Contents

1	PBTypeIntegrated Theory	3
	1.1 Datatypes	3
	1.2 Theorems	3
2	ssmPBIntegrated Theory 2.1 Theorems	4 5
3	i Bintegrated Ber Theory	11
	3.1 Definitions	
	3.2 Theorems	12

1 PBTypeIntegrated Theory

Built: 11 June 2018

Parent Theories: OMNIType

1.1 Datatypes

1.2 Theorems

```
[omniCommand_distinct_clauses]
```

```
\vdash ssmPlanPBComplete \neq ssmMoveToORPComplete \land
    ssmPlanPBComplete \neq ssmConductORPComplete \land
    ssmPlanPBComplete \neq ssmMoveToPBComplete \land
    {\tt ssmPlanPBComplete} \, \neq \, {\tt ssmConductPBComplete} \, \, \wedge \,
    ssmPlanPBComplete \neq invalidOmniCommand \land
    ssmMoveToORPComplete \neq ssmConductORPComplete \land
    {\tt ssmMoveToORPComplete} \ \neq \ {\tt ssmMoveToPBComplete} \ \land \\
    {\tt ssmMoveToORPComplete} \ \neq \ {\tt ssmConductPBComplete} \ \land \\
    {\tt ssmMoveToORPComplete} \, \neq \, {\tt invalidOmniCommand} \, \, \wedge \, \,
    ssmConductORPComplete \neq ssmMoveToPBComplete \land
    ssmConductORPComplete \neq ssmConductPBComplete \land
    {\tt ssmConductORPComplete} \neq {\tt invalidOmniCommand} \ \land \\
    {\tt ssmMoveToPBComplete} \, \neq \, {\tt ssmConductPBComplete} \, \, \wedge \,
    ssmMoveToPBComplete \neq invalidOmniCommand \land
    ssmConductPBComplete \neq invalidOmniCommand
[plCommand_distinct_clauses]
 \vdash crossLD \neq conductORP \land crossLD \neq moveToPB \land
    crossLD \neq conductPB \land crossLD \neq completePB \land
```

 $crossLD \neq incomplete \land conductORP \neq moveToPB \land$

```
conductORP \neq conductPB \land conductORP \neq completePB \land
     \verb|conductORP| \neq \verb|incomplete| \land \verb|moveToPB| \neq \verb|conductPB| \land
     moveToPB \neq completePB \land moveToPB \neq incomplete \land
     conductPB \neq completePB \land conductPB \neq incomplete \land
     completePB \neq incomplete
[slCommand_distinct_clauses]
 \vdash \forall a' \ a. \ PL \ a \neq OMNI \ a'
[slCommand_one_one]
 \vdash (\forall a \ a'. (PL a = PL \ a') \iff (a = a')) \land
     \forall a \ a'. (OMNI a = OMNI \ a') \iff (a = a')
[slOutput_distinct_clauses]
 \vdash PlanPB \neq MoveToORP \land PlanPB \neq ConductORP \land
     {\tt PlanPB} \neq {\tt MoveToPB} \ \land \ {\tt PlanPB} \neq {\tt ConductPB} \ \land
     {\tt PlanPB} \neq {\tt CompletePB} \ \land \ {\tt PlanPB} \neq {\tt unAuthenticated} \ \land
     PlanPB \neq unAuthorized \land MoveToORP \neq ConductORP \land
     MoveToORP \neq MoveToPB \land MoveToORP \neq ConductPB \land
     {\tt MoveToORP} \neq {\tt CompletePB} \ \land \ {\tt MoveToORP} \neq {\tt unAuthenticated} \ \land
     \texttt{MoveToORP} \neq \texttt{unAuthorized} \ \land \ \texttt{ConductORP} \neq \texttt{MoveToPB} \ \land \\
     \mathtt{ConductORP} \neq \mathtt{ConductPB} \land \mathtt{ConductORP} \neq \mathtt{CompletePB} \land
     {\tt ConductORP} \neq {\tt unAuthenticated} \ \land \ {\tt ConductORP} \neq {\tt unAuthorized} \ \land
     \texttt{MoveToPB} \, \neq \, \texttt{ConductPB} \, \, \land \, \, \texttt{MoveToPB} \, \neq \, \texttt{CompletePB} \, \, \land \, \,
     	exttt{MoveToPB} 
eq 	ext{unAuthenticated} 
\wedge 	ext{MoveToPB} 
eq 	ext{unAuthorized} 
\wedge
     ConductPB \neq CompletePB \land ConductPB \neq unAuthenticated \land
     ConductPB \neq unAuthorized \land CompletePB \neq unAuthenticated \land
     CompletePB \neq unAuthorized \land unAuthenticated \neq unAuthorized
[slState_distinct_clauses]
 \vdash PLAN_PB \neq MOVE_TO_ORP \land PLAN_PB \neq CONDUCT_ORP \land
     PLAN_PB \neq MOVE_TO_PB \wedge PLAN_PB \neq CONDUCT_PB \wedge
     {\tt PLAN\_PB} \, \neq \, {\tt COMPLETE\_PB} \, \wedge \, {\tt MOVE\_TO\_ORP} \, \neq \, {\tt CONDUCT\_ORP} \, \wedge \,
     \texttt{MOVE\_TO\_ORP} \ \neq \ \texttt{MOVE\_TO\_PB} \ \land \ \texttt{MOVE\_TO\_ORP} \ \neq \ \texttt{CONDUCT\_PB} \ \land \\
     MOVE_TO_ORP ≠ COMPLETE_PB ∧ CONDUCT_ORP ≠ MOVE_TO_PB ∧
     {\tt CONDUCT\_ORP} \ \neq \ {\tt CONDUCT\_PB} \ \land \ {\tt CONDUCT\_ORP} \ \neq \ {\tt COMPLETE\_PB} \ \land
     MOVE_TO_PB ≠ CONDUCT_PB ∧ MOVE_TO_PB ≠ COMPLETE_PB ∧
     CONDUCT_PB ≠ COMPLETE_PB
[stateRole_distinct_clauses]
 \vdash PlatoonLeader \neq Omni
```

