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# 1 PBTypeIntegrated Theory

**Built:** 16 May 2018

**Parent Theories:** OMNIType

## 1.1 Datatypes

```
omniCommand = ssmPlanPBComplete | ssmMoveToORPComplete  
              | ssmConductORPComplete | ssmMoveToPBComplete  
              | ssmConductPBComplete | invalidOmniCommand
```

```
plCommand = crossLD | conductORP | moveToPB | conductPB  
            | completePB | incomplete
```

```
slCommand = PL plCommand | OMNI omniCommand
```

```
slOutput = PlanPB | MoveToORP | ConductORP | MoveToPB  
           | ConductPB | CompletePB | unAuthenticated  
           | unAuthorized
```

```
slState = PLAN_PB | MOVE_TO_ORP | CONDUCT_ORP | MOVE_TO_PB  
          | CONDUCT_PB | COMPLETE_PB
```

```
stateRole = PlatoonLeader | Omni
```

## 1.2 Theorems

[omniCommand\_distinct\_clauses]

```
⊢ ssmPlanPBComplete ≠ ssmMoveToORPComplete ∧  
  ssmPlanPBComplete ≠ ssmConductORPComplete ∧  
  ssmPlanPBComplete ≠ ssmMoveToPBComplete ∧  
  ssmPlanPBComplete ≠ ssmConductPBComplete ∧  
  ssmPlanPBComplete ≠ invalidOmniCommand ∧  
  ssmMoveToORPComplete ≠ ssmConductORPComplete ∧  
  ssmMoveToORPComplete ≠ ssmMoveToPBComplete ∧  
  ssmMoveToORPComplete ≠ ssmConductPBComplete ∧  
  ssmMoveToORPComplete ≠ invalidOmniCommand ∧  
  ssmConductORPComplete ≠ ssmMoveToPBComplete ∧  
  ssmConductORPComplete ≠ ssmConductPBComplete ∧  
  ssmConductORPComplete ≠ invalidOmniCommand ∧  
  ssmMoveToPBComplete ≠ ssmConductPBComplete ∧  
  ssmMoveToPBComplete ≠ invalidOmniCommand ∧  
  ssmConductPBComplete ≠ invalidOmniCommand
```

[plCommand\_distinct\_clauses]

```
⊢ crossLD ≠ conductORP ∧ crossLD ≠ moveToPB ∧  
  crossLD ≠ conductPB ∧ crossLD ≠ completePB ∧  
  crossLD ≠ incomplete ∧ conductORP ≠ moveToPB ∧
```

$\text{conductORP} \neq \text{conductPB} \wedge \text{conductORP} \neq \text{completePB} \wedge$   
 $\text{conductORP} \neq \text{incomplete} \wedge \text{moveToPB} \neq \text{conductPB} \wedge$   
 $\text{moveToPB} \neq \text{completePB} \wedge \text{moveToPB} \neq \text{incomplete} \wedge$   
 $\text{conductPB} \neq \text{completePB} \wedge \text{conductPB} \neq \text{incomplete} \wedge$   
 $\text{completePB} \neq \text{incomplete}$

[slCommand\_distinct\_clauses]

$\vdash \forall a' a. \text{PL } a \neq \text{OMNI } a'$

[slCommand\_one\_one]

$\vdash (\forall a a'. (\text{PL } a = \text{PL } a') \iff (a = a')) \wedge$   
 $\forall a a'. (\text{OMNI } a = \text{OMNI } a') \iff (a = a')$

[slOutput\_distinct\_clauses]

$\vdash \text{PlanPB} \neq \text{MoveToORP} \wedge \text{PlanPB} \neq \text{ConductORP} \wedge$   
 $\text{PlanPB} \neq \text{MoveToPB} \wedge \text{PlanPB} \neq \text{ConductPB} \wedge$   
 $\text{PlanPB} \neq \text{CompletePB} \wedge \text{PlanPB} \neq \text{unAuthenticated} \wedge$   
 $\text{PlanPB} \neq \text{unAuthorized} \wedge \text{MoveToORP} \neq \text{ConductORP} \wedge$   
 $\text{MoveToORP} \neq \text{MoveToPB} \wedge \text{MoveToORP} \neq \text{ConductPB} \wedge$   
 $\text{MoveToORP} \neq \text{CompletePB} \wedge \text{MoveToORP} \neq \text{unAuthenticated} \wedge$   
 $\text{MoveToORP} \neq \text{unAuthorized} \wedge \text{ConductORP} \neq \text{MoveToPB} \wedge$   
 $\text{ConductORP} \neq \text{ConductPB} \wedge \text{ConductORP} \neq \text{CompletePB} \wedge$   
 $\text{ConductORP} \neq \text{unAuthenticated} \wedge \text{ConductORP} \neq \text{unAuthorized} \wedge$   
 $\text{MoveToPB} \neq \text{ConductPB} \wedge \text{MoveToPB} \neq \text{CompletePB} \wedge$   
 $\text{MoveToPB} \neq \text{unAuthenticated} \wedge \text{MoveToPB} \neq \text{unAuthorized} \wedge$   
 $\text{ConductPB} \neq \text{CompletePB} \wedge \text{ConductPB} \neq \text{unAuthenticated} \wedge$   
 $\text{ConductPB} \neq \text{unAuthorized} \wedge \text{CompletePB} \neq \text{unAuthenticated} \wedge$   
 $\text{CompletePB} \neq \text{unAuthorized} \wedge \text{unAuthenticated} \neq \text{unAuthorized}$

[slState\_distinct\_clauses]

