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# 1 projectTypes Theory

**Built:** 27 December 2018

**Parent Theories:** indexedLists, patternMatches

## 1.1 Datatypes

```
commands = PlatoonLeaderCOM platoonLeaderCom | OmniCOM omniCom

omniCom = none | omniNA

output = Move_to_ORP | Form | Move | Secure_halt | NoActionTaken
        | UnAuthenticated | Unauthorized

platoonLeaderCom = form | move | secureHalt

principal = PlatoonLeader | Omni

state = MOVE_TO_PB | FORM | MOVE | SECURE_HALT
```

## 1.2 Theorems

[commands\_distinct\_clauses]

$\vdash \forall a' a. \text{PlatoonLeaderCOM } a \neq \text{OmniCOM } a'$

[commands\_one\_one]

$\vdash (\forall a a'. (\text{PlatoonLeaderCOM } a = \text{PlatoonLeaderCOM } a') \iff (a = a')) \wedge$   
 $\forall a a'. (\text{OmniCOM } a = \text{OmniCOM } a') \iff (a = a')$

[omniCom\_distinct\_clauses]

$\vdash \text{none} \neq \text{omniNA}$

[output\_distinct\_clauses]

$\vdash \text{Move\_to\_ORP} \neq \text{Form} \wedge \text{Move\_to\_ORP} \neq \text{Move} \wedge$   
 $\text{Move\_to\_ORP} \neq \text{Secure\_halt} \wedge \text{Move\_to\_ORP} \neq \text{NoActionTaken} \wedge$   
 $\text{Move\_to\_ORP} \neq \text{UnAuthenticated} \wedge \text{Move\_to\_ORP} \neq \text{Unauthorized} \wedge$   
 $\text{Form} \neq \text{Move} \wedge \text{Form} \neq \text{Secure\_halt} \wedge \text{Form} \neq \text{NoActionTaken} \wedge$   
 $\text{Form} \neq \text{UnAuthenticated} \wedge \text{Form} \neq \text{Unauthorized} \wedge$   
 $\text{Move} \neq \text{Secure\_halt} \wedge \text{Move} \neq \text{NoActionTaken} \wedge$   
 $\text{Move} \neq \text{UnAuthenticated} \wedge \text{Move} \neq \text{Unauthorized} \wedge$   
 $\text{Secure\_halt} \neq \text{NoActionTaken} \wedge \text{Secure\_halt} \neq \text{UnAuthenticated} \wedge$   
 $\text{Secure\_halt} \neq \text{Unauthorized} \wedge$   
 $\text{NoActionTaken} \neq \text{UnAuthenticated} \wedge$   
 $\text{NoActionTaken} \neq \text{Unauthorized} \wedge \text{UnAuthenticated} \neq \text{Unauthorized}$

[platoonLeaderCom\_distinct\_clauses]

$\vdash \text{form} \neq \text{move} \wedge \text{form} \neq \text{secureHalt} \wedge \text{move} \neq \text{secureHalt}$

[principal\_distinct\_clauses]

⊢ PlatoonLeader ≠ Omni

[state\_distinct\_clauses]

⊢ MOVE\_TO\_PB ≠ FORM ∧ MOVE\_TO\_PB ≠ MOVE ∧  
MOVE\_TO\_PB ≠ SECURE\_HALT ∧ FORM ≠ MOVE ∧ FORM ≠ SECURE\_HALT ∧  
MOVE ≠ SECURE\_HALT

## 2 projectUtilities Theory

**Built:** 27 December 2018

**Parent Theories:** projectTypes, satList

### 2.1 Theorems

[getOmniCOM\_def]

⊢ (getOmniCOM [] = NONE) ∧  
(∀ xs cmd.  
  getOmniCOM (SOME (OmniCOM cmd)::xs) =  
  SOME (OmniCOM cmd)) ∧  
(∀ xs. getOmniCOM (NONE::xs) = getOmniCOM xs) ∧  
∀ xs v<sub>4</sub>.  
  getOmniCOM (SOME (PlatoonLeaderCOM v<sub>4</sub>::xs) = getOmniCOM xs

[getOmniCOM\_ind]

⊢ ∀ P.  
  P [] ∧ (∀ cmd xs. P (SOME (OmniCOM cmd)::xs)) ∧  
  (∀ xs. P xs ⇒ P (NONE::xs)) ∧  
  (∀ v<sub>4</sub> xs. P xs ⇒ P (SOME (PlatoonLeaderCOM v<sub>4</sub>::xs))) ⇒  
  ∀ v. P v

[getOmniCOMx\_def]

⊢ (getOmniCOMx [] = NONE) ∧  
(∀ xs cmd.  
  getOmniCOMx  
  (Name Omni says prop (SOME (OmniCOM cmd)::xs) =  
  SOME (OmniCOM cmd)) ∧  
(∀ xs. getOmniCOMx (TT::xs) = getOmniCOMx xs) ∧  
(∀ xs. getOmniCOMx (FF::xs) = getOmniCOMx xs) ∧  
(∀ xs v<sub>2</sub>. getOmniCOMx (prop v<sub>2</sub>::xs) = getOmniCOMx xs) ∧  
(∀ xs v<sub>3</sub>. getOmniCOMx (notf v<sub>3</sub>::xs) = getOmniCOMx xs) ∧  
(∀ xs v<sub>5</sub> v<sub>4</sub>. getOmniCOMx (v<sub>4</sub> andf v<sub>5</sub>::xs) = getOmniCOMx xs) ∧  
(∀ xs v<sub>7</sub> v<sub>6</sub>. getOmniCOMx (v<sub>6</sub> orf v<sub>7</sub>::xs) = getOmniCOMx xs) ∧  
(∀ xs v<sub>9</sub> v<sub>8</sub>. getOmniCOMx (v<sub>8</sub> impf v<sub>9</sub>::xs) = getOmniCOMx xs) ∧  
(∀ xs v<sub>11</sub> v<sub>10</sub>.  
  getOmniCOMx (v<sub>10</sub> eqf v<sub>11</sub>::xs) = getOmniCOMx xs) ∧

$$\begin{aligned}
& (\forall xs \ v_{12}. \text{getOmniCOMx } (v_{12} \text{ says TT}::xs) = \text{getOmniCOMx } xs) \wedge \\
& (\forall xs \ v_{12}. \text{getOmniCOMx } (v_{12} \text{ says FF}::xs) = \text{getOmniCOMx } xs) \wedge \\
& (\forall xs \ v_{134}. \\
& \quad \text{getOmniCOMx } (\text{Name } v_{134} \text{ says prop NONE}::xs) = \\
& \quad \text{getOmniCOMx } xs) \wedge \\
& (\forall xs \ v_{144}. \\
& \quad \text{getOmniCOMx} \\
& \quad (\text{Name PlatoonLeader says prop (SOME } v_{144})::xs) = \\
& \quad \text{getOmniCOMx } xs) \wedge \\
& (\forall xs \ v_{146}. \\
& \quad \text{getOmniCOMx} \\
& \quad (\text{Name Omni says prop (SOME (PlatoonLeaderCOM } v_{146}))::xs) = \\
& \quad \text{getOmniCOMx } xs) \wedge \\
& (\forall xs \ v_{68} \ v_{136} \ v_{135}. \\
& \quad \text{getOmniCOMx } (v_{135} \text{ meet } v_{136} \text{ says prop } v_{68}::xs) = \\
& \quad \text{getOmniCOMx } xs) \wedge \\
& (\forall xs \ v_{68} \ v_{138} \ v_{137}. \\
& \quad \text{getOmniCOMx } (v_{137} \text{ quoting } v_{138} \text{ says prop } v_{68}::xs) = \\
& \quad \text{getOmniCOMx } xs) \wedge \\
& (\forall xs \ v_{69} \ v_{12}. \\
& \quad \text{getOmniCOMx } (v_{12} \text{ says notf } v_{69}::xs) = \text{getOmniCOMx } xs) \wedge \\
& (\forall xs \ v_{71} \ v_{70} \ v_{12}. \\
& \quad \text{getOmniCOMx } (v_{12} \text{ says } (v_{70} \text{ andf } v_{71})::xs) = \\
& \quad \text{getOmniCOMx } xs) \wedge \\
& (\forall xs \ v_{73} \ v_{72} \ v_{12}. \\
& \quad \text{getOmniCOMx } (v_{12} \text{ says } (v_{72} \text{ orf } v_{73})::xs) = \\
& \quad \text{getOmniCOMx } xs) \wedge \\
& (\forall xs \ v_{75} \ v_{74} \ v_{12}. \\
& \quad \text{getOmniCOMx } (v_{12} \text{ says } (v_{74} \text{ impf } v_{75})::xs) = \\
& \quad \text{getOmniCOMx } xs) \wedge \\
& (\forall xs \ v_{77} \ v_{76} \ v_{12}. \\
& \quad \text{getOmniCOMx } (v_{12} \text{ says } (v_{76} \text{ eqf } v_{77})::xs) = \\
& \quad \text{getOmniCOMx } xs) \wedge \\
& (\forall xs \ v_{79} \ v_{78} \ v_{12}. \\
& \quad \text{getOmniCOMx } (v_{12} \text{ says } v_{78} \text{ says } v_{79}::xs) = \\
& \quad \text{getOmniCOMx } xs) \wedge \\
& (\forall xs \ v_{81} \ v_{80} \ v_{12}. \\
& \quad \text{getOmniCOMx } (v_{12} \text{ says } v_{80} \text{ speaks\_for } v_{81}::xs) = \\
& \quad \text{getOmniCOMx } xs) \wedge \\
& (\forall xs \ v_{83} \ v_{82} \ v_{12}. \\
& \quad \text{getOmniCOMx } (v_{12} \text{ says } v_{82} \text{ controls } v_{83}::xs) = \\
& \quad \text{getOmniCOMx } xs) \wedge \\
& (\forall xs \ v_{86} \ v_{85} \ v_{84} \ v_{12}. \\
& \quad \text{getOmniCOMx } (v_{12} \text{ says reps } v_{84} \ v_{85} \ v_{86}::xs) = \\
& \quad \text{getOmniCOMx } xs) \wedge \\
& (\forall xs \ v_{88} \ v_{87} \ v_{12}. \\
& \quad \text{getOmniCOMx } (v_{12} \text{ says } v_{87} \text{ domi } v_{88}::xs) = \\
& \quad \text{getOmniCOMx } xs) \wedge
\end{aligned}$$