2 ssmPBIntegrated Theory

Built: 11 June 2018

Parent Theories: PBIntegratedDef, ssm

2.1 Theorems

```
[inputOK_cmd_reject_lemma]
 \vdash \ orall \ cmd . \lnot \mathtt{inputOK} (prop (SOME cmd))
[inputOK_def]
 \vdash (inputOK (Name PlatoonLeader says prop cmd) \iff T) \land
     (inputOK (Name Omni says prop cmd) \iff T) \land
     (inputOK TT \iff F) \land (inputOK FF \iff F) \land
     (inputOK (prop v) \iff F) \land (inputOK (notf v_1) \iff F) \land
     (inputOK (v_2 andf v_3) \iff F) \wedge (inputOK (v_4 orf v_5) \iff F) \wedge
     (inputOK (v_6 impf v_7) \iff F) \land (inputOK (v_8 eqf v_9) \iff F) \land
     (inputOK (v_{10} \text{ says TT}) \iff \text{F}) \land (\text{inputOK } (v_{10} \text{ says FF}) \iff \text{F}) \land
     (inputOK (v133 meet v134 says prop v_{66}) \iff F) \land
     (inputOK (v135 quoting v136 says prop v_{66}) \iff F) \land
     (inputOK (v_{10} says notf v_{67}) \iff F) \land
     (inputOK (v_{10} says (v_{68} andf v_{69})) \iff F) \land
     (inputOK (v_{10} says (v_{70} orf v_{71})) \iff F) \wedge
     (inputOK (v_{10} says (v_{72} impf v_{73})) \iff F) \land
     (inputOK (v_{10} says (v_{74} eqf v_{75})) \iff F) \land
     (inputOK (v_{10} says v_{76} says v_{77}) \iff F) \land
     (inputOK (v_{10} says v_{78} speaks_for v_{79}) \iff F) \wedge
     (inputOK (v_{10} says v_{80} controls v_{81}) \iff F) \wedge
     (inputOK (v_{10} says reps v_{82} v_{83} v_{84}) \iff F) \land
     (inputOK (v_{10} says v_{85} domi v_{86}) \iff F) \wedge
     (inputOK (v_{10} says v_{87} eqi v_{88}) \iff F) \wedge
     (inputOK (v_{10} says v_{89} doms v_{90}) \iff F) \wedge
     (inputOK (v_{10} says v_{91} eqs v_{92}) \iff F) \land
     (inputOK (v_{10} says v_{93} eqn v_{94}) \iff F) \wedge
     (inputOK (v_{10} says v_{95} lte v_{96}) \iff F) \wedge
     (inputOK (v_{10} says v_{97} lt v_{98}) \iff F) \wedge
     (inputOK (v_{12} speaks_for v_{13}) \iff F) \wedge
     (inputOK (v_{14} controls v_{15}) \iff F) \wedge
     (inputOK (reps v_{16} v_{17} v_{18}) \iff F) \wedge
     (inputOK (v_{19} domi v_{20}) \iff F) \wedge
     (inputOK (v_{21} eqi v_{22}) \iff F) \wedge
     (inputOK (v_{23} doms v_{24}) \iff F) \wedge
     (inputOK (v_{25} eqs v_{26}) \iff F) \wedge (inputOK (v_{27} eqn v_{28}) \iff F) \wedge
     (inputOK (v_{29} lte v_{30}) \iff F) \wedge (inputOK (v_{31} lt v_{32}) \iff F)
[inputOK_ind]
 \vdash \forall P.
        (\forall \, cmd \, . \, P \, (\texttt{Name PlatoonLeader says prop} \, \, cmd)) \, \land \,
        (\forall \, cmd \, . \, P \, \, ({\tt Name \, \, Omni \, \, says \, \, prop \, \, } cmd)) \, \wedge \, P \, \, {\tt TT} \, \wedge \, P \, \, {\tt FF} \, \, \wedge \,
        (\forall v. P (prop v)) \land (\forall v_1. P (notf v_1)) \land
        (\forall v_2 \ v_3. \ P \ (v_2 \ \text{andf} \ v_3)) \ \land \ (\forall v_4 \ v_5. \ P \ (v_4 \ \text{orf} \ v_5)) \ \land
        (\forall v_6 \ v_7. \ P \ (v_6 \ \text{impf} \ v_7)) \land (\forall v_8 \ v_9. \ P \ (v_8 \ \text{eqf} \ v_9)) \land
        (\forall v_{10}. \ P \ (v_{10} \ \text{says TT})) \land (\forall v_{10}. \ P \ (v_{10} \ \text{says FF})) \land
        (\forall v133 \ v134 \ v_{66}. \ P \ (v133 \ \text{meet} \ v134 \ \text{says prop} \ v_{66})) \land
```

```
(\forall v135 \ v136 \ v_{66}. \ P \ (v135 \ \text{quoting} \ v136 \ \text{says prop} \ v_{66})) \ \land
           (\forall v_{10} \ v_{67}. \ P \ (v_{10} \ \text{says notf} \ v_{67})) \ \land
           (\forall v_{10} \ v_{68} \ v_{69}. \ P \ (v_{10} \ \text{says} \ (v_{68} \ \text{andf} \ v_{69}))) \ \land
           (\forall v_{10} \ v_{70} \ v_{71}. \ P \ (v_{10} \ \text{says} \ (v_{70} \ \text{orf} \ v_{71}))) \ \land
           (\forall v_{10} \ v_{72} \ v_{73}. \ P \ (v_{10} \ \text{says} \ (v_{72} \ \text{impf} \ v_{73}))) \ \land
           (\forall\,v_{10}\ v_{74}\ v_{75}. P (v_{10} says (v_{74} eqf v_{75}))) \wedge
           (\forall v_{10} \ v_{76} \ v_{77}. \ P \ (v_{10} \ \text{says} \ v_{76} \ \text{says} \ v_{77})) \ \land
           (\forall v_{10} \ v_{78} \ v_{79}. \ P \ (v_{10} \ \text{says} \ v_{78} \ \text{speaks\_for} \ v_{79})) \ \land
           (\forall v_{10} \ v_{80} \ v_{81}. \ P \ (v_{10} \ \text{says} \ v_{80} \ \text{controls} \ v_{81})) \ \land
           (\forall v_{10} \ v_{82} \ v_{83} \ v_{84}. \ P \ (v_{10} \ \text{says reps} \ v_{82} \ v_{83} \ v_{84})) \ \land
           (\forall v_{10} \ v_{85} \ v_{86}. \ P \ (v_{10} \ \text{says} \ v_{85} \ \text{domi} \ v_{86})) \ \land
