10} \ v_{97} \ v_{98}. \ P \ (v_{10} \ \text{says} \ v_{97} \ \text{lt} \ v_{98})) \ \land
          (\forall v_{12} \ v_{13}. \ P \ (v_{12} \ \text{speaks\_for} \ v_{13})) \ \land
          (\forall v_{14} \ v_{15}. P (v_{14} controls v_{15})) \land
          (\forall v_{16} \ v_{17} \ v_{18}. \ P \ (reps \ v_{16} \ v_{17} \ v_{18})) \ \land
          (\forall v_{19} \ v_{20}. \ P \ (v_{19} \ \text{domi} \ v_{20})) \land
          (\forall v_{21} \ v_{22}. \ P \ (v_{21} \ \text{eqi} \ v_{22})) \ \land
          (\forall v_{23} \ v_{24}. \ P \ (v_{23} \ \text{doms} \ v_{24})) \ \land
          (\forall v_{25} \ v_{26}. \ P \ (v_{25} \ \text{eqs} \ v_{26})) \ \land \ (\forall v_{27} \ v_{28}. \ P \ (v_{27} \ \text{eqn} \ v_{28})) \ \land
          (\forall v_{29} \ v_{30}. \ P \ (v_{29} \ \text{lte} \ v_{30})) \land (\forall v_{31} \ v_{32}. \ P \ (v_{31} \ \text{lt} \ v_{32})) \Rightarrow
         \forall v. P v
[conductORPNS_def]
  ├ (conductORPNS CONDUCT_ORP (exec (PL secure)) = SECURE) ∧
      (conductORPNS CONDUCT_ORP (exec (PL plIncomplete)) =
        CONDUCT_ORP) \
      (conductORPNS SECURE (exec (PSG actionsIn)) = ACTIONS_IN) \land
      (conductORPNS SECURE (exec (PSG psgIncomplete)) = SECURE) \land
       (conductORPNS ACTIONS_IN (exec (PL withdraw)) = WITHDRAW) \( \)
      (conductORPNS ACTIONS_IN (exec (PL plIncomplete)) =
       ACTIONS_IN) \
      (conductORPNS WITHDRAW (exec (PL complete)) = COMPLETE) \(\lambda\)
      (conductORPNS WITHDRAW (exec (PL plIncomplete)) = WITHDRAW) \land
      (conductORPNS s (trap (PL cmd')) = s) \land
      (conductORPNS s (trap (PSG cmd)) = s) \land
      (conductORPNS s (discard (PL cmd')) = s) \land
      (conductORPNS \ s \ (discard \ (PSG \ cmd)) = s)
[conductORPNS_ind]
  \vdash \forall P.
         P CONDUCT_ORP (exec (PL secure)) \wedge
```

```
P CONDUCT_ORP (exec (PL plIncomplete)) \wedge
      P SECURE (exec (PSG actionsIn)) \wedge
      P SECURE (exec (PSG psgIncomplete)) \wedge
      P ACTIONS_IN (exec (PL withdraw)) \wedge
      P ACTIONS_IN (exec (PL plIncomplete)) \land
      P WITHDRAW (exec (PL complete)) \wedge
      P WITHDRAW (exec (PL plIncomplete)) \wedge
      (\forall s \ cmd. \ P \ s \ (trap \ (PL \ cmd))) \land
      (\forall s \ cmd. \ P \ s \ (trap \ (PSG \ cmd))) \land
      (\forall s \ cmd. \ P \ s \ (discard \ (PL \ cmd))) \land
      (\forall s \ cmd. \ P \ s \ (\texttt{discard} \ (\texttt{PSG} \ cmd))) \ \land
      P CONDUCT_ORP (exec (PL withdraw)) \wedge
      P CONDUCT_ORP (exec (PL complete)) \wedge
      (\forall v_{11}. P CONDUCT_ORP (exec (PSG v_{11}))) \land
      (\forall v_{13}. P SECURE (exec (PL v_{13}))) \land
      P ACTIONS_IN (exec (PL secure)) \wedge
      P ACTIONS_IN (exec (PL complete)) \wedge
      (\forall v_{17}. \ P \ ACTIONS_IN \ (exec \ (PSG \ v_{17}))) \land
      P WITHDRAW (exec (PL secure)) \wedge
      P WITHDRAW (exec (PL withdraw)) \wedge
      (\forall v_{20}. \ P \ \text{WITHDRAW} \ (\text{exec (PSG} \ v_{20}))) \ \land
      (\forall v_{21}. \ P \ \texttt{COMPLETE} \ (\texttt{exec} \ v_{21})) \Rightarrow
      \forall v \ v_1 . \ P \ v \ v_1
[conductORPOut_def]
 \vdash (conductORPOut CONDUCT_ORP (exec (PL secure)) = Secure) \land
    (conductORPOut CONDUCT_ORP (exec (PL plincomplete)) =
     ConductORP) ∧
    (conductORPOut SECURE (exec (PSG actionsIn)) = ActionsIn) \( \)
    (conductORPOut SECURE (exec (PSG psgIncomplete)) = Secure) \( \lambda \)
    (conductORPOut ACTIONS_IN (exec (PL withdraw)) = Withdraw) \( \lambda \)
    (conductORPOut ACTIONS_IN (exec (PL plIncomplete)) =
     ActionsIn) \( \)
    (conductORPOut WITHDRAW (exec (PL complete)) = Complete) \( \)
    (conductORPOut WITHDRAW (exec (PL plIncomplete)) =
    (conductORPOut s (trap (PL cmd')) = unAuthorized) \land
    (conductORPOut s (trap (PSG cmd)) = unAuthorized) \land
    (conductORPOut s (discard (PL cmd')) = unAuthenticated) \land
    (conductORPOut s (discard (PSG cmd)) = unAuthenticated)
[conductORPOut_ind]
 \vdash \forall P.
      P CONDUCT_ORP (exec (PL secure)) \wedge
      P CONDUCT_ORP (exec (PL plIncomplete)) \wedge
      P SECURE (exec (PSG actionsIn)) \wedge
      P SECURE (exec (PSG psgIncomplete)) \wedge
      P ACTIONS_IN (exec (PL withdraw)) \wedge
      P ACTIONS_IN (exec (PL plIncomplete)) \wedge
```

```
P WITHDRAW (exec (PL complete)) \wedge
      P WITHDRAW (exec (PL plIncomplete)) \wedge
      (\forall s \ cmd. \ P \ s \ (trap \ (PL \ cmd))) \ \land
       (\forall s \ cmd. \ P \ s \ (trap \ (PSG \ cmd))) \ \land
       (\forall s \ cmd. \ P \ s \ (\texttt{discard} \ (\texttt{PL} \ cmd))) \ \land
       (\forall s \ cmd. \ P \ s \ (\texttt{discard} \ (\texttt{PSG} \ cmd))) \ \land
      P CONDUCT_ORP (exec (PL withdraw)) \wedge
      P CONDUCT_ORP (exec (PL complete)) \wedge
       (\forall v_{11}. P CONDUCT_ORP (exec (PSG <math>v_{11}))) \land
       (\forall v_{13}. P SECURE (exec (PL <math>v_{13}))) \land
      P ACTIONS_IN (exec (PL secure)) \wedge
      P ACTIONS_IN (exec (PL complete)) \wedge
       (\forall v_{17}. P ACTIONS_{IN} (exec (PSG <math>v_{17}))) \land
       P WITHDRAW (exec (PL secure)) \wedge
      P WITHDRAW (exec (PL withdraw)) \wedge
      (\forall v_{20}. P WITHDRAW (exec (PSG v_{20}))) \wedge
       (\forall v_{21}. \ P \ \texttt{COMPLETE} \ (\texttt{exec} \ v_{21})) \Rightarrow
      \forall v \ v_1 . \ P \ v \ v_1
[PlatoonLeader_exec_plCommand_justified_thm]
 \vdash \ \forall NS \ Out \ M \ Oi \ Os.
      TR (M, Oi, Os) (exec (SLc (PL plCommand)))
         (CFG authTestConductORP ssmConductORPStateInterp
             (secContextConductORP plCommand psqCommand incomplete)
             (Name PlatoonLeader says
              prop (SOME (SLc (PL plCommand)))::ins) s outs)
         ({\tt CFG}\ auth{\tt TestConductORP}\ {\tt ssmConductORPStateInterp}
             (secContextConductORP \ plCommand \ psgCommand \ incomplete)
             ins (NS s (exec (SLc (PL plCommand))))
             (Out \ s \ (exec \ (SLc \ (PL \ plCommand)))::outs)) \iff
      authTestConductORP
         (Name PlatoonLeader says
          prop (SOME (SLc (PL plCommand)))) \cap

      CFGInterpret (M, Oi, Os)
         (CFG authTestConductORP ssmConductORPStateInterp
             (secContextConductORP plCommand psgCommand incomplete)
             (Name PlatoonLeader says
              prop (SOME (SLc (PL plCommand)))::ins) s outs) \land
       (M,Oi,Os) sat prop (SOME (SLc (PL plCommand)))
[PlatoonLeader_plCommand_lemma]
 \vdash CFGInterpret (M, Oi, Os)
       (CFG authTestConductORP ssmConductORPStateInterp
          (secContextConductORP plCommand psgCommand incomplete)
          (Name PlatoonLeader says
           prop (SOME (SLc (PL plCommand)))::ins) s outs) \Rightarrow
    (M, Oi, Os) sat prop (SOME (SLc (PL plCommand)))
```

```
PlatoonSergeant_exec_psgCommand_justified_thm
 \vdash \forall NS \ Out \ M \ Oi \ Os.
     TR (M, Oi, Os) (exec (SLc (PSG psgCommand)))
        (CFG authTestConductORP ssmConductORPStateInterp
           (secContextConductORP plCommand psgCommand incomplete)
           (Name PlatoonSergeant says
           prop (SOME (SLc (PSG psgCommand)))::ins) s outs)
        (CFG authTestConductORP ssmConductORPStateInterp
           (\verb"secContextConductORP" plCommand psgCommand incomplete)
           ins (NS s (exec (SLc (PSG psgCommand))))
           (Out \ s \ (exec \ (SLc \ (PSG \ psgCommand)))::outs)) \iff
     authTestConductORP
        (Name PlatoonSergeant says
        prop (SOME (SLc (PSG psgCommand)))) \land
     CFGInterpret (M, Oi, Os)
        (CFG authTestConductORP ssmConductORPStateInterp
           (\verb|secContextConductORP|| plCommand|| psgCommand|| incomplete)
           (Name PlatoonSergeant says
           prop (SOME (SLc (PSG psgCommand)))::ins) s outs) \land
     (M, Oi, Os) sat prop (SOME (SLc (PSG psgCommand)))
[PlatoonSergeant_psgCommand_lemma]
 \vdash CFGInterpret (M, Oi, Os)
     (CFG authTestConductORP ssmConductORPStateInterp
         (secContextConductORP plCommand psgCommand incomplete)
         (Name PlatoonSergeant says
         prop (SOME (SLc (PSG psgCommand)))::ins) s outs) \Rightarrow
   (M,Oi,Os) sat prop (SOME (SLc (PSG psgCommand)))
```

# 9 ConductORPType Theory

**Built:** 13 May 2018

Parent Theories: indexedLists, patternMatches

#### 9.1 Datatypes

```
plCommand = secure | withdraw | complete | plIncomplete

psgCommand = actionsIn | psgIncomplete

slCommand =
    PL ConductORPType$plCommand
    | PSG ConductORPType$psgCommand

slOutput = ConductORP | Secure | ActionsIn | Withdraw | Complete | unAuthenticated | unAuthorized

slState = CONDUCT_ORP | SECURE | ACTIONS_IN | WITHDRAW | COMPLETE

stateRole = PlatoonLeader | PlatoonSergeant
```

#### 9.2 Theorems

```
[plCommand_distinct_clauses]
 \vdash secure \neq withdraw \land secure \neq complete \land
     secure \neq plIncomplete \land withdraw \neq complete \land
     withdraw \neq plIncomplete \wedge complete \neq plIncomplete
[psgCommand_distinct_clauses]
 \vdash actionsIn \neq psgIncomplete
[slCommand_distinct_clauses]
 \vdash \forall a' \ a. \ PL \ a \neq PSG \ a'
[slCommand_one_one]
 \vdash (\forall a \ a'. (PL a = PL \ a') \iff (a = a')) \land
    \forall a \ a'. (PSG a = PSG \ a') \iff (a = a')
[slOutput_distinct_clauses]
 \vdash ConductORP \neq Secure \land ConductORP \neq ActionsIn \land
     \texttt{ConductORP} \neq \texttt{Withdraw} \ \land \ \texttt{ConductORP} \neq \texttt{Complete} \ \land
     {\tt ConductORP} \, \neq \, {\tt unAuthenticated} \, \wedge \, {\tt ConductORP} \, \neq \, {\tt unAuthorized} \, \wedge \,
     Secure \neq ActionsIn \wedge Secure \neq Withdraw \wedge Secure \neq Complete \wedge
     Secure \neq unAuthenticated \wedge Secure \neq unAuthorized \wedge
     ActionsIn \neq Withdraw \wedge ActionsIn \neq Complete \wedge
     ActionsIn \neq unAuthenticated \wedge ActionsIn \neq unAuthorized \wedge
     Withdraw \neq Complete \wedge Withdraw \neq unAuthenticated \wedge
     Withdraw \neq unAuthorized \wedge Complete \neq unAuthenticated \wedge
     {\tt Complete} \neq {\tt unAuthorized} \ \land \ {\tt unAuthenticated} \neq {\tt unAuthorized}
[slRole_distinct_clauses]
 ⊢ PlatoonLeader ≠ PlatoonSergeant
[slState_distinct_clauses]
 \vdash CONDUCT_ORP \neq SECURE \land CONDUCT_ORP \neq ACTIONS_IN \land
     {\tt CONDUCT\_ORP} \ \neq \ {\tt WITHDRAW} \ \land \ {\tt CONDUCT\_ORP} \ \neq \ {\tt COMPLETE} \ \land
     \mathtt{SECURE} \neq \mathtt{ACTIONS\_IN} \ \land \ \mathtt{SECURE} \neq \mathtt{WITHDRAW} \ \land \ \mathtt{SECURE} \neq \mathtt{COMPLETE} \ \land
     ACTIONS_IN \neq WITHDRAW \wedge ACTIONS_IN \neq COMPLETE \wedge
     WITHDRAW \neq COMPLETE
```

# 10 ssmConductPB Theory

**Built:** 13 May 2018

Parent Theories: ConductPBType, ssm11, OMNIType

#### 10.1 Definitions

```
[secContextConductPB_def]
 \vdash \forall plcmd psgcmd incomplete.
      {\tt secContextConductPB}\ plcmd\ psgcmd\ incomplete =
      [Name PlatoonLeader controls prop (SOME (SLc (PL plcmd)));
       Name PlatoonSergeant controls
       prop (SOME (SLc (PSG psgcmd)));
       Name PlatoonLeader says
       prop (SOME (SLc (PSG psgcmd))) impf prop NONE;
       Name PlatoonSergeant says
       prop (SOME (SLc (PL plcmd))) impf prop NONE]
[ssmConductPBStateInterp_def]
 \vdash \forall slState. ssmConductPBStateInterp slState = TT
10.2
       Theorems
[authTestConductPB_cmd_reject_lemma]
 \vdash \forall \, cmd. \neg authTestConductPB (prop (SOME cmd))
[authTestConductPB_def]
 \vdash (authTestConductPB (Name PlatoonLeader says prop cmd) \iff T) \land
    (authTestConductPB (Name PlatoonSergeant says prop cmd) \iff
    T) \land (authTestConductPB TT \iff F) \land
    (authTestConductPB FF \iff F) \land
    (authTestConductPB (prop v) \iff F) \land
    (authTestConductPB (notf v_1) \iff F) \land
    (authTestConductPB (v_2 andf v_3) \iff F) \wedge
    (authTestConductPB (v_4 orf v_5) \iff F) \land
    (authTestConductPB (v_6 impf v_7) \iff F) \wedge
    (authTestConductPB (v_8 eqf v_9) \iff F) \land
    (authTestConductPB (v_{10} says TT) \iff F) \wedge
    (authTestConductPB (v_{10} says FF) \iff F) \wedge
    (authTestConductPB (v133 meet v134 says prop v_{66}) \iff F) \land
    (authTestConductPB (v135 quoting v136 says prop v_{66}) \iff F) \land
    (authTestConductPB (v_{10} says notf v_{67}) \iff F) \wedge
    (authTestConductPB (v_{10} says (v_{68} andf v_{69})) \iff F) \land
    (authTestConductPB (v_{10} says (v_{70} orf v_{71})) \iff F) \land
    (authTestConductPB (v_{10} says (v_{72} impf v_{73})) \iff F) \land
    (authTestConductPB (v_{10} says (v_{74} eqf v_{75})) \iff F) \land
    (authTestConductPB (v_{10} says v_{76} says v_{77}) \iff F) \wedge
    (authTestConductPB (v_{10} says v_{78} speaks_for v_{79}) \iff F) \wedge
    (authTestConductPB (v_{10} says v_{80} controls v_{81}) \iff F) \wedge
    (authTestConductPB (v_{10} says reps v_{82} v_{83} v_{84}) \iff F) \wedge
    (authTestConductPB (v_{10} says v_{85} domi v_{86}) \iff F) \wedge
    (authTestConductPB (v_{10} says v_{87} eqi v_{88}) \iff F) \land
    (authTestConductPB (v_{10} says v_{89} doms v_{90}) \iff F) \wedge
```

```
(authTestConductPB (v_{10} says v_{91} eqs v_{92}) \iff F) \wedge
       (authTestConductPB (v_{10} says v_{93} eqn v_{94}) \iff F) \wedge
       (authTestConductPB (v_{10} says v_{95} lte v_{96}) \iff F) \wedge
       (authTestConductPB (v_{10} says v_{97} lt v_{98}) \iff F) \land
       (authTestConductPB (v_{12} speaks_for v_{13}) \iff F) \land
       (authTestConductPB (v_{14} controls v_{15}) \iff F) \wedge
       (authTestConductPB (reps v_{16} v_{17} v_{18}) \iff F) \wedge
       (authTestConductPB (v_{19} domi v_{20}) \iff F) \wedge
       (authTestConductPB (v_{21} eqi v_{22}) \iff F) \land
       (authTestConductPB (v_{23} doms v_{24}) \iff F) \land
       (authTestConductPB (v_{25} eqs v_{26}) \iff F) \land
       (authTestConductPB (v_{27} eqn v_{28}) \iff F) \land (authTestConductPB (v_{29} lte v_{30}) \iff F) \land
       (authTestConductPB (v_{31} lt v_{32}) \iff F)
[authTestConductPB_ind]
  \vdash \forall P.
          (\forall \, cmd \, . \, P \, \, ({\tt Name \, PlatoonLeader \, says \, prop \, } \, cmd)) \, \, \wedge \, \,
           (\forall \, cmd \, . \, P \, (\texttt{Name PlatoonSergeant says prop} \, cmd)) \, \land \, P \, \texttt{TT} \, \land \,
          P FF \land (\forall v. P (prop v)) \land (\forall v_1. P (notf v_1)) \land
           (\forall v_2 \ v_3. \ P \ (v_2 \ \text{andf} \ v_3)) \ \land \ (\forall v_4 \ v_5. \ P \ (v_4 \ \text{orf} \ v_5)) \ \land
           (\forall v_6 \ v_7. \ P \ (v_6 \ \text{impf} \ v_7)) \ \land \ (\forall v_8 \ v_9. \ P \ (v_8 \ \text{eqf} \ v_9)) \ \land
           (\forall v_{10}. \ P \ (v_{10} \ \text{says TT})) \ \land \ (\forall v_{10}. \ P \ (v_{10} \ \text{says FF})) \ \land
           (\forall\,v133\ v134\ v_{66}. P (v133\ \mathrm{meet}\ v134\ \mathrm{says}\ \mathrm{prop}\ v_{66})) \wedge
           (\forall v135 \ v136 \ v_{66}. \ P \ (v135 \ \text{quoting} \ v136 \ \text{says prop} \ v_{66})) \ \land
           (\forall v_{10} \ v_{67}. \ P \ (v_{10} \ \text{says notf} \ v_{67})) \land
           (\forall v_{10} \ v_{68} \ v_{69}. \ P \ (v_{10} \ \text{says} \ (v_{68} \ \text{andf} \ v_{69}))) \land
           (\forall v_{10} \ v_{70} \ v_{71}. \ P \ (v_{10} \ \text{says} \ (v_{70} \ \text{orf} \ v_{71}))) \land
           (\forall v_{10} \ v_{72} \ v_{73}. \ P \ (v_{10} \ \text{says} \ (v_{72} \ \text{impf} \ v_{73}))) \ \land
           (\forall v_{10} \ v_{74} \ v_{75}. \ P \ (v_{10} \ \text{says} \ (v_{74} \ \text{eqf} \ v_{75}))) \ \land
           (\forall v_{10} \ v_{76} \ v_{77}. \ P \ (v_{10} \ \text{says} \ v_{76} \ \text{says} \ v_{77})) \ \land
           (\forall v_{10} \ v_{78} \ v_{79}. P (v_{10} says v_{78} speaks_for v_{79})) \wedge
           (\forall v_{10} \ v_{80} \ v_{81}. \ P \ (v_{10} \ \text{says} \ v_{80} \ \text{controls} \ v_{81})) \ \land
           (\forall v_{10} \ v_{82} \ v_{83} \ v_{84}. \ P \ (v_{10} \ {\tt says \ reps} \ v_{82} \ v_{83} \ v_{84})) \ \land
           (\forall v_{10} \ v_{85} \ v_{86}. \ P \ (v_{10} \ {\tt says} \ v_{85} \ {\tt domi} \ v_{86})) \ \land
           (\forall v_{10} \ v_{89} \ v_{90}. \ P \ (v_{10} \ \text{says} \ v_{89} \ \text{doms} \ v_{90})) \ \land
           (\forall v_{10} \ v_{91} \ v_{92}. \ P \ (v_{10} \ {\tt says} \ v_{91} \ {\tt eqs} \ v_{92})) \ \land \ 
           (\forall v_{10} \ v_{93} \ v_{94}. \ P \ (v_{10} \ \text{says} \ v_{93} \ \text{eqn} \ v_{94})) \ \land
           (\forall v_{10} \ v_{95} \ v_{96}. \ P \ (v_{10} \ \text{says} \ v_{95} \ \text{lte} \ v_{96})) \ \land
           (\forall v_{10} \ v_{97} \ v_{98}. \ P \ (v_{10} \ \text{says} \ v_{97} \ \text{lt} \ v_{98})) \land
           (\forall v_{12} \ v_{13}. P (v_{12} speaks_for v_{13})) \land
           (\forall v_{14} \ v_{15}. P (v_{14} controls v_{15})) \land
           (\forall v_{16} \ v_{17} \ v_{18}. \ P \ (reps \ v_{16} \ v_{17} \ v_{18})) \ \land
           (\forall v_{19} \ v_{20}. P (v_{19} domi v_{20})) \land
           (\forall v_{21} \ v_{22}. \ P \ (v_{21} \ \text{eqi} \ v_{22})) \ \land
           (\forall v_{23} \ v_{24}. \ P \ (v_{23} \ \text{doms} \ v_{24})) \land
           (\forall v_{25} \ v_{26}. \ P \ (v_{25} \ \text{eqs} \ v_{26})) \land (\forall v_{27} \ v_{28}. \ P \ (v_{27} \ \text{eqn} \ v_{28})) \land
           (\forall v_{29} \ v_{30}. \ P \ (v_{29} \ \text{lte} \ v_{30})) \land (\forall v_{31} \ v_{32}. \ P \ (v_{31} \ \text{lt} \ v_{32})) \Rightarrow
```