$(\forall xs \ v_{90} \ v_{89} \ v_{12}.$   
 $\quad \text{getOmniCOMx } (v_{12} \text{ says } v_{89} \text{ eqi } v_{90}::xs) = \text{getOmniCOMx } xs) \wedge$   
 $(\forall xs \ v_{92} \ v_{91} \ v_{12}.$   
 $\quad \text{getOmniCOMx } (v_{12} \text{ says } v_{91} \text{ doms } v_{92}::xs) =$   
 $\quad \text{getOmniCOMx } xs) \wedge$   
 $(\forall xs \ v_{94} \ v_{93} \ v_{12}.$   
 $\quad \text{getOmniCOMx } (v_{12} \text{ says } v_{93} \text{ eqs } v_{94}::xs) = \text{getOmniCOMx } xs) \wedge$   
 $(\forall xs \ v_{96} \ v_{95} \ v_{12}.$   
 $\quad \text{getOmniCOMx } (v_{12} \text{ says } v_{95} \text{ eqn } v_{96}::xs) = \text{getOmniCOMx } xs) \wedge$   
 $(\forall xs \ v_{98} \ v_{97} \ v_{12}.$   
 $\quad \text{getOmniCOMx } (v_{12} \text{ says } v_{97} \text{ lte } v_{98}::xs) = \text{getOmniCOMx } xs) \wedge$   
 $(\forall xs \ v_{99} \ v_{12} \ v100.$   
 $\quad \text{getOmniCOMx } (v_{12} \text{ says } v_{99} \text{ lt } v100::xs) = \text{getOmniCOMx } xs) \wedge$   
 $(\forall xs \ v_{15} \ v_{14}.$   
 $\quad \text{getOmniCOMx } (v_{14} \text{ speaks\_for } v_{15}::xs) = \text{getOmniCOMx } xs) \wedge$   
 $(\forall xs \ v_{17} \ v_{16}.$   
 $\quad \text{getOmniCOMx } (v_{16} \text{ controls } v_{17}::xs) = \text{getOmniCOMx } xs) \wedge$   
 $(\forall xs \ v_{20} \ v_{19} \ v_{18}.$   
 $\quad \text{getOmniCOMx } (\text{reps } v_{18} \ v_{19} \ v_{20}::xs) = \text{getOmniCOMx } xs) \wedge$   
 $(\forall xs \ v_{22} \ v_{21}.$   
 $\quad \text{getOmniCOMx } (v_{21} \text{ domi } v_{22}::xs) = \text{getOmniCOMx } xs) \wedge$   
 $(\forall xs \ v_{24} \ v_{23}.$   
 $\quad \text{getOmniCOMx } (v_{23} \text{ eqi } v_{24}::xs) = \text{getOmniCOMx } xs) \wedge$   
 $(\forall xs \ v_{26} \ v_{25}.$   
 $\quad \text{getOmniCOMx } (v_{25} \text{ doms } v_{26}::xs) = \text{getOmniCOMx } xs) \wedge$   
 $(\forall xs \ v_{28} \ v_{27}.$   
 $\quad \text{getOmniCOMx } (v_{27} \text{ eqs } v_{28}::xs) = \text{getOmniCOMx } xs) \wedge$   
 $(\forall xs \ v_{30} \ v_{29}.$   
 $\quad \text{getOmniCOMx } (v_{29} \text{ eqn } v_{30}::xs) = \text{getOmniCOMx } xs) \wedge$   
 $(\forall xs \ v_{32} \ v_{31}.$   
 $\quad \text{getOmniCOMx } (v_{31} \text{ lte } v_{32}::xs) = \text{getOmniCOMx } xs) \wedge$   
 $\forall xs \ v_{34} \ v_{33}.$ 
 $\text{getOmniCOMx } (v_{33} \text{ lt } v_{34}::xs) = \text{getOmniCOMx } xs$

[getOmniCOMx\_ind]

$\vdash \forall P.$   
 $\quad P \ [] \wedge$   
 $\quad (\forall cmd \ xs.$   
 $\quad \quad P \ (\text{Name Omni says prop (SOME (OmniCOM cmd))}::xs)) \wedge$   
 $\quad (\forall xs. P \ xs \Rightarrow P \ (\text{TT}::xs)) \wedge (\forall xs. P \ xs \Rightarrow P \ (\text{FF}::xs)) \wedge$   
 $\quad (\forall v_2 \ xs. P \ xs \Rightarrow P \ (\text{prop } v_2::xs)) \wedge$   
 $\quad (\forall v_3 \ xs. P \ xs \Rightarrow P \ (\text{notf } v_3::xs)) \wedge$   
 $\quad (\forall v_4 \ v_5 \ xs. P \ xs \Rightarrow P \ (v_4 \text{ andf } v_5::xs)) \wedge$   
 $\quad (\forall v_6 \ v_7 \ xs. P \ xs \Rightarrow P \ (v_6 \text{ orf } v_7::xs)) \wedge$   
 $\quad (\forall v_8 \ v_9 \ xs. P \ xs \Rightarrow P \ (v_8 \text{ impf } v_9::xs)) \wedge$   
 $\quad (\forall v_{10} \ v_{11} \ xs. P \ xs \Rightarrow P \ (v_{10} \text{ eqf } v_{11}::xs)) \wedge$   
 $\quad (\forall v_{12} \ xs. P \ xs \Rightarrow P \ (v_{12} \text{ says TT}::xs)) \wedge$   
 $\quad (\forall v_{12} \ xs. P \ xs \Rightarrow P \ (v_{12} \text{ says FF}::xs)) \wedge$   
 $\quad (\forall v134 \ xs. P \ xs \Rightarrow P \ (\text{Name } v134 \text{ says prop NONE}::xs)) \wedge$   
 $\quad (\forall v144 \ xs.$