           (\forall v_{10} \ v_{87} \ v_{88}. \ P \ (v_{10} \ \text{says} \ v_{87} \ \text{eqi} \ v_{88})) \ \land
           (\forall \, v_{10} \ v_{89} \ v_{90} \, . \ P \ (v_{10} \ {\tt says} \ v_{89} \ {\tt doms} \ v_{90})) \ \land
           (\forall v_{10} \ v_{91} \ v_{92}. \ P \ (v_{10} \ \text{says} \ v_{91} \ \text{eqs} \ v_{92})) \ \land
           (\forall v_{10} \ v_{93} \ v_{94}. P (v_{10} says v_{93} eqn v_{94})) \land
           (\forall v_{10} \ v_{95} \ v_{96}. \ P \ (v_{10} \ \text{says} \ v_{95} \ \text{lte} \ v_{96})) \ \land
           (\forall v_{10} \ v_{97} \ v_{98}. \ P \ (v_{10} \ \text{says} \ v_{97} \ \text{lt} \ v_{98})) \ \land
           (\forall v_{12} \ v_{13}. \ P \ (v_{12} \ \text{speaks\_for} \ v_{13})) \ \land
           (\forall v_{14} \ v_{15}. \ P \ (v_{14} \ \text{controls} \ v_{15})) \ \land
           (\forall v_{16} \ v_{17} \ v_{18}. P (reps v_{16} \ v_{17} \ v_{18})) \land
           (\forall v_{19} \ v_{20}. \ P \ (v_{19} \ \text{domi} \ v_{20})) \ \land
           (\forall v_{21} \ v_{22}. \ P \ (v_{21} \ \text{eqi} \ v_{22})) \ \land
           (\forall v_{23} \ v_{24}. \ P \ (v_{23} \ \text{doms} \ v_{24})) \ \land
           (\forall v_{25} \ v_{26}. \ P \ (v_{25} \ \text{eqs} \ v_{26})) \land (\forall v_{27} \ v_{28}. \ P \ (v_{27} \ \text{eqn} \ v_{28})) \land
           (\forall v_{29} \ v_{30}. \ P \ (v_{29} \ \text{lte} \ v_{30})) \land (\forall v_{31} \ v_{32}. \ P \ (v_{31} \ \text{lt} \ v_{32})) \Rightarrow
          \forall v. P v
[PBNS_def]
  \vdash (PBNS PLAN_PB (exec x) =
        if getPlCom x = crossLD then MOVE_TO_ORP else PLAN_PB) \wedge
       (PBNS MOVE_TO_ORP (exec x) =
        if getPlCom x = conductORP then CONDUCT_ORP
        else MOVE_TO_ORP) 
       (PBNS CONDUCT_ORP (exec x) =
        if getPlCom x = moveToPB then MOVE_TO_PB else CONDUCT_ORP) \wedge
       (PBNS MOVE_TO_PB (exec x) =
        if getPlCom x = conductPB then CONDUCT_PB else MOVE_TO_PB) \wedge
       (PBNS CONDUCT_PB (exec x) =
        if getPlCom x = completePB then COMPLETE_PB
        else CONDUCT_PB) \land (PBNS s (trap v_0) = s) \land
       (PBNS s (discard v_1) = s)
[PBNS_ind]
  \vdash \forall P.
           (\forall x. \ P \ \text{PLAN_PB (exec } x)) \land (\forall x. \ P \ \text{MOVE\_TO\_ORP (exec } x)) \land
           (\forall x. \ P \ \texttt{CONDUCT\_ORP} \ (\texttt{exec} \ x)) \ \land
           (\forall x. \ P \ \texttt{MOVE\_TO\_PB} \ (\texttt{exec} \ x)) \ \land \ (\forall x. \ P \ \texttt{CONDUCT\_PB} \ (\texttt{exec} \ x)) \ \land
           (\forall s \ v_0. \ P \ s \ (\mathsf{trap} \ v_0)) \ \land \ (\forall s \ v_1. \ P \ s \ (\mathsf{discard} \ v_1)) \ \land
           (\forall v_6. \ P \ \texttt{COMPLETE\_PB} \ (\texttt{exec} \ v_6)) \Rightarrow
          \forall v \ v_1 . \ P \ v \ v_1
```

```
[PBOut_def]
 \vdash (PBOut PLAN_PB (exec x) =
     if getPlCom x = crossLD then MoveToORP else PlanPB) \wedge
    (PBOut MOVE_TO_ORP (exec x) =
     if getPlCom x = conductORP then ConductORP else MoveToORP) \land
     (PBOut CONDUCT_ORP (exec x) =
     if getPlCom x = moveToPB then MoveToORP else ConductORP) \wedge
    (PBOut MOVE_TO_PB (exec x) =
     if getPlCom x = conductPB then ConductPB else MoveToPB) \land
    (PBOut CONDUCT_PB (exec x) =
     if getPlCom x = completePB then CompletePB else ConductPB) \land
    (PBOut s (trap v_0) = unAuthorized) \wedge
    (PBOut s (discard v_1) = unAuthenticated)
[PBOut_ind]
 \vdash \forall P.
       (\forall x. \ P \ \text{PLAN\_PB (exec } x)) \ \land \ (\forall x. \ P \ \text{MOVE\_TO\_ORP (exec } x)) \ \land
       (\forall x. \ P \ \texttt{CONDUCT\_ORP} \ (\texttt{exec} \ x)) \ \land
       (\forall \, x. \ P \ \texttt{MOVE\_TO\_PB} \ (\texttt{exec} \ x)) \ \land \ (\forall \, x. \ P \ \texttt{CONDUCT\_PB} \ (\texttt{exec} \ x)) \ \land \\
       (\forall s \ v_0. \ P \ s \ (\mathsf{trap} \ v_0)) \ \land \ (\forall s \ v_1. \ P \ s \ (\mathsf{discard} \ v_1)) \ \land
       (\forall v_6. \ P \ \texttt{COMPLETE\_PB} \ (\texttt{exec} \ v_6)) \Rightarrow
       \forall v \ v_1. \ P \ v \ v_1
[PlatoonLeader_Omni_notDiscard_slCommand_thm]
 \vdash \forall NS \ Out \ M \ Oi \ Os.
       \neg TR (M, Oi, Os)
           (discard
               [SOME (SLc (PL plCommand));
               SOME (SLc (OMNI omniCommand))])
           (CFG inputOK secContext secAuthorization
               ([Name Omni says prop (SOME (SLc (PL plCommand)));