$\vdash \text{PLAN\_PB} \neq \text{MOVE\_TO\_ORP} \wedge \text{PLAN\_PB} \neq \text{CONDUCT\_ORP} \wedge$   
 $\text{PLAN\_PB} \neq \text{MOVE\_TO\_PB} \wedge \text{PLAN\_PB} \neq \text{CONDUCT\_PB} \wedge$   
 $\text{PLAN\_PB} \neq \text{COMPLETE\_PB} \wedge \text{MOVE\_TO\_ORP} \neq \text{CONDUCT\_ORP} \wedge$   
 $\text{MOVE\_TO\_ORP} \neq \text{MOVE\_TO\_PB} \wedge \text{MOVE\_TO\_ORP} \neq \text{CONDUCT\_PB} \wedge$   
 $\text{MOVE\_TO\_ORP} \neq \text{COMPLETE\_PB} \wedge \text{CONDUCT\_ORP} \neq \text{MOVE\_TO\_PB} \wedge$   
 $\text{CONDUCT\_ORP} \neq \text{CONDUCT\_PB} \wedge \text{CONDUCT\_ORP} \neq \text{COMPLETE\_PB} \wedge$   
 $\text{MOVE\_TO\_PB} \neq \text{CONDUCT\_PB} \wedge \text{MOVE\_TO\_PB} \neq \text{COMPLETE\_PB} \wedge$   
 $\text{CONDUCT\_PB} \neq \text{COMPLETE\_PB}$

[stateRole\_distinct\_clauses]

$\vdash \text{PlatoonLeader} \neq \text{Omni}$

## 2 ssmPB Theory

**Built:** 16 May 2018

**Parent Theories:** PBType, ssm11, OMNIType

## 2.1 Definitions

[secContext\_def]

$$\vdash \forall cmd. \\ \text{secContext } cmd = \\ [\text{Name PlatoonLeader controls prop (SOME (SLc cmd))}]$$

[ssmPBStateInterp\_def]

$$\vdash \forall state. \text{ssmPBStateInterp } state = \text{TT}$$

## 2.2 Theorems

[authenticationTest\_cmd\_reject\_lemma]

$$\vdash \forall cmd. \neg \text{authenticationTest (prop (SOME cmd))}$$

[authenticationTest\_def]

$$\vdash (\text{authenticationTest (Name PlatoonLeader says prop cmd)} \iff \\ \text{T}) \wedge (\text{authenticationTest TT} \iff \text{F}) \wedge \\ (\text{authenticationTest FF} \iff \text{F}) \wedge \\ (\text{authenticationTest (prop } v) \iff \text{F}) \wedge \\ (\text{authenticationTest (notf } v_1) \iff \text{F}) \wedge \\ (\text{authenticationTest (} v_2 \text{ andf } v_3) \iff \text{F}) \wedge \\ (\text{authenticationTest (} v_4 \text{ orf } v_5) \iff \text{F}) \wedge \\ (\text{authenticationTest (} v_6 \text{ impf } v_7) \iff \text{F}) \wedge \\ (\text{authenticationTest (} v_8 \text{ eqf } v_9) \iff \text{F}) \wedge \\ (\text{authenticationTest (} v_{10} \text{ says TT) } \iff \text{F}) \wedge \\ (\text{authenticationTest (} v_{10} \text{ says FF) } \iff \text{F}) \wedge \\ (\text{authenticationTest (} v_{133} \text{ meet } v_{134} \text{ says prop } v_{66}) \iff \text{F}) \wedge \\ (\text{authenticationTest (} v_{135} \text{ quoting } v_{136} \text{ says prop } v_{66}) \iff \text{F}) \wedge \\ (\text{authenticationTest (} v_{10} \text{ says notf } v_{67}) \iff \text{F}) \wedge \\ (\text{authenticationTest (} v_{10} \text{ says (} v_{68} \text{ andf } v_{69}) \iff \text{F}) \wedge \\ (\text{authenticationTest (} v_{10} \text{ says (} v_{70} \text{ orf } v_{71}) \iff \text{F}) \wedge \\ (\text{authenticationTest (} v_{10} \text{ says (} v_{72} \text{ impf } v_{73}) \iff \text{F}) \wedge \\ (\text{authenticationTest (} v_{10} \text{ says (} v_{74} \text{ eqf } v_{75}) \iff \text{F}) \wedge \\ (\text{authenticationTest (} v_{10} \text{ says } v_{76} \text{ says } v_{77}) \iff \text{F}) \wedge \\ (\text{authenticationTest (} v_{10} \text{ says } v_{78} \text{ speaks\_for } v_{79}) \iff \text{F}) \wedge \\ (\text{authenticationTest (} v_{10} \text{ says } v_{80} \text{ controls } v_{81}) \iff \text{F}) \wedge \\ (\text{authenticationTest (} v_{10} \text{ says reps } v_{82} \text{ } v_{83} \text{ } v_{84}) \iff \text{F}) \wedge \\ (\text{authenticationTest (} v_{10} \text{ says } v_{85} \text{ domi } v_{86}) \iff \text{F}) \wedge \\ (\text{authenticationTest (} v_{10} \text{ says } v_{87} \text{ eqi } v_{88}) \iff \text{F}) \wedge \\ (\text{authenticationTest (} v_{10} \text{ says } v_{89} \text{ doms } v_{90}) \iff \text{F}) \wedge \\ (\text{authenticationTest (} v_{10} \text{ says } v_{91} \text{ eqs } v_{92}) \iff \text{F}) \wedge \\ (\text{authenticationTest (} v_{10} \text{ says } v_{93} \text{ eqn } v_{94}) \iff \text{F}) \wedge \\ (\text{authenticationTest (} v_{10} \text{ says } v_{95} \text{ lte } v_{96}) \iff \text{F}) \wedge \\ (\text{authenticationTest (} v_{10} \text{ says } v_{97} \text{ lt } v_{98}) \iff \text{F}) \wedge \\ (\text{authenticationTest (} v_{12} \text{ speaks\_for } v_{13}) \iff \text{F}) \wedge \\ (\text{authenticationTest (} v_{14} \text{ controls } v_{15}) \iff \text{F}) \wedge \\ (\text{authenticationTest (reps } v_{16} \text{ } v_{17} \text{ } v_{18}) \iff \text{F}) \wedge$$

$(\text{authenticationTest } (v_{19} \text{ domi } v_{20}) \iff F) \wedge$   
 $(\text{authenticationTest } (v_{21} \text{ eqi } v_{22}) \iff F) \wedge$   
 $(\text{authenticationTest } (v_{23} \text{ doms } v_{24}) \iff F) \wedge$   
 $(\text{authenticationTest } (v_{25} \text{ eqs } v_{26}) \iff F) \wedge$   
 $(\text{authenticationTest } (v_{27} \text{ eqn } v_{28}) \iff F) \wedge$   
 $(\text{authenticationTest } (v_{29} \text{ lte } v_{30}) \iff F) \wedge$   
 $(\text{authenticationTest } (v_{31} \text{ lt } v_{32}) \iff F)$