$$\begin{aligned}
& P \text{ } xs \Rightarrow \\
& P (\text{Name PlatoonLeader says prop (SOME } v144)::xs)) \wedge \\
& (\forall v146 \text{ } xs. \\
& P \text{ } xs \Rightarrow \\
& P \\
& (\text{Name Omni says prop (SOME (PlatoonLeaderCOM } v146):: \\
& \quad xs)) \wedge \\
& (\forall v135 \text{ } v136 \text{ } v68 \text{ } xs. \\
& P \text{ } xs \Rightarrow P (v135 \text{ meet } v136 \text{ says prop } v68::xs)) \wedge \\
& (\forall v137 \text{ } v138 \text{ } v68 \text{ } xs. \\
& P \text{ } xs \Rightarrow P (v137 \text{ quoting } v138 \text{ says prop } v68::xs)) \wedge \\
& (\forall v12 \text{ } v69 \text{ } xs. P \text{ } xs \Rightarrow P (v12 \text{ says notf } v69::xs)) \wedge \\
& (\forall v12 \text{ } v70 \text{ } v71 \text{ } xs. P \text{ } xs \Rightarrow P (v12 \text{ says (} v70 \text{ andf } v71)::xs)) \wedge \\
& (\forall v12 \text{ } v72 \text{ } v73 \text{ } xs. P \text{ } xs \Rightarrow P (v12 \text{ says (} v72 \text{ orf } v73)::xs)) \wedge \\
& (\forall v12 \text{ } v74 \text{ } v75 \text{ } xs. P \text{ } xs \Rightarrow P (v12 \text{ says (} v74 \text{ impf } v75)::xs)) \wedge \\
& (\forall v12 \text{ } v76 \text{ } v77 \text{ } xs. P \text{ } xs \Rightarrow P (v12 \text{ says (} v76 \text{ eqf } v77)::xs)) \wedge \\
& (\forall v12 \text{ } v78 \text{ } v79 \text{ } xs. P \text{ } xs \Rightarrow P (v12 \text{ says } v78 \text{ says } v79::xs)) \wedge \\
& (\forall v12 \text{ } v80 \text{ } v81 \text{ } xs. \\
& P \text{ } xs \Rightarrow P (v12 \text{ says } v80 \text{ speaks\_for } v81::xs)) \wedge \\
& (\forall v12 \text{ } v82 \text{ } v83 \text{ } xs. \\
& P \text{ } xs \Rightarrow P (v12 \text{ says } v82 \text{ controls } v83::xs)) \wedge \\
& (\forall v12 \text{ } v84 \text{ } v85 \text{ } v86 \text{ } xs. \\
& P \text{ } xs \Rightarrow P (v12 \text{ says reps } v84 \text{ } v85 \text{ } v86::xs)) \wedge \\
& (\forall v12 \text{ } v87 \text{ } v88 \text{ } xs. P \text{ } xs \Rightarrow P (v12 \text{ says } v87 \text{ domi } v88::xs)) \wedge \\
& (\forall v12 \text{ } v89 \text{ } v90 \text{ } xs. P \text{ } xs \Rightarrow P (v12 \text{ says } v89 \text{ eqi } v90::xs)) \wedge \\
& (\forall v12 \text{ } v91 \text{ } v92 \text{ } xs. P \text{ } xs \Rightarrow P (v12 \text{ says } v91 \text{ doms } v92::xs)) \wedge \\
& (\forall v12 \text{ } v93 \text{ } v94 \text{ } xs. P \text{ } xs \Rightarrow P (v12 \text{ says } v93 \text{ eqs } v94::xs)) \wedge \\
& (\forall v12 \text{ } v95 \text{ } v96 \text{ } xs. P \text{ } xs \Rightarrow P (v12 \text{ says } v95 \text{ eqn } v96::xs)) \wedge \\
& (\forall v12 \text{ } v97 \text{ } v98 \text{ } xs. P \text{ } xs \Rightarrow P (v12 \text{ says } v97 \text{ lte } v98::xs)) \wedge \\
& (\forall v12 \text{ } v99 \text{ } v100 \text{ } xs. P \text{ } xs \Rightarrow P (v12 \text{ says } v99 \text{ lt } v100::xs)) \wedge \\
& (\forall v14 \text{ } v15 \text{ } xs. P \text{ } xs \Rightarrow P (v14 \text{ speaks\_for } v15::xs)) \wedge \\
& (\forall v16 \text{ } v17 \text{ } xs. P \text{ } xs \Rightarrow P (v16 \text{ controls } v17::xs)) \wedge \\
& (\forall v18 \text{ } v19 \text{ } v20 \text{ } xs. P \text{ } xs \Rightarrow P (\text{reps } v18 \text{ } v19 \text{ } v20::xs)) \wedge \\
& (\forall v21 \text{ } v22 \text{ } xs. P \text{ } xs \Rightarrow P (v21 \text{ domi } v22::xs)) \wedge \\
& (\forall v23 \text{ } v24 \text{ } xs. P \text{ } xs \Rightarrow P (v23 \text{ eqi } v24::xs)) \wedge \\
& (\forall v25 \text{ } v26 \text{ } xs. P \text{ } xs \Rightarrow P (v25 \text{ doms } v26::xs)) \wedge \\
& (\forall v27 \text{ } v28 \text{ } xs. P \text{ } xs \Rightarrow P (v27 \text{ eqs } v28::xs)) \wedge \\
& (\forall v29 \text{ } v30 \text{ } xs. P \text{ } xs \Rightarrow P (v29 \text{ eqn } v30::xs)) \wedge \\
& (\forall v31 \text{ } v32 \text{ } xs. P \text{ } xs \Rightarrow P (v31 \text{ lte } v32::xs)) \wedge \\
& (\forall v33 \text{ } v34 \text{ } xs. P \text{ } xs \Rightarrow P (v33 \text{ lt } v34::xs)) \Rightarrow \\
& \forall v. P \text{ } v
\end{aligned}$$

[getPlatoonLeaderCOM\_def]

$$\begin{aligned}
& \vdash (\text{getPlatoonLeaderCOM []} = \text{NONE}) \wedge \\
& (\forall xs \text{ } cmd. \\
& \quad \text{getPlatoonLeaderCOM (SOME (PlatoonLeaderCOM } cmd)::xs) =} \\
& \quad \text{SOME (PlatoonLeaderCOM } cmd)) \wedge \\
& (\forall xs. \\
& \quad \text{getPlatoonLeaderCOM (NONE::xs) = getPlatoonLeaderCOM } xs) \wedge
\end{aligned}$$

$\forall xs \ v_5.$   
 $\text{getPlatoonLeaderCOM} (\text{SOME} (\text{OmniCOM } v_5)::xs) =$   
 $\text{getPlatoonLeaderCOM } xs$

[getPlatoonLeaderCOM\_ind]

$\vdash \forall P.$   
 $P [] \wedge (\forall cmd \ xs. P (\text{SOME} (\text{PlatoonLeaderCOM } cmd)::xs)) \wedge$   
 $(\forall xs. P \ xs \Rightarrow P (\text{NONE}::xs)) \wedge$   
 $(\forall v_5 \ xs. P \ xs \Rightarrow P (\text{SOME} (\text{OmniCOM } v_5)::xs)) \Rightarrow$   
 $\forall v. P \ v$

[getPlatoonLeaderCOMx\_def]