                 Name PlatoonLeader says
                 prop (SOME (SLc (OMNI omniCommand)))]::ins) PLAN_PB
               outs)
           (CFG inputOK secContext secAuthorization ins
               (NS PLAN_PB
                  (discard
                       [SOME (SLc (PL plCommand));
                       SOME (SLc (OMNI omniCommand))]))
               (Out PLAN_PB
                   (discard
                       [SOME (SLc (PL plCommand));
                       SOME (SLc (OMNI omniCommand))])::outs))
[PlatoonLeader_PLAN_PB_exec_justified_lemma]
 \vdash \ \forall NS \ Out \ M \ Oi \ Os.
      TR (M, Oi, Os)
         (exec
```

```
(inputList
              [Name Omni says
              prop (SOME (SLc (OMNI ssmPlanPBComplete)));
              Name PlatoonLeader says
              prop (SOME (SLc (PL crossLD)))]))
       (CFG inputOK secContext secAuthorization
          ([Name Omni says
            prop (SOME (SLc (OMNI ssmPlanPBComplete)));
            Name PlatoonLeader says
            prop (SOME (SLc (PL crossLD)))]::ins) PLAN_PB outs)
       (CFG inputOK secContext secAuthorization ins
           (NS PLAN_PB
              (exec
                 (inputList
                    [Name Omni says
                     prop (SOME (SLc (OMNI ssmPlanPBComplete)));
                     Name PlatoonLeader says
                     prop (SOME (SLc (PL crossLD)))])))
           (Out PLAN_PB
              (exec
                 (inputList
                    [Name Omni says
                     prop (SOME (SLc (OMNI ssmPlanPBComplete)));
                     Name PlatoonLeader says
                     prop (SOME (SLc (PL crossLD)))]))::outs)) <=>
     authenticationTest inputOK
       [Name Omni says
        prop (SOME (SLc (OMNI ssmPlanPBComplete)));
        Name PlatoonLeader says
        prop (SOME (SLc (PL crossLD)))] \cap 
     CFGInterpret (M, Oi, Os)
       (CFG inputOK secContext secAuthorization
           ([Name Omni says
            prop (SOME (SLc (OMNI ssmPlanPBComplete)));
            Name PlatoonLeader says
            prop (SOME (SLc (PL crossLD)))]::ins) PLAN_PB
          outs) \land
     (M,Oi,Os) satList
     propCommandList
       [Name Omni says
        prop (SOME (SLc (OMNI ssmPlanPBComplete)));
        Name PlatoonLeader says prop (SOME (SLc (PL crossLD)))]
[PlatoonLeader_PLAN_PB_exec_justified_thm]
 \vdash \ \forall \, NS \ Out \ M \ Oi \ Os.
     TR (M, Oi, Os)
       (exec
           [SOME (SLc (OMNI ssmPlanPBComplete));
           SOME (SLc (PL crossLD))])
```

```
(CFG inputOK secContext secAuthorization
           ([Name Omni says
             prop (SOME (SLc (OMNI ssmPlanPBComplete)));
             Name PlatoonLeader says
             prop (SOME (SLc (PL crossLD)))]::ins) PLAN_PB outs)
        (CFG inputOK secContext secAuthorization ins
           (NS PLAN_PB
              (exec
                  [SOME (SLc (OMNI ssmPlanPBComplete));
                  SOME (SLc (PL crossLD))]))
           (Out\ PLAN_PB
              (exec
                  [SOME (SLc (OMNI ssmPlanPBComplete));
                  SOME (SLc (PL crossLD))])::outs)) \iff
     \verb"authenticationTest" input OK"
        [Name Omni says
        prop (SOME (SLc (OMNI ssmPlanPBComplete)));
        Name PlatoonLeader says
        prop (SOME (SLc (PL crossLD)))] \cap 
     CFGInterpret (M, Oi, Os)
        (CFG inputOK secContext secAuthorization
           ([Name Omni says
             prop (SOME (SLc (OMNI ssmPlanPBComplete)));
             Name PlatoonLeader says
             prop (SOME (SLc (PL crossLD)))]::ins) PLAN_PB
           outs) \land
      (M,Oi,Os) satList
      [prop (SOME (SLc (OMNI ssmPlanPBComplete)));
      prop (SOME (SLc (PL crossLD)))]
[PlatoonLeader_PLAN_PB_exec_lemma]
 \vdash \ \forall M \ Oi \ Os.
     CFGInterpret (M, Oi, Os)
        (CFG inputOK secContext secAuthorization
           ([Name Omni says
             prop (SOME (SLc (OMNI ssmPlanPBComplete)));
             Name PlatoonLeader says
             prop (SOME (SLc (PL crossLD)))]::ins) PLAN_PB
           outs) \Rightarrow
      (M, Oi, Os) satList
     propCommandList
        [Name Omni says
        prop (SOME (SLc (OMNI ssmPlanPBComplete)));
        Name PlatoonLeader says prop (SOME (SLc (PL crossLD)))]
[PlatoonLeader_PLAN_PB_trap_justified_lemma]
 \vdash \ omniCommand \neq  ssmPlanPBComplete \Rightarrow
   (s = PLAN_PB) \Rightarrow
   \forall NS \ Out \ M \ Oi \ Os.
```

