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1 ConductPBType Theory

Built: 16 May 2018

Parent Theories: indexedLists, patternMatches

1.1 Datatypes

```
plCommandPB = securePB | withdrawPB | completePB
              | plIncompletePB

psgCommandPB = actionsInPB | psgIncompletePB

slCommand = PL plCommandPB | PSG psgCommandPB

slOutput = ConductPB | SecurePB | ActionsInPB | WithdrawPB
           | CompletePB | unAuthenticated | unAuthorized

slState = CONDUCT_PB | SECURE_PB | ACTIONS_IN_PB | WITHDRAW_PB
          | COMPLETE_PB

stateRole = PlatoonLeader | PlatoonSergeant
```

1.2 Theorems

```
[plCommandPB_distinct_clauses]
⊢ securePB ≠ withdrawPB ∧ securePB ≠ completePB ∧
  securePB ≠ plIncompletePB ∧ withdrawPB ≠ completePB ∧
  withdrawPB ≠ plIncompletePB ∧ completePB ≠ plIncompletePB

[psgCommandPB_distinct_clauses]
⊢ actionsInPB ≠ psgIncompletePB

[slCommand_distinct_clauses]
⊢ ∀ a' a. PL a ≠ PSG a'

[slCommand_one_one]
⊢ (∀ a a'. (PL a = PL a') ⇔ (a = a')) ∧
  ∀ a a'. (PSG a = PSG a') ⇔ (a = a')

[slOutput_distinct_clauses]
⊢ ConductPB ≠ SecurePB ∧ ConductPB ≠ ActionsInPB ∧
  ConductPB ≠ WithdrawPB ∧ ConductPB ≠ CompletePB ∧
  ConductPB ≠ unAuthenticated ∧ ConductPB ≠ unAuthorized ∧
  SecurePB ≠ ActionsInPB ∧ SecurePB ≠ WithdrawPB ∧
  SecurePB ≠ CompletePB ∧ SecurePB ≠ unAuthenticated ∧
  SecurePB ≠ unAuthorized ∧ ActionsInPB ≠ WithdrawPB ∧
  ActionsInPB ≠ CompletePB ∧ ActionsInPB ≠ unAuthenticated ∧
  ActionsInPB ≠ unAuthorized ∧ WithdrawPB ≠ CompletePB ∧
  WithdrawPB ≠ unAuthenticated ∧ WithdrawPB ≠ unAuthorized ∧
  CompletePB ≠ unAuthenticated ∧ CompletePB ≠ unAuthorized ∧
  unAuthenticated ≠ unAuthorized
```

[slRole_distinct_clauses]

⊢ PlatoonLeader ≠ PlatoonSergeant

[slState_distinct_clauses]

⊢ CONDUCT_PB ≠ SECURE_PB ∧ CONDUCT_PB ≠ ACTIONS_IN_PB ∧
 CONDUCT_PB ≠ WITHDRAW_PB ∧ CONDUCT_PB ≠ COMPLETE_PB ∧
 SECURE_PB ≠ ACTIONS_IN_PB ∧ SECURE_PB ≠ WITHDRAW_PB ∧
 SECURE_PB ≠ COMPLETE_PB ∧ ACTIONS_IN_PB ≠ WITHDRAW_PB ∧
 ACTIONS_IN_PB ≠ COMPLETE_PB ∧ WITHDRAW_PB ≠ COMPLETE_PB

2 ssmConductPB Theory

Built: 16 May 2018

Parent Theories: ConductPBType, ssm11, OMNIType

2.1 Definitions

[secContextConductPB_def]

⊢ ∀ plcmd psgcmd incomplete.
 secContextConductPB plcmd psgcmd incomplete =
 [Name PlatoonLeader controls prop (SOME (SLc (PL plcmd)))];
 Name PlatoonSergeant controls
 prop (SOME (SLc (PSG psgcmd)));
 Name PlatoonLeader says
 prop (SOME (SLc (PSG psgcmd))) impf prop NONE;
 Name PlatoonSergeant says
 prop (SOME (SLc (PL plcmd))) impf prop NONE]

[ssmConductPBStateInterp_def]

⊢ ∀ slState. ssmConductPBStateInterp slState = TT

2.2 Theorems

[authTestConductPB_cmd_reject_lemma]