$\vdash (\text{getPlatoonLeaderCOMx } [] = \text{NONE}) \wedge$   
 $(\forall xs \ cmd.$   
 $\text{getPlatoonLeaderCOMx}$   
 $(\text{Name PlatoonLeader says}$   
 $\text{prop } (\text{SOME} (\text{PlatoonLeaderCOM } cmd))::xs) =$   
 $\text{SOME} (\text{PlatoonLeaderCOM } cmd)) \wedge$   
 $(\forall xs.$   
 $\text{getPlatoonLeaderCOMx } (\text{TT}::xs) = \text{getPlatoonLeaderCOMx } xs) \wedge$   
 $(\forall xs.$   
 $\text{getPlatoonLeaderCOMx } (\text{FF}::xs) = \text{getPlatoonLeaderCOMx } xs) \wedge$   
 $(\forall xs \ v_2.$   
 $\text{getPlatoonLeaderCOMx } (\text{prop } v_2::xs) =$   
 $\text{getPlatoonLeaderCOMx } xs) \wedge$   
 $(\forall xs \ v_3.$   
 $\text{getPlatoonLeaderCOMx } (\text{notf } v_3::xs) =$   
 $\text{getPlatoonLeaderCOMx } xs) \wedge$   
 $(\forall xs \ v_5 \ v_4.$   
 $\text{getPlatoonLeaderCOMx } (v_4 \ \text{andf } v_5::xs) =$   
 $\text{getPlatoonLeaderCOMx } xs) \wedge$   
 $(\forall xs \ v_7 \ v_6.$   
 $\text{getPlatoonLeaderCOMx } (v_6 \ \text{orf } v_7::xs) =$   
 $\text{getPlatoonLeaderCOMx } xs) \wedge$   
 $(\forall xs \ v_9 \ v_8.$   
 $\text{getPlatoonLeaderCOMx } (v_8 \ \text{impf } v_9::xs) =$   
 $\text{getPlatoonLeaderCOMx } xs) \wedge$   
 $(\forall xs \ v_{11} \ v_{10}.$   
 $\text{getPlatoonLeaderCOMx } (v_{10} \ \text{eqf } v_{11}::xs) =$   
 $\text{getPlatoonLeaderCOMx } xs) \wedge$   
 $(\forall xs \ v_{12}.$   
 $\text{getPlatoonLeaderCOMx } (v_{12} \ \text{says TT}::xs) =$   
 $\text{getPlatoonLeaderCOMx } xs) \wedge$   
 $(\forall xs \ v_{12}.$   
 $\text{getPlatoonLeaderCOMx } (v_{12} \ \text{says FF}::xs) =$   
 $\text{getPlatoonLeaderCOMx } xs) \wedge$   
 $(\forall xs \ v134.$   
 $\text{getPlatoonLeaderCOMx } (\text{Name } v134 \ \text{says prop NONE}::xs) =$   
 $\text{getPlatoonLeaderCOMx } xs) \wedge$



```

(∀ xs v147.
  getPlatoonLeaderCOMx
    (Name PlatoonLeader says prop (SOME (OmniCOM v147)))::
      xs) =
  getPlatoonLeaderCOMx xs) ∧
(∀ xs v144.
  getPlatoonLeaderCOMx
    (Name Omni says prop (SOME v144)::xs) =
  getPlatoonLeaderCOMx xs) ∧
(∀ xs v68 v136 v135.
  getPlatoonLeaderCOMx (v135 meet v136 says prop v68::xs) =
  getPlatoonLeaderCOMx xs) ∧
(∀ xs v68 v138 v137.
  getPlatoonLeaderCOMx
    (v137 quoting v138 says prop v68::xs) =
  getPlatoonLeaderCOMx xs) ∧
(∀ xs v69 v12.
  getPlatoonLeaderCOMx (v12 says notf v69::xs) =
  getPlatoonLeaderCOMx xs) ∧
(∀ xs v71 v70 v12.
  getPlatoonLeaderCOMx (v12 says (v70 andf v71)::xs) =
  getPlatoonLeaderCOMx xs) ∧
(∀ xs v73 v72 v12.
  getPlatoonLeaderCOMx (v12 says (v72 orf v73)::xs) =
  getPlatoonLeaderCOMx xs) ∧
(∀ xs v75 v74 v12.
  getPlatoonLeaderCOMx (v12 says (v74 impf v75)::xs) =
  getPlatoonLeaderCOMx xs) ∧
(∀ xs v77 v76 v12.
  getPlatoonLeaderCOMx (v12 says (v76 eqf v77)::xs) =
  getPlatoonLeaderCOMx xs) ∧
(∀ xs v79 v78 v12.
  getPlatoonLeaderCOMx (v12 says v78 says v79::xs) =
  getPlatoonLeaderCOMx xs) ∧
(∀ xs v81 v80 v12.
  getPlatoonLeaderCOMx (v12 says v80 speaks_for v81::xs) =
  getPlatoonLeaderCOMx xs) ∧
(∀ xs v83 v82 v12.
  getPlatoonLeaderCOMx (v12 says v82 controls v83::xs) =
  getPlatoonLeaderCOMx xs) ∧
(∀ xs v86 v85 v84 v12.
  getPlatoonLeaderCOMx (v12 says reps v84 v85 v86::xs) =
  getPlatoonLeaderCOMx xs) ∧
(∀ xs v88 v87 v12.
  getPlatoonLeaderCOMx (v12 says v87 domi v88::xs) =
  getPlatoonLeaderCOMx xs) ∧
(∀ xs v90 v89 v12.
  getPlatoonLeaderCOMx (v12 says v89 eqi v90::xs) =
  getPlatoonLeaderCOMx xs) ∧

```

$(\forall xs \ v_{92} \ v_{91} \ v_{12}.$   
 $\quad \text{getPlatoonLeaderCOMx } (v_{12} \text{ says } v_{91} \text{ doms } v_{92}::xs) =$   
 $\quad \text{getPlatoonLeaderCOMx } xs) \wedge$   
 $(\forall xs \ v_{94} \ v_{93} \ v_{12}.$   
 $\quad \text{getPlatoonLeaderCOMx } (v_{12} \text{ says } v_{93} \text{ eqs } v_{94}::xs) =$   
 $\quad \text{getPlatoonLeaderCOMx } xs) \wedge$   
 $(\forall xs \ v_{96} \ v_{95} \ v_{12}.$   
 $\quad \text{getPlatoonLeaderCOMx } (v_{12} \text{ says } v_{95} \text{ eqn } v_{96}::xs) =$   
 $\quad \text{getPlatoonLeaderCOMx } xs) \wedge$   
 $(\forall xs \ v_{98} \ v_{97} \ v_{12}.$   
 $\quad \text{getPlatoonLeaderCOMx } (v_{12} \text{ says } v_{97} \text{ lte } v_{98}::xs) =$   
 $\quad \text{getPlatoonLeaderCOMx } xs) \wedge$   
 $(\forall xs \ v_{99} \ v_{12} \ v_{100}.$   
 $\quad \text{getPlatoonLeaderCOMx } (v_{12} \text{ says } v_{99} \text{ lt } v_{100}::xs) =$   
 $\quad \text{getPlatoonLeaderCOMx } xs) \wedge$   
 $(\forall xs \ v_{15} \ v_{14}.$   
 $\quad \text{getPlatoonLeaderCOMx } (v_{14} \text{ speaks\_for } v_{15}::xs) =$   
 $\quad \text{getPlatoonLeaderCOMx } xs) \wedge$   
 $(\forall xs \ v_{17} \ v_{16}.$   
 $\quad \text{getPlatoonLeaderCOMx } (v_{16} \text{ controls } v_{17}::xs) =$   
 $\quad \text{getPlatoonLeaderCOMx } xs) \wedge$   
 $(\forall xs \ v_{20} \ v_{19} \ v_{18}.$   
 $\quad \text{getPlatoonLeaderCOMx } (\text{reps } v_{18} \ v_{19} \ v_{20}::xs) =$   
 $\quad \text{getPlatoonLeaderCOMx } xs) \wedge$   
 $(\forall xs \ v_{22} \ v_{21}.$   
 $\quad \text{getPlatoonLeaderCOMx } (v_{21} \text{ domi } v_{22}::xs) =$   
 $\quad \text{getPlatoonLeaderCOMx } xs) \wedge$   
 $(\forall xs \ v_{24} \ v_{23}.$   
 $\quad \text{getPlatoonLeaderCOMx } (v_{23} \text{ eqi } v_{24}::xs) =$   
 $\quad \text{getPlatoonLeaderCOMx } xs) \wedge$   
 $(\forall xs \ v_{26} \ v_{25}.$   
 $\quad \text{getPlatoonLeaderCOMx } (v_{25} \text{ doms } v_{26}::xs) =$   
 $\quad \text{getPlatoonLeaderCOMx } xs) \wedge$   
 $(\forall xs \ v_{28} \ v_{27}.$   
 $\quad \text{getPlatoonLeaderCOMx } (v_{27} \text{ eqs } v_{28}::xs) =$   
 $\quad \text{getPlatoonLeaderCOMx } xs) \wedge$   
 $(\forall xs \ v_{30} \ v_{29}.$   
 $\quad \text{getPlatoonLeaderCOMx } (v_{29} \text{ eqn } v_{30}::xs) =$   
 $\quad \text{getPlatoonLeaderCOMx } xs) \wedge$   
 $(\forall xs \ v_{32} \ v_{31}.$   
 $\quad \text{getPlatoonLeaderCOMx } (v_{31} \text{ lte } v_{32}::xs) =$   
 $\quad \text{getPlatoonLeaderCOMx } xs) \wedge$   
 $\forall xs \ v_{34} \ v_{33}.$   
 $\quad \text{getPlatoonLeaderCOMx } (v_{33} \text{ lt } v_{34}::xs) =$   
 $\quad \text{getPlatoonLeaderCOMx } xs$

[getPlatoonLeaderCOMx\_ind]