TR (M, Oi, Os)

```
(trap
           (inputList
              [Name Omni says
               prop (SOME (SLc (OMNI omniCommand)));
               Name PlatoonLeader says
               prop (SOME (SLc (PL crossLD)))]))
        (CFG inputOK secContext secAuthorization
           ([Name Omni says prop (SOME (SLc (OMNI omniCommand)));
             Name PlatoonLeader says
             prop (SOME (SLc (PL crossLD)))]::ins) PLAN_PB outs)
        (CFG inputOK secContext secAuthorization ins
           (NS PLAN_PB
              (trap
                 (inputList
                    [Name Omni says
                     prop (SOME (SLc (OMNI omniCommand)));
                     Name PlatoonLeader says
                     prop (SOME (SLc (PL crossLD)))])))
           (Out PLAN_PB
              (trap
                 (inputList
                    [Name Omni says
                     prop (SOME (SLc (OMNI omniCommand)));
                     Name PlatoonLeader says
                     prop (SOME (SLc (PL crossLD)))]))::outs)) \iff
     authenticationTest inputOK
        [Name Omni says prop (SOME (SLc (OMNI omniCommand)));
        Name PlatoonLeader says
        prop (SOME (SLc (PL crossLD)))] \cap \)
     CFGInterpret (M, Oi, Os)
        (CFG inputOK secContext secAuthorization
           ([Name Omni says prop (SOME (SLc (OMNI omniCommand)));
             Name PlatoonLeader says
             prop (SOME (SLc (PL crossLD)))]::ins) PLAN_PB
           outs) \land (M, Oi, Os) sat prop NONE
[PlatoonLeader_PLAN_PB_trap_justified_thm]
 \vdash \ omniCommand \neq \texttt{ssmPlanPBComplete} \Rightarrow
   (s = PLAN_PB) \Rightarrow
   \forall NS \ Out \ M \ Oi \ Os.
     TR (M, Oi, Os)
        (trap
           [SOME (SLc (OMNI omniCommand));
           SOME (SLc (PL crossLD))])
        (CFG inputOK secContext secAuthorization
           ([Name Omni says prop (SOME (SLc (OMNI omniCommand)));
             Name PlatoonLeader says
             prop (SOME (SLc (PL crossLD)))]::ins) PLAN_PB outs)
```

```
(CFG inputOK secContext secAuthorization ins
           (NS PLAN_PB
              (trap
                  [SOME (SLc (OMNI omniCommand));
                  SOME (SLc (PL crossLD))]))
           (Out PLAN_PB
              (trap
                 [SOME (SLc (OMNI omniCommand));
                  SOME (SLc (PL crossLD))])::outs)) \iff
     authenticationTest inputOK
        [Name Omni says prop (SOME (SLc (OMNI omniCommand)));
        Name PlatoonLeader says
        prop (SOME (SLc (PL crossLD)))] \cap \)
     CFGInterpret (M, Oi, Os)
        (CFG inputOK secContext secAuthorization
           ([Name Omni says prop (SOME (SLc (OMNI omniCommand)));
             Name PlatoonLeader says
             prop (SOME (SLc (PL crossLD)))]::ins) PLAN_PB
           outs) \land (M, Oi, Os) sat prop NONE
[PlatoonLeader_PLAN_PB_trap_lemma]
 \vdash \ omniCommand \neq \texttt{ssmPlanPBComplete} \Rightarrow
    (s = PLAN_PB) \Rightarrow
   \forall M \ Oi \ Os.
     CFGInterpret (M, Oi, Os)
        (CFG inputOK secContext secAuthorization
           ([Name Omni says prop (SOME (SLc (OMNI omniCommand)));
             Name PlatoonLeader says
             prop (SOME (SLc (PL crossLD)))]::ins) PLAN_PB
           outs) \Rightarrow
      (M,Oi,Os) sat prop NONE
```