[authenticationTest\_ind]

$\vdash \forall P.$

$(\forall \text{cmd}. P (\text{Name PlatoonLeader says prop cmd})) \wedge P \text{ TT} \wedge$   
 $P \text{ FF} \wedge (\forall v. P (\text{prop } v)) \wedge (\forall v_1. P (\text{notf } v_1)) \wedge$   
 $(\forall v_2 v_3. P (v_2 \text{ andf } v_3)) \wedge (\forall v_4 v_5. P (v_4 \text{ orf } v_5)) \wedge$   
 $(\forall v_6 v_7. P (v_6 \text{ impf } v_7)) \wedge (\forall v_8 v_9. P (v_8 \text{ eqf } v_9)) \wedge$   
 $(\forall v_{10}. P (v_{10} \text{ says TT})) \wedge (\forall v_{10}. P (v_{10} \text{ says FF})) \wedge$   
 $(\forall v_{133} v_{134} v_{66}. P (v_{133} \text{ meet } v_{134} \text{ says prop } v_{66})) \wedge$   
 $(\forall v_{135} v_{136} v_{66}. P (v_{135} \text{ quoting } v_{136} \text{ says prop } v_{66})) \wedge$   
 $(\forall v_{10} v_{67}. P (v_{10} \text{ says notf } v_{67})) \wedge$   
 $(\forall v_{10} v_{68} v_{69}. P (v_{10} \text{ says } (v_{68} \text{ andf } v_{69}))) \wedge$   
 $(\forall v_{10} v_{70} v_{71}. P (v_{10} \text{ says } (v_{70} \text{ orf } v_{71}))) \wedge$   
 $(\forall v_{10} v_{72} v_{73}. P (v_{10} \text{ says } (v_{72} \text{ impf } v_{73}))) \wedge$   
 $(\forall v_{10} v_{74} v_{75}. P (v_{10} \text{ says } (v_{74} \text{ eqf } v_{75}))) \wedge$   
 $(\forall v_{10} v_{76} v_{77}. P (v_{10} \text{ says } v_{76} \text{ says } v_{77})) \wedge$   
 $(\forall v_{10} v_{78} v_{79}. P (v_{10} \text{ says } v_{78} \text{ speaks\_for } v_{79})) \wedge$   
 $(\forall v_{10} v_{80} v_{81}. P (v_{10} \text{ says } v_{80} \text{ controls } v_{81})) \wedge$   
 $(\forall v_{10} v_{82} v_{83} v_{84}. P (v_{10} \text{ says reps } v_{82} v_{83} v_{84})) \wedge$   
 $(\forall v_{10} v_{85} v_{86}. P (v_{10} \text{ says } v_{85} \text{ domi } v_{86})) \wedge$   
 $(\forall v_{10} v_{87} v_{88}. P (v_{10} \text{ says } v_{87} \text{ eqi } v_{88})) \wedge$   
 $(\forall v_{10} v_{89} v_{90}. P (v_{10} \text{ says } v_{89} \text{ doms } v_{90})) \wedge$   
 $(\forall v_{10} v_{91} v_{92}. P (v_{10} \text{ says } v_{91} \text{ eqs } v_{92})) \wedge$   
 $(\forall v_{10} v_{93} v_{94}. P (v_{10} \text{ says } v_{93} \text{ eqn } v_{94})) \wedge$   
 $(\forall v_{10} v_{95} v_{96}. P (v_{10} \text{ says } v_{95} \text{ lte } v_{96})) \wedge$   
 $(\forall v_{10} v_{97} v_{98}. P (v_{10} \text{ says } v_{97} \text{ lt } v_{98})) \wedge$   
 $(\forall v_{12} v_{13}. P (v_{12} \text{ speaks\_for } v_{13})) \wedge$   
 $(\forall v_{14} v_{15}. P (v_{14} \text{ controls } v_{15})) \wedge$   
 $(\forall v_{16} v_{17} v_{18}. P (\text{reps } v_{16} v_{17} v_{18})) \wedge$   
 $(\forall v_{19} v_{20}. P (v_{19} \text{ domi } v_{20})) \wedge$   
 $(\forall v_{21} v_{22}. P (v_{21} \text{ eqi } v_{22})) \wedge$   
 $(\forall v_{23} v_{24}. P (v_{23} \text{ doms } v_{24})) \wedge$   
 $(\forall v_{25} v_{26}. P (v_{25} \text{ eqs } v_{26})) \wedge (\forall v_{27} v_{28}. P (v_{27} \text{ eqn } v_{28})) \wedge$   
 $(\forall v_{29} v_{30}. P (v_{29} \text{ lte } v_{30})) \wedge (\forall v_{31} v_{32}. P (v_{31} \text{ lt } v_{32})) \Rightarrow$   
 $\forall v. P v$

[PBNS\_def]

$\vdash (\text{PBNS PLAN\_PB } (\text{exec } (\text{SLc crossLD})) = \text{MOVE\_TO\_ORP}) \wedge$   
 $(\text{PBNS PLAN\_PB } (\text{exec } (\text{SLc incomplete})) = \text{PLAN\_PB}) \wedge$   
 $(\text{PBNS MOVE\_TO\_ORP } (\text{exec } (\text{SLc conductorORP})) = \text{CONDUCT\_ORP}) \wedge$   
 $(\text{PBNS MOVE\_TO\_ORP } (\text{exec } (\text{SLc incomplete})) = \text{MOVE\_TO\_ORP}) \wedge$   
 $(\text{PBNS CONDUCT\_ORP } (\text{exec } (\text{SLc moveToPB})) = \text{MOVE\_TO\_PB}) \wedge$