$\vdash \forall P.$   
 $\quad P \ [] \ \wedge$

---

$(\forall \text{cmd } xs.$   
 $\quad P$   
 $\quad (\text{Name PlatoonLeader says}$   
 $\quad \quad \text{prop (SOME (PlatoonLeaderCOM cmd))::xs)) \wedge$   
 $(\forall xs. P \ xs \Rightarrow P \ (\text{TT::xs})) \wedge (\forall xs. P \ xs \Rightarrow P \ (\text{FF::xs})) \wedge$   
 $(\forall v_2 \ xs. P \ xs \Rightarrow P \ (\text{prop } v_2::xs)) \wedge$   
 $(\forall v_3 \ xs. P \ xs \Rightarrow P \ (\text{notf } v_3::xs)) \wedge$   
 $(\forall v_4 \ v_5 \ xs. P \ xs \Rightarrow P \ (v_4 \ \text{andf } v_5::xs)) \wedge$   
 $(\forall v_6 \ v_7 \ xs. P \ xs \Rightarrow P \ (v_6 \ \text{orf } v_7::xs)) \wedge$   
 $(\forall v_8 \ v_9 \ xs. P \ xs \Rightarrow P \ (v_8 \ \text{impf } v_9::xs)) \wedge$   
 $(\forall v_{10} \ v_{11} \ xs. P \ xs \Rightarrow P \ (v_{10} \ \text{eqf } v_{11}::xs)) \wedge$   
 $(\forall v_{12} \ xs. P \ xs \Rightarrow P \ (v_{12} \ \text{says TT::xs})) \wedge$   
 $(\forall v_{12} \ xs. P \ xs \Rightarrow P \ (v_{12} \ \text{says FF::xs})) \wedge$   
 $(\forall v_{134} \ xs. P \ xs \Rightarrow P \ (\text{Name } v_{134} \ \text{says prop NONE::xs})) \wedge$   
 $(\forall v_{147} \ xs.$   
 $\quad P \ xs \Rightarrow$   
 $\quad P$   
 $\quad (\text{Name PlatoonLeader says prop (SOME (OmniCOM } v_{147}))::$   
 $\quad \quad xs)) \wedge$   
 $(\forall v_{144} \ xs.$   
 $\quad P \ xs \Rightarrow P \ (\text{Name Omni says prop (SOME } v_{144}))::xs)) \wedge$   
 $(\forall v_{135} \ v_{136} \ v_{68} \ xs.$   
 $\quad P \ xs \Rightarrow P \ (v_{135} \ \text{meet } v_{136} \ \text{says prop } v_{68}::xs)) \wedge$   
 $(\forall v_{137} \ v_{138} \ v_{68} \ xs.$   
 $\quad P \ xs \Rightarrow P \ (v_{137} \ \text{quoting } v_{138} \ \text{says prop } v_{68}::xs)) \wedge$   
 $(\forall v_{12} \ v_{69} \ xs. P \ xs \Rightarrow P \ (v_{12} \ \text{says notf } v_{69}::xs)) \wedge$   
 $(\forall v_{12} \ v_{70} \ v_{71} \ xs. P \ xs \Rightarrow P \ (v_{12} \ \text{says } (v_{70} \ \text{andf } v_{71})::xs)) \wedge$   
 $(\forall v_{12} \ v_{72} \ v_{73} \ xs. P \ xs \Rightarrow P \ (v_{12} \ \text{says } (v_{72} \ \text{orf } v_{73})::xs)) \wedge$   
 $(\forall v_{12} \ v_{74} \ v_{75} \ xs. P \ xs \Rightarrow P \ (v_{12} \ \text{says } (v_{74} \ \text{impf } v_{75})::xs)) \wedge$   
 $(\forall v_{12} \ v_{76} \ v_{77} \ xs. P \ xs \Rightarrow P \ (v_{12} \ \text{says } (v_{76} \ \text{eqf } v_{77})::xs)) \wedge$   
 $(\forall v_{12} \ v_{78} \ v_{79} \ xs. P \ xs \Rightarrow P \ (v_{12} \ \text{says } v_{78} \ \text{says } v_{79}::xs)) \wedge$   
 $(\forall v_{12} \ v_{80} \ v_{81} \ xs.$   
 $\quad P \ xs \Rightarrow P \ (v_{12} \ \text{says } v_{80} \ \text{speaks\_for } v_{81}::xs)) \wedge$   
 $(\forall v_{12} \ v_{82} \ v_{83} \ xs.$   
 $\quad P \ xs \Rightarrow P \ (v_{12} \ \text{says } v_{82} \ \text{controls } v_{83}::xs)) \wedge$   
 $(\forall v_{12} \ v_{84} \ v_{85} \ v_{86} \ xs.$   
 $\quad P \ xs \Rightarrow P \ (v_{12} \ \text{says reps } v_{84} \ v_{85} \ v_{86}::xs)) \wedge$   
 $(\forall v_{12} \ v_{87} \ v_{88} \ xs. P \ xs \Rightarrow P \ (v_{12} \ \text{says } v_{87} \ \text{domi } v_{88}::xs)) \wedge$   
 $(\forall v_{12} \ v_{89} \ v_{90} \ xs. P \ xs \Rightarrow P \ (v_{12} \ \text{says } v_{89} \ \text{eqi } v_{90}::xs)) \wedge$   
 $(\forall v_{12} \ v_{91} \ v_{92} \ xs. P \ xs \Rightarrow P \ (v_{12} \ \text{says } v_{91} \ \text{doms } v_{92}::xs)) \wedge$   
 $(\forall v_{12} \ v_{93} \ v_{94} \ xs. P \ xs \Rightarrow P \ (v_{12} \ \text{says } v_{93} \ \text{eqs } v_{94}::xs)) \wedge$   
 $(\forall v_{12} \ v_{95} \ v_{96} \ xs. P \ xs \Rightarrow P \ (v_{12} \ \text{says } v_{95} \ \text{eqn } v_{96}::xs)) \wedge$   
 $(\forall v_{12} \ v_{97} \ v_{98} \ xs. P \ xs \Rightarrow P \ (v_{12} \ \text{says } v_{97} \ \text{lte } v_{98}::xs)) \wedge$   
 $(\forall v_{12} \ v_{99} \ v_{100} \ xs. P \ xs \Rightarrow P \ (v_{12} \ \text{says } v_{99} \ \text{lt } v_{100}::xs)) \wedge$   
 $(\forall v_{14} \ v_{15} \ xs. P \ xs \Rightarrow P \ (v_{14} \ \text{speaks\_for } v_{15}::xs)) \wedge$   
 $(\forall v_{16} \ v_{17} \ xs. P \ xs \Rightarrow P \ (v_{16} \ \text{controls } v_{17}::xs)) \wedge$   
 $(\forall v_{18} \ v_{19} \ v_{20} \ xs. P \ xs \Rightarrow P \ (\text{reps } v_{18} \ v_{19} \ v_{20}::xs)) \wedge$   
 $(\forall v_{21} \ v_{22} \ xs. P \ xs \Rightarrow P \ (v_{21} \ \text{domi } v_{22}::xs)) \wedge$   
 $(\forall v_{23} \ v_{24} \ xs. P \ xs \Rightarrow P \ (v_{23} \ \text{eqi } v_{24}::xs)) \wedge$

---

$$\begin{aligned}
& (\forall v_{25} v_{26} xs. P xs \Rightarrow P (v_{25} \text{ doms } v_{26} :: xs)) \wedge \\
& (\forall v_{27} v_{28} xs. P xs \Rightarrow P (v_{27} \text{ eqs } v_{28} :: xs)) \wedge \\
& (\forall v_{29} v_{30} xs. P xs \Rightarrow P (v_{29} \text{ eqn } v_{30} :: xs)) \wedge \\
& (\forall v_{31} v_{32} xs. P xs \Rightarrow P (v_{31} \text{ lte } v_{32} :: xs)) \wedge \\
& (\forall v_{33} v_{34} xs. P xs \Rightarrow P (v_{33} \text{ lt } v_{34} :: xs)) \Rightarrow \\
& \forall v. P v
\end{aligned}$$