3 PBIntegratedDef Theory

```
Built: 11 June 2018
```

Parent Theories: PBTypeIntegrated, aclfoundation

3.1 Definitions

```
Name PlatoonLeader controls
          prop (SOME (SLc (PL crossLD)))]
       else [prop NONE]) ∧
    (\forall xs.
       secContext MOVE\_TO\_ORP xs =
       if getOmniCommand xs = ssmMoveToORPComplete then
         [prop (SOME (SLc (OMNI ssmMoveToORPComplete))) impf
          Name PlatoonLeader controls
          prop (SOME (SLc (PL conductORP)))]
       else [prop NONE]) ∧
    (\forall xs.
       secContext CONDUCT_ORP xs =
       if getOmniCommand xs = ssmConductORPComplete then
         [prop (SOME (SLc (OMNI ssmConductORPComplete))) impf
          Name PlatoonLeader controls
          prop (SOME (SLc (PL moveToPB)))]
       else [prop NONE]) ∧
    (\forall xs.
       secContext MOVE_TO_PB xs =
       if getOmniCommand xs = ssmConductORPComplete then
         [prop (SOME (SLc (OMNI ssmMoveToPBComplete))) impf
          Name PlatoonLeader controls
          prop (SOME (SLc (PL conductPB)))]
       else [prop NONE]) ∧
      secContext CONDUCT_PB xs =
      if getOmniCommand xs = ssmConductPBComplete then
        [prop (SOME (SLc (OMNI ssmConductPBComplete))) impf
         Name PlatoonLeader controls
         prop (SOME (SLc (PL completePB)))]
      else [prop NONE]
[secHelper_def]
 \vdash \forall cmd.
      secHelper \ cmd =
      [Name Omni controls prop (SOME (SLc (OMNI cmd)))]
3.2
      Theorems
[getOmniCommand_def]
 ├ (get0mniCommand [] = invalid0mniCommand) ∧
    (\forall xs \ cmd.
       get0mniCommand
         (Name Omni says prop (SOME (SLc (OMNI cmd)))::xs) =
       cmd) \wedge
    (\forall xs. \text{ getOmniCommand } (\text{TT}::xs) = \text{getOmniCommand } xs) \land
    (\forall xs. \text{ getOmniCommand } (\text{FF}::xs) = \text{getOmniCommand } xs) \land
    (\forall xs \ v_2. \ \text{getOmniCommand (prop } v_2::xs) = \text{getOmniCommand } xs) \land
```

```
(\forall xs \ v_3. \ \text{getOmniCommand (notf} \ v_3::xs) = \text{getOmniCommand} \ xs) \land
(\forall xs \ v_5 \ v_4.
   getOmniCommand (v_4 andf v_5::xs) = getOmniCommand xs) \land
(\forall xs \ v_7 \ v_6.
   getOmniCommand (v_6 orf v_7::x_8) = getOmniCommand x_8) \land
(\forall xs \ v_9 \ v_8.
   getOmniCommand (v_8 impf v_9::x_8) = getOmniCommand x_8) \land
(\forall xs \ v_{11} \ v_{10}.
   getOmniCommand (v_{10} eqf v_{11}::xs) = getOmniCommand xs) \land
(\forall xs \ v_{12}.
   getOmniCommand (v_{12} says TT::xs) = getOmniCommand xs) \land
(\forall xs \ v_{12}.
   getOmniCommand (v_{12} says FF::xs) = getOmniCommand xs) \land
(\forall xs \ v134.
   getOmniCommand (Name v134 says prop NONE::xs) =
   getOmniCommand xs) \land
(\forall xs \ v144.
   get0mniCommand
      (Name PlatoonLeader says prop (SOME v144)::xs) =
   getOmniCommand xs) \land
(\forall xs \ v146.
   get0mniCommand
      (Name Omni says prop (SOME (ESCc v146))::xs) =
   getOmniCommand xs) \land
(\forall xs \ v150.
   get0mniCommand
      (Name Omni says prop (SOME (SLc (PL v150)))::xs) =
   getOmniCommand xs) \land
(\forall xs \ v_{68} \ v136 \ v135.
   getOmniCommand (v135 meet v136 says prop v_{68}::xs) =
   getOmniCommand xs) \land
(\forall xs \ v_{68} \ v138 \ v137.
   getOmniCommand (v137 quoting v138 says prop v_{68}::xs) =
   getOmniCommand xs) \land
(\forall xs \ v_{69} \ v_{12}.
   getOmniCommand (v_{12} says notf v_{69}::xs) =
   getOmniCommand xs) \land
(\forall xs \ v_{71} \ v_{70} \ v_{12}.
   getOmniCommand (v_{12} says (v_{70} andf v_{71})::xs) =
   getOmniCommand xs) \land
(\forall xs \ v_{73} \ v_{72} \ v_{12}.
   getOmniCommand (v_{12} says (v_{72} orf v_{73})::xs) =
   getOmniCommand xs) \land
(\forall xs \ v_{75} \ v_{74} \ v_{12}.
   getOmniCommand (v_{12} says (v_{74} impf v_{75})::xs) =
   getOmniCommand xs) \land
(\forall xs \ v_{77} \ v_{76} \ v_{12}.
   getOmniCommand (v_{12} says (v_{76} eqf v_{77})::xs) =
   getOmniCommand xs) \land
```

```
(\forall xs \ v_{79} \ v_{78} \ v_{12}.
    getOmniCommand (v_{12} says v_{78} says v_{79}::xs) =
    getOmniCommand xs) \land
(\forall xs \ v_{81} \ v_{80} \ v_{12}.
    getOmniCommand (v_{12} says v_{80} speaks_for v_{81}::xs) =
    getOmniCommand xs) \land
(\forall xs \ v_{83} \ v_{82} \ v_{12}.
    getOmniCommand (v_{12} says v_{82} controls v_{83}::xs) =
    getOmniCommand xs) \land
(\forall xs \ v_{86} \ v_{85} \ v_{84} \ v_{12}.
    getOmniCommand (v_{12} says reps v_{84} v_{85} v_{86}::xs) =
    getOmniCommand xs) \land
(\forall xs \ v_{88} \ v_{87} \ v_{12}.
    getOmniCommand (v_{12} says v_{87} domi v_{88}::xs) =
    getOmniCommand xs) \land
(\forall xs \ v_{90} \ v_{89} \ v_{12}.
    getOmniCommand (v_{12} says v_{89} eqi v_{90}::xs) =
    getOmniCommand xs) \land
(\forall xs \ v_{92} \ v_{91} \ v_{12}.
    getOmniCommand (v_{12} says v_{91} doms v_{92}::xs) =
    getOmniCommand xs) \land
(\forall xs \ v_{94} \ v_{93} \ v_{12}.
    getOmniCommand (v_{12} says v_{93} eqs v_{94}::xs) =
    getOmniCommand xs) \land
(\forall xs \ v_{96} \ v_{95} \ v_{12}.
    getOmniCommand (v_{12} says v_{95} eqn v_{96}::xs) =
    getOmniCommand xs) \wedge
(\forall xs \ v_{98} \ v_{97} \ v_{12}.
    getOmniCommand (v_{12} says v_{97} lte v_{98}::xs) =
    getOmniCommand xs) \land
(\forall xs \ v_{99} \ v_{12} \ v_{100}.
    getOmniCommand (v_{12} says v_{99} lt v100::xs) =
    getOmniCommand xs) \land
(\forall xs \ v_{15} \ v_{14}.
    getOmniCommand (v_{14} speaks_for v_{15}::x_{5}) =
    getOmniCommand xs) \land
(\forall xs \ v_{17} \ v_{16}.
    getOmniCommand (v_{16} controls v_{17}::xs) =
    getOmniCommand xs) \land
(\forall xs \ v_{20} \ v_{19} \ v_{18}.
    getOmniCommand (reps v_{18} v_{19} v_{20}::xs) =
    getOmniCommand xs) \wedge
(\forall xs \ v_{22} \ v_{21}.
    getOmniCommand (v_{21} domi v_{22}::xs) = getOmniCommand xs) \land
(\forall xs \ v_{24} \ v_{23}.
    getOmniCommand (v_{23} eqi v_{24}::x_s) = getOmniCommand x_s) \land
(\forall xs \ v_{26} \ v_{25}.
    getOmniCommand (v_{25} doms v_{26}::xs) = getOmniCommand xs) \land
(\forall xs \ v_{28} \ v_{27}.
```

```
getOmniCommand (v_{27} eqs v_{28}::xs) = getOmniCommand xs) \land
      (\forall xs \ v_{30} \ v_{29}.
            getOmniCommand (v_{29} eqn v_{30}::xs) = getOmniCommand xs) \land
      (\forall xs \ v_{32} \ v_{31}.