$(\text{PBNS CONDUCT\_ORP (exec (SLc incomplete))} = \text{CONDUCT\_ORP}) \wedge$   
 $(\text{PBNS MOVE\_TO\_PB (exec (SLc conductPB))} = \text{CONDUCT\_PB}) \wedge$   
 $(\text{PBNS MOVE\_TO\_PB (exec (SLc incomplete))} = \text{MOVE\_TO\_PB}) \wedge$   
 $(\text{PBNS CONDUCT\_PB (exec (SLc completePB))} = \text{COMPLETE\_PB}) \wedge$   
 $(\text{PBNS CONDUCT\_PB (exec (SLc incomplete))} = \text{CONDUCT\_PB}) \wedge$   
 $(\text{PBNS } s \text{ (trap (SLc cmd))} = s) \wedge$   
 $(\text{PBNS } s \text{ (discard (SLc cmd))} = s)$

[PBNS\_ind]

$\vdash \forall P.$

$P \text{ PLAN\_PB (exec (SLc crossLD))} \wedge$   
 $P \text{ PLAN\_PB (exec (SLc incomplete))} \wedge$   
 $P \text{ MOVE\_TO\_ORP (exec (SLc conductORP))} \wedge$   
 $P \text{ MOVE\_TO\_ORP (exec (SLc incomplete))} \wedge$   
 $P \text{ CONDUCT\_ORP (exec (SLc moveToPB))} \wedge$   
 $P \text{ CONDUCT\_ORP (exec (SLc incomplete))} \wedge$   
 $P \text{ MOVE\_TO\_PB (exec (SLc conductPB))} \wedge$   
 $P \text{ MOVE\_TO\_PB (exec (SLc incomplete))} \wedge$   
 $P \text{ CONDUCT\_PB (exec (SLc completePB))} \wedge$   
 $P \text{ CONDUCT\_PB (exec (SLc incomplete))} \wedge$   
 $(\forall s \text{ cmd. } P \text{ } s \text{ (trap (SLc cmd))}) \wedge$   
 $(\forall s \text{ cmd. } P \text{ } s \text{ (discard (SLc cmd))}) \wedge$   
 $(\forall s \text{ } v_6. P \text{ } s \text{ (discard (ESCc } v_6))}) \wedge$   
 $(\forall s \text{ } v_9. P \text{ } s \text{ (trap (ESCc } v_9))}) \wedge$   
 $(\forall v_{12}. P \text{ PLAN\_PB (exec (ESCc } v_{12}))}) \wedge$   
 $P \text{ PLAN\_PB (exec (SLc conductORP))} \wedge$   
 $P \text{ PLAN\_PB (exec (SLc moveToPB))} \wedge$   
 $P \text{ PLAN\_PB (exec (SLc conductPB))} \wedge$   
 $P \text{ PLAN\_PB (exec (SLc completePB))} \wedge$   
 $(\forall v_{15}. P \text{ MOVE\_TO\_ORP (exec (ESCc } v_{15}))}) \wedge$   
 $P \text{ MOVE\_TO\_ORP (exec (SLc crossLD))} \wedge$   
 $P \text{ MOVE\_TO\_ORP (exec (SLc moveToPB))} \wedge$   
 $P \text{ MOVE\_TO\_ORP (exec (SLc conductPB))} \wedge$   
 $P \text{ MOVE\_TO\_ORP (exec (SLc completePB))} \wedge$   
 $(\forall v_{18}. P \text{ CONDUCT\_ORP (exec (ESCc } v_{18}))}) \wedge$   
 $P \text{ CONDUCT\_ORP (exec (SLc crossLD))} \wedge$   
 $P \text{ CONDUCT\_ORP (exec (SLc conductORP))} \wedge$   
 $P \text{ CONDUCT\_ORP (exec (SLc conductPB))} \wedge$   
 $P \text{ CONDUCT\_ORP (exec (SLc completePB))} \wedge$   
 $(\forall v_{21}. P \text{ MOVE\_TO\_PB (exec (ESCc } v_{21}))}) \wedge$   
 $P \text{ MOVE\_TO\_PB (exec (SLc crossLD))} \wedge$   
 $P \text{ MOVE\_TO\_PB (exec (SLc conductORP))} \wedge$   
 $P \text{ MOVE\_TO\_PB (exec (SLc moveToPB))} \wedge$   
 $P \text{ MOVE\_TO\_PB (exec (SLc completePB))} \wedge$   
 $(\forall v_{24}. P \text{ CONDUCT\_PB (exec (ESCc } v_{24}))}) \wedge$   
 $P \text{ CONDUCT\_PB (exec (SLc crossLD))} \wedge$   
 $P \text{ CONDUCT\_PB (exec (SLc conductORP))} \wedge$   
 $P \text{ CONDUCT\_PB (exec (SLc moveToPB))} \wedge$   
 $P \text{ CONDUCT\_PB (exec (SLc conductPB))} \wedge$

$$(\forall v_{26}. P \text{ COMPLETE\_PB } (\text{exec } v_{26})) \Rightarrow \\ \forall v \ v_1. P \ v \ v_1$$

[PBOut\_def]

$$\begin{aligned} \vdash & (\text{PBOut PLAN\_PB } (\text{exec } (\text{SLc crossLD})) = \text{MoveToORP}) \wedge \\ & (\text{PBOut PLAN\_PB } (\text{exec } (\text{SLc incomplete})) = \text{PlanPB}) \wedge \\ & (\text{PBOut MOVE\_TO\_ORP } (\text{exec } (\text{SLc conductORP})) = \text{ConductORP}) \wedge \\ & (\text{PBOut MOVE\_TO\_ORP } (\text{exec } (\text{SLc incomplete})) = \text{MoveToORP}) \wedge \\ & (\text{PBOut CONDUCT\_ORP } (\text{exec } (\text{SLc moveToPB})) = \text{MoveToPB}) \wedge \\ & (\text{PBOut CONDUCT\_ORP } (\text{exec } (\text{SLc incomplete})) = \text{ConductORP}) \wedge \\ & (\text{PBOut MOVE\_TO\_PB } (\text{exec } (\text{SLc conductPB})) = \text{ConductPB}) \wedge \\ & (\text{PBOut MOVE\_TO\_PB } (\text{exec } (\text{SLc incomplete})) = \text{MoveToPB}) \wedge \\ & (\text{PBOut CONDUCT\_PB } (\text{exec } (\text{SLc completePB})) = \text{CompletePB}) \wedge \\ & (\text{PBOut CONDUCT\_PB } (\text{exec } (\text{SLc incomplete})) = \text{ConductPB}) \wedge \\ & (\text{PBOut } s \ (\text{trap } (\text{SLc } cmd)) = \text{unAuthorized}) \wedge \\ & (\text{PBOut } s \ (\text{discard } (\text{SLc } cmd)) = \text{unAuthenticated}) \end{aligned}$$

