

Contents

1	projectTypes Theory	3
1.1	Datatypes	3
1.2	Theorems	3
2	projectUtilities Theory	4
2.1	Theorems	4
3	projectSM Theory	18
3.1	Theorems	18
4	projectSecurity Theory	19
4.1	Definitions	20
4.2	Theorems	20
5	projectAssuranceExec Theory	23
5.1	Theorems	23

1 projectTypes Theory

Built: 27 December 2018

Parent Theories: indexedLists, patternMatches

1.1 Datatypes

```
commands =  
  PlatoonLeaderCOM platoonLeaderCom  
  | PlatoonSergeantCOM platoonSergeantCom  
  | OmniCOM omniCom  
  
omniCom = none | omniNA  
  
output = Secure | Withdraw | Complete | ActionsIn  
        | NoActionTaken | UnAuthenticated | Unauthorized  
  
platoonLeaderCom = secure | withdraw | complete  
  
platoonSergeantCom = actionsIn | psgNA  
  
principal = PlatoonLeader | PlatoonSergeant | Omni  
  
state = CONDUCT_PB | SECURE | ACTIONS_IN | WITHDRAW | COMPLETE
```

1.2 Theorems

[commands_distinct_clauses]

$$\vdash (\forall a' a. \text{PlatoonLeaderCOM } a \neq \text{PlatoonSergeantCOM } a') \wedge$$
$$(\forall a' a. \text{PlatoonLeaderCOM } a \neq \text{OmniCOM } a') \wedge$$
$$\forall a' a. \text{PlatoonSergeantCOM } a \neq \text{OmniCOM } a'$$

[commands_one_one]

$$\vdash (\forall a a'.$$
$$(\text{PlatoonLeaderCOM } a = \text{PlatoonLeaderCOM } a') \iff (a = a')) \wedge$$
$$(\forall a a'.$$
$$(\text{PlatoonSergeantCOM } a = \text{PlatoonSergeantCOM } a') \iff$$
$$(a = a')) \wedge \forall a a'. (\text{OmniCOM } a = \text{OmniCOM } a') \iff (a = a')$$

[omniCom_distinct_clauses]

$$\vdash \text{none} \neq \text{omniNA}$$

[output_distinct_clauses]

$\vdash \text{Secure} \neq \text{Withdraw} \wedge \text{Secure} \neq \text{Complete} \wedge \text{Secure} \neq \text{ActionsIn} \wedge$
 $\text{Secure} \neq \text{NoActionTaken} \wedge \text{Secure} \neq \text{UnAuthenticated} \wedge$
 $\text{Secure} \neq \text{Unauthorized} \wedge \text{Withdraw} \neq \text{Complete} \wedge$
 $\text{Withdraw} \neq \text{ActionsIn} \wedge \text{Withdraw} \neq \text{NoActionTaken} \wedge$
 $\text{Withdraw} \neq \text{UnAuthenticated} \wedge \text{Withdraw} \neq \text{Unauthorized} \wedge$
 $\text{Complete} \neq \text{ActionsIn} \wedge \text{Complete} \neq \text{NoActionTaken} \wedge$
 $\text{Complete} \neq \text{UnAuthenticated} \wedge \text{Complete} \neq \text{Unauthorized} \wedge$
 $\text{ActionsIn} \neq \text{NoActionTaken} \wedge \text{ActionsIn} \neq \text{UnAuthenticated} \wedge$
 $\text{ActionsIn} \neq \text{Unauthorized} \wedge \text{NoActionTaken} \neq \text{UnAuthenticated} \wedge$
 $\text{NoActionTaken} \neq \text{Unauthorized} \wedge \text{UnAuthenticated} \neq \text{Unauthorized}$

[platoonLeaderCom_distinct_clauses]

$\vdash \text{secure} \neq \text{withdraw} \wedge \text{secure} \neq \text{complete} \wedge \text{withdraw} \neq \text{complete}$

[platoonSergeantCom_distinct_clauses]

$\vdash \text{actionsIn} \neq \text{psgNA}$

[principal_distinct_clauses]