⊢ ∀ cmd. ¬authTestConductPB (prop (SOME cmd))

[authTestConductPB_def]

⊢ (authTestConductPB (Name PlatoonLeader says prop cmd) ⇔ T) ∧
 (authTestConductPB (Name PlatoonSergeant says prop cmd) ⇔
 T) ∧ (authTestConductPB TT ⇔ F) ∧
 (authTestConductPB FF ⇔ F) ∧
 (authTestConductPB (prop v) ⇔ F) ∧
 (authTestConductPB (notf v₁) ⇔ F) ∧
 (authTestConductPB (v₂ andf v₃) ⇔ F) ∧
 (authTestConductPB (v₄ orf v₅) ⇔ F) ∧
 (authTestConductPB (v₆ impf v₇) ⇔ F) ∧

$(\text{authTestConductPB } (v_8 \text{ eqf } v_9) \iff F) \wedge$
 $(\text{authTestConductPB } (v_{10} \text{ says TT}) \iff F) \wedge$
 $(\text{authTestConductPB } (v_{10} \text{ says FF}) \iff F) \wedge$
 $(\text{authTestConductPB } (v_{133} \text{ meet } v_{134} \text{ says prop } v_{66}) \iff F) \wedge$
 $(\text{authTestConductPB } (v_{135} \text{ quoting } v_{136} \text{ says prop } v_{66}) \iff F) \wedge$
 $(\text{authTestConductPB } (v_{10} \text{ says notf } v_{67}) \iff F) \wedge$
 $(\text{authTestConductPB } (v_{10} \text{ says } (v_{68} \text{ andf } v_{69})) \iff F) \wedge$
 $(\text{authTestConductPB } (v_{10} \text{ says } (v_{70} \text{ orf } v_{71})) \iff F) \wedge$
 $(\text{authTestConductPB } (v_{10} \text{ says } (v_{72} \text{ impf } v_{73})) \iff F) \wedge$
 $(\text{authTestConductPB } (v_{10} \text{ says } (v_{74} \text{ eqf } v_{75})) \iff F) \wedge$
 $(\text{authTestConductPB } (v_{10} \text{ says } v_{76} \text{ says } v_{77}) \iff F) \wedge$
 $(\text{authTestConductPB } (v_{10} \text{ says } v_{78} \text{ speaks_for } v_{79}) \iff F) \wedge$
 $(\text{authTestConductPB } (v_{10} \text{ says } v_{80} \text{ controls } v_{81}) \iff F) \wedge$
 $(\text{authTestConductPB } (v_{10} \text{ says reps } v_{82} \ v_{83} \ v_{84}) \iff F) \wedge$
 $(\text{authTestConductPB } (v_{10} \text{ says } v_{85} \text{ domi } v_{86}) \iff F) \wedge$
 $(\text{authTestConductPB } (v_{10} \text{ says } v_{87} \text{ eqi } v_{88}) \iff F) \wedge$
 $(\text{authTestConductPB } (v_{10} \text{ says } v_{89} \text{ doms } v_{90}) \iff F) \wedge$
 $(\text{authTestConductPB } (v_{10} \text{ says } v_{91} \text{ eqs } v_{92}) \iff F) \wedge$
 $(\text{authTestConductPB } (v_{10} \text{ says } v_{93} \text{ eqn } v_{94}) \iff F) \wedge$
 $(\text{authTestConductPB } (v_{10} \text{ says } v_{95} \text{ lte } v_{96}) \iff F) \wedge$
 $(\text{authTestConductPB } (v_{10} \text{ says } v_{97} \text{ lt } v_{98}) \iff F) \wedge$
 $(\text{authTestConductPB } (v_{12} \text{ speaks_for } v_{13}) \iff F) \wedge$
 $(\text{authTestConductPB } (v_{14} \text{ controls } v_{15}) \iff F) \wedge$
 $(\text{authTestConductPB } (\text{reps } v_{16} \ v_{17} \ v_{18}) \iff F) \wedge$
 $(\text{authTestConductPB } (v_{19} \text{ domi } v_{20}) \iff F) \wedge$
 $(\text{authTestConductPB } (v_{21} \text{ eqi } v_{22}) \iff F) \wedge$
 $(\text{authTestConductPB } (v_{23} \text{ doms } v_{24}) \iff F) \wedge$
 $(\text{authTestConductPB } (v_{25} \text{ eqs } v_{26}) \iff F) \wedge$
 $(\text{authTestConductPB } (v_{27} \text{ eqn } v_{28}) \iff F) \wedge$
 $(\text{authTestConductPB } (v_{29} \text{ lte } v_{30}) \iff F) \wedge$
 $(\text{authTestConductPB } (v_{31} \text{ lt } v_{32}) \iff F)$