[PBOut\_ind]

$$\begin{aligned} \vdash & \forall P. \\ & P \text{ PLAN\_PB } (\text{exec } (\text{SLc crossLD})) \wedge \\ & P \text{ PLAN\_PB } (\text{exec } (\text{SLc incomplete})) \wedge \\ & P \text{ MOVE\_TO\_ORP } (\text{exec } (\text{SLc conductORP})) \wedge \\ & P \text{ MOVE\_TO\_ORP } (\text{exec } (\text{SLc incomplete})) \wedge \\ & P \text{ CONDUCT\_ORP } (\text{exec } (\text{SLc moveToPB})) \wedge \\ & P \text{ CONDUCT\_ORP } (\text{exec } (\text{SLc incomplete})) \wedge \\ & P \text{ MOVE\_TO\_PB } (\text{exec } (\text{SLc conductPB})) \wedge \\ & P \text{ MOVE\_TO\_PB } (\text{exec } (\text{SLc incomplete})) \wedge \\ & P \text{ CONDUCT\_PB } (\text{exec } (\text{SLc completePB})) \wedge \\ & P \text{ CONDUCT\_PB } (\text{exec } (\text{SLc incomplete})) \wedge \\ & (\forall s \ cmd. P \ s \ (\text{trap } (\text{SLc } cmd))) \wedge \\ & (\forall s \ cmd. P \ s \ (\text{discard } (\text{SLc } cmd))) \wedge \\ & (\forall s \ v_6. P \ s \ (\text{discard } (\text{ESCc } v_6))) \wedge \\ & (\forall s \ v_9. P \ s \ (\text{trap } (\text{ESCc } v_9))) \wedge \\ & (\forall v_{12}. P \text{ PLAN\_PB } (\text{exec } (\text{ESCc } v_{12}))) \wedge \\ & P \text{ PLAN\_PB } (\text{exec } (\text{SLc conductORP})) \wedge \\ & P \text{ PLAN\_PB } (\text{exec } (\text{SLc moveToPB})) \wedge \\ & P \text{ PLAN\_PB } (\text{exec } (\text{SLc conductPB})) \wedge \\ & P \text{ PLAN\_PB } (\text{exec } (\text{SLc completePB})) \wedge \\ & (\forall v_{15}. P \text{ MOVE\_TO\_ORP } (\text{exec } (\text{ESCc } v_{15}))) \wedge \\ & P \text{ MOVE\_TO\_ORP } (\text{exec } (\text{SLc crossLD})) \wedge \\ & P \text{ MOVE\_TO\_ORP } (\text{exec } (\text{SLc moveToPB})) \wedge \\ & P \text{ MOVE\_TO\_ORP } (\text{exec } (\text{SLc conductPB})) \wedge \\ & P \text{ MOVE\_TO\_ORP } (\text{exec } (\text{SLc completePB})) \wedge \\ & (\forall v_{18}. P \text{ CONDUCT\_ORP } (\text{exec } (\text{ESCc } v_{18}))) \wedge \\ & P \text{ CONDUCT\_ORP } (\text{exec } (\text{SLc crossLD})) \wedge \\ & P \text{ CONDUCT\_ORP } (\text{exec } (\text{SLc conductORP})) \wedge \\ & P \text{ CONDUCT\_ORP } (\text{exec } (\text{SLc conductPB})) \wedge \\ & P \text{ CONDUCT\_ORP } (\text{exec } (\text{SLc completePB})) \wedge \\ & (\forall v_{21}. P \text{ MOVE\_TO\_PB } (\text{exec } (\text{ESCc } v_{21}))) \wedge \end{aligned}$$



$$\begin{aligned}
& P \text{ MOVE\_TO\_PB } (\text{exec } (\text{SLc crossLD})) \wedge \\
& P \text{ MOVE\_TO\_PB } (\text{exec } (\text{SLc conductORP})) \wedge \\
& P \text{ MOVE\_TO\_PB } (\text{exec } (\text{SLc moveToPB})) \wedge \\
& P \text{ MOVE\_TO\_PB } (\text{exec } (\text{SLc completePB})) \wedge \\
& (\forall v_{24}. P \text{ CONDUCT\_PB } (\text{exec } (\text{ESCc } v_{24}))) \wedge \\
& P \text{ CONDUCT\_PB } (\text{exec } (\text{SLc crossLD})) \wedge \\
& P \text{ CONDUCT\_PB } (\text{exec } (\text{SLc conductORP})) \wedge \\
& P \text{ CONDUCT\_PB } (\text{exec } (\text{SLc moveToPB})) \wedge \\
& P \text{ CONDUCT\_PB } (\text{exec } (\text{SLc conductPB})) \wedge \\
& (\forall v_{26}. P \text{ COMPLETE\_PB } (\text{exec } v_{26})) \Rightarrow \\
& \forall v \ v_1. P \ v \ v_1
\end{aligned}$$