$\vdash \text{PlatoonLeader} \neq \text{PlatoonSergeant} \wedge \text{PlatoonLeader} \neq \text{Omni} \wedge$
 $\text{PlatoonSergeant} \neq \text{Omni}$

[state_distinct_clauses]

$\vdash \text{CONDUCT_PB} \neq \text{SECURE} \wedge \text{CONDUCT_PB} \neq \text{ACTIONS_IN} \wedge$
 $\text{CONDUCT_PB} \neq \text{WITHDRAW} \wedge \text{CONDUCT_PB} \neq \text{COMPLETE} \wedge$
 $\text{SECURE} \neq \text{ACTIONS_IN} \wedge \text{SECURE} \neq \text{WITHDRAW} \wedge \text{SECURE} \neq \text{COMPLETE} \wedge$
 $\text{ACTIONS_IN} \neq \text{WITHDRAW} \wedge \text{ACTIONS_IN} \neq \text{COMPLETE} \wedge$
 $\text{WITHDRAW} \neq \text{COMPLETE}$

2 projectUtilities Theory

Built: 27 December 2018

Parent Theories: projectTypes, satList

2.1 Theorems

[getOmniCOM_def]

$\vdash (\text{getOmniCOM } [] = \text{NONE}) \wedge$
 $(\forall xs \text{ cmd.}$
 $\quad \text{getOmniCOM (SOME (OmniCOM cmd))::xs} =$
 $\quad \text{SOME (OmniCOM cmd)}) \wedge$
 $(\forall xs. \text{getOmniCOM (NONE::xs)} = \text{getOmniCOM xs}) \wedge$
 $(\forall xs \ v_4.$
 $\quad \text{getOmniCOM (SOME (PlatoonLeaderCOM } v_4)\text{)::xs} =$
 $\quad \text{getOmniCOM xs}) \wedge$
 $\forall xs \ v_5.$
 $\quad \text{getOmniCOM (SOME (PlatoonSergeantCOM } v_5)\text{)::xs} =$
 $\quad \text{getOmniCOM xs}$

[getOmniCOM_ind]

$\vdash \forall P.$
 $P [] \wedge (\forall cmd\ xs. P (SOME (OmniCOM\ cmd)::xs)) \wedge$
 $(\forall xs. P\ xs \Rightarrow P (NONE::xs)) \wedge$
 $(\forall v_4\ xs. P\ xs \Rightarrow P (SOME (PlatoonLeaderCOM\ v_4)::xs)) \wedge$
 $(\forall v_5\ xs. P\ xs \Rightarrow P (SOME (PlatoonSergeantCOM\ v_5)::xs)) \Rightarrow$
 $\forall v. P\ v$

[getOmniCOMx_def]