$[\text{authTestConductPB_ind}]$

$\vdash \forall P.$

$(\forall \text{cmd}. P (\text{Name PlatoonLeader says prop cmd})) \wedge$
 $(\forall \text{cmd}. P (\text{Name PlatoonSergeant says prop cmd})) \wedge P \text{ TT} \wedge$
 $P \text{ FF} \wedge (\forall v. P (\text{prop } v)) \wedge (\forall v_1. P (\text{notf } v_1)) \wedge$
 $(\forall v_2 \ v_3. P (v_2 \text{ andf } v_3)) \wedge (\forall v_4 \ v_5. P (v_4 \text{ orf } v_5)) \wedge$
 $(\forall v_6 \ v_7. P (v_6 \text{ impf } v_7)) \wedge (\forall v_8 \ v_9. P (v_8 \text{ eqf } v_9)) \wedge$
 $(\forall v_{10}. P (v_{10} \text{ says TT})) \wedge (\forall v_{10}. P (v_{10} \text{ says FF})) \wedge$
 $(\forall v_{133} \ v_{134} \ v_{66}. P (v_{133} \text{ meet } v_{134} \text{ says prop } v_{66})) \wedge$
 $(\forall v_{135} \ v_{136} \ v_{66}. P (v_{135} \text{ quoting } v_{136} \text{ says prop } v_{66})) \wedge$
 $(\forall v_{10} \ v_{67}. P (v_{10} \text{ says notf } v_{67})) \wedge$
 $(\forall v_{10} \ v_{68} \ v_{69}. P (v_{10} \text{ says } (v_{68} \text{ andf } v_{69}))) \wedge$
 $(\forall v_{10} \ v_{70} \ v_{71}. P (v_{10} \text{ says } (v_{70} \text{ orf } v_{71}))) \wedge$
 $(\forall v_{10} \ v_{72} \ v_{73}. P (v_{10} \text{ says } (v_{72} \text{ impf } v_{73}))) \wedge$
 $(\forall v_{10} \ v_{74} \ v_{75}. P (v_{10} \text{ says } (v_{74} \text{ eqf } v_{75}))) \wedge$
 $(\forall v_{10} \ v_{76} \ v_{77}. P (v_{10} \text{ says } v_{76} \text{ says } v_{77})) \wedge$
 $(\forall v_{10} \ v_{78} \ v_{79}. P (v_{10} \text{ says } v_{78} \text{ speaks_for } v_{79})) \wedge$

$$\begin{aligned}
& (\forall v_{10} v_{80} v_{81}. P (v_{10} \text{ says } v_{80} \text{ controls } v_{81})) \wedge \\
& (\forall v_{10} v_{82} v_{83} v_{84}. P (v_{10} \text{ says reps } v_{82} v_{83} v_{84})) \wedge \\
& (\forall v_{10} v_{85} v_{86}. P (v_{10} \text{ says } v_{85} \text{ domi } v_{86})) \wedge \\
& (\forall v_{10} v_{87} v_{88}. P (v_{10} \text{ says } v_{87} \text{ eqi } v_{88})) \wedge \\
& (\forall v_{10} v_{89} v_{90}. P (v_{10} \text{ says } v_{89} \text{ doms } v_{90})) \wedge \\
& (\forall v_{10} v_{91} v_{92}. P (v_{10} \text{ says } v_{91} \text{ eqs } v_{92})) \wedge \\
& (\forall v_{10} v_{93} v_{94}. P (v_{10} \text{ says } v_{93} \text{ eqn } v_{94})) \wedge \\
& (\forall v_{10} v_{95} v_{96}. P (v_{10} \text{ says } v_{95} \text{ lte } v_{96})) \wedge \\
& (\forall v_{10} v_{97} v_{98}. P (v_{10} \text{ says } v_{97} \text{ lt } v_{98})) \wedge \\
& (\forall v_{12} v_{13}. P (v_{12} \text{ speaks_for } v_{13})) \wedge \\
& (\forall v_{14} v_{15}. P (v_{14} \text{ controls } v_{15})) \wedge \\
& (\forall v_{16} v_{17} v_{18}. P (\text{reps } v_{16} v_{17} v_{18})) \wedge \\
& (\forall v_{19} v_{20}. P (v_{19} \text{ domi } v_{20})) \wedge \\
& (\forall v_{21} v_{22}. P (v_{21} \text{ eqi } v_{22})) \wedge \\
& (\forall v_{23} v_{24}. P (v_{23} \text{ doms } v_{24})) \wedge \\
& (\forall v_{25} v_{26}. P (v_{25} \text{ eqs } v_{26})) \wedge (\forall v_{27} v_{28}. P (v_{27} \text{ eqn } v_{28})) \wedge \\
& (\forall v_{29} v_{30}. P (v_{29} \text{ lte } v_{30})) \wedge (\forall v_{31} v_{32}. P (v_{31} \text{ lt } v_{32})) \Rightarrow \\
& \forall v. P v
\end{aligned}$$