[PlatoonLeader\_exec\_slCommand\_justified\_thm]

$$\begin{aligned}
& \vdash \forall NS \text{ Out } M \text{ } Oi \text{ } Os. \\
& \text{TR } (M, Oi, Os) (\text{exec } (\text{SLc slCommand})) \\
& \quad (\text{CFG authenticationTest ssmPBStateInterp} \\
& \quad \quad (\text{secContext slCommand}) \\
& \quad \quad (\text{Name PlatoonLeader says prop (SOME (SLc slCommand))} :: \\
& \quad \quad \quad \text{ins) s outs})) \\
& \quad (\text{CFG authenticationTest ssmPBStateInterp} \\
& \quad \quad (\text{secContext slCommand}) \text{ ins} \\
& \quad \quad (NS \ s \ (\text{exec } (\text{SLc slCommand}))) \\
& \quad \quad (\text{Out } s \ (\text{exec } (\text{SLc slCommand})) :: \text{outs})) \iff \\
& \text{authenticationTest} \\
& \quad (\text{Name PlatoonLeader says prop (SOME (SLc slCommand))}) \wedge \\
& \text{CFGInterpret } (M, Oi, Os) \\
& \quad (\text{CFG authenticationTest ssmPBStateInterp} \\
& \quad \quad (\text{secContext slCommand}) \\
& \quad \quad (\text{Name PlatoonLeader says prop (SOME (SLc slCommand))} :: \\
& \quad \quad \quad \text{ins) s outs}) \wedge \\
& \quad (M, Oi, Os) \text{ sat prop (SOME (SLc slCommand))})
\end{aligned}$$

[PlatoonLeader\_slCommand\_lemma]

$$\begin{aligned}
& \vdash \text{CFGInterpret } (M, Oi, Os) \\
& \quad (\text{CFG authenticationTest ssmPBStateInterp} \\
& \quad \quad (\text{secContext slCommand}) \\
& \quad \quad (\text{Name PlatoonLeader says prop (SOME (SLc slCommand))} :: \\
& \quad \quad \quad \text{ins) s outs}) \Rightarrow \\
& \quad (M, Oi, Os) \text{ sat prop (SOME (SLc slCommand))})
\end{aligned}$$

### 3 PBIntegratedDef Theory

**Built:** 16 May 2018

**Parent Theories:** PBTypeIntegrated, aclfoundation

#### 3.1 Definitions

[secAuthorization\_def]

$\vdash \forall xs. \text{secAuthorization } xs = \text{secHelper } (\text{getOmniCommand } xs)$

[secHelper\_def]

$\vdash \forall cmd.$   
 $\text{secHelper } cmd =$   
 $[\text{Name Omni controls prop (SOME (SLc (OMNI } cmd)))]$

### 3.2 Theorems

[getOmniCommand\_def]

$\vdash (\text{getOmniCommand } [] = \text{invalidOmniCommand}) \wedge$   
 $(\forall xs \text{ } cmd.$   
 $\text{getOmniCommand}$   
 $(\text{Name Omni controls prop (SOME (SLc (OMNI } cmd))):xs) =$   
 $cmd) \wedge$   
 $(\forall xs. \text{getOmniCommand } (TT::xs) = \text{getOmniCommand } xs) \wedge$   
 $(\forall xs. \text{getOmniCommand } (FF::xs) = \text{getOmniCommand } xs) \wedge$   
 $(\forall xs \text{ } v_2. \text{getOmniCommand } (\text{prop } v_2::xs) = \text{getOmniCommand } xs) \wedge$   
 $(\forall xs \text{ } v_3. \text{getOmniCommand } (\text{notf } v_3::xs) = \text{getOmniCommand } xs) \wedge$   
 $(\forall xs \text{ } v_5 \text{ } v_4.$   
 $\text{getOmniCommand } (v_4 \text{ andf } v_5::xs) = \text{getOmniCommand } xs) \wedge$   
 $(\forall xs \text{ } v_7 \text{ } v_6.$   
 $\text{getOmniCommand } (v_6 \text{ orf } v_7::xs) = \text{getOmniCommand } xs) \wedge$   
 $(\forall xs \text{ } v_9 \text{ } v_8.$   
 $\text{getOmniCommand } (v_8 \text{ impf } v_9::xs) = \text{getOmniCommand } xs) \wedge$   
 $(\forall xs \text{ } v_{11} \text{ } v_{10}.$   
 $\text{getOmniCommand } (v_{10} \text{ eqf } v_{11}::xs) = \text{getOmniCommand } xs) \wedge$   
 $(\forall xs \text{ } v_{13} \text{ } v_{12}.$   
 $\text{getOmniCommand } (v_{12} \text{ says } v_{13}::xs) = \text{getOmniCommand } xs) \wedge$   
 $(\forall xs \text{ } v_{15} \text{ } v_{14}.$   
 $\text{getOmniCommand } (v_{14} \text{ speaks\_for } v_{15}::xs) =$   
 $\text{getOmniCommand } xs) \wedge$   
 $(\forall xs \text{ } v_{16}.$   
 $\text{getOmniCommand } (v_{16} \text{ controls } TT::xs) =$   
 $\text{getOmniCommand } xs) \wedge$   
 $(\forall xs \text{ } v_{16}.$   
 $\text{getOmniCommand } (v_{16} \text{ controls } FF::xs) =$   
 $\text{getOmniCommand } xs) \wedge$   
 $(\forall xs \text{ } v_{134}.$   
 $\text{getOmniCommand } (\text{Name } v_{134} \text{ controls prop NONE::xs) =}$   
 $\text{getOmniCommand } xs) \wedge$   
 $(\forall xs \text{ } v_{144}.$   
 $\text{getOmniCommand}$   
 $(\text{Name PlatoonLeader controls prop (SOME } v_{144}):xs) =$   
 $\text{getOmniCommand } xs) \wedge$   
 $(\forall xs \text{ } v_{146}.$   
 $\text{getOmniCommand}$

```

      (Name Omni controls prop (SOME (ESCc v146))::xs) =
      getOmniCommand xs) ∧
(∀ xs v150.
  getOmniCommand
    (Name Omni controls prop (SOME (SLc (PL v150)))::xs) =
    getOmniCommand xs) ∧
(∀ xs v68 v136 v135.
  getOmniCommand (v135 meet v136 controls prop v68::xs) =
  getOmniCommand xs) ∧
(∀ xs v68 v138 v137.
  getOmniCommand (v137 quoting v138 controls prop v68::xs) =
  getOmniCommand xs) ∧
(∀ xs v69 v16.
  getOmniCommand (v16 controls notif v69::xs) =
  getOmniCommand xs) ∧
(∀ xs v71 v70 v16.
  getOmniCommand (v16 controls (v70 andf v71)::xs) =
  getOmniCommand xs) ∧
(∀ xs v73 v72 v16.
  getOmniCommand (v16 controls (v72 orf v73)::xs) =
  getOmniCommand xs) ∧
(∀ xs v75 v74 v16.
  getOmniCommand (v16 controls (v74 impf v75)::xs) =
  getOmniCommand xs) ∧
(∀ xs v77 v76 v16.
  getOmniCommand (v16 controls (v76 eqf v77)::xs) =
  getOmniCommand xs) ∧
(∀ xs v79 v78 v16.
  getOmniCommand (v16 controls v78 says v79::xs) =
  getOmniCommand xs) ∧
(∀ xs v81 v80 v16.
  getOmniCommand (v16 controls v80 speaks_for v81::xs) =
  getOmniCommand xs) ∧
(∀ xs v83 v82 v16.
  getOmniCommand (v16 controls v82 controls v83::xs) =
  getOmniCommand xs) ∧
(∀ xs v86 v85 v84 v16.
  getOmniCommand (v16 controls reps v84 v85 v86::xs) =
  getOmniCommand xs) ∧
(∀ xs v88 v87 v16.
  getOmniCommand (v16 controls v87 domi v88::xs) =
  getOmniCommand xs) ∧
(∀ xs v90 v89 v16.
  getOmniCommand (v16 controls v89 eqi v90::xs) =
  getOmniCommand xs) ∧
(∀ xs v92 v91 v16.
  getOmniCommand (v16 controls v91 doms v92::xs) =
  getOmniCommand xs) ∧
(∀ xs v94 v93 v16.