            getOmniCommand (v_{31} lte v_{32}::xs) = getOmniCommand xs) \land
      \forall xs \ v_{34} \ v_{33}.
         getOmniCommand (v_{33} lt v_{34}::xs) = getOmniCommand xs
[getOmniCommand_ind]
  \vdash \forall P.
          P [] \land
          (\forall cmd xs.
                P (Name Omni says prop (SOME (SLc (OMNI cmd)))::xs)) \wedge
          (\forall xs. \ P \ xs \Rightarrow P \ (TT::xs)) \land (\forall xs. \ P \ xs \Rightarrow P \ (FF::xs)) \land
          (\forall v_2 \ xs. \ P \ xs \Rightarrow P \ (prop \ v_2::xs)) \land
          (\forall v_3 \ xs. \ P \ xs \Rightarrow P \ (notf \ v_3::xs)) \land
          (\forall v_4 \ v_5 \ xs. \ P \ xs \Rightarrow P \ (v_4 \ \text{andf} \ v_5::xs)) \ \land
          (\forall v_6 \ v_7 \ xs. \ P \ xs \Rightarrow P \ (v_6 \ \text{orf} \ v_7::xs)) \land
          (\forall v_8 \ v_9 \ xs. \ P \ xs \Rightarrow P \ (v_8 \ \text{impf} \ v_9::xs)) \land
          (\forall v_{10} \ v_{11} \ xs. \ P \ xs \Rightarrow P \ (v_{10} \ \text{eqf} \ v_{11}::xs)) \land
          (\forall v_{12} \ xs. \ P \ xs \Rightarrow P \ (v_{12} \ \text{says TT}::xs)) \land
          (\forall v_{12} \ xs. \ P \ xs \Rightarrow P \ (v_{12} \ \text{says FF}::xs)) \land
          (\forall v134 \ xs. \ P \ xs \Rightarrow P (Name v134 \ \text{says prop NONE::} xs)) \land
          (∀ v144 xs.
                P xs \Rightarrow
                P (Name PlatoonLeader says prop (SOME v144)::xs)) \wedge
          (\forall v146 \ xs.
                P xs \Rightarrow P \text{ (Name Omni says prop (SOME (ESCc } v146))::xs))} \land
          (\forall v150 \ xs.
                P xs \Rightarrow
                P (Name Omni says prop (SOME (SLc (PL v150)))::xs)) \land
          (\forall v135 \ v136 \ v_{68} \ xs.
                P \ xs \Rightarrow P \ (v135 \ \text{meet} \ v136 \ \text{says prop} \ v_{68}::xs)) \land
          (\forall v137 \ v138 \ v_{68} \ xs.
                P xs \Rightarrow P (v137 \text{ quoting } v138 \text{ says prop } v_{68}::xs)) \land
          (\forall v_{12} \ v_{69} \ xs. \ P \ xs \Rightarrow P \ (v_{12} \ {\tt says \ notf} \ v_{69}\!::\!xs)) \ \land
          (\forall v_{12} \ v_{70} \ v_{71} \ xs. \ P \ xs \Rightarrow P \ (v_{12} \ {\tt says} \ (v_{70} \ {\tt andf} \ v_{71})::xs)) \ \land
          (\forall v_{12} \ v_{72} \ v_{73} \ xs. \ P \ xs \Rightarrow P \ (v_{12} \ \text{says} \ (v_{72} \ \text{orf} \ v_{73})::xs)) \ \land
          (\forall v_{12} \ v_{74} \ v_{75} \ xs. \ P \ xs \Rightarrow P \ (v_{12} \ {\tt says} \ (v_{74} \ {\tt impf} \ v_{75})::xs)) \ \land
          (\forall v_{12} \ v_{76} \ v_{77} \ xs. \ P \ xs \Rightarrow P \ (v_{12} \ \text{says} \ (v_{76} \ \text{eqf} \ v_{77})::xs)) \ \land
          (\forall v_{12} \ v_{78} \ v_{79} \ xs. \ P \ xs \Rightarrow P \ (v_{12} \ \text{says} \ v_{78} \ \text{says} \ v_{79}::xs)) \land
          (\forall v_{12} \ v_{80} \ v_{81} \ xs.
               P xs \Rightarrow P (v_{12} \text{ says } v_{80} \text{ speaks\_for } v_{81} :: xs)) \land
          (\forall v_{12} \ v_{82} \ v_{83} \ xs.
               P xs \Rightarrow P (v_{12} \text{ says } v_{82} \text{ controls } v_{83} :: xs)) \land
          (\forall v_{12} \ v_{84} \ v_{85} \ v_{86} \ xs.
               P xs \Rightarrow P (v_{12} \text{ says reps } v_{84} v_{85} v_{86}::xs)) \land
          (\forall v_{12} \ v_{87} \ v_{88} \ xs. \ P \ xs \Rightarrow P \ (v_{12} \ \text{says} \ v_{87} \ \text{domi} \ v_{88}::xs)) \land
          (\forall v_{12} \ v_{89} \ v_{90} \ xs. \ P \ xs \Rightarrow P \ (v_{12} \ \text{says} \ v_{89} \ \text{eqi} \ v_{90}::xs)) \ \land
```

```
(\forall v_{12} \ v_{91} \ v_{92} \ xs. \ P \ xs \Rightarrow P \ (v_{12} \ \text{says} \ v_{91} \ \text{doms} \ v_{92} :: xs)) \ \land
           (\forall v_{12} \ v_{93} \ v_{94} \ xs. \ P \ xs \Rightarrow P \ (v_{12} \ \text{says} \ v_{93} \ \text{eqs} \ v_{94}::xs)) \ \land
           (\forall v_{12} \ v_{95} \ v_{96} \ xs. \ P \ xs \Rightarrow P \ (v_{12} \ \text{says} \ v_{95} \ \text{eqn} \ v_{96} :: xs)) \ \land
           (\forall v_{12} \ v_{97} \ v_{98} \ xs. \ P \ xs \Rightarrow P \ (v_{12} \ \text{says} \ v_{97} \ \text{lte} \ v_{98} :: xs)) \ \land
           (\forall v_{12} \ v_{99} \ v100 \ xs. \ P \ xs \Rightarrow P \ (v_{12} \ {\tt says} \ v_{99} \ {\tt lt} \ v100::xs)) \ \land
           (\forall v_{14} \ v_{15} \ xs. \ P \ xs \Rightarrow P (v_{14} speaks_for v_{15}::xs)) \land
           (\forall v_{16} \ v_{17} \ xs. \ P \ xs \Rightarrow P \ (v_{16} \ \texttt{controls} \ v_{17} :: xs)) \ \land
           (\forall v_{18} \ v_{19} \ v_{20} \ xs. \ P \ xs \Rightarrow P \ (reps \ v_{18} \ v_{19} \ v_{20}::xs)) \ \land
           (\forall v_{21} \ v_{22} \ xs. \ P \ xs \Rightarrow P \ (v_{21} \ \text{domi} \ v_{22}\!::\!xs)) \ \land
           (\forall v_{23} \ v_{24} \ xs. \ P \ xs \Rightarrow P \ (v_{23} \ \text{eqi} \ v_{24}::xs)) \land
           (\forall v_{25} \ v_{26} \ xs. \ P \ xs \Rightarrow P \ (v_{25} \ \text{doms} \ v_{26}::xs)) \land
           (\forall v_{27} \ v_{28} \ xs. \ P \ xs \Rightarrow P \ (v_{27} \ \text{eqs} \ v_{28}::xs)) \land
           (\forall v_{29} \ v_{30} \ xs. \ P \ xs \Rightarrow P \ (v_{29} \ \text{eqn} \ v_{30} \colon : xs)) \land
           (\forall v_{31} \ v_{32} \ xs. \ P \ xs \Rightarrow P \ (v_{31} \ \text{lte} \ v_{32}{::}xs)) \ \land
           (\forall v_{33} \ v_{34} \ xs. \ P \ xs \Rightarrow P \ (v_{33} \ \text{lt} \ v_{34}{::}xs)) \Rightarrow
           \forall v. P v
[getPlCom_def]
  ⊢ (getPlCom [] = incomplete) ∧
       (\forall xs \ cmd. \ \text{getPlCom} \ (\text{SOME} \ (\text{SLc} \ (\text{PL} \ cmd))::xs) = cmd) \land
       (\forall xs. \text{ getPlCom (NONE::} xs) = \text{getPlCom } xs) \land
       (\forall xs \ v_4. \ \text{getPlCom} \ (\text{SOME} \ (\text{ESCc} \ v_4)::xs) = \text{getPlCom} \ xs) \land
       \forall xs \ v_9. getPlCom (SOME (SLc (OMNI v_9))::xs) = getPlCom xs
[getPlCom_ind]
  \vdash \forall P.
           P \ [] \land (\forall cmd \ xs. \ P \ (SOME \ (SLc \ (PL \ cmd))::xs)) \land
           (\forall xs. P xs \Rightarrow P (NONE::xs)) \land
           (\forall v_4 \ xs. \ P \ xs \Rightarrow P \ (SOME \ (ESCc \ v_4)::xs)) \land
           (\forall v_9 \ xs. \ P \ xs \Rightarrow P \ (SOME \ (SLc \ (OMNI \ v_9))::xs)) \Rightarrow
           \forall v. P v
```