[conductPBNS_def]

$$\begin{aligned}
& \vdash (\text{conductPBNS CONDUCT_PB (exec (PL securePB))} = \text{SECURE_PB}) \wedge \\
& (\text{conductPBNS CONDUCT_PB (exec (PL plIncompletePB))} = \\
& \quad \text{CONDUCT_PB}) \wedge \\
& (\text{conductPBNS SECURE_PB (exec (PSG actionsInPB))} = \\
& \quad \text{ACTIONS_IN_PB}) \wedge \\
& (\text{conductPBNS SECURE_PB (exec (PSG psgIncompletePB))} = \\
& \quad \text{SECURE_PB}) \wedge \\
& (\text{conductPBNS ACTIONS_IN_PB (exec (PL withdrawPB))} = \\
& \quad \text{WITHDRAW_PB}) \wedge \\
& (\text{conductPBNS ACTIONS_IN_PB (exec (PL plIncompletePB))} = \\
& \quad \text{ACTIONS_IN_PB}) \wedge \\
& (\text{conductPBNS WITHDRAW_PB (exec (PL completePB))} = \\
& \quad \text{COMPLETE_PB}) \wedge \\
& (\text{conductPBNS WITHDRAW_PB (exec (PL plIncompletePB))} = \\
& \quad \text{WITHDRAW_PB}) \wedge (\text{conductPBNS } s \text{ (trap (PL cmd'))} = s) \wedge \\
& (\text{conductPBNS } s \text{ (trap (PSG cmd))} = s) \wedge \\
& (\text{conductPBNS } s \text{ (discard (PL cmd'))} = s) \wedge \\
& (\text{conductPBNS } s \text{ (discard (PSG cmd))} = s)
\end{aligned}$$

[conductPBNS_ind]

$$\begin{aligned}
& \vdash \forall P. \\
& \quad P \text{ CONDUCT_PB (exec (PL securePB))} \wedge \\
& \quad P \text{ CONDUCT_PB (exec (PL plIncompletePB))} \wedge \\
& \quad P \text{ SECURE_PB (exec (PSG actionsInPB))} \wedge \\
& \quad P \text{ SECURE_PB (exec (PSG psgIncompletePB))} \wedge \\
& \quad P \text{ ACTIONS_IN_PB (exec (PL withdrawPB))} \wedge \\
& \quad P \text{ ACTIONS_IN_PB (exec (PL plIncompletePB))} \wedge \\
& \quad P \text{ WITHDRAW_PB (exec (PL completePB))} \wedge \\
& \quad P \text{ WITHDRAW_PB (exec (PL plIncompletePB))} \wedge
\end{aligned}$$