```
\forall v. P v
[conductPBNS_def]
 \vdash (conductPBNS CONDUCT_PB (exec (PL securePB)) = SECURE_PB) \land
    (conductPBNS CONDUCT_PB (exec (PL plIncompletePB)) =
     CONDUCT_PB) \
    (conductPBNS SECURE_PB (exec (PSG actionsInPB)) =
     ACTIONS_IN_PB) ∧
    (conductPBNS SECURE_PB (exec (PSG psgIncompletePB)) =
     SECURE_PB) \
    (conductPBNS ACTIONS_IN_PB (exec (PL withdrawPB)) =
     WITHDRAW_PB) \
    (conductPBNS ACTIONS_IN_PB (exec (PL plIncompletePB)) =
     ACTIONS_IN_PB) ∧
    (conductPBNS WITHDRAW_PB (exec (PL completePB)) =
     COMPLETE_PB) ∧
    (conductPBNS WITHDRAW_PB (exec (PL plIncompletePB)) =
     WITHDRAW_PB) \land (conductPBNS s (trap (PL cmd')) = s) \land
    (conductPBNS s (trap (PSG cmd)) = s) \land
    (conductPBNS s (discard (PL cmd')) = s) \land
    (conductPBNS s (discard (PSG cmd)) = s)
[conductPBNS_ind]
 \vdash \forall P.
       P CONDUCT_PB (exec (PL securePB)) \wedge
      P CONDUCT_PB (exec (PL plIncompletePB)) \wedge
      P SECURE_PB (exec (PSG actionsInPB)) \wedge
      P SECURE_PB (exec (PSG psgIncompletePB)) \wedge
      P ACTIONS_IN_PB (exec (PL withdrawPB)) \wedge
      P ACTIONS_IN_PB (exec (PL plIncompletePB)) \wedge
      P WITHDRAW_PB (exec (PL completePB)) \wedge
      P WITHDRAW_PB (exec (PL plIncompletePB)) \wedge
       (\forall s \ cmd. \ P \ s \ (trap \ (PL \ cmd))) \ \land
       (\forall s \ cmd. \ P \ s \ (trap \ (PSG \ cmd))) \land
       (\forall s \ cmd. \ P \ s \ (\texttt{discard} \ (\texttt{PL} \ cmd))) \ \land
       (\forall s \ cmd. \ P \ s \ (\texttt{discard} \ (\texttt{PSG} \ cmd))) \ \land
       P CONDUCT_PB (exec (PL withdrawPB)) \wedge
       P CONDUCT_PB (exec (PL completePB)) \wedge
       (\forall v_{11}. P CONDUCT_{PB} (exec (PSG v_{11}))) \land
       (\forall v_{13}. \ P \ \texttt{SECURE\_PB} \ (\texttt{exec} \ (\texttt{PL} \ v_{13}))) \ \land
       P ACTIONS_IN_PB (exec (PL securePB)) \wedge
      P ACTIONS_IN_PB (exec (PL completePB)) \wedge
       (\forall v_{17}.\ P ACTIONS_IN_PB (exec (PSG v_{17}))) \land
       P WITHDRAW_PB (exec (PL securePB)) \wedge
       P WITHDRAW_PB (exec (PL withdrawPB)) \wedge
       (\forall v_{20}. \ P \ \text{WITHDRAW\_PB (exec (PSG} \ v_{20}))) \ \land
       (\forall v_{21}. \ P \ \texttt{COMPLETE\_PB} \ (\texttt{exec} \ v_{21})) \Rightarrow
      \forall v \ v_1 . \ P \ v \ v_1
```

```
[conductPBOut_def]
 ⊢ (conductPBOut CONDUCT_PB (exec (PL securePB)) = ConductPB) ∧
    (conductPBOut CONDUCT_PB (exec (PL plIncompletePB)) =
     ConductPB) ∧
    (conductPBOut SECURE_PB (exec (PSG actionsInPB)) =
     SecurePB) ∧
    (conductPBOut SECURE_PB (exec (PSG psgIncompletePB)) =
     SecurePB) ∧
    (conductPBOut ACTIONS_IN_PB (exec (PL withdrawPB)) =
     ActionsInPB) \( \)
    (conductPBOut ACTIONS_IN_PB (exec (PL plIncompletePB)) =
     ActionsInPB) \( \)
    (conductPBOut WITHDRAW_PB (exec (PL completePB)) =
     WithdrawPB) ∧
    (conductPBOut WITHDRAW_PB (exec (PL plIncompletePB)) =
     WithdrawPB) ∧
    (conductPBOut s (trap (PL cmd')) = unAuthorized) \land
    (conductPBOut s (trap (PSG cmd)) = unAuthorized) \land
    (conductPBOut s (discard (PL cmd')) = unAuthenticated) \land
    (conductPBOut s (discard (PSG cmd)) = unAuthenticated)
[conductPBOut_ind]
 \vdash \forall P.
      P CONDUCT_PB (exec (PL securePB)) \wedge
      P CONDUCT_PB (exec (PL plIncompletePB)) \wedge
      P SECURE_PB (exec (PSG actionsInPB)) \wedge
      P SECURE_PB (exec (PSG psgIncompletePB)) \wedge
      P ACTIONS_IN_PB (exec (PL withdrawPB)) \wedge
      P ACTIONS_IN_PB (exec (PL plIncompletePB)) \wedge
      P WITHDRAW_PB (exec (PL completePB)) \wedge
      P WITHDRAW_PB (exec (PL plIncompletePB)) \wedge
       (\forall s \ cmd. \ P \ s \ (trap \ (PL \ cmd))) \land
       (\forall s \ cmd. \ P \ s \ (trap \ (PSG \ cmd))) \ \land
       (\forall s \ cmd. \ P \ s \ (discard \ (PL \ cmd))) \ \land
       (\forall s \ cmd. \ P \ s \ (discard \ (PSG \ cmd))) \ \land
       P CONDUCT_PB (exec (PL withdrawPB)) \wedge
      P CONDUCT_PB (exec (PL completePB)) \wedge
       (\forall v_{11}. \ P \ \texttt{CONDUCT\_PB} \ (\texttt{exec} \ (\texttt{PSG} \ v_{11}))) \ \land
       (\forall v_{13}. \ P \ \texttt{SECURE\_PB} \ (\texttt{exec} \ (\texttt{PL} \ v_{13}))) \ \land
       P ACTIONS_IN_PB (exec (PL securePB)) \wedge
       P ACTIONS_IN_PB (exec (PL completePB)) \wedge
       (\forall v_{17}. \ P \ ACTIONS_IN_PB \ (exec \ (PSG \ v_{17}))) \land
       P WITHDRAW_PB (exec (PL securePB)) \wedge
      P WITHDRAW_PB (exec (PL withdrawPB)) \wedge
       (\forall v_{20}. \ P \ \texttt{WITHDRAW\_PB} \ (\texttt{exec} \ (\texttt{PSG} \ v_{20}))) \ \land
       (\forall v_{21}. \ P \ \texttt{COMPLETE\_PB} \ (\texttt{exec} \ v_{21})) \Rightarrow
      \forall v \ v_1 . \ P \ v \ v_1
```

```
PlatoonLeader_exec_plCommandPB_justified_thm
 \vdash \forall NS \ Out \ M \ Oi \ Os.
     TR (M, Oi, Os) (exec (SLc (PL plCommand)))
       (CFG authTestConductPB ssmConductPBStateInterp
           (secContextConductPB plCommand psgCommand incomplete)
           (Name PlatoonLeader says
           prop (SOME (SLc (PL plCommand)))::ins) s outs)
       (CFG authTestConductPB ssmConductPBStateInterp
           (secContextConductPB plCommand psgCommand incomplete)
           ins (NS s (exec (SLc (PL plCommand))))
           (Out \ s \ (exec \ (SLc \ (PL \ plCommand)))::outs)) \iff
     authTestConductPB
       (Name PlatoonLeader says
        prop (SOME (SLc (PL plCommand)))) ∧
     CFGInterpret (M, Oi, Os)
       (CFG authTestConductPB ssmConductPBStateInterp
           (secContextConductPB plCommand psqCommand incomplete)
           (Name PlatoonLeader says
           prop (SOME (SLc (PL plCommand)))::ins) s outs) \land
     (M, Oi, Os) sat prop (SOME (SLc (PL plCommand)))
[PlatoonLeader_plCommandPB_lemma]
 \vdash CFGInterpret (M, Oi, Os)
     (CFG authTestConductPB ssmConductPBStateInterp
         (secContextConductPB plCommand psqCommand incomplete)
         (Name PlatoonLeader says
         prop (SOME (SLc (PL plCommand)))::ins) s outs) \Rightarrow
   (M, Oi, Os) sat prop (SOME (SLc (PL plCommand)))
[PlatoonSergeant_exec_psgCommandPB_justified_thm]
 \vdash \ \forall \, NS \ Out \ M \ Oi \ Os.
     TR (M, Oi, Os) (exec (SLc (PSG psgCommand)))
       (CFG authTestConductPB ssmConductPBStateInterp
           (secContextConductPB plCommand psgCommand incomplete)
           (Name PlatoonSergeant says
           prop (SOME (SLc (PSG psgCommand)))::ins) s outs)
       (CFG authTestConductPB ssmConductPBStateInterp
           (secContextConductPB plCommand psgCommand incomplete)
           ins (NS s (exec (SLc (PSG psgCommand))))
           (Out \ s \ (exec \ (SLc \ (PSG \ psgCommand)))::outs)) \iff
     authTestConductPB
       (Name PlatoonSergeant says
        prop (SOME (SLc (PSG psgCommand)))) \cap \langle 
     CFGInterpret (M, Oi, Os)
       (CFG authTestConductPB ssmConductPBStateInterp
           (secContextConductPB plCommand psgCommand incomplete)
           (Name PlatoonSergeant says
           prop (SOME (SLc (PSG psgCommand)))::ins) s outs) \land
     (M, Oi, Os) sat prop (SOME (SLc (PSG psgCommand)))
```

```
[PlatoonSergeant_psgCommandPB_lemma]
 \vdash CFGInterpret (M, Oi, Os)
      (CFG authTestConductPB ssmConductPBStateInterp
          (secContextConductPB plCommand psgCommand incomplete)
         (Name PlatoonSergeant says
          prop (SOME (SLc (PSG psgCommand)))::ins) s outs) \Rightarrow
    (M, Oi, Os) sat prop (SOME (SLc (PSG psgCommand)))
11
       ConductPBType Theory
Built: 13 May 2018
Parent Theories: indexedLists, patternMatches
11.1 Datatypes
plCommandPB = securePB | withdrawPB | completePB
              | plIncompletePB
psgCommandPB = actionsInPB | psgIncompletePB
slCommand = PL plCommandPB | PSG psgCommandPB
slOutput = ConductPB | SecurePB | ActionsInPB | WithdrawPB
          | CompletePB | unAuthenticated | unAuthorized
slState = {\tt CONDUCT\_PB} \mid {\tt SECURE\_PB} \mid {\tt ACTIONS\_IN\_PB} \mid {\tt WITHDRAW\_PB}
         | COMPLETE_PB
stateRole = PlatoonLeader | PlatoonSergeant
11.2
       Theorems
[plCommandPB_distinct_clauses]
 \vdash securePB \neq withdrawPB \land securePB \neq completePB \land
    \texttt{securePB} \neq \texttt{plIncompletePB} \ \land \ \texttt{withdrawPB} \neq \texttt{completePB} \ \land \\
    withdrawPB \neq plIncompletePB \wedge completePB \neq plIncompletePB
[psgCommandPB_distinct_clauses]
 \vdash actionsInPB \neq psgIncompletePB
[slCommand_distinct_clauses]
 \vdash \ \forall \ a' \ a. PL a \neq \ \mathtt{PSG} \ a'
[slCommand_one_one]
```

 $\vdash$  ( $\forall a \ a'$ . (PL  $a = PL \ a'$ )  $\iff$  (a = a'))  $\land$   $\forall a \ a'$ . (PSG  $a = PSG \ a'$ )  $\iff$  (a = a')

[slOutput\_distinct\_clauses]

```
\vdash ConductPB \neq SecurePB \land ConductPB \neq ActionsInPB \land
     ConductPB \neq WithdrawPB \land ConductPB \neq CompletePB \land
     {\tt ConductPB} \, \neq \, {\tt unAuthenticated} \, \wedge \, {\tt ConductPB} \, \neq \, {\tt unAuthorized} \, \wedge \,
     \texttt{SecurePB} \neq \texttt{ActionsInPB} \ \land \ \texttt{SecurePB} \neq \texttt{WithdrawPB} \ \land \\
     SecurePB \neq CompletePB \wedge SecurePB \neq unAuthenticated \wedge
     \texttt{SecurePB} \neq \texttt{unAuthorized} \ \land \ \texttt{ActionsInPB} \neq \texttt{WithdrawPB} \ \land
     {\tt ActionsInPB} \neq {\tt CompletePB} \ \land \ {\tt ActionsInPB} \neq {\tt unAuthenticated} \ \land \\
     {\tt ActionsInPB} \neq {\tt unAuthorized} \ \land \ {\tt WithdrawPB} \neq {\tt CompletePB} \ \land \\
     WithdrawPB \neq unAuthenticated \wedge WithdrawPB \neq unAuthorized \wedge
     {\tt CompletePB} \neq {\tt unAuthenticated} \ \land \ {\tt CompletePB} \neq {\tt unAuthorized} \ \land \\
     unAuthenticated \neq unAuthorized
[slRole_distinct_clauses]
 ⊢ PlatoonLeader ≠ PlatoonSergeant
[slState_distinct_clauses]
 \vdash CONDUCT_PB \neq SECURE_PB \land CONDUCT_PB \neq ACTIONS_IN_PB \land
     {\tt CONDUCT\_PB} \ \neq \ {\tt WITHDRAW\_PB} \ \land \ {\tt CONDUCT\_PB} \ \neq \ {\tt COMPLETE\_PB} \ \land
     {\tt SECURE\_PB} \ \neq \ {\tt ACTIONS\_IN\_PB} \ \land \ {\tt SECURE\_PB} \ \neq \ {\tt WITHDRAW\_PB} \ \land \\
     {\tt SECURE\_PB} \ \neq \ {\tt COMPLETE\_PB} \ \land \ {\tt ACTIONS\_IN\_PB} \ \neq \ {\tt WITHDRAW\_PB} \ \land \\
     {\tt ACTIONS\_IN\_PB} \ \neq \ {\tt COMPLETE\_PB} \ \land \ {\tt WITHDRAW\_PB} \ \neq \ {\tt COMPLETE\_PB}
12
         ssmMoveToORP Theory
Built: 13 May 2018
Parent Theories: MoveToORPType, ssm11, OMNIType
12.1
          Definitions
[secContextMoveToORP_def]
 \vdash \forall cmd.
        {\tt secContextMoveToORP}\ cmd =
        [Name PlatoonLeader controls prop (SOME (SLc cmd))]
[ssmMoveToORPStateInterp_def]
 \vdash \ \forall \, state. ssmMoveToORPStateInterp state = TT
12.2
          Theorems
[authTestMoveToORP_cmd_reject_lemma]
 \vdash \ \forall \ cmd. \neg \texttt{authTestMoveToORP} (prop (SOME cmd))
```

```
[authTestMoveToORP_def]
 \vdash (authTestMoveToORP (Name PlatoonLeader says prop cmd) \iff T) \land
     (authTestMoveToORP TT \iff F) \land (authTestMoveToORP FF \iff F) \land
     (authTestMoveToORP (prop v) \iff F) \land
     (authTestMoveToORP (notf v_1) \iff F) \land
     (authTestMoveToORP (v_2 andf v_3) \iff F) \wedge
     (authTestMoveToORP (v_4 orf v_5) \iff F) \land
     (authTestMoveToORP (v_6 impf v_7) \iff F) \land
     (authTestMoveToORP (v_8 eqf v_9) \iff F) \land
    (authTestMoveToORP (v_{10} says TT) \iff F) \wedge
    (authTestMoveToORP (v_{10} says FF) \iff F) \land
    (authTestMoveToORP (v133 meet v134 says prop v_{66}) \iff F) \land
    (authTestMoveToORP (v135 quoting v136 says prop v_{66}) \iff F) \land
     (authTestMoveToORP (v_{10} says notf v_{67}) \iff F) \wedge
     (authTestMoveToORP (v_{10} says (v_{68} andf v_{69})) \iff F) \land
     (authTestMoveToORP (v_{10} says (v_{70} orf v_{71})) \iff F) \land
     (authTestMoveToORP (v_{10} says (v_{72} impf v_{73})) \iff F) \wedge
     (authTestMoveToORP (v_{10} says (v_{74} eqf v_{75})) \iff F) \wedge
     (authTestMoveToORP (v_{10} says v_{76} says v_{77}) \iff F) \land
     (authTestMoveToORP (v_{10} says v_{78} speaks_for v_{79}) \iff F) \wedge
     (authTestMoveToORP (v_{10} says v_{80} controls v_{81}) \iff F) \wedge
     (authTestMoveToORP (v_{10} says reps v_{82} v_{83} v_{84}) \iff F) \wedge
     (authTestMoveToORP (v_{10} says v_{85} domi v_{86}) \iff F) \wedge
     (authTestMoveToORP (v_{10} says v_{87} eqi v_{88}) \iff F) \wedge
     (authTestMoveToORP (v_{10} says v_{89} doms v_{90}) \iff F) \wedge
    (authTestMoveToORP (v_{10} says v_{91} eqs v_{92}) \iff F) \wedge
     (authTestMoveToORP (v_{10} says v_{93} eqn v_{94}) \iff F) \wedge
     (authTestMoveToORP (v_{10} says v_{95} lte v_{96}) \iff F) \wedge
     (authTestMoveToORP (v_{10} says v_{97} lt v_{98}) \iff F) \wedge
     (authTestMoveToORP (v_{12} speaks_for v_{13}) \iff F) \land
     (authTestMoveToORP (v_{14} controls v_{15}) \iff F) \wedge
     (authTestMoveToORP (reps v_{16} v_{17} v_{18}) \iff F) \wedge
    (authTestMoveToORP (v_{19} domi v_{20}) \iff F) \wedge
     (authTestMoveToORP (v_{21} eqi v_{22}) \iff F) \wedge
     (authTestMoveToORP (v_{23} doms v_{24}) \iff F) \wedge
     (authTestMoveToORP (v_{25} eqs v_{26}) \iff F) \land
     (authTestMoveToORP (v_{27} eqn v_{28}) \iff F) \wedge
     (authTestMoveToORP (v_{29} lte v_{30}) \iff F) \wedge
     (authTestMoveToORP (v_{31} lt v_{32}) \iff F)
[authTestMoveToORP_ind]
 \vdash \forall P.
       (\forall \, cmd \, . \, P \, \, (\text{Name PlatoonLeader says prop} \, \, cmd)) \, \wedge \, P \, \, \text{TT} \, \wedge \,
       P FF \wedge (\forall v. P (prop v)) \wedge (\forall v_1. P (notf v_1)) \wedge
       (\forall v_2 \ v_3. \ P \ (v_2 \ \text{andf} \ v_3)) \land (\forall v_4 \ v_5. \ P \ (v_4 \ \text{orf} \ v_5)) \land
       (\forall v_6 \ v_7. \ P \ (v_6 \ \text{impf} \ v_7)) \ \land \ (\forall v_8 \ v_9. \ P \ (v_8 \ \text{eqf} \ v_9)) \ \land
       (\forall v_{10}. \ P \ (v_{10} \ \text{says TT})) \land (\forall v_{10}. \ P \ (v_{10} \ \text{says FF})) \land
       (\forall v133 \ v134 \ v_{66}. \ P \ (v133 \ \text{meet} \ v134 \ \text{says prop} \ v_{66})) \ \land
       (\forall v135 \ v136 \ v_{66}. \ P \ (v135 \ \text{quoting} \ v136 \ \text{says prop} \ v_{66})) \ \land
```