### 3 projectSM Theory

**Built:** 27 December 2018

**Parent Theories:** projectUtilities, ssm

#### 3.1 Theorems

[NOut\_def]

```

⊢ (NOut MOVE_TO_PB (exec x) =
  if getPlatoonLeaderCOM x = SOME (PlatoonLeaderCOM form) then
    Form
  else NoActionTaken) ∧
(NOut FORM (exec x) =
  if getPlatoonLeaderCOM x = SOME (PlatoonLeaderCOM move) then
    Move
  else NoActionTaken) ∧
(NOut MOVE (exec x) =
  if
    getPlatoonLeaderCOM x = SOME (PlatoonLeaderCOM secureHalt)
  then
    Secure_halt
  else NoActionTaken) ∧ (NOut s (trap v0) = Unauthorized) ∧
(NOut s (discard v1) = UnAuthenticated)

```

[NOut\_ind]

```

⊢ ∀ P.
  (∀ x. P MOVE_TO_PB (exec x)) ∧ (∀ x. P FORM (exec x)) ∧
  (∀ x. P MOVE (exec x)) ∧ (∀ s v0. P s (trap v0)) ∧
  (∀ s v1. P s (discard v1)) ∧
  (∀ v6. P SECURE_HALT (exec v6)) ⇒
  ∀ v v1. P v v1

```

[NS\_def]

```

⊢ (NS MOVE_TO_PB (exec x) =
  if getPlatoonLeaderCOM x = SOME (PlatoonLeaderCOM form) then
    FORM
  else MOVE_TO_PB) ∧
(NS FORM (exec x) =
  if getPlatoonLeaderCOM x = SOME (PlatoonLeaderCOM move) then
    MOVE

```

```

else FORM)  $\wedge$ 
(NS MOVE (exec  $x$ ) =
  if
    getPlatoonLeaderCOM  $x$  = SOME (PlatoonLeaderCOM secureHalt)
  then
    SECURE_HALT
  else MOVE)  $\wedge$  (NS  $s$  (trap  $v_0$ ) =  $s$ )  $\wedge$  (NS  $s$  (discard  $v_1$ ) =  $s$ )

```

[NS\_ind]

```

 $\vdash \forall P.$ 
  ( $\forall x. P$  MOVE_TO_PB (exec  $x$ ))  $\wedge$  ( $\forall x. P$  FORM (exec  $x$ ))  $\wedge$ 
  ( $\forall x. P$  MOVE (exec  $x$ ))  $\wedge$  ( $\forall s v_0. P s$  (trap  $v_0$ ))  $\wedge$ 
  ( $\forall s v_1. P s$  (discard  $v_1$ ))  $\wedge$ 
  ( $\forall v_6. P$  SECURE_HALT (exec  $v_6$ ))  $\Rightarrow$ 
   $\forall v v_1. P v v_1$ 

```

## 4 projectSecurity Theory

**Built:** 27 December 2018

**Parent Theories:** projectUtilities, ssm

### 4.1 Definitions

[globalAuth\_def]

```

 $\vdash \forall x. \text{globalAuth } x = [\text{TT}]$ 

```

[stateAuth\_def]

```

 $\vdash \forall s x.$ 
  stateAuth  $s x$  =
  if  $s = \text{MOVE\_TO\_PB}$  then
    if
      getPlatoonLeaderCOMx  $x$  = SOME (PlatoonLeaderCOM form)
    then
      [Name PlatoonLeader controls
       prop (SOME (PlatoonLeaderCOM form))]
    else [prop NONE]
  else if  $s = \text{FORM}$  then
    if
      getPlatoonLeaderCOMx  $x$  = SOME (PlatoonLeaderCOM move)
    then
      [Name PlatoonLeader controls
       prop (SOME (PlatoonLeaderCOM move))]
    else [prop NONE]
  else if  $s = \text{MOVE}$  then
    if
      getPlatoonLeaderCOMx  $x$  =
        SOME (PlatoonLeaderCOM secureHalt)

```

```

then
  [Name PlatoonLeader controls
   prop (SOME (PlatoonLeaderCOM secureHalt))]
else [prop NONE]
else [prop NONE]

```

## 4.2 Theorems

[authentication\_def]

```

⊢ (authentication
  (Name PlatoonLeader says
    prop (SOME (PlatoonLeaderCOM x')))) ⇔ T) ∧
(authentication (Name Omni says prop (SOME (OmniCOM x))) ⇔
  T) ∧ (authentication TT ⇔ F) ∧ (authentication FF ⇔ F) ∧
(authentication (prop v) ⇔ F) ∧
(authentication (notf v1) ⇔ F) ∧
(authentication (v2 andf v3) ⇔ F) ∧
(authentication (v4 orf v5) ⇔ F) ∧
(authentication (v6 impf v7) ⇔ F) ∧
(authentication (v8 eqf v9) ⇔ F) ∧
(authentication (Name v66 says TT) ⇔ F) ∧
(authentication (Name v66 says FF) ⇔ F) ∧
(authentication (Name v66 says prop NONE) ⇔ F) ∧
(authentication
  (Name Omni says prop (SOME (PlatoonLeaderCOM v144)))) ⇔
  F) ∧
(authentication
  (Name PlatoonLeader says prop (SOME (OmniCOM v145)))) ⇔
  F) ∧ (authentication (Name v66 says notf v77) ⇔ F) ∧
(authentication (Name v66 says (v78 andf v79)) ⇔ F) ∧
(authentication (Name v66 says (v80 orf v81)) ⇔ F) ∧
(authentication (Name v66 says (v82 impf v83)) ⇔ F) ∧
(authentication (Name v66 says (v84 eqf v85)) ⇔ F) ∧
(authentication (Name v66 says v86 says v87) ⇔ F) ∧
(authentication (Name v66 says v88 speaks_for v89) ⇔ F) ∧
(authentication (Name v66 says v90 controls v91) ⇔ F) ∧
(authentication (Name v66 says reps v92 v93 v94) ⇔ F) ∧
(authentication (Name v66 says v95 domi v96) ⇔ F) ∧
(authentication (Name v66 says v97 eqi v98) ⇔ F) ∧
(authentication (Name v66 says v99 doms v100) ⇔ F) ∧
(authentication (Name v66 says v101 eqs v102) ⇔ F) ∧
(authentication (Name v66 says v103 eqn v104) ⇔ F) ∧
(authentication (Name v66 says v105 lte v106) ⇔ F) ∧
(authentication (Name v66 says v107 lt v108) ⇔ F) ∧
(authentication (v67 meet v68 says v11) ⇔ F) ∧
(authentication (v69 quoting v70 says v11) ⇔ F) ∧
(authentication (v12 speaks_for v13) ⇔ F) ∧
(authentication (v14 controls v15) ⇔ F) ∧
(authentication (reps v16 v17 v18) ⇔ F) ∧

```

(authentication (v<sub>19</sub> domi v<sub>20</sub>)  $\iff$  F)  $\wedge$   
 (authentication (v<sub>21</sub> eqi v<sub>22</sub>)  $\iff$  F)  $\wedge$   
 (authentication (v<sub>23</sub> doms v<sub>24</sub>)  $\iff$  F)  $\wedge$   
 (authentication (v<sub>25</sub> eqs v<sub>26</sub>)  $\iff$  F)  $\wedge$   
 (authentication (v<sub>27</sub> eqn v<sub>28</sub>)  $\iff$  F)  $\wedge$   
 (authentication (v<sub>29</sub> lte v<sub>30</sub>)  $\iff$  F)  $\wedge$   
 (authentication (v<sub>31</sub> lt v<sub>32</sub>)  $\iff$  F)

[authentication\_ind]

$\vdash \forall P.$

( $\forall x.$

$P$

(Name PlatoonLeader says

prop (SOME (PlatoonLeaderCOM x))))  $\wedge$

( $\forall x. P$  (Name Omni says prop (SOME (OmniCOM x))))  $\wedge P$  TT  $\wedge$

$P$  FF  $\wedge$  ( $\forall v. P$  (prop v))  $\wedge$  ( $\forall v_1. P$  (notf v<sub>1</sub>))  $\wedge$

( $\forall v_2 v_3. P$  (v<sub>2</sub> andf v<sub>3</sub>))  $\wedge$  ( $\forall v_4 v_5. P$  (v<sub>4</sub> orf v<sub>5</sub>))  $\wedge$

( $\forall v_6 v_7. P$  (v<sub>6</sub> impf v<sub>7</sub>))  $\wedge$  ( $\forall v_8 v_9. P$  (v<sub>8</sub> eqf v<sub>9</sub>))  $\wedge$