```

```

      getOmniCommand (v16 controls v93 eqs v94::xs) =
      getOmniCommand xs) ∧
(∀ xs v96 v95 v16.
  getOmniCommand (v16 controls v95 eqn v96::xs) =
  getOmniCommand xs) ∧
(∀ xs v98 v97 v16.
  getOmniCommand (v16 controls v97 lte v98::xs) =
  getOmniCommand xs) ∧
(∀ xs v99 v16 v100.
  getOmniCommand (v16 controls v99 lt v100::xs) =
  getOmniCommand xs) ∧
(∀ xs v20 v19 v18.
  getOmniCommand (reps v18 v19 v20::xs) =
  getOmniCommand xs) ∧
(∀ xs v22 v21.
  getOmniCommand (v21 domi v22::xs) = getOmniCommand xs) ∧
(∀ xs v24 v23.
  getOmniCommand (v23 eqi v24::xs) = getOmniCommand xs) ∧
(∀ xs v26 v25.
  getOmniCommand (v25 doms v26::xs) = getOmniCommand xs) ∧
(∀ xs v28 v27.
  getOmniCommand (v27 eqs v28::xs) = getOmniCommand xs) ∧
(∀ xs v30 v29.
  getOmniCommand (v29 eqn v30::xs) = getOmniCommand xs) ∧
(∀ xs v32 v31.
  getOmniCommand (v31 lte v32::xs) = getOmniCommand xs) ∧
∀ xs v34 v33.
  getOmniCommand (v33 lt v34::xs) = getOmniCommand xs

```

[getOmniCommand\_ind]

```

⊢ ∀ P.
  P [] ∧
  (∀ cmd xs.
    P
      (Name Omni controls prop (SOME (SLc (OMNI cmd)))::
        xs)) ∧ (∀ xs. P xs ⇒ P (TT::xs)) ∧
  (∀ xs. P xs ⇒ P (FF::xs)) ∧
  (∀ v2 xs. P xs ⇒ P (prop v2::xs)) ∧
  (∀ v3 xs. P xs ⇒ P (notf v3::xs)) ∧
  (∀ v4 v5 xs. P xs ⇒ P (v4 andf v5::xs)) ∧
  (∀ v6 v7 xs. P xs ⇒ P (v6 orf v7::xs)) ∧
  (∀ v8 v9 xs. P xs ⇒ P (v8 impf v9::xs)) ∧
  (∀ v10 v11 xs. P xs ⇒ P (v10 eqf v11::xs)) ∧
  (∀ v12 v13 xs. P xs ⇒ P (v12 says v13::xs)) ∧
  (∀ v14 v15 xs. P xs ⇒ P (v14 speaks_for v15::xs)) ∧
  (∀ v16 xs. P xs ⇒ P (v16 controls TT::xs)) ∧
  (∀ v16 xs. P xs ⇒ P (v16 controls FF::xs)) ∧
  (∀ v134 xs. P xs ⇒ P (Name v134 controls prop NONE::xs)) ∧
  (∀ v144 xs.