```
(\forall v_{10} \ v_{67}. \ P \ (v_{10} \ \text{says notf} \ v_{67})) \land
         (\forall v_{10} \ v_{68} \ v_{69}. \ P \ (v_{10} \ \text{says} \ (v_{68} \ \text{andf} \ v_{69}))) \ \land
         (\forall v_{10} \ v_{70} \ v_{71}. \ P \ (v_{10} \ \text{says} \ (v_{70} \ \text{orf} \ v_{71}))) \ \land
         (\forall v_{10} \ v_{72} \ v_{73}. \ P \ (v_{10} \ {\tt says} \ (v_{72} \ {\tt impf} \ v_{73}))) \ \land
         (\forall v_{10} \ v_{74} \ v_{75}. \ P \ (v_{10} \ \text{says} \ (v_{74} \ \text{eqf} \ v_{75}))) \ \land
         (\forall v_{10} \ v_{76} \ v_{77}. P (v_{10} says v_{76} says v_{77})) \land
         (\forall v_{10} \ v_{78} \ v_{79}. \ P \ (v_{10} \ \text{says} \ v_{78} \ \text{speaks\_for} \ v_{79})) \ \land
         (\forall v_{10} \ v_{80} \ v_{81}. \ P \ (v_{10} \ \text{says} \ v_{80} \ \text{controls} \ v_{81})) \ \land
         (\forall v_{10} \ v_{82} \ v_{83} \ v_{84}. \ P \ (v_{10} \ \text{says reps} \ v_{82} \ v_{83} \ v_{84})) \ \land
         (\forall v_{10} \ v_{85} \ v_{86}. \ P \ (v_{10} \ \text{says} \ v_{85} \ \text{domi} \ v_{86})) \ \land
         (\forall v_{10} \ v_{87} \ v_{88}. \ P \ (v_{10} \ \text{says} \ v_{87} \ \text{eqi} \ v_{88})) \ \land
         (\forall v_{10} \ v_{89} \ v_{90}. \ P \ (v_{10} \ \text{says} \ v_{89} \ \text{doms} \ v_{90})) \ \land
         (\forall v_{10} \ v_{91} \ v_{92}. \ P \ (v_{10} \ {\tt says} \ v_{91} \ {\tt eqs} \ v_{92})) \ \land
         (\forall v_{10} \ v_{93} \ v_{94}. P (v_{10} says v_{93} eqn v_{94})) \land
         (\forall\,v_{10}\ v_{95}\ v_{96}. P (v_{10} says v_{95} lte v_{96})) \wedge
         (\forall v_{10} \ v_{97} \ v_{98}. \ P \ (v_{10} \ \text{says} \ v_{97} \ \text{lt} \ v_{98})) \land
         (\forall v_{12} \ v_{13}. \ P \ (v_{12} \ \text{speaks\_for} \ v_{13})) \ \land
         (\forall \, v_{14} \ v_{15}. P (v_{14} controls v_{15})) \wedge
         (\forall v_{16} \ v_{17} \ v_{18}. \ P \ (\text{reps} \ v_{16} \ v_{17} \ v_{18})) \ \land
         (\forall v_{19} \ v_{20}. \ P \ (v_{19} \ \text{domi} \ v_{20})) \land
         (\forall v_{21} \ v_{22}. \ P \ (v_{21} \ \text{eqi} \ v_{22})) \ \land
         (\forall v_{23} \ v_{24}. \ P \ (v_{23} \ \text{doms} \ v_{24})) \ \land
         (\forall v_{25} \ v_{26}. \ P \ (v_{25} \ \text{eqs} \ v_{26})) \land (\forall v_{27} \ v_{28}. \ P \ (v_{27} \ \text{eqn} \ v_{28})) \land
         (\forall v_{29} \ v_{30}. \ P \ (v_{29} \ \text{lte} \ v_{30})) \land (\forall v_{31} \ v_{32}. \ P \ (v_{31} \ \text{lt} \ v_{32})) \Rightarrow
         \forall v. P v
[moveToORPNS_def]
  ⊢ (moveToORPNS MOVE_TO_ORP (exec (SLc pltForm)) = PLT_FORM) ∧
      (moveToORPNS MOVE_TO_ORP (exec (SLc incomplete)) =
       MOVE TO ORP) ∧
      (moveToORPNS PLT_FORM (exec (SLc pltMove)) = PLT_MOVE) \land
      (moveToORPNS PLT_FORM (exec (SLc incomplete)) = PLT_FORM) \(\lambda\)
      (moveToORPNS PLT_MOVE (exec (SLc pltSecureHalt)) =
       PLT_SECURE_HALT) \( \tag{ }
      (moveToORPNS PLT_MOVE (exec (SLc incomplete)) = PLT_MOVE) \(\lambda\)
      (moveToORPNS PLT_SECURE_HALT (exec (SLc complete)) =
       COMPLETE) ∧
      (moveToORPNS PLT_SECURE_HALT (exec (SLc incomplete)) =
       PLT_SECURE_HALT) \land (moveToORPNS s (trap (SLc cmd)) = s) \land
      (moveToORPNS s (discard (SLc cmd)) = s)
[moveToORPNS_ind]
  \vdash \forall P.
         P MOVE_TO_ORP (exec (SLc pltForm)) \wedge
         P MOVE_TO_ORP (exec (SLc incomplete)) \land
         P PLT_FORM (exec (SLc pltMove)) \wedge
         P PLT_FORM (exec (SLc incomplete)) \wedge
         P PLT_MOVE (exec (SLc pltSecureHalt)) \wedge
         P PLT_MOVE (exec (SLc incomplete)) \wedge
```

```
P PLT_SECURE_HALT (exec (SLc complete)) \wedge
       P PLT_SECURE_HALT (exec (SLc incomplete)) \wedge
       (\forall s \ cmd. \ P \ s \ (trap \ (SLc \ cmd))) \ \land
       (\forall s \ cmd. \ P \ s \ (\texttt{discard} \ (\texttt{SLc} \ cmd))) \ \land
       (\forall s \ v_6. \ P \ s \ (\texttt{discard} \ (\texttt{ESCc} \ v_6))) \ \land
       (\forall s \ v_9. \ P \ s \ (trap \ (ESCc \ v_9))) \land
       (\forall v_{12}. P MOVE_TO_ORP (exec (ESCc v_{12}))) \land
       P MOVE_TO_ORP (exec (SLc pltMove)) \wedge
      P MOVE_TO_ORP (exec (SLc pltSecureHalt)) \wedge
      P MOVE_TO_ORP (exec (SLc complete)) \wedge
       (\forall v_{15}.\ P\ \mathtt{PLT\_FORM}\ (\mathtt{exec}\ (\mathtt{ESCc}\ v_{15})))\ \land
      P PLT_FORM (exec (SLc pltForm)) \wedge
      P PLT_FORM (exec (SLc pltSecureHalt)) \wedge
      P PLT_FORM (exec (SLc complete)) \wedge
       (\forall v_{18}.\ P PLT_MOVE (exec (ESCc v_{18}))) \land
       P PLT_MOVE (exec (SLc pltForm)) \wedge
      P PLT_MOVE (exec (SLc pltMove)) \wedge
      P PLT_MOVE (exec (SLc complete)) \wedge
      (\forall v_{21}. \ P \ \text{PLT\_SECURE\_HALT (exec (ESCc} \ v_{21}))) \ \land
      P PLT_SECURE_HALT (exec (SLc pltForm)) \wedge
      P PLT_SECURE_HALT (exec (SLc pltMove)) \wedge
      P PLT_SECURE_HALT (exec (SLc pltSecureHalt)) \wedge
      (\forall v_{23}. \ P \ \texttt{COMPLETE} \ (\texttt{exec} \ v_{23})) \Rightarrow
      \forall v \ v_1 . \ P \ v \ v_1
[moveToORPOut_def]
 ⊢ (moveToORPOut MOVE_TO_ORP (exec (SLc pltForm)) = PLTForm) ∧
    (moveToORPOut MOVE_TO_ORP (exec (SLc incomplete)) =
     MoveToORP) ∧
    (moveToORPOut PLT_FORM (exec (SLc pltMove)) = PLTMove) \cap \)
    (moveToORPOut PLT_FORM (exec (SLc incomplete)) = PLTForm) \( \)
    (moveToORPOut PLT_MOVE (exec (SLc pltSecureHalt)) =
     PLTSecureHalt) ∧
    (moveToORPOut PLT_MOVE (exec (SLc incomplete)) = PLTMove) \( \)
    (moveToORPOut PLT_SECURE_HALT (exec (SLc complete)) =
     Complete) \( \)
    (moveToORPOut PLT_SECURE_HALT (exec (SLc incomplete)) =
     PLTSecureHalt) \wedge
    (moveToORPOut s (trap (SLc cmd)) = unAuthorized) \land
    (moveToORPOut s (discard (SLc cmd)) = unAuthenticated)
[moveToORPOut_ind]
 \vdash \forall P.
      P MOVE_TO_ORP (exec (SLc pltForm)) \wedge
      P MOVE_TO_ORP (exec (SLc incomplete)) \wedge
      P PLT_FORM (exec (SLc pltMove)) \wedge
      P PLT_FORM (exec (SLc incomplete)) \wedge
      P PLT_MOVE (exec (SLc pltSecureHalt)) \wedge
      P PLT_MOVE (exec (SLc incomplete)) \wedge
```

```
P PLT_SECURE_HALT (exec (SLc complete)) \wedge
       P PLT_SECURE_HALT (exec (SLc incomplete)) \wedge
       (\forall s \ cmd. \ P \ s \ (trap \ (SLc \ cmd))) \ \land
       (\forall s \ cmd. \ P \ s \ (\texttt{discard} \ (\texttt{SLc} \ cmd))) \ \land
       (\forall s \ v_6. \ P \ s \ (discard \ (ESCc \ v_6))) \ \land
       (\forall s \ v_9. \ P \ s \ (trap \ (ESCc \ v_9))) \ \land
       (\forall v_{12}.\ P MOVE_TO_ORP (exec (ESCc v_{12}))) \land
       P MOVE_TO_ORP (exec (SLc pltMove)) \wedge
      P MOVE_TO_ORP (exec (SLc pltSecureHalt)) \wedge
      P MOVE_TO_ORP (exec (SLc complete)) \wedge
       (\forall v_{15}. \ P \ \mathtt{PLT\_FORM} \ (\mathtt{exec} \ (\mathtt{ESCc} \ v_{15}))) \ \land
       P PLT_FORM (exec (SLc pltForm)) \wedge
       P PLT_FORM (exec (SLc pltSecureHalt)) \( \)
       P PLT_FORM (exec (SLc complete)) \wedge
       (\forall v_{18}. \ P \ \text{PLT\_MOVE} \ (\text{exec (ESCc} \ v_{18}))) \ \land
       P PLT_MOVE (exec (SLc pltForm)) \wedge
       P PLT_MOVE (exec (SLc pltMove)) \wedge
       P PLT_MOVE (exec (SLc complete)) \wedge
       (\forall v_{21}. \ P \ \text{PLT\_SECURE\_HALT (exec (ESCc} \ v_{21}))) \ \land
       P PLT_SECURE_HALT (exec (SLc pltForm)) \wedge
       P PLT_SECURE_HALT (exec (SLc pltMove)) \wedge
       P PLT_SECURE_HALT (exec (SLc pltSecureHalt)) \wedge
       (\forall v_{23}. \ P \ \texttt{COMPLETE} \ (\texttt{exec} \ v_{23})) \Rightarrow
      \forall v \ v_1 . \ P \ v \ v_1
[PlatoonLeader_exec_slCommand_justified_thm]
 \vdash \ \forall NS \ Out \ M \ Oi \ Os.
      TR (M, Oi, Os) (exec (SLc slCommand))
         (CFG authTestMoveToORP ssmMoveToORPStateInterp
             (secContextMoveToORP slCommand)
             (Name PlatoonLeader says prop (SOME (SLc slCommand))::
                   ins) s outs)
         (CFG authTestMoveToORP ssmMoveToORPStateInterp
             (secContextMoveToORP slCommand) ins
             (NS \ s (exec (SLc \ slCommand)))
             (Out \ s \ (exec \ (SLc \ slCommand))::outs)) \iff
       authTestMoveToORP
         (Name PlatoonLeader says prop (SOME (SLc slCommand))) \land
      CFGInterpret (M, Oi, Os)
         (CFG authTestMoveToORP ssmMoveToORPStateInterp
             (secContextMoveToORP slCommand)
             (Name PlatoonLeader says prop (SOME (SLc slCommand))::
                   ins) s outs) \wedge
       (M, Oi, Os) sat prop (SOME (SLc slCommand))
[PlatoonLeader_slCommand_lemma]
 \vdash CFGInterpret (M, Oi, Os)
       (CFG authTestMoveToORP ssmMoveToORPStateInterp
           (secContextMoveToORP slCommand)
```

```
(Name PlatoonLeader says prop (SOME (SLc slCommand))::
          ins) s outs) \Rightarrow
(M, Oi, Os) sat prop (SOME (SLc slCommand))
```

#### 13 MoveToORPType Theory

**Built:** 13 May 2018

Parent Theories: indexedLists, patternMatches

# 13.1 Datatypes

```
slCommand = pltForm | pltMove | pltSecureHalt | complete
            | incomplete
slOutput = MoveToORP | PLTForm | PLTMove | PLTSecureHalt
           | Complete | unAuthorized | unAuthenticated
slState = \texttt{MOVE\_TO\_ORP} \mid \texttt{PLT\_FORM} \mid \texttt{PLT\_MOVE} \mid \texttt{PLT\_SECURE\_HALT}
          | COMPLETE
stateRole = PlatoonLeader
13.2
        Theorems
[slCommand_distinct_clauses]
```

```
\vdash pltForm \neq pltMove \land pltForm \neq pltSecureHalt \land
           pltForm \neq complete \land pltForm \neq incomplete \land
           pltMove \neq pltSecureHalt \land pltMove \neq complete \land
           pltMove \neq incomplete \land pltSecureHalt \neq complete \land
           pltSecureHalt \neq incomplete \land complete \neq incomplete
[slOutput_distinct_clauses]
    \vdash MoveToORP \neq PLTForm \land MoveToORP \neq PLTMove \land
           \texttt{MoveToORP} \neq \texttt{PLTSecureHalt} \ \land \ \texttt{MoveToORP} \neq \texttt{Complete} \ \land
           {	t MoveToORP} 
eq {	t unAuthorized} \land {	t MoveToORP} 
eq {	t unAuthenticated} \land
           {\tt PLTForm} \neq {\tt PLTMove} \ \land \ {\tt PLTForm} \neq {\tt PLTSecureHalt} \ \land
           PLTForm \neq Complete \land PLTForm \neq unAuthorized \land
           {\tt PLTForm} \neq {\tt unAuthenticated} \ \land \ {\tt PLTMove} \neq {\tt PLTSecureHalt} \ \land \\
           {\tt PLTMove} \neq {\tt Complete} \ \land \ {\tt PLTMove} \neq {\tt unAuthorized} \ \land \\
          PLTMove \neq unAuthenticated \wedge PLTSecureHalt \neq Complete \wedge
          PLTSecureHalt \neq unAuthorized \land
          {\tt PLTSecureHalt} \, \neq \, {\tt unAuthenticated} \, \wedge \, {\tt Complete} \, \neq \, {\tt unAuthorized} \, \wedge \,
          {\tt Complete} \, \neq \, {\tt unAuthenticated} \, \wedge \, {\tt unAuthorized} \, \neq \, {\tt unAuthenticated}
slState_distinct_clauses
    \vdash MOVE_TO_ORP \neq PLT_FORM \land MOVE_TO_ORP \neq PLT_MOVE \land
           	exttt{MOVE\_TO\_ORP} 
eq 	exttt{PLT\_SECURE\_HALT} 
which wove\_TO\_ORP 
eq 	exttt{COMPLETE} 
which wove\_TO_ORP 
eq 	exttt{COMPLE
           {\tt PLT\_FORM} \ \neq \ {\tt PLT\_MOVE} \ \land \ {\tt PLT\_FORM} \ \neq \ {\tt PLT\_SECURE\_HALT} \ \land \\
           PLT\_FORM \neq COMPLETE \land PLT\_MOVE \neq PLT\_SECURE\_HALT \land
           PLT_MOVE ≠ COMPLETE ∧ PLT_SECURE_HALT ≠ COMPLETE
```

**Built:** 13 May 2018

# 14 ssmMoveToPB Theory

Parent Theories: MoveToPBType, ssm11, OMNIType

```
14.1
        Definitions
[secContextMoveToPB_def]
 \vdash \forall cmd.
      secContextMoveToPB \ cmd =
      [Name PlatoonLeader controls prop (SOME (SLc cmd))]
[ssmMoveToPBStateInterp_def]
 \vdash \ \forall \, state. ssmMoveToPBStateInterp state = TT
        Theorems
14.2
[authTestMoveToPB_cmd_reject_lemma]
 \vdash \forall \, cmd. \neg authTestMoveToPB (prop (SOME cmd))
[authTestMoveToPB_def]
 \vdash (authTestMoveToPB (Name PlatoonLeader says prop cmd) \iff T) \land
    (authTestMoveToPB TT \iff F) \land (authTestMoveToPB FF \iff F) \land
    (authTestMoveToPB (prop v) \iff F) \land
    (authTestMoveToPB (notf v_1) \iff F) \land
    (authTestMoveToPB (v_2 andf v_3) \iff F) \wedge
    (authTestMoveToPB (v_4 orf v_5) \iff F) \wedge
    (authTestMoveToPB (v_6 impf v_7) \iff F) \land
    (authTestMoveToPB (v_8 eqf v_9) \iff F) \land
    (authTestMoveToPB (v_{10} says TT) \iff F) \wedge
    (authTestMoveToPB (v_{10} says FF) \iff F) \wedge
    (authTestMoveToPB (v133 meet v134 says prop v_{66}) \iff F) \land
    (authTestMoveToPB (v135 quoting v136 says prop v_{66}) \iff F) \wedge
    (authTestMoveToPB (v_{10} says notf v_{67}) \iff F) \wedge
    (authTestMoveToPB (v_{10} says (v_{68} andf v_{69})) \iff F) \land
    (authTestMoveToPB (v_{10} says (v_{70} orf v_{71})) \iff F) \land
    (authTestMoveToPB (v_{10} says (v_{72} impf v_{73})) \iff F) \land
    (authTestMoveToPB (v_{10} says (v_{74} eqf v_{75})) \iff F) \land
    (authTestMoveToPB (v_{10} says v_{76} says v_{77}) \iff F) \land
    (authTestMoveToPB (v_{10} says v_{78} speaks_for v_{79}) \iff F) \wedge
    (authTestMoveToPB (v_{10} says v_{80} controls v_{81}) \iff F) \wedge
    (authTestMoveToPB (v_{10} says reps v_{82} v_{83} v_{84}) \iff F) \wedge
    (authTestMoveToPB (v_{10} says v_{85} domi v_{86}) \iff F) \wedge
    (authTestMoveToPB (v_{10} says v_{87} eqi v_{88}) \iff F) \wedge
    (authTestMoveToPB (v_{10} says v_{89} doms v_{90}) \iff F) \land
    (authTestMoveToPB (v_{10} says v_{91} eqs v_{92}) \iff F) \land
```

(authTestMoveToPB ( $v_{10}$  says  $v_{93}$  eqn  $v_{94}$ )  $\iff$  F)  $\wedge$ 