( $\forall v_{66}. P$  (Name v<sub>66</sub> says TT))  $\wedge$

( $\forall v_{66}. P$  (Name v<sub>66</sub> says FF))  $\wedge$

( $\forall v_{66}. P$  (Name v<sub>66</sub> says prop NONE))  $\wedge$

( $\forall v_{144}.$

$P$

(Name Omni says

prop (SOME (PlatoonLeaderCOM v<sub>144</sub>))))  $\wedge$

( $\forall v_{145}.$

$P$

(Name PlatoonLeader says

prop (SOME (OmniCOM v<sub>145</sub>))))  $\wedge$

( $\forall v_{66} v_{77}. P$  (Name v<sub>66</sub> says notf v<sub>77</sub>))  $\wedge$

( $\forall v_{66} v_{78} v_{79}. P$  (Name v<sub>66</sub> says (v<sub>78</sub> andf v<sub>79</sub>)))  $\wedge$

( $\forall v_{66} v_{80} v_{81}. P$  (Name v<sub>66</sub> says (v<sub>80</sub> orf v<sub>81</sub>)))  $\wedge$

( $\forall v_{66} v_{82} v_{83}. P$  (Name v<sub>66</sub> says (v<sub>82</sub> impf v<sub>83</sub>)))  $\wedge$

( $\forall v_{66} v_{84} v_{85}. P$  (Name v<sub>66</sub> says (v<sub>84</sub> eqf v<sub>85</sub>)))  $\wedge$

( $\forall v_{66} v_{86} v_{87}. P$  (Name v<sub>66</sub> says v<sub>86</sub> says v<sub>87</sub>))  $\wedge$

( $\forall v_{66} v_{88} v_{89}. P$  (Name v<sub>66</sub> says v<sub>88</sub> speaks\_for v<sub>89</sub>))  $\wedge$

( $\forall v_{66} v_{90} v_{91}. P$  (Name v<sub>66</sub> says v<sub>90</sub> controls v<sub>91</sub>))  $\wedge$

( $\forall v_{66} v_{92} v_{93} v_{94}. P$  (Name v<sub>66</sub> says reps v<sub>92</sub> v<sub>93</sub> v<sub>94</sub>))  $\wedge$

( $\forall v_{66} v_{95} v_{96}. P$  (Name v<sub>66</sub> says v<sub>95</sub> domi v<sub>96</sub>))  $\wedge$

( $\forall v_{66} v_{97} v_{98}. P$  (Name v<sub>66</sub> says v<sub>97</sub> eqi v<sub>98</sub>))  $\wedge$

( $\forall v_{66} v_{99} v_{100}. P$  (Name v<sub>66</sub> says v<sub>99</sub> doms v<sub>100</sub>))  $\wedge$

( $\forall v_{66} v_{101} v_{102}. P$  (Name v<sub>66</sub> says v<sub>101</sub> eqs v<sub>102</sub>))  $\wedge$

( $\forall v_{66} v_{103} v_{104}. P$  (Name v<sub>66</sub> says v<sub>103</sub> eqn v<sub>104</sub>))  $\wedge$

( $\forall v_{66} v_{105} v_{106}. P$  (Name v<sub>66</sub> says v<sub>105</sub> lte v<sub>106</sub>))  $\wedge$

( $\forall v_{66} v_{107} v_{108}. P$  (Name v<sub>66</sub> says v<sub>107</sub> lt v<sub>108</sub>))  $\wedge$

( $\forall v_{67} v_{68} v_{11}. P$  (v<sub>67</sub> meet v<sub>68</sub> says v<sub>11</sub>))  $\wedge$

( $\forall v_{69} v_{70} v_{11}. P$  (v<sub>69</sub> quoting v<sub>70</sub> says v<sub>11</sub>))  $\wedge$

( $\forall v_{12} v_{13}. P$  (v<sub>12</sub> speaks\_for v<sub>13</sub>))  $\wedge$

( $\forall v_{14} v_{15}. P$  (v<sub>14</sub> controls v<sub>15</sub>))  $\wedge$

$$\begin{aligned}
& (\forall v_{16} v_{17} v_{18}. P (\text{reps } v_{16} v_{17} v_{18})) \wedge \\
& (\forall v_{19} v_{20}. P (v_{19} \text{ domi } v_{20})) \wedge \\
& (\forall v_{21} v_{22}. P (v_{21} \text{ eqi } v_{22})) \wedge \\
& (\forall v_{23} v_{24}. P (v_{23} \text{ doms } v_{24})) \wedge \\
& (\forall v_{25} v_{26}. P (v_{25} \text{ eqs } v_{26})) \wedge (\forall v_{27} v_{28}. P (v_{27} \text{ eqn } v_{28})) \wedge \\
& (\forall v_{29} v_{30}. P (v_{29} \text{ lte } v_{30})) \wedge (\forall v_{31} v_{32}. P (v_{31} \text{ lt } v_{32})) \Rightarrow \\
& \forall v. P v
\end{aligned}$$

## 5 projectAssuranceExec Theory

**Built:** 27 December 2018

**Parent Theories:** projectSecurity

### 5.1 Theorems

[FORM\_exec\_move\_lemma1]

$$\begin{aligned}
& \vdash \forall M \text{ } Oi \text{ } Os. \\
& \quad \text{CFGInterpret } (M, Oi, Os) \\
& \quad \quad (\text{CFG authentication stateAuth globalAuth} \\
& \quad \quad \quad ([\text{Name PlatoonLeader says} \\
& \quad \quad \quad \quad \text{prop (SOME (PlatoonLeaderCOM move))}]::ins) \text{ FORM} \\
& \quad \quad \quad outs) \Rightarrow \\
& \quad (M, Oi, Os) \text{ satList} \\
& \quad \text{propCommandList} \\
& \quad \quad [\text{Name PlatoonLeader says} \\
& \quad \quad \quad \text{prop (SOME (PlatoonLeaderCOM move))}]
\end{aligned}$$

[FORM\_exec\_move\_lemma2]

$$\begin{aligned}
& \vdash \forall NS \text{ } Out \text{ } M \text{ } Oi \text{ } Os. \\
& \quad \text{TR } (M, Oi, Os) \\
& \quad \quad (\text{exec} \\
& \quad \quad \quad (\text{inputList} \\
& \quad \quad \quad \quad [\text{Name PlatoonLeader says} \\
& \quad \quad \quad \quad \quad \text{prop (SOME (PlatoonLeaderCOM move))}])) \\
& \quad \quad (\text{CFG authentication stateAuth globalAuth} \\
& \quad \quad \quad ([\text{Name PlatoonLeader says} \\
& \quad \quad \quad \quad \text{prop (SOME (PlatoonLeaderCOM move))}]::ins) \text{ FORM} \\
& \quad \quad \quad outs) \\
& \quad \quad (\text{CFG authentication stateAuth globalAuth } ins \\
& \quad \quad \quad (NS \text{ FORM} \\
& \quad \quad \quad \quad (\text{exec} \\
& \quad \quad \quad \quad \quad (\text{inputList} \\
& \quad \quad \quad \quad \quad \quad [\text{Name PlatoonLeader says} \\
& \quad \quad \quad \quad \quad \quad \quad \text{prop (SOME (PlatoonLeaderCOM move))}])))) \\
& \quad \quad (Out \text{ FORM} \\
& \quad \quad \quad (\text{exec} \\
& \quad \quad \quad \quad (\text{inputList}
\end{aligned}$$



```

      [Name PlatoonLeader says
        prop (SOME (PlatoonLeaderCOM move))]])::
    outs))  $\iff$ 
authenticationTest authentication
  [Name PlatoonLeader says
    prop (SOME (PlatoonLeaderCOM move))]  $\wedge$ 
CFGInterpret (M, Oi, Os)
  (CFG authentication stateAuth globalAuth
    ([Name PlatoonLeader says
      prop (SOME (PlatoonLeaderCOM move))]::ins) FORM
    outs)  $\wedge$ 
  (M, Oi, Os) satList
propCommandList
  [Name PlatoonLeader says
    prop (SOME (PlatoonLeaderCOM move))]