```

---

$P \text{ } xs \Rightarrow$   
 $P (\text{Name PlatoonLeader controls prop (SOME } v144)::xs)) \wedge$   
 $(\forall v146 \text{ } xs.$   
 $P \text{ } xs \Rightarrow$   
 $P (\text{Name Omni controls prop (SOME (ESCc } v146)::xs)) \wedge$   
 $(\forall v150 \text{ } xs.$   
 $P \text{ } xs \Rightarrow$   
 $P$   
 $(\text{Name Omni controls prop (SOME (SLc (PL } v150)))::$   
 $xs)) \wedge$   
 $(\forall v135 \text{ } v136 \text{ } v68 \text{ } xs.$   
 $P \text{ } xs \Rightarrow P (v135 \text{ meet } v136 \text{ controls prop } v68::xs)) \wedge$   
 $(\forall v137 \text{ } v138 \text{ } v68 \text{ } xs.$   
 $P \text{ } xs \Rightarrow P (v137 \text{ quoting } v138 \text{ controls prop } v68::xs)) \wedge$   
 $(\forall v16 \text{ } v69 \text{ } xs. P \text{ } xs \Rightarrow P (v16 \text{ controls notf } v69::xs)) \wedge$   
 $(\forall v16 \text{ } v70 \text{ } v71 \text{ } xs.$   
 $P \text{ } xs \Rightarrow P (v16 \text{ controls } (v70 \text{ andf } v71)::xs)) \wedge$   
 $(\forall v16 \text{ } v72 \text{ } v73 \text{ } xs.$   
 $P \text{ } xs \Rightarrow P (v16 \text{ controls } (v72 \text{ orf } v73)::xs)) \wedge$   
 $(\forall v16 \text{ } v74 \text{ } v75 \text{ } xs.$   
 $P \text{ } xs \Rightarrow P (v16 \text{ controls } (v74 \text{ impf } v75)::xs)) \wedge$   
 $(\forall v16 \text{ } v76 \text{ } v77 \text{ } xs.$   
 $P \text{ } xs \Rightarrow P (v16 \text{ controls } (v76 \text{ eqf } v77)::xs)) \wedge$   
 $(\forall v16 \text{ } v78 \text{ } v79 \text{ } xs.$   
 $P \text{ } xs \Rightarrow P (v16 \text{ controls } v78 \text{ says } v79::xs)) \wedge$   
 $(\forall v16 \text{ } v80 \text{ } v81 \text{ } xs.$   
 $P \text{ } xs \Rightarrow P (v16 \text{ controls } v80 \text{ speaks\_for } v81::xs)) \wedge$   
 $(\forall v16 \text{ } v82 \text{ } v83 \text{ } xs.$   
 $P \text{ } xs \Rightarrow P (v16 \text{ controls } v82 \text{ controls } v83::xs)) \wedge$   
 $(\forall v16 \text{ } v84 \text{ } v85 \text{ } v86 \text{ } xs.$   
 $P \text{ } xs \Rightarrow P (v16 \text{ controls reps } v84 \text{ } v85 \text{ } v86::xs)) \wedge$   
 $(\forall v16 \text{ } v87 \text{ } v88 \text{ } xs.$   
 $P \text{ } xs \Rightarrow P (v16 \text{ controls } v87 \text{ domi } v88::xs)) \wedge$   
 $(\forall v16 \text{ } v89 \text{ } v90 \text{ } xs.$   
 $P \text{ } xs \Rightarrow P (v16 \text{ controls } v89 \text{ eqi } v90::xs)) \wedge$   
 $(\forall v16 \text{ } v91 \text{ } v92 \text{ } xs.$   
 $P \text{ } xs \Rightarrow P (v16 \text{ controls } v91 \text{ doms } v92::xs)) \wedge$   
 $(\forall v16 \text{ } v93 \text{ } v94 \text{ } xs.$   
 $P \text{ } xs \Rightarrow P (v16 \text{ controls } v93 \text{ eqs } v94::xs)) \wedge$   
 $(\forall v16 \text{ } v95 \text{ } v96 \text{ } xs.$   
 $P \text{ } xs \Rightarrow P (v16 \text{ controls } v95 \text{ eqn } v96::xs)) \wedge$   
 $(\forall v16 \text{ } v97 \text{ } v98 \text{ } xs.$   
 $P \text{ } xs \Rightarrow P (v16 \text{ controls } v97 \text{ lte } v98::xs)) \wedge$   
 $(\forall v16 \text{ } v99 \text{ } v100 \text{ } xs.$   
 $P \text{ } xs \Rightarrow P (v16 \text{ controls } v99 \text{ lt } v100::xs)) \wedge$   
 $(\forall v18 \text{ } v19 \text{ } v20 \text{ } xs. P \text{ } xs \Rightarrow P (\text{reps } v18 \text{ } v19 \text{ } v20::xs)) \wedge$   
 $(\forall v21 \text{ } v22 \text{ } xs. P \text{ } xs \Rightarrow P (v21 \text{ domi } v22::xs)) \wedge$   
 $(\forall v23 \text{ } v24 \text{ } xs. P \text{ } xs \Rightarrow P (v23 \text{ eqi } v24::xs)) \wedge$   
 $(\forall v25 \text{ } v26 \text{ } xs. P \text{ } xs \Rightarrow P (v25 \text{ doms } v26::xs)) \wedge$

---

$$\begin{aligned}
& (\forall v_{27} v_{28} xs. P xs \Rightarrow P (v_{27} \text{ eqs } v_{28} :: xs)) \wedge \\
& (\forall v_{29} v_{30} xs. P xs \Rightarrow P (v_{29} \text{ eqn } v_{30} :: xs)) \wedge \\
& (\forall v_{31} v_{32} xs. P xs \Rightarrow P (v_{31} \text{ lte } v_{32} :: xs)) \wedge \\
& (\forall v_{33} v_{34} xs. P xs \Rightarrow P (v_{33} \text{ lt } v_{34} :: xs)) \Rightarrow \\
& \forall v. P v
\end{aligned}$$

[secContext\_def]

```

⊢ (secContext PLAN_PB (x::xs) =
  [prop (SOME (SLc (OMNI ssmPlanPBComplete))) impf
   Name PlatoonLeader controls
   prop (SOME (SLc (PL crossLD)))]) ∧
(secContext MOVE_TO_ORP (x::xs) =
  [prop (SOME (SLc (OMNI ssmMoveToORPComplete))) impf
   Name PlatoonLeader controls
   prop (SOME (SLc (PL conductORP)))]) ∧
(secContext CONDUCT_ORP (x::xs) =
  [prop (SOME (SLc (OMNI ssmConductORPComplete))) impf
   Name PlatoonLeader controls
   prop (SOME (SLc (PL moveToPB)))]) ∧
(secContext MOVE_TO_PB (x::xs) =
  [prop (SOME (SLc (OMNI ssmMoveToPBComplete))) impf
   Name PlatoonLeader controls
   prop (SOME (SLc (PL conductPB)))]) ∧
(secContext CONDUCT_PB (x::xs) =
  [prop (SOME (SLc (OMNI ssmConductPBComplete))) impf
   Name PlatoonLeader controls
   prop (SOME (SLc (PL completePB)))])

```

[secContext\_ind]

```

⊢ ∀ P.
  (∀ x xs. P PLAN_PB (x::xs)) ∧
  (∀ x xs. P MOVE_TO_ORP (x::xs)) ∧
  (∀ x xs. P CONDUCT_ORP (x::xs)) ∧
  (∀ x xs. P MOVE_TO_PB (x::xs)) ∧
  (∀ x xs. P CONDUCT_PB (x::xs)) ∧ (∀ v4. P v4 []) ∧
  (∀ v5 v6. P COMPLETE_PB (v5::v6)) ⇒
  ∀ v v1. P v v1

```

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