```
(authTestMoveToPB (v_{10} says v_{95} lte v_{96}) \iff F) \wedge
       (authTestMoveToPB (v_{10} says v_{97} lt v_{98}) \iff F) \wedge
       (authTestMoveToPB (v_{12} speaks_for v_{13}) \iff F) \wedge
       (authTestMoveToPB (v_{14} controls v_{15}) \iff F) \wedge
       (authTestMoveToPB (reps v_{16} v_{17} v_{18}) \iff F) \land
       (authTestMoveToPB (v_{19} domi v_{20}) \iff F) \wedge
      (authTestMoveToPB (v_{21} eqi v_{22}) \iff F) \wedge
      (authTestMoveToPB (v_{23} doms v_{24}) \iff F) \wedge
      (authTestMoveToPB (v_{25} eqs v_{26}) \iff F) \land
       (authTestMoveToPB (v_{27} eqn v_{28}) \iff F) \wedge
       (authTestMoveToPB (v_{29} lte v_{30}) \iff F) \wedge
       (authTestMoveToPB (v_{31} lt v_{32}) \iff F)
[authTestMoveToPB_ind]
  \vdash \forall P.
          (\forall \, cmd \,.\,\, P (Name PlatoonLeader says prop cmd)) \land \,\, P TT \land
          P \text{ FF } \wedge (\forall v. P \text{ (prop } v)) \wedge (\forall v_1. P \text{ (notf } v_1)) \wedge
           (\forall \ v_2 \ v_3 . P (v_2 andf v_3)) \wedge (\forall \ v_4 \ v_5 . P (v_4 orf v_5)) \wedge
           (\forall v_6 \ v_7. \ P \ (v_6 \ \text{impf} \ v_7)) \land (\forall v_8 \ v_9. \ P \ (v_8 \ \text{eqf} \ v_9)) \land
           (\forall v_{10}. \ P \ (v_{10} \ \text{says TT})) \land (\forall v_{10}. \ P \ (v_{10} \ \text{says FF})) \land
           (\forall v133 \ v134 \ v_{66}. \ P \ (v133 \ \text{meet} \ v134 \ \text{says prop} \ v_{66})) \ \land
           (\forall\,v135\ v136\ v_{66}. P (v135 quoting v136 says prop v_{66})) \wedge
           (\forall v_{10} \ v_{67}. \ P \ (v_{10} \ \text{says notf} \ v_{67})) \land
           (\forall v_{10} \ v_{68} \ v_{69}. \ P \ (v_{10} \ \text{says} \ (v_{68} \ \text{andf} \ v_{69}))) \land
           (\forall v_{10} \ v_{70} \ v_{71}. \ P \ (v_{10} \ \text{says} \ (v_{70} \ \text{orf} \ v_{71}))) \land
           (\forall v_{10} \ v_{72} \ v_{73}. \ P \ (v_{10} \ \text{says} \ (v_{72} \ \text{impf} \ v_{73}))) \ \land
           (\forall v_{10} \ v_{74} \ v_{75}. \ P \ (v_{10} \ \text{says} \ (v_{74} \ \text{eqf} \ v_{75}))) \ \land
           (\forall v_{10} \ v_{76} \ v_{77}. \ P \ (v_{10} \ \text{says} \ v_{76} \ \text{says} \ v_{77})) \ \land
           (\forall \, v_{10} \ v_{78} \ v_{79}. P (v_{10} says v_{78} speaks_for v_{79})) \wedge
           (\forall \, v_{10} \ v_{80} \ v_{81}. P (v_{10} says v_{80} controls v_{81})) \wedge
           (\forall v_{10} \ v_{82} \ v_{83} \ v_{84}. \ P \ (v_{10} \ \text{says reps} \ v_{82} \ v_{83} \ v_{84})) \ \land
           (\forall v_{10} \ v_{85} \ v_{86}. P (v_{10} says v_{85} domi v_{86})) \land
           (\forall v_{10} \ v_{87} \ v_{88}. P (v_{10} says v_{87} eqi v_{88})) \land
           (\forall v_{10} \ v_{89} \ v_{90}. \ P \ (v_{10} \ {\tt says} \ v_{89} \ {\tt doms} \ v_{90})) \ \land
           (\forall v_{10} \ v_{91} \ v_{92}. P (v_{10} says v_{91} eqs v_{92})) \land
           (\forall v_{10} \ v_{93} \ v_{94}. \ P \ (v_{10} \ \text{says} \ v_{93} \ \text{eqn} \ v_{94})) \ \land
           (\forall v_{10} \ v_{95} \ v_{96}. \ P \ (v_{10} \ {\tt says} \ v_{95} \ {\tt lte} \ v_{96})) \ \land
           (\forall v_{10} \ v_{97} \ v_{98}. \ P \ (v_{10} \ {\tt says} \ v_{97} \ {\tt lt} \ v_{98})) \ \land \ 
           (\forall v_{12} \ v_{13}. \ P \ (v_{12} \ \text{speaks\_for} \ v_{13})) \land
           (\forall v_{14} \ v_{15}. \ P \ (v_{14} \ \text{controls} \ v_{15})) \land
           (\forall v_{16} \ v_{17} \ v_{18}. \ P \ (reps \ v_{16} \ v_{17} \ v_{18})) \ \land
           (\forall v_{19} \ v_{20}. P (v_{19} domi v_{20})) \land
           (\forall v_{21} \ v_{22}. \ P \ (v_{21} \ \mathsf{eqi} \ v_{22})) \ \land
           (\forall v_{23} \ v_{24}. \ P \ (v_{23} \ \text{doms} \ v_{24})) \land
           (\forall v_{25} \ v_{26}. \ P \ (v_{25} \ \text{eqs} \ v_{26})) \ \land \ (\forall v_{27} \ v_{28}. \ P \ (v_{27} \ \text{eqn} \ v_{28})) \ \land
           (\forall v_{29} \ v_{30}. \ P \ (v_{29} \ \text{lte} \ v_{30})) \land (\forall v_{31} \ v_{32}. \ P \ (v_{31} \ \text{lt} \ v_{32})) \Rightarrow
          \forall v. P v
```

[moveToPBNS\_def]

```
⊢ (moveToPBNS MOVE_TO_PB (exec (SLc pltForm)) = PLT_FORM) ∧
    (moveToPBNS MOVE_TO_PB (exec (SLc incomplete)) =
     MOVE_TO_PB) ∧
    (moveToPBNS PLT_FORM (exec (SLc pltMove)) = PLT_MOVE) \cap \)
    (moveToPBNS PLT_FORM (exec (SLc incomplete)) = PLT_FORM) \(\lambda\)
    (moveToPBNS PLT_MOVE (exec (SLc pltHalt)) = PLT_HALT) \cap 
    (moveToPBNS PLT_MOVE (exec (SLc incomplete)) = PLT_MOVE) \cap \( \)
    (moveToPBNS PLT_HALT (exec (SLc complete)) = COMPLETE) \land
    (moveToPBNS PLT_HALT (exec (SLc incomplete)) = PLT_HALT) \cap \( \)
    (moveToPBNS s (trap (SLc cmd)) = s) \land
    (moveToPBNS s (discard (SLc cmd)) = s)
[moveToPBNS_ind]
 \vdash \forall P.
       P MOVE_TO_PB (exec (SLc pltForm)) \wedge
      P MOVE_TO_PB (exec (SLc incomplete)) \land
      P PLT_FORM (exec (SLc pltMove)) \wedge
      P PLT_FORM (exec (SLc incomplete)) \wedge
      P PLT_MOVE (exec (SLc pltHalt)) \wedge
      P PLT_MOVE (exec (SLc incomplete)) \wedge
      P PLT_HALT (exec (SLc complete)) \wedge
      P PLT_HALT (exec (SLc incomplete)) \wedge
       (\forall s \ cmd. \ P \ s \ (trap \ (SLc \ cmd))) \ \land
       (\forall s \ cmd. \ P \ s \ (\texttt{discard} \ (\texttt{SLc} \ cmd))) \ \land
       (\forall s \ v_6. \ P \ s \ (discard \ (ESCc \ v_6))) \ \land
       (\forall s \ v_9. \ P \ s \ (trap \ (ESCc \ v_9))) \ \land
       (\forall v_{12}.\ P MOVE_TO_PB (exec (ESCc v_{12}))) \land
       P MOVE_TO_PB (exec (SLc pltMove)) \wedge
      P MOVE_TO_PB (exec (SLc pltHalt)) \wedge
       P MOVE_TO_PB (exec (SLc complete)) \wedge
       (\forall v_{15}. \ P \ \mathtt{PLT\_FORM} \ (\mathtt{exec} \ (\mathtt{ESCc} \ v_{15}))) \ \land
       P PLT_FORM (exec (SLc pltForm)) \wedge
      P PLT_FORM (exec (SLc pltHalt)) \wedge
      P PLT_FORM (exec (SLc complete)) \wedge
       (\forall v_{18}.\ P PLT_MOVE (exec (ESCc v_{18}))) \land
       P PLT_MOVE (exec (SLc pltForm)) \wedge
      P PLT_MOVE (exec (SLc pltMove)) \wedge
      P PLT_MOVE (exec (SLc complete)) \wedge
       (\forall v_{21}. \ P \ PLT\_HALT \ (exec \ (ESCc \ v_{21}))) \land
      P PLT_HALT (exec (SLc pltForm)) \wedge
      P PLT_HALT (exec (SLc pltMove)) \wedge
       P PLT_HALT (exec (SLc pltHalt)) \wedge
       (\forall v_{23}. \ P \ \texttt{COMPLETE} \ (\texttt{exec} \ v_{23})) \Rightarrow
      \forall v \ v_1 . \ P \ v \ v_1
[moveToPBOut_def]
 ⊢ (moveToPBOut MOVE_TO_PB (exec (SLc pltForm)) = PLTForm) ∧
    (moveToPBOut MOVE_TO_PB (exec (SLc incomplete)) = MoveToPB) \cap \( \)
    (moveToPBOut PLT_FORM (exec (SLc pltMove)) = PLTMove) \(\lambda\)
```

```
(moveToPBOut PLT_FORM (exec (SLc incomplete)) = PLTForm) \( \)
    (moveToPBOut PLT_MOVE (exec (SLc pltHalt)) = PLTHalt) \(\lambda\)
    (moveToPBOut PLT_MOVE (exec (SLc incomplete)) = PLTMove) \( \text{\chi} \)
    (moveToPBOut PLT_HALT (exec (SLc complete)) = Complete) ^
    (moveToPBOut PLT_HALT (exec (SLc incomplete)) = PLTHalt) \(\lambda\)
    (moveToPBOut s (trap (SLc cmd)) = unAuthorized) \land
    (moveToPBOut s (discard (SLc cmd)) = unAuthenticated)
[moveToPBOut_ind]
 \vdash \forall P.
       P MOVE_TO_PB (exec (SLc pltForm)) \wedge
       P MOVE_TO_PB (exec (SLc incomplete)) \wedge
       P PLT_FORM (exec (SLc pltMove)) \wedge
       P PLT_FORM (exec (SLc incomplete)) \wedge
       P PLT_MOVE (exec (SLc pltHalt)) \wedge
       P PLT_MOVE (exec (SLc incomplete)) \wedge
       P PLT_HALT (exec (SLc complete)) \wedge
       P PLT_HALT (exec (SLc incomplete)) \wedge
       (\forall s \ cmd. \ P \ s \ (trap \ (SLc \ cmd))) \ \land
       (\forall s \ cmd. \ P \ s \ (discard \ (SLc \ cmd))) \ \land
       (\forall s \ v_6. \ P \ s \ (discard \ (ESCc \ v_6))) \land
       (\forall s \ v_9. \ P \ s \ (trap \ (ESCc \ v_9))) \land
       (\forall v_{12}. \ P \ \texttt{MOVE\_TO\_PB} \ (\texttt{exec} \ (\texttt{ESCc} \ v_{12}))) \ \land
       P MOVE_TO_PB (exec (SLc pltMove)) \wedge
       P MOVE_TO_PB (exec (SLc pltHalt)) \wedge
       P MOVE_TO_PB (exec (SLc complete)) \wedge
       (\forall v_{15}.\ P\ \mathtt{PLT\_FORM}\ (\mathtt{exec}\ (\mathtt{ESCc}\ v_{15})))\ \land
       P PLT_FORM (exec (SLc pltForm)) \wedge
       P PLT_FORM (exec (SLc pltHalt)) \wedge
       P PLT_FORM (exec (SLc complete)) \wedge
       (\forall v_{18}.\ P PLT_MOVE (exec (ESCc v_{18}))) \land
       P PLT_MOVE (exec (SLc pltForm)) \wedge
       P PLT_MOVE (exec (SLc pltMove)) \wedge
       P PLT_MOVE (exec (SLc complete)) \wedge
       (\forall v_{21}. \ P \ \text{PLT\_HALT} \ (\text{exec (ESCc} \ v_{21}))) \ \land
       P PLT_HALT (exec (SLc pltForm)) \wedge
       P PLT_HALT (exec (SLc pltMove)) \wedge
       P PLT_HALT (exec (SLc pltHalt)) \wedge
       (\forall v_{23}. \ P \ \texttt{COMPLETE} \ (\texttt{exec} \ v_{23})) \Rightarrow
      \forall v \ v_1 . \ P \ v \ v_1
[PlatoonLeader_exec_slCommand_justified_thm]
 \vdash \ \forall NS \ Out \ M \ Oi \ Os.
       TR (M, Oi, Os) (exec (SLc slCommand))
         (CFG authTestMoveToPB ssmMoveToPBStateInterp
             (secContextMoveToPB slCommand)
             (Name PlatoonLeader says prop (SOME (SLc slCommand))::
                   ins) s outs)
         (CFG authTestMoveToPB ssmMoveToPBStateInterp
```

```
(secContextMoveToPB slCommand) ins
           (NS \ s \ (exec \ (SLc \ slCommand)))
           (Out \ s \ (exec \ (SLc \ slCommand))::outs)) \iff
     authTestMoveToPB
        (Name PlatoonLeader says prop (SOME (SLc slCommand))) \land
     CFGInterpret (M, Oi, Os)
        (CFG authTestMoveToPB ssmMoveToPBStateInterp
           (secContextMoveToPB slCommand)
           (Name PlatoonLeader says prop (SOME (SLc slCommand))::
                ins) s outs) \wedge
      (M, Oi, Os) sat prop (SOME (SLc slCommand))
[PlatoonLeader_slCommand_lemma]
 \vdash CFGInterpret (M, Oi, Os)
      (CFG authTestMoveToPB ssmMoveToPBStateInterp
         ({\tt secContextMoveToPB}\ \mathit{slCommand})
         (Name PlatoonLeader says prop (SOME (SLc slCommand))::
              ins) s outs) \Rightarrow
    (M, Oi, Os) sat prop (SOME (SLc slCommand))
```

# 15 MoveToPBType Theory

**Built:** 13 May 2018

Parent Theories: indexedLists, patternMatches

### 15.1 Datatypes

### 15.2 Theorems

```
[slCommand_distinct_clauses]

⊢ pltForm ≠ pltMove ∧ pltForm ≠ pltHalt ∧ pltForm ≠ complete ∧
    pltForm ≠ incomplete ∧ pltMove ≠ pltHalt ∧
    pltMove ≠ complete ∧ pltMove ≠ incomplete ∧
    pltHalt ≠ complete ∧ pltHalt ≠ incomplete ∧
    complete ≠ incomplete
```

```
[slOutput_distinct_clauses]
  \vdash MoveToPB \neq PLTForm \land MoveToPB \neq PLTMove \land
     MoveToPB \neq PLTHalt \land MoveToPB \neq Complete \land
     	exttt{MoveToPB} 
eq 	exttt{unAuthorized} 
abla 	exttt{MoveToPB} 
eq 	exttt{unAuthenticated} 
abla 
     {\tt PLTForm} \neq {\tt PLTMove} \ \land \ {\tt PLTForm} \neq {\tt PLTHalt} \ \land \ {\tt PLTForm} \neq {\tt Complete} \ \land
     {\tt PLTForm} \neq {\tt unAuthorized} \ \land \ {\tt PLTForm} \neq {\tt unAuthenticated} \ \land
     {\tt PLTMove} \neq {\tt PLTHalt} \ \land \ {\tt PLTMove} \neq {\tt Complete} \ \land
     {\tt PLTMove} \, \neq \, {\tt unAuthorized} \, \wedge \, {\tt PLTMove} \, \neq \, {\tt unAuthenticated} \, \wedge \,
     {\tt PLTHalt} \neq {\tt Complete} \ \land \ {\tt PLTHalt} \neq {\tt unAuthorized} \ \land \\
     PLTHalt \neq unAuthenticated \wedge Complete \neq unAuthorized \wedge
     {\tt Complete} \neq {\tt unAuthenticated} \ \land \ {\tt unAuthorized} \neq {\tt unAuthenticated}
[slState_distinct_clauses]
 \vdash MOVE_TO_PB \neq PLT_FORM \land MOVE_TO_PB \neq PLT_MOVE \land
     	exttt{MOVE\_TO\_PB} \neq 	exttt{PLT\_HALT} \land 	exttt{MOVE\_TO\_PB} \neq 	exttt{COMPLETE} \land
     {\tt PLT\_FORM} \, \neq \, {\tt PLT\_MOVE} \, \wedge \, {\tt PLT\_FORM} \, \neq \, {\tt PLT\_HALT} \, \wedge \,
     \mathtt{PLT\_FORM} \neq \mathtt{COMPLETE} \ \land \ \mathtt{PLT\_MOVE} \neq \mathtt{PLT\_HALT} \ \land
     PLT\_MOVE \neq COMPLETE \land PLT\_HALT \neq COMPLETE
```

# 16 ssmPlanPB Theory

**Built:** 13 May 2018

Parent Theories: PlanPBDef, ssm

#### 16.1 Theorems

```
[inputOK_def]
```

```
\vdash (inputOK (Name PlatoonLeader says prop cmd) \iff T) \land
   (inputOK (Name PlatoonSergeant says prop cmd) \iff T) \land
   (inputOK TT \iff F) \land (inputOK FF \iff F) \land
   (inputOK (prop v) \iff F) \land (inputOK (notf v_1) \iff F) \land
   (inputOK (v_2 andf v_3) \iff F) \wedge (inputOK (v_4 orf v_5) \iff F) \wedge
   (inputOK (v_6 impf v_7) \iff F) \land (inputOK (v_8 eqf v_9) \iff F) \land
   (inputOK (v_{10} says TT) \iff F) \wedge (inputOK (v_{10} says FF) \iff F) \wedge
   (inputOK (v133 meet v134 says prop v_{66}) \iff F) \land
   (inputOK (v135 quoting v136 says prop v_{66}) \iff F) \land
   (inputOK (v_{10} says notf v_{67}) \iff F) \wedge
   (inputOK (v_{10} says (v_{68} andf v_{69})) \iff F) \land
   (inputOK (v_{10} says (v_{70} orf v_{71})) \iff F) \land
   (inputOK (v_{10} says (v_{72} impf v_{73})) \iff F) \wedge
   (inputOK (v_{10} says (v_{74} eqf v_{75})) \iff F) \land
   (inputOK (v_{10} says v_{76} says v_{77}) \iff F) \wedge
   (inputOK (v_{10} says v_{78} speaks_for v_{79}) \iff F) \wedge
   (inputOK (v_{10} says v_{80} controls v_{81}) \iff F) \wedge
   (inputOK (v_{10} says reps v_{82} v_{83} v_{84}) \iff F) \land
   (inputOK (v_{10} says v_{85} domi v_{86}) \iff F) \wedge
   (inputOK (v_{10} says v_{87} eqi v_{88}) \iff F) \wedge
```

```
(inputOK (v_{10} says v_{89} doms v_{90}) \iff F) \land
       (inputOK (v_{10} says v_{91} eqs v_{92}) \iff F) \land
       (inputOK (v_{10} says v_{93} eqn v_{94}) \iff F) \wedge
       (inputOK (v_{10} says v_{95} lte v_{96}) \iff F) \wedge
       (inputOK (v_{10} says v_{97} lt v_{98}) \iff F) \wedge
       (inputOK (v_{12} speaks_for v_{13}) \iff F) \wedge
       (inputOK (v_{14} controls v_{15}) \iff F) \wedge
       (inputOK (reps v_{16} v_{17} v_{18}) \iff F) \land
       (inputOK (v_{19} domi v_{20}) \iff F) \land
       (inputOK (v_{21} eqi v_{22}) \iff F) \wedge
       (inputOK (v_{23} doms v_{24}) \iff F) \wedge
       (inputOK (v_{25} eqs v_{26}) \iff F) \wedge (inputOK (v_{27} eqn v_{28}) \iff F) \wedge (inputOK (v_{29} lte v_{30}) \iff F) \wedge (inputOK (v_{31} lt v_{32}) \iff F)
[inputOK_ind]
  \vdash \forall P.
           (\forall \, cmd \, . \, \, P \, \, ({\tt Name \, PlatoonLeader \, says \, prop \, } \, cmd)) \, \, \wedge \, \,
           (\forall \, cmd \,.\,\, P (Name PlatoonSergeant says prop cmd)) \wedge \,\, P TT \wedge
           P \text{ FF } \wedge (\forall v. P \text{ (prop } v)) \wedge (\forall v_1. P \text{ (notf } v_1)) \wedge
           (\forall v_2 \ v_3. \ P \ (v_2 \ \text{andf} \ v_3)) \land (\forall v_4 \ v_5. \ P \ (v_4 \ \text{orf} \ v_5)) \land
           (\forall v_6 \ v_7. \ P \ (v_6 \ \text{impf} \ v_7)) \land (\forall v_8 \ v_9. \ P \ (v_8 \ \text{eqf} \ v_9)) \land
           (\forall v_{10}. \ P \ (v_{10} \ \text{says TT})) \ \land \ (\forall v_{10}. \ P \ (v_{10} \ \text{says FF})) \ \land
           (\forall\,v133\ v134\ v_{66}. P (v133 meet v134 says prop v_{66})) \wedge
           (\forall v135 \ v136 \ v_{66}. P (v135 quoting v136 says prop v_{66})) \land
           (\forall v_{10} \ v_{67}. P (v_{10} says notf v_{67})) \land
           (\forall v_{10} \ v_{68} \ v_{69}. \ P \ (v_{10} \ \text{says} \ (v_{68} \ \text{andf} \ v_{69}))) \land
           (\forall v_{10} \ v_{70} \ v_{71}. \ P \ (v_{10} \ \text{says} \ (v_{70} \ \text{orf} \ v_{71}))) \land
           (\forall v_{10} \ v_{72} \ v_{73}. \ P \ (v_{10} \ \text{says} \ (v_{72} \ \text{impf} \ v_{73}))) \ \land
           (\forall v_{10} \ v_{74} \ v_{75}. \ P \ (v_{10} \ {\tt says} \ (v_{74} \ {\tt eqf} \ v_{75}))) \ \land
           (\forall v_{10} \ v_{76} \ v_{77}. \ P \ (v_{10} \ \text{says} \ v_{76} \ \text{says} \ v_{77})) \ \land
           (\forall \, v_{10} \ v_{78} \ v_{79}. P (v_{10} says v_{78} speaks_for v_{79})) \wedge
           (\forall v_{10} \ v_{80} \ v_{81}. \ P \ (v_{10} \ \text{says} \ v_{80} \ \text{controls} \ v_{81})) \ \land
           (\forall v_{10} \ v_{82} \ v_{83} \ v_{84}. \ P \ (v_{10} \ {\tt says \ reps} \ v_{82} \ v_{83} \ v_{84})) \ \land
           (\forall v_{10} v_{85} v_{86}. P (v_{10} says v_{85} domi v_{86})) \wedge
           (\forall v_{10} \ v_{87} \ v_{88}. \ P \ (v_{10} \ {\tt says} \ v_{87} \ {\tt eqi} \ v_{88})) \ \land
           (\forall v_{10} \ v_{89} \ v_{90}. \ P \ (v_{10} \ {\tt says} \ v_{89} \ {\tt doms} \ v_{90})) \ \land
           (\forall v_{10} \ v_{91} \ v_{92}. \ P \ (v_{10} \ \text{says} \ v_{91} \ \text{eqs} \ v_{92})) \ \land
           (\forall v_{10} \ v_{93} \ v_{94}. \ P \ (v_{10} \ \text{says} \ v_{93} \ \text{eqn} \ v_{94})) \ \land
           (\forall v_{10} \ v_{95} \ v_{96}. P (v_{10} says v_{95} lte v_{96})) \land
           (\forall v_{10} \ v_{97} \ v_{98}. \ P \ (v_{10} \ \text{says} \ v_{97} \ \text{lt} \ v_{98})) \ \land
           (\forall v_{12} \ v_{13}. \ P \ (v_{12} \ \text{speaks\_for} \ v_{13})) \land
           (\forall v_{14} \ v_{15}. \ P \ (v_{14} \ \text{controls} \ v_{15})) \ \land
           (\forall v_{16} \ v_{17} \ v_{18}. \ P \ (reps \ v_{16} \ v_{17} \ v_{18})) \ \land
           (\forall v_{19} \ v_{20}. \ P \ (v_{19} \ \text{domi} \ v_{20})) \ \land
           (\forall v_{21} \ v_{22}. \ P \ (v_{21} \ \text{eqi} \ v_{22})) \ \land
           (\forall v_{23} \ v_{24}. \ P \ (v_{23} \ \text{doms} \ v_{24})) \ \land
           (\forall v_{25} \ v_{26}. \ P \ (v_{25} \ \text{eqs} \ v_{26})) \land (\forall v_{27} \ v_{28}. \ P \ (v_{27} \ \text{eqn} \ v_{28})) \land
           (\forall v_{29} \ v_{30}. \ P \ (v_{29} \ \text{lte} \ v_{30})) \land (\forall v_{31} \ v_{32}. \ P \ (v_{31} \ \text{lt} \ v_{32})) \Rightarrow
          \forall v. P v
```