```

[FORM\_exec\_move\_thm]

```

 $\vdash \forall NS \text{ Out } M \text{ Oi } Os.$ 
  TR (M, Oi, Os) (exec [SOME (PlatoonLeaderCOM move)])
    (CFG authentication stateAuth globalAuth
      ([Name PlatoonLeader says
        prop (SOME (PlatoonLeaderCOM move))]::ins) FORM
      outs)
    (CFG authentication stateAuth globalAuth ins
      (NS FORM (exec [SOME (PlatoonLeaderCOM move)]))
      (Out FORM (exec [SOME (PlatoonLeaderCOM move))]::
        outs))  $\iff$ 
authenticationTest authentication
  [Name PlatoonLeader says
    prop (SOME (PlatoonLeaderCOM move))]  $\wedge$ 
CFGInterpret (M, Oi, Os)
  (CFG authentication stateAuth globalAuth
    ([Name PlatoonLeader says
      prop (SOME (PlatoonLeaderCOM move))]::ins) FORM
    outs)  $\wedge$ 
  (M, Oi, Os) satList [prop (SOME (PlatoonLeaderCOM move))]

```

[MOVE\_exec\_secureHalt\_lemma1]

```

 $\vdash \forall M \text{ Oi } Os.$ 
  CFGInterpret (M, Oi, Os)
    (CFG authentication stateAuth globalAuth
      ([Name PlatoonLeader says
        prop (SOME (PlatoonLeaderCOM secureHalt))]::ins)
      MOVE outs)  $\Rightarrow$ 
  (M, Oi, Os) satList
propCommandList
  [Name PlatoonLeader says
    prop (SOME (PlatoonLeaderCOM secureHalt))]

```

**[MOVE\_exec\_secureHalt\_lemma2]**

$\vdash \forall NS \text{ Out } M \text{ } Oi \text{ } Os.$   
 $TR \ (M, Oi, Os)$   
 $(exec$   
 $\quad (inputList$   
 $\quad \quad [Name \ PlatoonLeader \ says$   
 $\quad \quad \quad prop \ (SOME \ (PlatoonLeaderCOM \ secureHalt))])])$   
 $(CFG \ authentication \ stateAuth \ globalAuth$   
 $\quad ([Name \ PlatoonLeader \ says$   
 $\quad \quad prop \ (SOME \ (PlatoonLeaderCOM \ secureHalt))]::ins)$   
 $\quad MOVE \ outs)$   
 $(CFG \ authentication \ stateAuth \ globalAuth \ ins$   
 $\quad (NS \ MOVE$   
 $\quad \quad (exec$   
 $\quad \quad \quad (inputList$   
 $\quad \quad \quad \quad [Name \ PlatoonLeader \ says$   
 $\quad \quad \quad \quad \quad prop$   
 $\quad \quad \quad \quad \quad \quad (SOME \ (PlatoonLeaderCOM \ secureHalt))])])$   
 $\quad \quad (Out \ MOVE$   
 $\quad \quad \quad (exec$   
 $\quad \quad \quad \quad (inputList$   
 $\quad \quad \quad \quad \quad [Name \ PlatoonLeader \ says$   
 $\quad \quad \quad \quad \quad \quad prop$   
 $\quad \quad \quad \quad \quad \quad \quad (SOME \ (PlatoonLeaderCOM \ secureHalt))])])::$   
 $\quad \quad \quad outs)) \iff$   
 $authenticationTest \ authentication$   
 $\quad [Name \ PlatoonLeader \ says$   
 $\quad \quad prop \ (SOME \ (PlatoonLeaderCOM \ secureHalt))] \wedge$   
 $CFGInterpret \ (M, Oi, Os)$   
 $\quad (CFG \ authentication \ stateAuth \ globalAuth$   
 $\quad \quad ([Name \ PlatoonLeader \ says$   
 $\quad \quad \quad prop \ (SOME \ (PlatoonLeaderCOM \ secureHalt))]::ins)$   
 $\quad \quad MOVE \ outs) \wedge$   
 $(M, Oi, Os) \ satList$   
 $propCommandList$   
 $\quad [Name \ PlatoonLeader \ says$   
 $\quad \quad prop \ (SOME \ (PlatoonLeaderCOM \ secureHalt))]$

**[MOVE\_exec\_secureHalt\_thm]**

$\vdash \forall NS \text{ Out } M \text{ } Oi \text{ } Os.$   
 $TR \ (M, Oi, Os) \ (exec \ [SOME \ (PlatoonLeaderCOM \ secureHalt)])$   
 $(CFG \ authentication \ stateAuth \ globalAuth$   
 $\quad ([Name \ PlatoonLeader \ says$   
 $\quad \quad prop \ (SOME \ (PlatoonLeaderCOM \ secureHalt))]::ins)$   
 $\quad MOVE \ outs)$   
 $(CFG \ authentication \ stateAuth \ globalAuth \ ins$   
 $\quad (NS \ MOVE \ (exec \ [SOME \ (PlatoonLeaderCOM \ secureHalt)]))$   
 $\quad (Out \ MOVE$   
 $\quad \quad (exec \ [SOME \ (PlatoonLeaderCOM \ secureHalt)]))::$

```

outs))  $\iff$ 
authenticationTest authentication
  [Name PlatoonLeader says
    prop (SOME (PlatoonLeaderCOM secureHalt))]]  $\wedge$ 
CFGInterpret (M, Oi, Os)
  (CFG authentication stateAuth globalAuth
    ([Name PlatoonLeader says
      prop (SOME (PlatoonLeaderCOM secureHalt))]]::ins)
    MOVE outs)  $\wedge$ 
(M, Oi, Os) satList
[prop (SOME (PlatoonLeaderCOM secureHalt))]]

```

[MOVE\_TO\_PB\_exec\_form\_lemma1]

```

 $\vdash \forall M \text{ } Oi \text{ } Os.$ 
CFGInterpret (M, Oi, Os)
  (CFG authentication stateAuth globalAuth
    ([Name PlatoonLeader says
      prop (SOME (PlatoonLeaderCOM form))]]::ins)
    MOVE_TO_PB outs)  $\Rightarrow$ 
(M, Oi, Os) satList
propCommandList
  [Name PlatoonLeader says
    prop (SOME (PlatoonLeaderCOM form))]]

```

[MOVE\_TO\_PB\_exec\_form\_lemma2]

```

 $\vdash \forall NS \text{ } Out \text{ } M \text{ } Oi \text{ } Os.$ 
TR (M, Oi, Os)
  (exec
    (inputList
      [Name PlatoonLeader says
        prop (SOME (PlatoonLeaderCOM form))]))
  (CFG authentication stateAuth globalAuth
    ([Name PlatoonLeader says
      prop (SOME (PlatoonLeaderCOM form))]]::ins)
    MOVE_TO_PB outs)
  (CFG authentication stateAuth globalAuth ins
    (NS MOVE_TO_PB
      (exec
        (inputList
          [Name PlatoonLeader says
            prop (SOME (PlatoonLeaderCOM form))]))))
  (Out MOVE_TO_PB
    (exec
      (inputList
        [Name PlatoonLeader says
          prop (SOME (PlatoonLeaderCOM form))]))::
      outs))  $\iff$ 
authenticationTest authentication
  [Name PlatoonLeader says

```

```

    prop (SOME (PlatoonLeaderCOM form))] ∧
CFGInterpret (M, Oi, Os)
  (CFG authentication stateAuth globalAuth
    ([Name PlatoonLeader says
      prop (SOME (PlatoonLeaderCOM form))]::ins)
    MOVE_TO_PB outs) ∧
(M, Oi, Os) satList
propCommandList
  [Name PlatoonLeader says
    prop (SOME (PlatoonLeaderCOM form))]
[MOVE_TO_PB_exec_form_thm]
⊢ ∀ NS Out M Oi Os.
  TR (M, Oi, Os) (exec [SOME (PlatoonLeaderCOM form)])
  (CFG authentication stateAuth globalAuth
    ([Name PlatoonLeader says
      prop (SOME (PlatoonLeaderCOM form))]::ins)
    MOVE_TO_PB outs)
  (CFG authentication stateAuth globalAuth ins
    (NS MOVE_TO_PB (exec [SOME (PlatoonLeaderCOM form)])))
  (Out MOVE_TO_PB
    (exec [SOME (PlatoonLeaderCOM form))]::outs)) ⇔
authenticationTest authentication
  [Name PlatoonLeader says
    prop (SOME (PlatoonLeaderCOM form))] ∧
CFGInterpret (M, Oi, Os)
  (CFG authentication stateAuth globalAuth
    ([Name PlatoonLeader says
      prop (SOME (PlatoonLeaderCOM form))]::ins)
    MOVE_TO_PB outs) ∧
(M, Oi, Os) satList [prop (SOME (PlatoonLeaderCOM form))]

```

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