$$\begin{aligned}
& (\forall s \text{ cmd}. P \ s \ (\text{trap} \ (\text{PL} \ \text{cmd}))) \wedge \\
& (\forall s \text{ cmd}. P \ s \ (\text{trap} \ (\text{PSG} \ \text{cmd}))) \wedge \\
& (\forall s \text{ cmd}. P \ s \ (\text{discard} \ (\text{PL} \ \text{cmd}))) \wedge \\
& (\forall s \text{ cmd}. P \ s \ (\text{discard} \ (\text{PSG} \ \text{cmd}))) \wedge \\
& P \ \text{CONDUCT_PB} \ (\text{exec} \ (\text{PL} \ \text{withdrawPB})) \wedge \\
& P \ \text{CONDUCT_PB} \ (\text{exec} \ (\text{PL} \ \text{completePB})) \wedge \\
& (\forall v_{11}. P \ \text{CONDUCT_PB} \ (\text{exec} \ (\text{PSG} \ v_{11}))) \wedge \\
& (\forall v_{13}. P \ \text{SECURE_PB} \ (\text{exec} \ (\text{PL} \ v_{13}))) \wedge \\
& P \ \text{ACTIONS_IN_PB} \ (\text{exec} \ (\text{PL} \ \text{securePB})) \wedge \\
& P \ \text{ACTIONS_IN_PB} \ (\text{exec} \ (\text{PL} \ \text{completePB})) \wedge \\
& (\forall v_{17}. P \ \text{ACTIONS_IN_PB} \ (\text{exec} \ (\text{PSG} \ v_{17}))) \wedge \\
& P \ \text{WITHDRAW_PB} \ (\text{exec} \ (\text{PL} \ \text{securePB})) \wedge \\
& P \ \text{WITHDRAW_PB} \ (\text{exec} \ (\text{PL} \ \text{withdrawPB})) \wedge \\
& (\forall v_{20}. P \ \text{WITHDRAW_PB} \ (\text{exec} \ (\text{PSG} \ v_{20}))) \wedge \\
& (\forall v_{21}. P \ \text{COMPLETE_PB} \ (\text{exec} \ v_{21})) \Rightarrow \\
& \forall v \ v_1. P \ v \ v_1
\end{aligned}$$

[conductPBOut_def]

$$\begin{aligned}
& \vdash (\text{conductPBOut} \ \text{CONDUCT_PB} \ (\text{exec} \ (\text{PL} \ \text{securePB})) = \text{ConductPB}) \wedge \\
& (\text{conductPBOut} \ \text{CONDUCT_PB} \ (\text{exec} \ (\text{PL} \ \text{plIncompletePB})) = \\
& \quad \text{ConductPB}) \wedge \\
& (\text{conductPBOut} \ \text{SECURE_PB} \ (\text{exec} \ (\text{PSG} \ \text{actionsInPB})) = \\
& \quad \text{SecurePB}) \wedge \\
& (\text{conductPBOut} \ \text{SECURE_PB} \ (\text{exec} \ (\text{PSG} \ \text{psgIncompletePB})) = \\
& \quad \text{SecurePB}) \wedge \\
& (\text{conductPBOut} \ \text{ACTIONS_IN_PB} \ (\text{exec} \ (\text{PL} \ \text{withdrawPB})) = \\
& \quad \text{ActionsInPB}) \wedge \\
& (\text{conductPBOut} \ \text{ACTIONS_IN_PB} \ (\text{exec} \ (\text{PL} \ \text{plIncompletePB})) = \\
& \quad \text{ActionsInPB}) \wedge \\
& (\text{conductPBOut} \ \text{WITHDRAW_PB} \ (\text{exec} \ (\text{PL} \ \text{completePB})) = \\
& \quad \text{WithdrawPB}) \wedge \\
& (\text{conductPBOut} \ \text{WITHDRAW_PB} \ (\text{exec} \ (\text{PL} \ \text{plIncompletePB})) = \\
& \quad \text{WithdrawPB}) \wedge \\
& (\text{conductPBOut} \ s \ (\text{trap} \ (\text{PL} \ \text{cmd}')) = \text{unAuthorized}) \wedge \\
& (\text{conductPBOut} \ s \ (\text{trap} \ (\text{PSG} \ \text{cmd}')) = \text{unAuthorized}) \wedge \\
& (\text{conductPBOut} \ s \ (\text{discard} \ (\text{PL} \ \text{cmd}')) = \text{unAuthenticated}) \wedge \\
& (\text{conductPBOut} \ s \ (\text{discard} \ (\text{PSG} \ \text{cmd}')) = \text{unAuthenticated})
\end{aligned}$$