```
[planPBNS_def]
 \vdash (planPBNS WARNO (exec x) =
     if
        (getRecon x = [SOME (SLc (PL recon))]) \land
        (getTenativePlan x = [SOME (SLc (PL tentativePlan))]) \land
        (getReport x = [SOME (SLc (PL report1))]) \land
        (getInitMove x = [SOME (SLc (PSG initiateMovement))])
     then
        REPORT1
     else WARNO) ∧
     (planPBNS PLAN_PB (exec x) =
     if getPlCom x = receiveMission then RECEIVE_MISSION
     else PLAN_PB) ∧
     (planPBNS RECEIVE_MISSION (exec x) =
     if getPlCom x = warno then WARNO else RECEIVE_MISSION) \wedge
     (planPBNS REPORT1 (exec x) =
     if getPlCom x = completePlan then COMPLETE_PLAN
     else REPORT1) ∧
     (planPBNS COMPLETE_PLAN (exec x) =
     if getPlCom x = opoid then OPOID else COMPLETE_PLAN) \wedge
    (planPBNS OPOID (exec x) =
     if getPlCom x = supervise then SUPERVISE else OPOID) \wedge
    (planPBNS SUPERVISE (exec x) =
     if getPlCom x = report2 then REPORT2 else SUPERVISE) \wedge
     (planPBNS REPORT2 (exec x) =
     if getPlCom x = complete then COMPLETE else REPORT2) \wedge
     (planPBNS s (trap v_0) = s) \wedge (planPBNS s (discard v_1) = s)
[planPBNS_ind]
 \vdash \forall P.
       (\forall x. \ P \ \text{WARNO (exec} \ x)) \ \land \ (\forall x. \ P \ \text{PLAN\_PB (exec} \ x)) \ \land
       (\forall x. \ P \ \text{RECEIVE\_MISSION} \ (\text{exec} \ x)) \land
       (\forall x. \ P \ \text{REPORT1 (exec} \ x)) \land (\forall x. \ P \ \text{COMPLETE\_PLAN (exec} \ x)) \land
       (\forall x. \ P \ \text{OPOID (exec} \ x)) \ \land \ (\forall x. \ P \ \text{SUPERVISE (exec} \ x)) \ \land
       (\forall x. \ P \ \texttt{REPORT2} \ (\texttt{exec} \ x)) \ \land \ (\forall s \ v_0. \ P \ s \ (\texttt{trap} \ v_0)) \ \land
       (\forall s \ v_1. \ P \ s \ (\texttt{discard} \ v_1)) \ \land
       (\forall v_6. P TENTATIVE_PLAN (exec v_6)) \land
       (\forall v_7. P INITIATE_MOVEMENT (exec v_7)) \land
       (\forall v_8. \ P \ \text{RECON (exec} \ v_8)) \land (\forall v_9. \ P \ \text{COMPLETE (exec} \ v_9)) \Rightarrow
      \forall v \ v_1 . \ P \ v \ v_1
[planPBOut_def]
 \vdash (planPBOut WARNO (exec x) =
     if
        (getRecon x = [SOME (SLc (PL recon))]) \land
        (getTenativePlan x = [SOME (SLc (PL tentativePlan))]) \land
        (getReport x = [SOME (SLc (PL report1))]) \land
        (getInitMove x = [SOME (SLc (PSG initiateMovement))])
```

```
then
        Report1
     else unAuthorized) \wedge
    (planPBOut PLAN_PB (exec x) =
     if getPlCom x = receiveMission then ReceiveMission
     else unAuthorized) ∧
    (planPBOut RECEIVE_MISSION (exec x) =
     if getPlCom x = warno then Warno else unAuthorized) \land
    (planPBOut REPORT1 (exec x) =
     if getPlCom x = completePlan then CompletePlan
     \textbf{else} \text{ unAuthorized) } \land \\
    (planPBOut COMPLETE_PLAN (exec x) =
     if getPlCom x = opoid then Opoid else unAuthorized) \wedge
    (planPBOut OPOID (exec x) =
     if getPlCom x = supervise then Supervise
     else unAuthorized) ∧
    (planPBOut SUPERVISE (exec x) =
     if getPlCom x = report2 then Report2 else unAuthorized) \land
    (planPBOut REPORT2 (exec x) =
     if getPlCom x = complete then Complete else unAuthorized) \wedge
    (planPBOut s (trap v_0) = unAuthorized) \wedge
    (planPBOut s (discard v_1) = unAuthenticated)
[planPBOut_ind]
 \vdash \forall P.
       (\forall x. \ P \ \text{WARNO (exec} \ x)) \ \land \ (\forall x. \ P \ \text{PLAN\_PB (exec} \ x)) \ \land
       (\forall x.\ P\ \texttt{RECEIVE\_MISSION} (exec x)) \land
       (\forall x.\ P\ \text{REPORT1}\ (\text{exec}\ x))\ \land\ (\forall x.\ P\ \text{COMPLETE\_PLAN}\ (\text{exec}\ x))\ \land
       (\forall x. P \text{ OPOID (exec } x)) \land (\forall x. P \text{ SUPERVISE (exec } x)) \land
       (\forall x.\ P\ \text{REPORT2 (exec }x))\ \land\ (\forall s\ v_0.\ P\ s\ (\text{trap }v_0))\ \land
       (\forall s \ v_1. \ P \ s \ (discard \ v_1)) \ \land
       (\forall \, v_6 \,.\,\,P TENTATIVE_PLAN (exec v_6)) \land
       (\forall v_7. P \text{ INITIATE\_MOVEMENT (exec } v_7)) \land
       (\forall v_8. \ P \ \text{RECON (exec} \ v_8)) \land (\forall v_9. \ P \ \text{COMPLETE (exec} \ v_9)) \Rightarrow
       \forall v \ v_1. \ P \ v \ v_1
[PlatoonLeader_notWARNO_notreport1_exec_plCommand_justified_lemma]
 \vdash s \neq \mathtt{WARNO} \Rightarrow
    plCommand \neq invalidPlCommand \Rightarrow
    plCommand \neq report1 \Rightarrow
    \forall NS \ Out \ M \ Oi \ Os.
       TR (M, Oi, Os)
          (exec
              (inputList
                  [Name PlatoonLeader says
                   prop (SOME (SLc (PL plCommand)))]))
          (CFG inputOK secContext secContextNull
              ([Name PlatoonLeader says
                prop (SOME (SLc (PL plCommand)))]::ins) s outs)
```

```
(CFG inputOK secContext secContextNull ins
           (NS \ s
               (exec
                  (inputList
                     [Name PlatoonLeader says
                      prop (SOME (SLc (PL plCommand)))])))
           (Out s
               (exec
                  (inputList
                     [Name PlatoonLeader says
                      prop (SOME (SLc (PL plCommand)))]))::
                 outs)) \iff
      authenticationTest inputOK
        [Name PlatoonLeader says
         prop (SOME (SLc (PL plCommand)))] \land
     CFGInterpret (M, Oi, Os)
        (CFG inputOK secContext secContextNull
           ([Name PlatoonLeader says
             prop (SOME (SLc (PL plCommand)))]::ins) s outs) \land
      (M,Oi,Os) satList
     propCommandList
        [Name PlatoonLeader says
         prop (SOME (SLc (PL plCommand)))]
[PlatoonLeader_notWARNO_notreport1_exec_plCommand_justified_thm]
 \vdash s \neq \mathtt{WARNO} \Rightarrow
   plCommand \neq invalidPlCommand \Rightarrow
   plCommand \neq report1 \Rightarrow
   \forall NS \ Out \ M \ Oi \ Os.
      TR (M, Oi, Os) (exec [SOME (SLc (PL plCommand))])
        (CFG inputOK secContext secContextNull
           ([Name PlatoonLeader says
             prop (SOME (SLc (PL plCommand)))]::ins) s outs)
        (CFG inputOK secContext secContextNull ins
           (NS \ s \ (exec \ [SOME \ (SLc \ (PL \ plCommand))]))
           (Out \ s \ (exec \ [SOME \ (SLc \ (PL \ plCommand))])::outs)) \iff
      authenticationTest inputOK
        [Name PlatoonLeader says
         prop (SOME (SLc (PL plCommand)))] \land
     CFGInterpret (M, Oi, Os)
        (CFG inputOK secContext secContextNull
           ([Name PlatoonLeader says
             prop (SOME (SLc (PL plCommand)))]::ins) s outs) \land
      (M, Oi, Os) satList [prop (SOME (SLc (PL plCommand)))]
[PlatoonLeader_notWARNO_notreport1_exec_plCommand_lemma]
 \vdash s \neq WARNO \Rightarrow
   plCommand \neq invalidPlCommand \Rightarrow
   plCommand \neq report1 \Rightarrow
```

```
\forall M \ Oi \ Os.
     CFGInterpret (M, Oi, Os)
        (CFG inputOK secContext secContextNull
           ([Name PlatoonLeader says
             prop (SOME (SLc (PL plCommand)))]::ins) s outs) \Rightarrow
      (M,Oi,Os) satList
     propCommandList
        [Name PlatoonLeader says
         prop (SOME (SLc (PL plCommand)))]
[PlatoonLeader_psgCommand_notDiscard_thm]
 \vdash \ \forall NS \ Out \ M \ Oi \ Os.
      \neg \texttt{TR} \ (M, Oi, Os)
         (discard
            (inputList
               [Name PlatoonLeader says
                prop (SOME (SLc (PSG psgCommand)))]))
         (CFG inputOK secContext secContextNull
            ([Name PlatoonLeader says
              prop (SOME (SLc (PSG psgCommand)))]::ins) s outs)
         (CFG inputOK secContext secContextNull ins
            (NS \ s
               (discard
                   (inputList
                      [Name PlatoonLeader says
                       prop (SOME (SLc (PSG psgCommand)))])))
            (Out s
               (discard
                   (inputList
                      [Name PlatoonLeader says
                       prop (SOME (SLc (PSG psgCommand)))]))::
                  outs))
[PlatoonLeader_trap_psgCommand_justified_lemma]
 \vdash \ \forall NS \ Out \ M \ Oi \ Os.
     TR (M, Oi, Os)
        (trap
           (inputList
              [Name PlatoonLeader says
               prop (SOME (SLc (PSG psgCommand)))]))
        (CFG inputOK secContext secContextNull
           ([Name PlatoonLeader says
             \verb|prop (SOME (SLc (PSG | psgCommand)))]:: ins) | s | outs)|
        (CFG inputOK secContext secContextNull ins
           (NS s
              (trap
                  (inputList
                     [Name PlatoonLeader says
                      prop (SOME (SLc (PSG psgCommand)))])))
```

```
(Out \ s
              (trap
                 (inputList
                    [Name PlatoonLeader says
                     prop (SOME (SLc (PSG psgCommand)))]))::
                outs)) \iff
     authenticationTest inputOK
        [Name PlatoonLeader says
        prop (SOME (SLc (PSG psqCommand)))] \land
     CFGInterpret (M, Oi, Os)
        (CFG inputOK secContext secContextNull
           ([Name PlatoonLeader says
             prop (SOME (SLc (PSG psgCommand)))]::ins) s outs) \land
      (M,Oi,Os) sat prop NONE
[PlatoonLeader_trap_psgCommand_lemma]
 \vdash \forall M \ Oi \ Os.
     CFGInterpret (M, Oi, Os)
        (CFG inputOK secContext secContextNull
           ([Name PlatoonLeader says
             prop (SOME (SLc (PSG psgCommand)))]::ins) s outs) \Rightarrow
      (M,Oi,Os) sat prop NONE
[PlatoonLeader_WARNO_exec_report1_justified_lemma]
 \vdash \ \forall NS \ Out \ M \ Oi \ Os.
     TR (M, Oi, Os)
        (exec
           (inputList
              [Name PlatoonLeader says
               prop (SOME (SLc (PL recon)));
               Name PlatoonLeader says
               prop (SOME (SLc (PL tentativePlan)));
               Name PlatoonSergeant says
               prop (SOME (SLc (PSG initiateMovement)));
               Name PlatoonLeader says
               prop (SOME (SLc (PL report1)))]))
        (CFG inputOK secContext secContextNull
           ([Name PlatoonLeader says
             prop (SOME (SLc (PL recon)));
             Name PlatoonLeader says
             prop (SOME (SLc (PL tentativePlan)));
             Name PlatoonSergeant says
             prop (SOME (SLc (PSG initiateMovement)));
             Name PlatoonLeader says
             prop (SOME (SLc (PL report1)))]::ins) WARNO outs)
        (CFG inputOK secContext secContextNull ins
           (NS WARNO
              (exec
                 (inputList
```

```
[Name PlatoonLeader says
                     prop (SOME (SLc (PL recon)));
                     Name PlatoonLeader says
                     prop (SOME (SLc (PL tentativePlan)));
                     Name PlatoonSergeant says
                     prop (SOME (SLc (PSG initiateMovement)));
                     Name PlatoonLeader says
                     prop (SOME (SLc (PL report1)))])))
           (Out WARNO
              (exec
                 (inputList
                    [Name PlatoonLeader says
                     prop (SOME (SLc (PL recon)));
                     Name PlatoonLeader says
                     prop (SOME (SLc (PL tentativePlan)));
                     Name PlatoonSergeant says
                     prop (SOME (SLc (PSG initiateMovement)));
                     Name PlatoonLeader says
                     prop (SOME (SLc (PL report1)))]))::outs)) <=>
     authenticationTest inputOK
        [Name PlatoonLeader says prop (SOME (SLc (PL recon)));
        Name PlatoonLeader says
        prop (SOME (SLc (PL tentativePlan)));
        Name PlatoonSergeant says
        prop (SOME (SLc (PSG initiateMovement)));
        Name PlatoonLeader says
        prop (SOME (SLc (PL report1)))] \cap \)
     CFGInterpret (M, Oi, Os)
       (CFG inputOK secContext secContextNull
           ([Name PlatoonLeader says
            prop (SOME (SLc (PL recon)));
            Name PlatoonLeader says
            prop (SOME (SLc (PL tentativePlan)));
            Name PlatoonSergeant says
            prop (SOME (SLc (PSG initiateMovement)));
            Name PlatoonLeader says
            prop (SOME (SLc (PL report1)))]::ins) WARNO outs) \land
     (M,Oi,Os) satList
     propCommandList
       [Name PlatoonLeader says prop (SOME (SLc (PL recon)));
        Name PlatoonLeader says
        prop (SOME (SLc (PL tentativePlan)));
        Name PlatoonSergeant says
        prop (SOME (SLc (PSG initiateMovement)));
        Name PlatoonLeader says prop (SOME (SLc (PL report1)))]
[PlatoonLeader_WARNO_exec_report1_justified_thm]
 \vdash \ \forall \, NS \ Out \ M \ Oi \ Os.
     TR (M, Oi, Os)
```

```
(exec
     [SOME (SLc (PL recon)); SOME (SLc (PL tentativePlan));
      SOME (SLc (PSG initiateMovement));
      SOME (SLc (PL report1))])
  (CFG inputOK secContext secContextNull
     ([Name PlatoonLeader says
       prop (SOME (SLc (PL recon)));
       Name PlatoonLeader says
       prop (SOME (SLc (PL tentativePlan)));
       Name PlatoonSergeant says
       prop (SOME (SLc (PSG initiateMovement)));
       Name PlatoonLeader says
       prop (SOME (SLc (PL report1)))]::ins) WARNO outs)
  (CFG inputOK secContext secContextNull ins
     (NS WARNO
        (exec
           [SOME (SLc (PL recon));
            SOME (SLc (PL tentativePlan));
            SOME (SLc (PSG initiateMovement));
            SOME (SLc (PL report1))]))
     (Out WARNO
        (exec
           [SOME (SLc (PL recon));
            SOME (SLc (PL tentativePlan));
            SOME (SLc (PSG initiateMovement));
            SOME (SLc (PL report1))])::outs)) \iff
authenticationTest inputOK
  [Name PlatoonLeader says prop (SOME (SLc (PL recon)));
   Name PlatoonLeader says
   prop (SOME (SLc (PL tentativePlan)));
   Name PlatoonSergeant says
   prop (SOME (SLc (PSG initiateMovement)));
   Name PlatoonLeader says
   prop (SOME (SLc (PL report1)))] \cap \)
CFGInterpret (M, Oi, Os)
  (CFG inputOK secContext secContextNull
     ([Name PlatoonLeader says
       prop (SOME (SLc (PL recon)));
       Name PlatoonLeader says
       prop (SOME (SLc (PL tentativePlan)));
       Name PlatoonSergeant says
       prop (SOME (SLc (PSG initiateMovement)));
       Name PlatoonLeader says
       prop (SOME (SLc (PL report1)))]::ins) WARNO outs) \land
(M,Oi,Os) satList
[prop (SOME (SLc (PL recon)));
 prop (SOME (SLc (PL tentativePlan)));
 prop (SOME (SLc (PSG initiateMovement)));
 prop (SOME (SLc (PL report1)))]
```

```
PlatoonLeader_WARNO_exec_report1_lemma
 \vdash \forall M \ Oi \ Os.
     CFGInterpret (M, Oi, Os)
       (CFG inputOK secContext secContextNull
           ([Name PlatoonLeader says
            prop (SOME (SLc (PL recon)));
            Name PlatoonLeader says
            prop (SOME (SLc (PL tentativePlan)));
            Name PlatoonSergeant says
            prop (SOME (SLc (PSG initiateMovement)));
            Name PlatoonLeader says
            prop (SOME (SLc (PL report1)))]::ins) WARNO outs) \Rightarrow
     (M,Oi,Os) satList
     propCommandList
        [Name PlatoonLeader says prop (SOME (SLc (PL recon)));
        Name PlatoonLeader says
        prop (SOME (SLc (PL tentativePlan)));
        Name PlatoonSergeant says
        prop (SOME (SLc (PSG initiateMovement)));
        Name PlatoonLeader says prop (SOME (SLc (PL report1)))]
[PlatoonSergeant_trap_plCommand_justified_lemma]
 \vdash \forall NS \ Out \ M \ Oi \ Os.
     TR (M, Oi, Os)
       (trap
           (inputList
              [Name PlatoonSergeant says
               prop (SOME (SLc (PL plCommand)))]))
       (CFG inputOK secContext secContextNull
           ([Name PlatoonSergeant says
            prop (SOME (SLc (PL plCommand)))]::ins) s outs)
       (CFG inputOK secContext secContextNull ins
           (NS s
              (trap
                 (inputList
                    [Name PlatoonSergeant says
                     prop (SOME (SLc (PL plCommand)))])))
           (Out s
              (trap
                 (inputList
                    [Name PlatoonSergeant says
                     prop (SOME (SLc (PL plCommand)))]))::
                outs)) \iff
     authenticationTest inputOK
        [Name PlatoonSergeant says
        prop (SOME (SLc (PL plCommand)))] \land
     CFGInterpret (M, Oi, Os)
       (CFG inputOK secContext secContextNull
           ([Name PlatoonSergeant says
```