Index

```
PBIntegratedDef Theory, 11
                                               PlatoonLeader_PLAN_PB_trap_justi-
   Definitions, 11
                                                 fied_thm, 10
                                               PlatoonLeader_PLAN_PB_trap_lemma,
     secAuthorization_def, 11
                                                 11
     secContext_def, 11
     secHelper_def, 12
    Theorems, 12
     getOmniCommand_def, 12
     getOmniCommand_ind, 15
     getPlCom_def, 16
     getPlCom_ind, 16
PBTypeIntegrated Theory, 3
   Datatypes, 3
    Theorems, 3
     omniCommand_distinct_clauses, 3
     plCommand_distinct_clauses, 3
     slCommand_distinct_clauses, 4
     slCommand_one_one, 4
     slOutput_distinct_clauses, 4
     slState_distinct_clauses, 4
     stateRole_distinct_clauses, 4
ssmPBIntegrated Theory, 4
    Theorems, 5
     inputOK_cmd_reject_lemma, 5
     inputOK_def, 5
     inputOK_ind, 5
     PBNS_def, 6
     PBNS_ind, 6
     PBOut_def, 7
     PBOut_ind, 7
     PlatoonLeader_Omni_notDiscard_slCom-
       mand_thm, 7
     PlatoonLeader_PLAN_PB_exec_justi-
       fied_lemma, 7
     PlatoonLeader_PLAN_PB_exec_justi-
       fied_thm, 8
     PlatoonLeader_PLAN_PB_exec_lemma,
     PlatoonLeader_PLAN_PB_trap_justi-
       fied_lemma, 9
```