[conductPBOut_ind]

$$\begin{aligned}
& \vdash \forall P. \\
& \quad P \ \text{CONDUCT_PB} \ (\text{exec} \ (\text{PL} \ \text{securePB})) \wedge \\
& \quad P \ \text{CONDUCT_PB} \ (\text{exec} \ (\text{PL} \ \text{plIncompletePB})) \wedge \\
& \quad P \ \text{SECURE_PB} \ (\text{exec} \ (\text{PSG} \ \text{actionsInPB})) \wedge \\
& \quad P \ \text{SECURE_PB} \ (\text{exec} \ (\text{PSG} \ \text{psgIncompletePB})) \wedge \\
& \quad P \ \text{ACTIONS_IN_PB} \ (\text{exec} \ (\text{PL} \ \text{withdrawPB})) \wedge \\
& \quad P \ \text{ACTIONS_IN_PB} \ (\text{exec} \ (\text{PL} \ \text{plIncompletePB})) \wedge \\
& \quad P \ \text{WITHDRAW_PB} \ (\text{exec} \ (\text{PL} \ \text{completePB})) \wedge \\
& \quad P \ \text{WITHDRAW_PB} \ (\text{exec} \ (\text{PL} \ \text{plIncompletePB})) \wedge \\
& \quad (\forall s \ \text{cmd}. P \ s \ (\text{trap} \ (\text{PL} \ \text{cmd}))) \wedge
\end{aligned}$$

$$\begin{aligned}
& (\forall s \text{ cmd. } P \ s \ (\text{trap} \ (\text{PSG} \ \text{cmd}))) \wedge \\
& (\forall s \text{ cmd. } P \ s \ (\text{discard} \ (\text{PL} \ \text{cmd}))) \wedge \\
& (\forall s \text{ cmd. } P \ s \ (\text{discard} \ (\text{PSG} \ \text{cmd}))) \wedge \\
& P \ \text{CONDUCT_PB} \ (\text{exec} \ (\text{PL} \ \text{withdrawPB})) \wedge \\
& P \ \text{CONDUCT_PB} \ (\text{exec} \ (\text{PL} \ \text{completePB})) \wedge \\
& (\forall v_{11}. P \ \text{CONDUCT_PB} \ (\text{exec} \ (\text{PSG} \ v_{11}))) \wedge \\
& (\forall v_{13}. P \ \text{SECURE_PB} \ (\text{exec} \ (\text{PL} \ v_{13}))) \wedge \\
& P \ \text{ACTIONS_IN_PB} \ (\text{exec} \ (\text{PL} \ \text{securePB})) \wedge \\
& P \ \text{ACTIONS_IN_PB} \ (\text{exec} \ (\text{PL} \ \text{completePB})) \wedge \\
& (\forall v_{17}. P \ \text{ACTIONS_IN_PB} \ (\text{exec} \ (\text{PSG} \ v_{17}))) \wedge \\
& P \ \text{WITHDRAW_PB} \ (\text{exec} \ (\text{PL} \ \text{securePB})) \wedge \\
& P \ \text{WITHDRAW_PB} \ (\text{exec} \ (\text{PL} \ \text{withdrawPB})) \wedge \\
& (\forall v_{20}. P \ \text{WITHDRAW_PB} \ (\text{exec} \ (\text{PSG} \ v_{20}))) \wedge \\
& (\forall v_{21}. P \ \text{COMPLETE_PB} \ (\text{exec} \ v_{21})) \Rightarrow \\
& \forall v \ v_1. P \ v \ v_1
\end{aligned}$$

[PlatoonLeader_exec_plCommandPB_justified_thm]