```
prop (SOME (SLc (PL plCommand)))]::ins) s outs) \land
      (M,Oi,Os) sat prop NONE
[PlatoonSergeant_trap_plCommand_justified_thm]
 \vdash \ \forall NS \ Out \ M \ Oi \ Os.
     TR (M, Oi, Os) (trap [SOME (SLc (PL plCommand))])
        (CFG inputOK secContext secContextNull
           ([Name PlatoonSergeant says
             prop (SOME (SLc (PL plCommand)))]::ins) s outs)
        (CFG inputOK secContext secContextNull ins
           (NS \ s \ (trap \ [SOME \ (SLc \ (PL \ plCommand))]))
           (Out \ s \ (trap \ [SOME \ (SLc \ (PL \ plCommand))])::outs)) \iff
     authenticationTest inputOK
        [Name PlatoonSergeant says
         prop (SOME (SLc (PL plCommand)))] \land
     CFGInterpret (M, Oi, Os)
        (CFG inputOK secContext secContextNull
           ([Name PlatoonSergeant says
             prop (SOME (SLc (PL plCommand)))]::ins) s outs) \land
      (M,Oi,Os) sat prop NONE
[PlatoonSergeant_trap_plCommand_lemma]
 \vdash \forall M \ Oi \ Os.
     CFGInterpret (M, Oi, Os)
        (CFG inputOK secContext secContextNull
           ([Name PlatoonSergeant says
             prop (SOME (SLc (PL plCommand)))]::ins) s outs) \Rightarrow
      (M,Oi,Os) sat prop NONE
```

#### 17 PlanPBType Theory

**Built:** 13 May 2018

Parent Theories: indexedLists, patternMatches

#### 17.1 Datatypes

#### 17.2 Theorems

```
[plCommand_distinct_clauses]
 \vdash receiveMission \neq warno \land receiveMission \neq tentativePlan \land
    receiveMission \neq recon \land receiveMission \neq report1 \land
    {\tt receiveMission} \neq {\tt completePlan} \ \land \ {\tt receiveMission} \neq {\tt opoid} \ \land
    \verb|receiveMission| \neq \verb|supervise| \land \verb|receiveMission| \neq \verb|report2| \land
    receiveMission \neq complete \land receiveMission \neq plIncomplete \land
    receiveMission \neq invalidPlCommand \land warno \neq tentativePlan \land
    warno \neq recon \wedge warno \neq report1 \wedge warno \neq completePlan \wedge
    warno \neq opoid \wedge warno \neq supervise \wedge warno \neq report2 \wedge
    warno \neq complete \wedge warno \neq plIncomplete \wedge
    warno \neq invalidPlCommand \wedge tentativePlan \neq recon \wedge
    tentativePlan \neq report1 \land tentativePlan \neq completePlan \land
    tentativePlan \neq opoid \land tentativePlan \neq supervise \land
    tentativePlan \neq report2 \land tentativePlan \neq complete \land
    \texttt{tentativePlan} \neq \texttt{plIncomplete} \ \land
    \texttt{tentativePlan} \neq \texttt{invalidPlCommand} \ \land \ \texttt{recon} \neq \texttt{report1} \ \land
    recon \neq completePlan \land recon \neq opoid \land recon \neq supervise \land
    recon \neq report2 \land recon \neq complete \land recon \neq plIncomplete \land
    recon \neq invalidPlCommand \land report1 \neq completePlan \land
    report1 \neq opoid \land report1 \neq supervise \land report1 \neq report2 \land
    \texttt{report1} \neq \texttt{complete} \ \land \ \texttt{report1} \neq \texttt{plIncomplete} \ \land \\
    report1 \neq invalidPlCommand \wedge completePlan \neq opoid \wedge
    {\tt completePlan} \, \neq \, {\tt supervise} \, \wedge \, {\tt completePlan} \, \neq \, {\tt report2} \, \wedge \,
    {\tt completePlan} \neq {\tt complete} \ \land \ {\tt completePlan} \neq {\tt plIncomplete} \ \land
    completePlan \neq invalidPlCommand \land opoid \neq supervise \land
    opoid \neq report2 \wedge opoid \neq complete \wedge opoid \neq plIncomplete \wedge
    opoid \neq invalidPlCommand \land supervise \neq report2 \land
    supervise \neq complete \land supervise \neq plIncomplete \land
    supervise \neq invalidPlCommand \land report2 \neq complete \land
    report2 \neq plIncomplete \land report2 \neq invalidPlCommand \land
    complete \neq plIncomplete \land complete \neq invalidPlCommand \land
    plIncomplete \neq invalidPlCommand
[psgCommand_distinct_clauses]
 \vdash initiateMovement \neq psgIncomplete \land
    initiateMovement \neq invalidPsgCommand \land
    psgIncomplete \neq invalidPsgCommand
[slCommand_distinct_clauses]
```

 $\vdash \forall a' \ a. \ PL \ a \neq PSG \ a'$ 

```
[slCommand_one_one]
  \vdash (\forall a \ a'. (PL a = PL \ a') \iff (a = a')) \land
     \forall a \ a'. (PSG a = PSG \ a') \iff (a = a')
[slOutput_distinct_clauses]
  \vdash PlanPB \neq ReceiveMission \land PlanPB \neq Warno \land
     PlanPB \neq TentativePlan \land PlanPB \neq InitiateMovement \land
     {\tt PlanPB} \neq {\tt Recon} \ \land \ {\tt PlanPB} \neq {\tt Report1} \ \land \ {\tt PlanPB} \neq {\tt CompletePlan} \ \land \\
     {\tt PlanPB} \neq {\tt Opoid} \ \land \ {\tt PlanPB} \neq {\tt Supervise} \ \land \ {\tt PlanPB} \neq {\tt Report2} \ \land
     PlanPB \neq Complete \land PlanPB \neq unAuthenticated \land
     PlanPB \neq unAuthorized \land ReceiveMission \neq Warno \land
     {\tt Receive Mission} \neq {\tt Tentative Plan} \ \land
     \texttt{ReceiveMission} \neq \texttt{InitiateMovement} \ \land \ \texttt{ReceiveMission} \neq \texttt{Recon} \ \land
     ReceiveMission \neq Report1 \wedge ReceiveMission \neq CompletePlan \wedge
     \texttt{ReceiveMission} \neq \texttt{Opoid} \ \land \ \texttt{ReceiveMission} \neq \texttt{Supervise} \ \land
     \texttt{ReceiveMission} \neq \texttt{Report2} \ \land \ \texttt{ReceiveMission} \neq \texttt{Complete} \ \land
     {\tt ReceiveMission} \, \neq \, {\tt unAuthenticated} \, \, \wedge \,
     ReceiveMission \neq unAuthorized \land Warno \neq TentativePlan \land
     	exttt{Warno} 
eq 	exttt{InitiateMovement} 
\wedge 	exttt{Warno} 
eq 	exttt{Recon} 
\wedge 	exttt{Warno} 
eq 	exttt{Report1} 
\wedge
     \texttt{Warno} \neq \texttt{Report2} \ \land \ \texttt{Warno} \neq \texttt{Complete} \ \land
     Warno \neq unAuthenticated \wedge Warno \neq unAuthorized \wedge
     \texttt{TentativePlan} \neq \texttt{InitiateMovement} \ \land \ \texttt{TentativePlan} \neq \texttt{Recon} \ \land \\
     {\tt TentativePlan} \, \neq \, {\tt Report1} \, \wedge \, {\tt TentativePlan} \, \neq \, {\tt CompletePlan} \, \wedge \,
     \texttt{TentativePlan} \neq \texttt{Opoid} \ \land \ \texttt{TentativePlan} \neq \texttt{Supervise} \ \land
     TentativePlan \neq Report2 \wedge TentativePlan \neq Complete \wedge
     TentativePlan \neq unAuthenticated \wedge
     \texttt{TentativePlan} \neq \texttt{unAuthorized} \ \land \ \texttt{InitiateMovement} \neq \texttt{Recon} \ \land \\
     {\tt InitiateMovement} \, \neq \, {\tt Report1} \, \, \wedge \,
     InitiateMovement \neq CompletePlan \land InitiateMovement \neq Opoid \land
     {\tt InitiateMovement} \neq {\tt Supervise} \ \land \ {\tt InitiateMovement} \neq {\tt Report2} \ \land \\
     {\tt InitiateMovement} \, \neq \, {\tt Complete} \, \, \wedge \,
     InitiateMovement \neq unAuthenticated \land
     InitiateMovement \neq unAuthorized \wedge Recon \neq Report1 \wedge
     \texttt{Recon} \neq \texttt{CompletePlan} \ \land \ \texttt{Recon} \neq \texttt{Opoid} \ \land \ \texttt{Recon} \neq \texttt{Supervise} \ \land
     \texttt{Recon} \neq \texttt{Report2} \ \land \ \texttt{Recon} \neq \texttt{Complete} \ \land
     Recon \neq unAuthenticated \land Recon \neq unAuthorized \land
     \texttt{Report1} \neq \texttt{CompletePlan} \ \land \ \texttt{Report1} \neq \texttt{Opoid} \ \land
     \texttt{Report1} \neq \texttt{Supervise} \ \land \ \texttt{Report1} \neq \texttt{Report2} \ \land
     \texttt{Report1} \neq \texttt{Complete} \ \land \ \texttt{Report1} \neq \texttt{unAuthenticated} \ \land
     Report1 \neq unAuthorized \land CompletePlan \neq Opoid \land
     {\tt CompletePlan} \neq {\tt Supervise} \ \land \ {\tt CompletePlan} \neq {\tt Report2} \ \land
     {\tt CompletePlan} \neq {\tt Complete} \ \land \ {\tt CompletePlan} \neq {\tt unAuthenticated} \ \land \\
     {\tt CompletePlan} \neq {\tt unAuthorized} \ \land \ {\tt Opoid} \neq {\tt Supervise} \ \land \\
     Opoid \neq Report2 \wedge Opoid \neq Complete \wedge
     Opoid \neq unAuthenticated \wedge Opoid \neq unAuthorized \wedge
     Supervise \neq Report2 \wedge Supervise \neq Complete \wedge
     Supervise \neq unAuthenticated \wedge Supervise \neq unAuthorized \wedge
     Report2 \neq Complete \wedge Report2 \neq unAuthenticated \wedge
```

```
Report2 \neq unAuthorized \land Complete \neq unAuthenticated \land
        Complete \neq unAuthorized \wedge unAuthenticated \neq unAuthorized
[slRole_distinct_clauses]
  ⊢ PlatoonLeader ≠ PlatoonSergeant
[slState_distinct_clauses]
  \vdash PLAN_PB \neq RECEIVE_MISSION \land PLAN_PB \neq WARNO \land
        PLAN_PB \neq TENTATIVE_PLAN \land PLAN_PB \neq INITIATE_MOVEMENT \land
        {\tt PLAN\_PB} \, \neq \, {\tt RECON} \, \wedge \, {\tt PLAN\_PB} \, \neq \, {\tt REPORT1} \, \wedge \,
        {\tt PLAN\_PB} \, \neq \, {\tt COMPLETE\_PLAN} \, \wedge \, {\tt PLAN\_PB} \, \neq \, {\tt OPOID} \, \wedge \,
        PLAN_PB \neq SUPERVISE \wedge PLAN_PB \neq REPORT2 \wedge
        PLAN_PB \neq COMPLETE \wedge RECEIVE_MISSION \neq WARNO \wedge
        RECEIVE_MISSION \neq TENTATIVE_PLAN \wedge
        RECEIVE_MISSION \neq INITIATE_MOVEMENT \wedge
        \texttt{RECEIVE\_MISSION} \neq \texttt{RECON} \land \texttt{RECEIVE\_MISSION} \neq \texttt{REPORT1} \land
        RECEIVE_MISSION ≠ COMPLETE_PLAN ∧ RECEIVE_MISSION ≠ OPOID ∧
        RECEIVE_MISSION \neq SUPERVISE \wedge RECEIVE_MISSION \neq REPORT2 \wedge
        RECEIVE_MISSION \neq COMPLETE \wedge WARNO \neq TENTATIVE_PLAN \wedge
        	exttt{WARNO} 
eq 	exttt{INITIATE\_MOVEMENT} 
where \texttt{WARNO} 
eq 	exttt{RECON} 
where \texttt{WARNO} 
eq 	exttt{REPORT1} 
where \texttt{NECON} 
eq \texttt{NEC
        WARNO \neq COMPLETE_PLAN \wedge WARNO \neq OPOID \wedge WARNO \neq SUPERVISE \wedge
        WARNO \neq REPORT2 \land WARNO \neq COMPLETE \land
        TENTATIVE_PLAN \neq INITIATE_MOVEMENT \wedge TENTATIVE_PLAN \neq RECON \wedge
        TENTATIVE_PLAN \neq REPORT1 \wedge TENTATIVE_PLAN \neq COMPLETE_PLAN \wedge
        TENTATIVE_PLAN \neq OPOID \wedge TENTATIVE_PLAN \neq SUPERVISE \wedge
        TENTATIVE_PLAN \neq REPORT2 \wedge TENTATIVE_PLAN \neq COMPLETE \wedge
        INITIATE_MOVEMENT \neq RECON \wedge INITIATE_MOVEMENT \neq REPORT1 \wedge
        INITIATE\_MOVEMENT \neq COMPLETE\_PLAN \land
        {\tt INITIATE\_MOVEMENT} \neq {\tt OPOID} \ \land \ {\tt INITIATE\_MOVEMENT} \neq {\tt SUPERVISE} \ \land
        {\tt INITIATE\_MOVEMENT} \neq {\tt REPORT2} \ \land \ {\tt INITIATE\_MOVEMENT} \neq {\tt COMPLETE} \ \land \\
        \mathtt{RECON} \neq \mathtt{REPORT1} \ \land \ \mathtt{RECON} \neq \mathtt{COMPLETE\_PLAN} \ \land \ \mathtt{RECON} \neq \mathtt{OPOID} \ \land
        {\tt RECON} \neq {\tt SUPERVISE} \land {\tt RECON} \neq {\tt REPORT2} \land {\tt RECON} \neq {\tt COMPLETE} \land
        REPORT1 \neq COMPLETE_PLAN \wedge REPORT1 \neq OPOID \wedge
        \texttt{REPORT1} \neq \texttt{SUPERVISE} \ \land \ \texttt{REPORT1} \neq \texttt{REPORT2} \ \land
        REPORT1 \neq COMPLETE \wedge COMPLETE_PLAN \neq OPOID \wedge
        COMPLETE_PLAN \neq SUPERVISE \wedge COMPLETE_PLAN \neq REPORT2 \wedge
        \mathtt{COMPLETE\_PLAN} \neq \mathtt{COMPLETE} \land \mathtt{OPOID} \neq \mathtt{SUPERVISE} \land
        OPOID \neq REPORT2 \wedge OPOID \neq COMPLETE \wedge SUPERVISE \neq REPORT2 \wedge
        	ext{SUPERVISE} 
eq 	ext{COMPLETE} \wedge 	ext{REPORT2} 
eq 	ext{COMPLETE}
```

#### $\mathbf{Index}$

ConductORPType Theory, 38	$escState\_distinct\_clauses, 3$
Datatypes, 38	$output\_distinct\_clauses, 4$
Theorems, 39	$output\_one\_one, 4$
plCommand_distinct_clauses, 39	principal_one_one, 4
psgCommand_distinct_clauses, 39	$state\_distinct\_clauses, 4$
slCommand_distinct_clauses, 39	state_one_one, 4
slCommand_one_one, 39	
slOutput_distinct_clauses, 39	PBIntegratedDef Theory, 28
slRole_distinct_clauses, 39	Definitions, 28
slState_distinct_clauses, 39	secAuthorization_def, 28
ConductPBType Theory, 45	$secHelper\_def, 28$
Datatypes, 45	Theorems, 28
Theorems, 45	getOmniCommand_def, 28
plCommandPB_distinct_clauses, 45	getOmniCommand_ind, 31
psgCommandPB_distinct_clauses, 45	$secContext\_def, 32$
slCommand_distinct_clauses, 45	secContext_ind, 33
slCommand_one_one, 45	PBTypeIntegrated Theory, 26
slOutput_distinct_clauses, 46	Datatypes, 26
slRole_distinct_clauses, 46	Theorems, 27
slState_distinct_clauses, 46	omniCommand_distinct_clauses, $27$
	plCommand_distinct_clauses, 27
MoveToORPType Theory, 51	$slCommand\_distinct\_clauses, 27$
Datatypes, 51	$slCommand\_one\_one, 27$
Theorems, 51	$slOutput\_distinct\_clauses, 27$
slCommand_distinct_clauses, 51	slState_distinct_clauses, 28
slOutput_distinct_clauses, 51	$stateRole\_distinct\_clauses, 28$
$slState\_distinct\_clauses, 51$	PlanPBType Theory, 67
MoveToPBType Theory, 56	The second control of
	Datatypes, 67
Datatypes, 56	Theorems, 68
Datatypes, 56 Theorems, 56	Theorems, 68 plCommand_distinct_clauses, 68
Datatypes, 56 Theorems, 56 slCommand_distinct_clauses, 56	Theorems, 68 plCommand_distinct_clauses, 68 psgCommand_distinct_clauses, 68
Datatypes, 56 Theorems, 56	Theorems, 68 plCommand_distinct_clauses, 68
Datatypes, 56 Theorems, 56 slCommand_distinct_clauses, 56	Theorems, 68 plCommand_distinct_clauses, 68 psgCommand_distinct_clauses, 68 slCommand_distinct_clauses, 68 slCommand_one_one, 69
Datatypes, 56 Theorems, 56 slCommand_distinct_clauses, 56 slOutput_distinct_clauses, 57 slState_distinct_clauses, 57	Theorems, 68 plCommand_distinct_clauses, 68 psgCommand_distinct_clauses, 68 slCommand_distinct_clauses, 68 slCommand_one_one, 69 slOutput_distinct_clauses, 69
Datatypes, 56 Theorems, 56 slCommand_distinct_clauses, 56 slOutput_distinct_clauses, 57 slState_distinct_clauses, 57  OMNIType Theory, 3	Theorems, 68 plCommand_distinct_clauses, 68 psgCommand_distinct_clauses, 68 slCommand_distinct_clauses, 68 slCommand_one_one, 69 slOutput_distinct_clauses, 69 slRole_distinct_clauses, 70
Datatypes, 56 Theorems, 56 slCommand_distinct_clauses, 56 slOutput_distinct_clauses, 57 slState_distinct_clauses, 57  OMNIType Theory, 3 Datatypes, 3	Theorems, 68 plCommand_distinct_clauses, 68 psgCommand_distinct_clauses, 68 slCommand_distinct_clauses, 68 slCommand_one_one, 69 slOutput_distinct_clauses, 69
Datatypes, 56 Theorems, 56 slCommand_distinct_clauses, 56 slOutput_distinct_clauses, 57 slState_distinct_clauses, 57  OMNIType Theory, 3 Datatypes, 3 Theorems, 3	Theorems, 68 plCommand_distinct_clauses, 68 psgCommand_distinct_clauses, 68 slCommand_distinct_clauses, 68 slCommand_one_one, 69 slOutput_distinct_clauses, 69 slRole_distinct_clauses, 70 slState_distinct_clauses, 70
Datatypes, 56 Theorems, 56 slCommand_distinct_clauses, 56 slOutput_distinct_clauses, 57 slState_distinct_clauses, 57  OMNIType Theory, 3 Datatypes, 3 Theorems, 3 command_distinct_clauses, 3	Theorems, 68 plCommand_distinct_clauses, 68 psgCommand_distinct_clauses, 68 slCommand_distinct_clauses, 68 slCommand_one_one, 69 slOutput_distinct_clauses, 69 slRole_distinct_clauses, 70 slState_distinct_clauses, 70 satList Theory, 21
Datatypes, 56 Theorems, 56 slCommand_distinct_clauses, 56 slOutput_distinct_clauses, 57 slState_distinct_clauses, 57  OMNIType Theory, 3 Datatypes, 3 Theorems, 3 command_distinct_clauses, 3 command_one_one, 3	Theorems, 68 plCommand_distinct_clauses, 68 psgCommand_distinct_clauses, 68 slCommand_distinct_clauses, 68 slCommand_one_one, 69 slOutput_distinct_clauses, 69 slRole_distinct_clauses, 70 slState_distinct_clauses, 70 satList Theory, 21 Definitions, 21
Datatypes, 56 Theorems, 56 slCommand_distinct_clauses, 56 slOutput_distinct_clauses, 57 slState_distinct_clauses, 57  OMNIType Theory, 3 Datatypes, 3 Theorems, 3 command_distinct_clauses, 3	Theorems, 68 plCommand_distinct_clauses, 68 psgCommand_distinct_clauses, 68 slCommand_distinct_clauses, 68 slCommand_one_one, 69 slOutput_distinct_clauses, 69 slRole_distinct_clauses, 70 slState_distinct_clauses, 70 satList Theory, 21

satList_conj, 21	$TR_{cases}$ , 6
satList_CONS, 21	TR_discard_cmd_rule, 7
satList_nil, 21	TR_EQ_rules_thm, 7
ssm Theory, 11	TR_exec_cmd_rule, 8
Datatypes, 11	$TR\_ind, 8$
Definitions, 12	$TR_{rules}$ , 9
authenticationTest_def, 12	TR_strongind, 9
$commandList\_def, 12$	TR_trap_cmd_rule, 10
$inputList\_def, 12$	TRrule0, 10
$propCommandList\_def, 12$	TRrule1, 11
$TR_{-}def, 12$	trType_distinct_clauses, 11
Theorems, 13	$trType\_one\_one, 11$
$CFGInterpret\_def, 13$	ssmConductORP Theory, 33
CFGInterpret_ind, 13	Definitions, 33
configuration_one_one, 13	$secContextConductORP\_def, 33$
extractCommand_def, 13	$ssmConductORPStateInterp\_def, 33$
extractCommand_ind, 13	Theorems, 33
extractInput_def, 14	$authTestConductORP\_cmd\_reject\_lemma,$
extractInput_ind, 14	33
$extractPropCommand\_def, 15$	authTestConductORP_def, 34
extractPropCommand_ind, 15	authTestConductORP_ind, 34
TR_cases, 16	$conductORPNS\_def, 35$
TR_discard_cmd_rule, 17	conductORPNS_ind, 35
TR_EQ_rules_thm, 17	$conductORPOut\_def, 36$
TR_exec_cmd_rule, 17	conductORPOut_ind, 36
$TR_{-ind}$ , 18	$Plato on Leader\_exec\_pl Command\_jus-$
TR_rules, 18	$tifled_thm, 37$
TR_strongind, 19	PlatoonLeader_plCommand_lemma, 37
$TR_{trap\_cmd\_rule}$ , 20	$PlatoonSergeant\_exec\_psgCommand\$
TRrule0, 20	justified_thm, 38
TRrule1, 20	$Plato on Serge ant\_psg Command\_lemma,$
$trType\_distinct\_clauses, 20$	38
$trType\_one\_one, 21$	ssmConductPB Theory, 39
ssm11 Theory, 4	Definitions, 40
Datatypes, 4	secContextConductPB_def, 40
Definitions, 4	ssmConductPBStateInterp_def, 40
$TR_{-}def, 4$	Theorems, 40
Theorems, 5	authTestConductPB_cmd_reject_lemma,
CFGInterpret_def, 5	40
CFGInterpret_ind, 6	authTestConductPB_def, 40
configuration_one_one, 6	authTestConductPB_ind, 41
order_distinct_clauses, 6	conductPBNS_def, 42
order_one_one, 6	conductPBNS_ind, 42

$conductPBOut\_def, 43$	Definitions, 21
conductPBOut_ind, 43	secContext_def, 21
$PlatoonLeader\_exec\_plCommandPB\$	ssmPBStateInterp_def, 21
$justified_{-}thm, 44$	Theorems, 22
PlatoonLeader_plCommandPB_lemma,	authenticationTest_cmd_reject_lemma,
44	22
$Platoon Sergeant\_exec\_psg Command PB\$	authenticationTest_def, 22
$justified_{-}thm, 44$	authenticationTest_ind, 22
$Plato on Serge ant\_psg Command PB\_lemma,$	PBNS_def, 23
45	PBNS_ind, 23
ssmMoveToORP Theory, 46	PBOut_def, 24
Definitions, 46	PBOut_ind, 25
secContextMoveToORP_def, 46	PlatoonLeader_exec_slCommand_jus-
ssmMoveToORPStateInterp_def, 46	$tified\_thm, 26$
Theorems, 46	PlatoonLeader_slCommand_lemma, 26
$authTestMoveToORP\_cmd\_reject\_lemn\resem$	nPlanPB Theory, 57
46	Theorems, 57
$authTestMoveToORP\_def,47$	$inputOK_{-}def, 57$
authTestMoveToORP_ind, 47	inputOK_ind, 58
$moveToORPNS\_def, 48$	planPBNS_def, $59$
moveToORPNS_ind, 48	planPBNS_ind, 59
moveToORPOut_def, 49	$planPBOut_{-}def, 59$
moveToORPOut_ind, 49	planPBOut_ind, 60
PlatoonLeader_exec_slCommand_jus-	$PlatoonLeader\_notWARNO\_notreport1\$
$tified\_thm, 50$	$exec\_plCommand\_justified\_lemma, 60$
PlatoonLeader_slCommand_lemma, 50	$PlatoonLeader\_notWARNO\_notreport1\$
ssmMoveToPB Theory, 52	$exec\_plCommand\_justified\_thm, 61$
Definitions, 52	$PlatoonLeader\_notWARNO\_notreport1\$
$secContextMoveToPB\_def, 52$	exec_plCommand_lemma, 61
$ssmMoveToPBStateInterp\_def, 52$	PlatoonLeader_psgCommand_notDis-
Theorems, 52	$card\_thm, 62$
$auth Test Move To PB\_cmd\_reject\_lemma, \\ 52$	PlatoonLeader_trap_psgCommand_jus- tified_lemma, 62
$authTestMoveToPB\_def, 52$	$Plato on Leader\_trap\_psg Command\_lemma,$
authTestMoveToPB_ind, 53	63
$moveToPBNS\_def, 53$	PlatoonLeader_WARNO_exec_report1
moveToPBNS_ind, 54	justified_lemma, 63
$moveToPBOut\_def, 54$	$PlatoonLeader\_WARNO\_exec\_report1\$
$moveToPBOut\_ind, 55$	justified_thm, 64
PlatoonLeader_exec_slCommand_jus-	PlatoonLeader_WARNO_exec_report1
tified_thm, 55	lemma, 66
PlatoonLeader_slCommand_lemma, 56	PlatoonSergeant_trap_plCommand_jus-
ssmPB Theory, 21	tified_lemma, 66

PlatoonSergeant\_trap\_plCommand\_justified\_thm, 67
PlatoonSergeant\_trap\_plCommand\_lemma, 67

## Appendix C

# Secure State Machine Theories: HOL Script Files

#### C.1 ssm

```
(* Secure State Machine Theory: authentication, authorization, and state
 (* interpretation.
 (* Author: Shiu-Kai Chin
 (* Date: 27 November 2015
 structure ssmScript = struct
(* = = = Interactive \ mode = = = =
app load ["TypeBase", "ssminfRules", "listTheory", "optionTheory", "acl_infRules", "satListTheory", "ssmTheory"];
app\ load\ ["TypeBase",\ "ssminfRules"," list Theory"," option Theory"," acl\_infRules", Theory", "acl\_infRules", Theory "," option Theory", "acl\_infRules", Theory "," option Theory "," acl\_infRules", Theory "," option Theory "," acl\_infRules", Theory "," option Theory "," acl\_infRules", Theory Theory
                       "satListTheory"];
open TypeBase listTheory ssminfRules optionTheory acl_infRules satListTheory
           ssmTheory
 ==== end interactive mode ===== *)
open HolKernel boolLib Parse bossLib
open TypeBase listTheory optionTheory ssminfRules acl_infRules satListTheory
(********************************
(* create a new theory *)
 (*****************************
val _ = new_theory "ssm";
 (*\ Define\ the\ type\ of\ transition:\ discard\ ,\ execute\ ,\ or\ trap\ . We discard from
 (* the input stream those inputs that are not of the form P says command. We
 (* execute commands that users and supervisors are authorized for. We trap
 (* commands that users are not authorized to execute.
(* In keeping with virtual machine design principles as described by Popek
 (* and Goldberg, we add a TRAP instruction to the commands by users.
                                                                                                                                                                                      *)
 (* In effect, we are LIFTING the commands available to users to include the
 (* TRAP instruction used by the state machine to handle authorization errors.
```

```
val =
Datatype
trTvpe =
  discard 'cmdlist | trap 'cmdlist | exec 'cmdlist '
val trType_distinct_clauses = distinct_of '': 'cmdlist trType''
val _ = save_thm("trType_distinct_clauses", trType_distinct_clauses)
val trType_one_one = one_one_of '': 'cmdlist trType''
val _ = save_thm("trType_one_one", trType_one_one)
(* Define configuration to include the security context within which the
(*\ inputs\ are\ evaluated . The components are as follows: (1) the authentication*)
(* function, (2) the interretation of the state, (3) the security context,
(* (4) the input stream, (5) the state, and (6) the output stream.
(* -
val _ =
Datatype
'configuration =
CFG
  (('command option, 'principal, 'd, 'e)Form -> bool)
  (('state -> ('command option, 'principal, 'd, 'e)Form list ->
('command option, 'principal, 'd, 'e)Form list))
  ((('command option, 'principal, 'd, 'e)Form list) ->
((('command option, 'principal, 'd, 'e)Form list))
(((('command option, 'principal, 'd, 'e)Form list))
(((('command option, 'principal, 'd, 'e)Form) list) list)
    state)
  ('output list)'
(* Prove one-to-one properties of configuration
val configuration_one_one =
    one_one_of '': ('command option, 'd, 'e, 'output, 'principal, 'state) configuration ''
val _ = save_thm("configuration_one_one", configuration_one_one)
(* The interpretation of configuration is the conjunction of the formulas in
                                                                                           *)
(* the context and the first element of a non-empty input stream.
val CFGInterpret_def =
Define
`CFGInterpret
 ((M: ('command option, 'b, 'principal, 'd, 'e) Kripke), Oi: 'd po, Os: 'e po)
 (CFG
  (elementTest:('command option,'principal,'d,'e)Form -> bool)
  (stateInterp: state -> (('command option, 'principal, 'd, 'e)Form list) -> (('command option, 'principal, 'd, 'e)Form list))
  (context:(('command option, 'principal, 'd, 'e)Form list) ->
  (('command option, 'principal, 'd, 'e)Form list))
((x:('command option, 'principal, 'd, 'e)Form list)::ins)
  (state: 'state)
  (outStream: 'output list))
  ((M,Oi,Os) satList (context x)) /\
  ((M,Oi,Os) satList x) /\
  ((M,Oi,Os) satList (stateInterp state x))'
(* In the following definitions of authenticationTest, extractCommand, and
(* commandList, we implicitly assume that the only authenticated inputs are
                                                                                           * )
(* of the form P says phi, i.e., we know who is making statement phi.
val authenticationTest_def =
Define
`authentication Test\\
 (elementTest:('command option,'principal,'d,'e)Form -> bool)
(x:('command option,'principal,'d,'e)Form list) =
FOLDR (\p q.p /\ q) T (MAP elementTest x)';
```

```
val extractCommand_def =
Define
'extractCommand (P says (prop (SOME cmd)): ('command option, 'principal, 'd, 'e)Form) =
   cmd ';
val commandList_def =
Define
'commandList (x:('command option, 'principal, 'd, 'e)Form list) =
MAP extractCommand x';
val extractPropCommand_def =
Define
'(extractPropCommand (P says (prop (SOME cmd)):('command option,'principal,'d,'e)Form) =
   ((prop (SOME cmd)): ('command option, 'principal, 'd, 'e)Form)) ';
\mathbf{val} \ \mathbf{propCommandList\_def} =
'propCommandList (x:('command option,'principal,'d,'e)Form list) =
MAP extractPropCommand x';
val extractInput_def =
Define
'extractInput (P says (prop x):('command option,'principal,'d,'e)Form) = x';
val inputList_def =
Define
'inputList (xs:('command option,'principal,'d,'e)Form list) =
MAP extractInput xs';
(* Define transition relation among configurations. This definition is
(* parameterized in terms of next-state transition function and output
(* function.
(*
val (TR_rules, TR_ind, TR_cases) =
Hol_reln
'(!(elementTest:('command option,'principal,'d,'e)Form -> bool)
    (NS: 'state -> ('command option list) trType -> 'state) M Oi Os Out (s: 'state)
   (context:(('command option, 'principal, 'd, 'e)Form list) -> (('command option, 'principal, 'd, 'e)Form list))
    (stateInterp:'state -> ('command option, 'principal, 'd, 'e)Form list ->
    ('command option, 'principal, 'd, 'e)Form list)
(x:('command option, 'principal, 'd, 'e)Form list)
    (ins:('command option,'principal,'d,'e)Form list list)
    (outs: 'output list).
 (authenticationTest elementTest x) /\
 (CFGInterpret (M, Oi, Os)
  (CFG elementTest stateInterp context (x::ins) s outs)) =>>
 (TR
  ((M:('command option,'b,'principal,'d,'e)Kripke),Oi:'d po,Os:'e po)
  (exec (inputList x))
  (CFG elementTest stateInterp context (x::ins) s outs)
  (CFG elementTest stateInterp context ins
        (NS s (exec (inputList x)))
 ((Out s (exec (inputList x)))::outs)))) /\
(!(elementTest:('command option, 'principal, 'd, 'e)Form -> bool)
(NS: 'state -> ('command option list) trType -> 'state) M Oi Os Out (s:'state)
    (context:(('command option, 'principal, 'd, 'e)Form list) ->
   (('command option, 'principal, 'd, 'e)Form list))
    (stateInterp:'state -> ('command option, 'principal, 'd, 'e)Form list ->
    ('command option, 'principal, 'd, 'e)Form list)
(x:('command option, 'principal, 'd, 'e)Form list)
    (ins:('command option,'principal,'d,'e)Form list list)
    (outs: 'output list).
 (authenticationTest elementTest x)
 (CFGInterpret (M, Oi, Os)
  (CFG elementTest stateInterp context (x::ins) s outs)) ==>
 (TR.
  ((M: ('command option, 'b, 'principal, 'd, 'e) Kripke), Oi: 'd po, Os: 'e po)
  (trap (inputList x))
 (CFG elementTest stateInterp context (x::ins) s outs)
 (CFG elementTest stateInterp context ins
```

```
(NS s (trap (inputList x)))
 ((Out s (trap (inputList x)))::outs)))) /\
(!(elementTest:('command option,'principal,'d,'e)Form -> bool)
    (NS: 'state -> ('command option list) trType -> 'state) M Oi Os Out (s:'state)
   (context:(('command option, 'principal, 'd, 'e)Form list) ->
(('command option, 'principal, 'd, 'e)Form list))
    (stateInterp:'state -> ('command option, 'principal, 'd, 'e)Form list ->
    ('command option, 'principal, 'd, 'e)Form list)
(x:('command option, 'principal, 'd, 'e)Form list)
(ins:('command option, 'principal, 'd, 'e)Form list list)
    (outs: 'output list).
 ~(authenticationTest elementTest x) =>>
 (TR
  ((M:('command option,'b,'principal,'d,'e)Kripke),Oi:'d po,Os:'e po)
  (discard (inputList x))
 (CFG elementTest stateInterp context (x::ins) s outs)
 (CFG elementTest stateInterp context ins
       (NS \ s \ (discard \ (inputList \ x)))
       ((Out s (discard (inputList x)))::outs))))'
(* Split up TR_rules into individual clauses
(* -
val [rule0 , rule1 , rule2] = CONJUNCTS TR_rules
(* Prove the converse of rule0, rule1, and rule2
val TR_lemma0 =
TAC_PROOF(([], flip_TR_rules rule0),
DISCH_TAC THEN
IMP_RES_TAC TR_cases THEN
PAT_ASSUM
 ", exec \operatorname{cmd} = \operatorname{y}"
 (fn th => ASSUME_TAC(REWRITE_RULE[trType_one_one, trType_distinct_clauses]th)) THEN
PROVE.TAC [\ configuration\_one\_one\ , list\_11\ , trType\_distinct\_clauses\ ])
val TR_lemma1 =
TAC_PROOF(([], flip_TR_rules rule1),
DISCH_TAC THEN
IMP_RES_TAC TR_cases THEN
PAT_ASSUM
 "trap cmd = y"
 (fn th => ASSUME_TAC(REWRITE_RULE[trType_one_one,trType_distinct_clauses]th)) THEN
PROVE_TAC[configuration_one_one, list_11, trType_distinct_clauses])
val TR_lemma2 =
\begin{array}{l} {\rm TACPROOF(([]\,,flip\_T\,R\_rules\ rule2)\,,} \\ {\rm DISCH\_TAC\ THEN} \end{array}
IMP_RES_TAC TR_cases THEN
PAT_ASSUM
 ", discard (inputList x)= y"
 (fn th => ASSUME_TAC(REWRITE_RULE[trType_one_one, trType_distinct_clauses]th)) THEN
PROVE_TAC[configuration_one_one, list_11, trType_distinct_clauses])
val TR rules converse =
TAC_PROOF(([], flip_TR_rules TR_rules),
REWRITE_TAC[TR_lemma0, TR_lemma1, TR_lemma2])
val TR_EQ_rules_thm = TR_EQ_rules TR_rules_TR_rules_converse
val _ = save_thm("TR_EQ_rules_thm",TR_EQ_rules_thm)
val [TRrule0, TRrule1, TR_discard_cmd_rule] = CONJUNCTS TR_EQ_rules_thm
val _ = save_thm("TRrule0",TRrule0)
val _ = save_thm("TRrule1", TRrule1)
val _ = save_thm("TR_discard_cmd_rule", TR_discard_cmd_rule)
(* If (CFGInterpret
```

```
(*
(*
       (M, Oi, Os)
       (CFG\ elementTest\ stateInterpret\ certList
             ((P \ says \ (prop \ (CMD \ cmd)))::ins) \ s \ outs) ==>
(*
      ((M, Oi, Os) \ sat \ (prop \ (CMD \ cmd))))
(*
(* is a valid inference rule, then executing cmd the exec (CMD cmd) transition
(* occurs if and only if prop (CMD cmd), elementTest, and
(* CFGInterpret (M, Oi, Os)
(* (CFG elementTest stateInterpret certList (P says prop (CMD cmd)::ins) s outs)
(* are true.
                                                                                  * )
(*
val TR_exec_cmd_rule =
TAC_PROOF(([],
''!elementTest context stateInterp (x:('command option, 'principal, 'd, 'e)Form list)
   ins s outs.
 (!M Oi Os.
 (CFGInterpret
  ((M:('command option, 'b, 'principal, 'd, 'e) Kripke),(Oi:'d po), (Os:'e po))
  (CFG element Test
       (stateInterp:'state -> ('command option, 'principal, 'd, 'e)Form list ->
        ('command option, 'principal, 'd, 'e) Form list) context
       (x::ins)
       (s:'state) (outs:'output list))) ==>
  (M, Oi, Os) satList (propCommandList (x:('command option, 'principal, 'd, 'e)Form list))) =>
(!NS Out M Oi Os.
  ((M:('command option, 'b, 'principal, 'd, 'e) Kripke),(Oi:'d po),
   (Os: 'e po)) (exec (inputList x))
  ('command option, 'principal, 'd, 'e)Form list)
(context : ('command option, 'principal, 'd, 'e) Form list ->
            ('command option, 'principal, 'd, 'e) Form list)
            (x::ins)
           (s:'state) (outs:'output list))
   (CFG elementTest stateInterp context ins
            ((NS: 'state -> 'command option list trType -> 'state) s (exec (inputList x)))
            (Out s (exec (inputList x))::outs)) <=>
  (authenticationTest elementTest x) /\
  (CFGInterpret (M, Oi, Os)
   (CFG elementTest stateInterp context (x::ins) s outs)) /\
(M,Oi,Os) satList (propCommandList x))''), REWRITE_TAC[TRrule0] THEN
REPEAT STRIP_TAC THEN
EQ_TAC THEN
REPEAT STRIP_TAC THEN
PROVE_TAC[])
val _ = save_thm("TR_exec_cmd_rule", TR_exec_cmd_rule)
(* If (CFGInterpret
(*
       (M, Oi, Os)
(*
       (CFG\ element Test\ state Interpret\ cert List
(*
            ((P \ says \ (prop \ (CMD \ cmd)))::ins) \ s \ outs) \Longrightarrow
      ((M, Oi, Os) \ sat \ (prop \ TRAP)))
(*
(* is a valid inference rule, then executing cmd the trap(CMD cmd) transition
(* occurs if and only if prop TRAP, elementTest, and
(* CFGInterpret (M, Oi, Os)
    (CFG elementTest stateInterpret certList (P says prop (CMD cmd)::ins)
(*
         s outs) are true.
(* -
val TR_trap_cmd_rule =
TAC_PROOF(
([], ''!elementTest context stateInterp (x:('command option, 'principal, 'd, 'e)Form list)
   ins s outs.
 (!M Oi Os.
 (CFGInterpret
  ((M:('command option, 'b, 'principal, 'd, 'e) Kripke),(Oi:'d po), (Os:'e po))
  (CFG element Test
       (stateInterp:'state -> ('command option, 'principal, 'd, 'e)Form list ->
        ('command option, 'principal, 'd, 'e)Form list) context
       (x :: ins)
       (s:'state) (outs:'output list))) ==>
```

```
(M,Oi,Os) sat (prop NONE)) ==>
(!NS Out M Oi Os.
 TR.
  ((M:('command option, 'b, 'principal, 'd, 'e) Kripke),(Oi:'d po),
    (Os : 'e po)) (trap (inputList x))
  (CFG (elementTest : ('command option, 'principal, 'd, 'e) Form -> bool)