$$\begin{aligned}
& \vdash \forall NS \ Out \ M \ Oi \ Os. \\
& \quad \text{TR} \ (M, Oi, Os) \ (\text{exec} \ (\text{SLc} \ (\text{PL} \ plCommand))) \\
& \quad \quad (\text{CFG} \ \text{authTestConductPB} \ \text{ssmConductPBStateInterp} \\
& \quad \quad \quad (\text{secContextConductPB} \ plCommand \ psgCommand \ incomplete) \\
& \quad \quad \quad (\text{Name} \ \text{PlatoonLeader} \ \text{says} \\
& \quad \quad \quad \quad \text{prop} \ (\text{SOME} \ (\text{SLc} \ (\text{PL} \ plCommand)))::ins) \ s \ outs) \\
& \quad \quad \quad (\text{CFG} \ \text{authTestConductPB} \ \text{ssmConductPBStateInterp} \\
& \quad \quad \quad \quad (\text{secContextConductPB} \ plCommand \ psgCommand \ incomplete) \\
& \quad \quad \quad \quad \quad ins \ (NS \ s \ (\text{exec} \ (\text{SLc} \ (\text{PL} \ plCommand)))) \\
& \quad \quad \quad \quad \quad (\text{Out} \ s \ (\text{exec} \ (\text{SLc} \ (\text{PL} \ plCommand)))::outs)) \iff \\
& \quad \text{authTestConductPB} \\
& \quad \quad (\text{Name} \ \text{PlatoonLeader} \ \text{says} \\
& \quad \quad \quad \text{prop} \ (\text{SOME} \ (\text{SLc} \ (\text{PL} \ plCommand)))) \wedge \\
& \quad \text{CFGInterpret} \ (M, Oi, Os) \\
& \quad \quad (\text{CFG} \ \text{authTestConductPB} \ \text{ssmConductPBStateInterp} \\
& \quad \quad \quad (\text{secContextConductPB} \ plCommand \ psgCommand \ incomplete) \\
& \quad \quad \quad (\text{Name} \ \text{PlatoonLeader} \ \text{says} \\
& \quad \quad \quad \quad \text{prop} \ (\text{SOME} \ (\text{SLc} \ (\text{PL} \ plCommand)))::ins) \ s \ outs) \wedge \\
& \quad \quad \quad (M, Oi, Os) \ \text{sat} \ \text{prop} \ (\text{SOME} \ (\text{SLc} \ (\text{PL} \ plCommand)))
\end{aligned}$$

[PlatoonLeader_plCommandPB_lemma]

$$\begin{aligned}
& \vdash \text{CFGInterpret} \ (M, Oi, Os) \\
& \quad (\text{CFG} \ \text{authTestConductPB} \ \text{ssmConductPBStateInterp} \\
& \quad \quad (\text{secContextConductPB} \ plCommand \ psgCommand \ incomplete) \\
& \quad \quad (\text{Name} \ \text{PlatoonLeader} \ \text{says} \\
& \quad \quad \quad \text{prop} \ (\text{SOME} \ (\text{SLc} \ (\text{PL} \ plCommand)))::ins) \ s \ outs) \Rightarrow \\
& \quad (M, Oi, Os) \ \text{sat} \ \text{prop} \ (\text{SOME} \ (\text{SLc} \ (\text{PL} \ plCommand)))
\end{aligned}$$

[PlatoonSergeant_exec_psgCommandPB_justified_thm]

$$\begin{aligned}
& \vdash \forall NS \ Out \ M \ Oi \ Os. \\
& \quad \text{TR} \ (M, Oi, Os) \ (\text{exec} \ (\text{SLc} \ (\text{PSG} \ psgCommand)))
\end{aligned}$$


```

(CFG authTestConductPB ssmConductPBStateInterp
  (secContextConductPB plCommand psgCommand incomplete)
  (Name PlatoonSergeant says
    prop (SOME (SLc (PSG psgCommand))))::ins) s outs)
(CFG authTestConductPB ssmConductPBStateInterp
  (secContextConductPB plCommand psgCommand incomplete)
  ins (NS s (exec (SLc (PSG psgCommand))))
  (Out s (exec (SLc (PSG psgCommand))))::outs))  $\iff$ 
authTestConductPB
  (Name PlatoonSergeant says
    prop (SOME (SLc (PSG psgCommand))))  $\wedge$ 
CFGInterpret (M, Oi, Os)
  (CFG authTestConductPB ssmConductPBStateInterp
    (secContextConductPB plCommand psgCommand incomplete)
    (Name PlatoonSergeant says
      prop (SOME (SLc (PSG psgCommand))))::ins) s outs)  $\wedge$ 
  (M, Oi, Os) sat prop (SOME (SLc (PSG psgCommand)))

```

[PlatoonSergeant_psgCommandPB_lemma]

```

 $\vdash$  CFGInterpret (M, Oi, Os)
  (CFG authTestConductPB ssmConductPBStateInterp
    (secContextConductPB plCommand psgCommand incomplete)
    (Name PlatoonSergeant says
      prop (SOME (SLc (PSG psgCommand))))::ins) s outs)  $\Rightarrow$ 
  (M, Oi, Os) sat prop (SOME (SLc (PSG psgCommand)))

```


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