(stateInterp:'state -> ('command option, 'principal, 'd, 'e) Form list ->
             ('command option, 'principal, 'd, 'e)Form list)
(context : ('command option, 'principal, 'd, 'e) Form list ->
              ('command option, 'principal, 'd, 'e) Form list)
             (x::ins)
             (s:'state) (outs:'output list))
   (CFG elementTest stateInterp context ins
             ((NS: 'state -> 'command option list trType -> 'state) s (trap (inputList x)))
             (Out s (trap (inputList x))::outs)) <=>
  (authenticationTest elementTest x) /\
  (CFGInterpret (M, Oi, Os)
    (CFG elementTest stateInterp context (x::ins) s outs)) / 
    (M, Oi, Os) sat (prop NONE)) ''),
REWRITE_TAC[TRrule1] THEN
REPEAT STRIP_TAC THEN EQ_TAC THEN
REPEAT STRIP_TAC THEN
PROVE_TAC[])
val _ = save_thm("TR_trap_cmd_rule",TR_trap_cmd_rule)
(* = = start here =
==== end here ==== *)
val _ = export_theory ();
val _ = print_theory "-";
end (* structure *)
```

#### C.2 satList

```
(*\ Definition\ of\ satList\ for\ conjunctions\ of\ ACL\ formulas
                                                                          *)
(* Author: Shiu-Kai Chin
(* Date: 24 July 2014
structure satListScript = struct
(* interactive mode
app load
 ["TypeBase", "listTheory", "acl_infRules"];
open HolKernel boolLib Parse bossLib
open TypeBase acl_infRules listTheory
(*******
* create a new theory
********
val _ = new_theory "satList";
(*********************************
(* Configurations and policies are represented by lists
(* of formulas in the access-control logic.
(* Previously, for a formula f in the access-control logic,
(* we ultimately interpreted it within the context of a
(* Kripke structure M and partial orders Oi: 'Int po and
(* Os: 'Sec po. This is represented as (M, Oi, Os) sat f.
(* The natural extension is to interpret a list of formulas *)
(* [f0; ...; fn] as a conjunction:
(* (M, Oi, Os) \ sat \ fo \land \ldots \land (M, Oi, Os) \ sat \ fn
val _ set_fixity "satList" (Infixr 540);
```

```
val satList_def =
Define
'((M:('prop,'world,'pName,'Int,'Sec)Kripke),(Oi:'Int po),(Os:'Sec po))
 satList
 formList =
 FOLDR
 (\x y. x /\ y) T
 (MAP
  \label{eq:continuous_section} $$ (\ (f:('prop,'pName,'Int,'Sec)Form). $$ ((M:('prop,'world,'pName,'Int,'Sec)Kripke), $$ $$
    Oi: 'Int po, Os: 'Sec po) sat f) formList) ';
(* Properties of satList *)
(**********************************
val satList_nil =
TAC_PROOF(
([], ''((M:('prop,'world,'pName,'Int,'Sec)Kripke),(Oi:'Int po),(Os:'Sec po)) satList []''),
REWRITE_TAC[satList_def,FOLDR,MAP])
val _ = save_thm("satList_nil", satList_nil)
val satList_conj =
TAC_PROOF(
([]]
'!ll l2 M Oi Os.(((M:('prop, 'world, 'pName, 'Int, 'Sec)Kripke),(Oi:'Int po),(Os:'Sec po))
   satList l1) /\
  (((M:('prop,'world,'pName,'Int,'Sec)Kripke),(Oi:'Int po),(Os:'Sec po))
   satList 12) =
  (((M:('prop, 'world, 'pName, 'Int, 'Sec)Kripke),(Oi:'Int po),(Os:'Sec po))
   satList (l1 ++ l2))''),
Induct THEN
REWRITE_TAC[APPEND, satList_nil] THEN
REWRITE_TAC[satList_def,MAP] THEN
CONV_TAC(DEPTH_CONV BETA_CONV) THEN
REWRITE_TAC[FOLDR] THEN
CONV_TAC(DEPTH_CONV BETA_CONV) THEN
REWRITE_TAC[GSYM satList_def] THEN
PROVE_TAC[])
val _ = save_thm("satList_conj", satList_conj)
val satList_CONS =
TACPROOF(([],
''!h t M Oi Os.(((M:('prop,'world,'pName,'Int,'Sec)Kripke),(Oi:'Int po),(Os:'Sec po))
   satList (h::t)) =
  (((M,Oi,Os) sat h) /\
(((M:('prop,'world,'pName,'Int,'Sec)Kripke),(Oi:'Int po),(Os:'Sec po))
satList t))''),
REPEAT STRIP_TAC THEN
REWRITE_TAC[satList_def,MAP] THEN
CONV_TAC(DEPTH_CONV BETA_CONV) THEN
REWRITE_TAC[FOLDR] THEN
CONV.TAC(DEPTH.CONV BETA.CONV) THEN
REWRITE_TAC[])
val _ = save_thm("satList_CONS",satList_CONS)
val _ = export_theory ();
val _ = print_theory "-";
end (* structure *)
```

## Appendix D

# Secure State Machine Theories Applied to Patrol Base Operations: HOL Script Files

#### D.1 OMNILevel

```
(* OMNIScript
(* Author: Lori Pickering
(* Date: 10 May 2018
(*\ This\ file\ is\ intended\ to\ allow\ for\ integration\ among\ the\ ssms.\ The\ idea
(* is to provide an OMNI-level integrating theory, in the sense of a super-
(* conscious that knows when each ssm is complete and provides that info to
(* higher-level state machines.
structure OMNIScript = struct
(* ==== Interactive Mode ======
app\ load\ ["TypeBase"," list Theory", "option Theory",
        "OMNIType Theory",\\
"acl\_infRules", "aclDrulesTheory", "aclrulesTheory"]; open TypeBase listTheory optionTheory
    OMNIType\ Theory
    acl\_infRules aclDrulesTheory aclrulesTheory
=== End Interactive Mode ==== *)
open HolKernel Parse boolLib bossLib;
open TypeBase listTheory optionTheory
open OMNITypeTheory
\mathbf{open} \ \mathbf{acl\_infRules} \ \mathbf{aclDrulesTheory} \ \mathbf{aclrulesTheory}
val _ = new_theory "OMNI";
(* Define slCommands for OMNI.
(* ==== Area 52 ======
val =
Datatype 'stateRole = Omni'
```

```
val =
Datatype \quad `omniCommand \ = \ ssmPlanPBComplete
                     ssmMoveToORPComplete\\
                      ssmConductORPComplete
                      ssmMoveToPBComplete
                     ssmConductPBComplete\ `
val \ omniCommand\_distinct\_clauses = distinct\_of ``:omniCommand``
val = save_thm("omniCommand_distinct_clauses",
                omniCommand\_distinct\_clauses)
val =
Datatype 'slCommand = OMNI \ omniCommand'
val\ omniAuthentication\_def =
Define
`(omniAuthentication
        (\textit{Name Omni says prop } (\textit{cmd:} ((\textit{slCommand command}) \ \textit{option}))
        :((slCommand\ command)\ option\ ,\ stateRole\ ,\ 'd\ ,'e)Form)\ =\ T)\ /
 (omniAuthentication = F)
val\ omniAuthorization\_def =
Define
`(omniAuthorization")
        (Name Omni controls prop (cmd:((slCommand command) option))
        : ((slCommand\ command)\ option\ ,\ stateRole\ ,\ 'd\ , 'e)Form)\ =\ T)\ / \ 
 (omniAuthorization = F)
This may not be necessary...But, it is interesting. Save for a later time.
(* Prove that
(* Omni \ says \ omniCommand \Longrightarrow omniCommand
set\_goal([],
    ''(Name Omni says prop (cmd:((slCommand command) option))
       : ((slCommand\ command)\ option\ ,\ stateRole\ ,\ 'd\ , 'e)Form) = >
                    prop (cmd:((slCommand command) option))'')
val \ th \ 1 \ = \textit{ASSUME''(Name Omni says prop (cmd:((slCommand command) option))}
       :((slCommand\ command)\ option\ ,\ stateRole\ ,\ 'd\ ,'e)Form)=TT'
val th2 = REWRITE\_RULE[omniAuthentication\_def]th1
===== End Area 52 ==== *)
val = export_theory();
```

#### D.2 escapeLevel

#### D.3 TopLevel

#### D.3.1 PBTypeIntegrated Theory: Type Definitions

```
(*\ This\ theory\ contains\ the\ type\ definitions\ for\ ssmPBIntegrated
structure PBTypeIntegratedScript = struct
(* ==== Interactive Mode ====
app load ["TypeBase"]
open\ TypeBase
=== end Interactive Mode ==== *)
open HolKernel Parse boolLib bossLib;
\mathbf{open} \;\; \mathbf{TypeBase} \;\; \mathbf{OMNITypeTheory}
val _= new_theory "PBTypeIntegrated";
(* Define types
val _=
Datatype 'plCommand = crossLD (* Move to MOVE_TO_ORP state *)
                     conductORP
                     moveToPB
                     {\tt conductPB}
                     completePB
                    incomplete '
val plCommand_distinct_clauses = distinct_of ':plCommand'
val = save_thm("plCommand_distinct_clauses",
                plCommand_distinct_clauses)
val _=
Datatype 'omniCommand = ssmPlanPBComplete
                     ssmMoveToORPComplete
                     ssmConductORPComplete
                     ssmMoveToPBComplete
                     ssmConductPBComplete
                     invalidOmniCommand '
\mathbf{val} \ \mathtt{omniCommand\_distinct\_clauses} \ = \ \mathtt{distinct\_of} \ ``:\mathtt{omniCommand}``
val _= save_thm("omniCommand_distinct_clauses",
                omniCommand_distinct_clauses)
val =
{\tt Datatype \ `slCommand = PL \ plCommand}
                   | OMNI omniCommand '
val slCommand_distinct_clauses = distinct_of ':slCommand''
val _= save_thm("slCommand_distinct_clauses",
                slCommand_distinct_clauses)
val slCommand_one_one = one_one_of '':slCommand''
val _= save_thm("slCommand_one_one", slCommand_one_one)
val _=
Datatype 'stateRole = PlatoonLeader | Omni'
val stateRole_distinct_clauses = distinct_of ':stateRole''
val _= save_thm("stateRole_distinct_clauses",
                stateRole_distinct_clauses)
{\tt Datatype 'slState = PLAN\_PB}
                   MOVE_TO_ORP
                   CONDUCT_ORP
                   MOVE_TO_PB
                   CONDUCT_PB
```

#### | COMPLETE\_PB'

# D.3.2 PBIntegratedDef Theory: Authentication & Authorization Definitions

```
(* PBIntegratedDefTheory
(* Author: Lori Pickering
(* Date: 7 May 2018
(*\ Definitions\ for\ ssmPBIntegrated\ Theory\ .
structure PBIntegratedDefScript = struct
(* ==== Interactive Mode ====
"OMNITypeTheory"
          "PBIntegrated Def Theory", "PBType Integrated Theory"];\\
open\ TypeBase\ listTheory\ optionTheory
     a \, clsemantics \, Theory \quad a \, clfound at ion \, Theory
     u\,a\,v\,U\,t\,i\,l\,i\,t\,i\,e\,s
     OMNITypeTheory
     PBIntegrated Def Theory \ PBType Integrated Theory
   = end Interactive Mode === *)
open HolKernel Parse boolLib bossLib;
open TypeBase listTheory optionTheory
open uavUtilities
open OMNITypeTheory PBTypeIntegratedTheory
val _ = new_theory "PBIntegratedDef";
(* state Interpretation function
(* This function doesn't do anything but is necessary to specialize other
(* theorems.
val secContext_def = Define '
    secContext (x:((slCommand command)option, stateRole, 'd,'e)Form list) =
        [(TT:((slCommand command)option, stateRole, 'd, 'e)Form)]'
val secHelper =
Define '
  (secHelper (cmd:omniCommand) =
     [(Name Omni) controls prop (SOME (SLc (OMNI (cmd:omniCommand))))])'
val getOmniCommand\_def =
  (getOmniCommand \ ([]:((slCommand \ command) \ option \ , \ stateRole \ , \ 'd \ , 'e)Form \ list)
```

```
= invalidOmniCommand:omniCommand) /\
       (\texttt{getOmniCommand} \ (((\texttt{Name Omni}) \ \texttt{controls prop} \ (\texttt{SOME} \ (\texttt{SLc} \ (\texttt{OMNI} \ \texttt{cmd}))))) :: xs)
                                                                                   = (cmd:omniCommand)) /\
       (getOmniCommand ((x:((slCommand command)option, stateRole, 'd,'e)Form)::xs)
                                                                                  = (getOmniCommand xs))'
val secAuthorization_def =
Define '
       (secAuthorization (xs:((slCommand command)option, stateRole,'d,'e)Form list)
                                                                  = secHelper (getOmniCommand xs))
\mathbf{val} \ \sec \mathtt{Context\_def} =
Define '
   (secContext (PLAN_PB) ((x:((slCommand command)option, stateRole, 'd,'e)Form)::xs) =
                              [(prop (SOME (SLc (OMNI (ssmPlanPBComplete))))
                                   :((slCommand command)option, stateRole, 'd, 'e)Form) impf
                                  (Name PlatoonLeader) controls prop (SOME (SLc (PL crossLD))) :((slCommand command) option, stateRole, 'd,'e)Form])
   (secContext (MOVE_TO_ORP) ((x:((slCommand command) option, stateRole, 'd,'e)Form)::xs) = (secContext (MOVE_TO_ORP) ((x:((slCommand command) option, stateRole, 'd,'e)Form) ((x:((slCommand) option, stateRole, 'd,'e)Form) ((x:((slCommand) option, stateRole, 'd,'e)Form) ((x:((slCommand command) option, stateRole, 'd,'e)Form) ((x:((slCommand command) option, stateRole, 'd,'e)Form) ((x:((slCommand) option, stateRole, 'd,'e)Form)
                              [prop (SOME (SLc (OMNI (ssmMoveToORPComplete)))) impf
                                   (Name PlatoonLeader) controls prop (SOME (SLc (PL conductORP)))]) /
   (secContext (CONDUCT_ORP) ((x:((slCommand command)option, stateRole, 'd, 'e)Form)::xs) =
                              [prop (SOME (SLc (OMNI (ssmConductORPComplete)))) impf
   (Name PlatoonLeader) controls prop (SOME (SLc (PL moveToPB)))]) /\
(secContext (MOVE_TO_PB) ((x:((slCommand command) option, stateRole, 'd,'e)Form)::xs) =
                              [prop (SOME (SLc (OMNI (ssmMoveToPBComplete)))) impf
                                  (Name PlatoonLeader) controls prop (SOME (SLc (PL conductPB)))]) /
   (secContext \ (CONDUCT.PB) \ ((x:((slCommand \ command) \ option \ , \ stateRole \ , \ 'd \ , 'e)Form)::xs) = (secContext \ (CONDUCT.PB) \ ((x:((slCommand \ command) \ option \ , \ stateRole \ , \ 'd \ , 'e)Form)::xs) = (secContext \ (CONDUCT.PB) \ ((x:((slCommand \ command) \ option \ , \ stateRole \ , \ 'd \ , 'e)Form)::xs) = (secContext \ (CONDUCT.PB) \ ((x:((slCommand \ command) \ option \ , \ stateRole \ , \ 'd \ , 'e)Form)::xs) = (secContext \ (context \ context \ context \ (context \ context \ context \ context \ context \ (context \ context \ context
                              [prop (SOME (SLc (OMNI (ssmConductPBComplete)))) impf
                                   (Name PlatoonLeader) controls prop (SOME (SLc (PL completePB)))])'
 (* ==== Area 52 ====
   ==== End Area 52 ==== *)
val = export_theory();
end
```

#### D.3.3 ssmPlanPBIntegrated Theory: Theorems

```
(* ssmPBIntegratedTheory
(* Author: Lori Pickering
(* Date: 7 May 2018
(* This theory aims to integrate the topLevel ssm with the sublevel ssms.
(* does this by adding a condition to the security context. In particular, (* it requires that the "COMPLETE" state in the subLevel ssm must precede (* transition to the next state at the topLeve. I.e.,
     planPBComplete ==>
      PlatoonLeader\ controls\ crossLD .
(* In the ssmPlanPB ssm, the last state is COMPLETE. This is reached when the *)
(* the appropriate authority says complete and the transition is made.
(* Note that following the ACL, if P says x and P controls x, then x.
(* Therefore, it is not necessary for anyone to say x at the topLevel, because*)
(* it is already proved at the lower level.
(* However, indicating that at the topLevel remains something to workout.
structure ssmPBIntegratedScript = struct
(* ==== Interactive Mode ====
            ["TypeBase", "listTheory","optionTheory","listSyntax",
"acl_infRules","aclDrulesTheory","aclrulesTheory",
            "aclsemantics Theory", "aclfoundation Theory",
"satList Theory", "ssm Theory", "ssminfRules", "uav Utilities",
"OMNITypeTheory", "PB TypeIntegrated Theory", "PBIntegrated Def Theory",
            "ssmPBIntegratedTheory"];
open\ TypeBase\ listTheory\ optionTheory\ listSyntax
```

```
acl\_infRules aclDrulesTheory aclrulesTheory
     a clse mantics Theory \ a clfoundation Theory
     satListTheory \ ssmTheory \ ssminfRules \ uavUtilities
     OMNIType Theory \ PBType Integrated Theory \ PBIntegrated Def Theory
     ssmPBIntegratedTheory
   == end Interactive Mode ==== *)
open HolKernel Parse boolLib bossLib;
open TypeBase listTheory optionTheory
open acl_infRules aclDrulesTheory aclrulesTheory
{\bf open} \ \ {\bf satListTheory} \ \ {\bf ssmTheory} \ \ {\bf ssminfRules} \ \ {\bf uavUtilities}
open OMNITypeTheory PBTypeIntegratedTheory PBIntegratedDefTheory
val _ = new_theory "ssmPBIntegrated";
(* Define next-state and next-output functions
val PBNS_def =
Define '
(PBNS PLAN_PB
                  (exec [SOME (SLc (PL crossLD))])
                                                       = MOVE_TO_ORP) /\
(PBNS MOVE.TO.ORP (exec [SOME (SLc (PL conductORP))]) = CONDUCT.ORP) /\
(PBNS CONDUCT.ORP (exec [SOME (SLc (PL moveToPB))]) = MOVE.TO.PB) /\
(PBNS MOVE.TO.PB (exec [SOME (SLc (PL conductPB))]) = CONDUCT.PB) /\
(PBNS CONDUCT_PB (exec [SOME (SLc (PL completePB))]) = COMPLETE_PB) /\
(PBNS (s:slState) (trap _) = s) /\
(PBNS (s:slState) (discard _) = s) '
val PBOut_def =
Define '
(PBOut PLAN_PB
                    (exec [SOME (SLc (PL crossLD))])
                                                       = MoveToORP) /
(PBOut MOVE.TO.ORP (exec [SOME (SLc (PL conductORP))]) = ConductORP) /\
(PBOut CONDUCT.ORP (exec [SOME (SLc (PL moveToPB))]) = MoveToPB) /\
(PBOut MOVE.TO.PB (exec [SOME (SLc (PL conductPB))]) = ConductPB) /\
(PBOut CONDUCT_PB (exec [SOME (SLc (PL completePB))]) = CompletePB) /\
(PBOut (s:slState) (trap _) = unAuthorized) /\
(PBOut (s:slState) (discard _) = unAuthenticated) '
(* Define authentication function
(***********************
val inputOK_def =
Define '
(inputOK (((Name PlatoonLeader) says prop (cmd:((slCommand command)option)))
           :((slCommand command)option, stateRole, 'd, 'e)Form) = T) /\
(inputOK (((Name Omni) says prop (cmd:((slCommand command)option)))
           :((slCommand command)option, stateRole, 'd, 'e)Form) = T) /\
(inputOK _ = F)
(* Prove that commands are rejected unless that are requested by a properly
(* authenticated principal.
val inputOK_cmd_reject_lemma =
Q. prove ('!cmd. ~(inputOK
                  ((prop (SOME cmd))))',
                               (PROVE_TAC[inputOK_def]))
(* ==== Just playing around with this ====
val\ inputOK\_not\_reject\_lemma =
Q. prove ( '!cmd.
          (input OK \ (((Name \ PlatoonLeader) \ says \ prop \ (cmd:((slCommand \ command) \ option)))
           :((slCommand\ command)\ option\ ,\ stateRole\ ,\ 'd\ ,\ 'e)Form))\ \setminus /
          (inputOK\ (((Name\ Omni)\ says\ prop\ (cmd:((slCommand\ command)\ option)))
           :((slCommand command)option, stateRole,'d,'e)Form)))
```

```
==== OK, done fooling around ==== *)

val _ = export_theory();
end
```

#### D.4 Horizontal Slice

D.4.1	ssmPlanPB
D.4.1.1	PlanPBType Theory: Type Definitions
D.4.1.2	PlanPBDef Theory: Authentication & Authorization Definitions
D.4.1.3	ssmPlanPB Theory: Theorems
D.4.2	${\bf ssmMoveToORP}$
D.4.2.1	MoveToORPType Theory: Type Definitions
D.4.2.2	MoveToORPDef Theory: Authentication & Authorization Definitions
D.4.2.3	ssmMoveToORP Theory: Theorems
D.4.3	$\operatorname{ssmConductORP}$
D.4.3.1	ConductORPType Theory: Type Definitions
D.4.3.2	ConductORPDef Theory: Authentication & Authorization Definitions
D.4.3.3	ssmConductORP Theory: Theorems
D.4.4	ssmMoveToPB
D.4.4.1	MoveToPBType Theory: Type Definitions
D.4.4.2	MoveToPBDef Theory: Authentication & Authorization Definitions

159

D.4.5 ssmConductPB

D.4.4.3 ssmMoveToPB Theory: Theorems

# Appendix E

Map of The File Folder Structure

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