$\vdash (getOmniCOMx\ [] = NONE) \wedge$
 $(\forall xs\ cmd.$
 $getOmniCOMx$
 $(Name\ Omni\ says\ prop\ (SOME\ (OmniCOM\ cmd)::xs) =$
 $SOME\ (OmniCOM\ cmd)) \wedge$
 $(\forall xs. getOmniCOMx\ (TT::xs) = getOmniCOMx\ xs) \wedge$
 $(\forall xs. getOmniCOMx\ (FF::xs) = getOmniCOMx\ xs) \wedge$
 $(\forall xs\ v_2. getOmniCOMx\ (prop\ v_2::xs) = getOmniCOMx\ xs) \wedge$
 $(\forall xs\ v_3. getOmniCOMx\ (notf\ v_3::xs) = getOmniCOMx\ xs) \wedge$
 $(\forall xs\ v_5\ v_4. getOmniCOMx\ (v_4\ andf\ v_5::xs) = getOmniCOMx\ xs) \wedge$
 $(\forall xs\ v_7\ v_6. getOmniCOMx\ (v_6\ orf\ v_7::xs) = getOmniCOMx\ xs) \wedge$
 $(\forall xs\ v_9\ v_8. getOmniCOMx\ (v_8\ impf\ v_9::xs) = getOmniCOMx\ xs) \wedge$
 $(\forall xs\ v_{11}\ v_{10}.$
 $getOmniCOMx\ (v_{10}\ eqf\ v_{11}::xs) = getOmniCOMx\ xs) \wedge$
 $(\forall xs\ v_{12}. getOmniCOMx\ (v_{12}\ says\ TT::xs) = getOmniCOMx\ xs) \wedge$
 $(\forall xs\ v_{12}. getOmniCOMx\ (v_{12}\ says\ FF::xs) = getOmniCOMx\ xs) \wedge$
 $(\forall xs\ v_{134}.$
 $getOmniCOMx\ (Name\ v_{134}\ says\ prop\ NONE::xs) =$
 $getOmniCOMx\ xs) \wedge$
 $(\forall xs\ v_{144}.$
 $getOmniCOMx$
 $(Name\ PlatoonLeader\ says\ prop\ (SOME\ v_{144}::xs) =$
 $getOmniCOMx\ xs) \wedge$
 $(\forall xs\ v_{144}.$
 $getOmniCOMx$
 $(Name\ PlatoonSergeant\ says\ prop\ (SOME\ v_{144}::xs) =$
 $getOmniCOMx\ xs) \wedge$
 $(\forall xs\ v_{146}.$
 $getOmniCOMx$
 $(Name\ Omni\ says\ prop\ (SOME\ (PlatoonLeaderCOM\ v_{146}))::$
 $xs) =$
 $getOmniCOMx\ xs) \wedge$
 $(\forall xs\ v_{147}.$
 $getOmniCOMx$
 $(Name\ Omni\ says\ prop\ (SOME\ (PlatoonSergeantCOM\ v_{147}))::$
 $xs) =$
 $getOmniCOMx\ xs) \wedge$
 $(\forall xs\ v_{68}\ v_{136}\ v_{135}.$
 $getOmniCOMx\ (v_{135}\ meet\ v_{136}\ says\ prop\ v_{68}::xs) =$
 $getOmniCOMx\ xs) \wedge$

```

(∀ xs v68 v138 v137.
  getOmniCOMx (v137 quoting v138 says prop v68::xs) =
  getOmniCOMx xs) ∧
(∀ xs v69 v12.
  getOmniCOMx (v12 says notf v69::xs) = getOmniCOMx xs) ∧
(∀ xs v71 v70 v12.
  getOmniCOMx (v12 says (v70 andf v71)::xs) =
  getOmniCOMx xs) ∧
(∀ xs v73 v72 v12.
  getOmniCOMx (v12 says (v72 orf v73)::xs) =
  getOmniCOMx xs) ∧
(∀ xs v75 v74 v12.
  getOmniCOMx (v12 says (v74 impf v75)::xs) =
  getOmniCOMx xs) ∧
(∀ xs v77 v76 v12.
  getOmniCOMx (v12 says (v76 eqf v77)::xs) =
  getOmniCOMx xs) ∧
(∀ xs v79 v78 v12.
  getOmniCOMx (v12 says v78 says v79::xs) =
  getOmniCOMx xs) ∧
(∀ xs v81 v80 v12.
  getOmniCOMx (v12 says v80 speaks_for v81::xs) =
  getOmniCOMx xs) ∧
(∀ xs v83 v82 v12.
  getOmniCOMx (v12 says v82 controls v83::xs) =
  getOmniCOMx xs) ∧
(∀ xs v86 v85 v84 v12.
  getOmniCOMx (v12 says reps v84 v85 v86::xs) =
  getOmniCOMx xs) ∧
(∀ xs v88 v87 v12.
  getOmniCOMx (v12 says v87 domi v88::xs) =
  getOmniCOMx xs) ∧
(∀ xs v90 v89 v12.
  getOmniCOMx (v12 says v89 eqi v90::xs) = getOmniCOMx xs) ∧
(∀ xs v92 v91 v12.
  getOmniCOMx (v12 says v91 doms v92::xs) =
  getOmniCOMx xs) ∧
(∀ xs v94 v93 v12.
  getOmniCOMx (v12 says v93 eqs v94::xs) = getOmniCOMx xs) ∧
(∀ xs v96 v95 v12.
  getOmniCOMx (v12 says v95 eqn v96::xs) = getOmniCOMx xs) ∧
(∀ xs v98 v97 v12.
  getOmniCOMx (v12 says v97 lte v98::xs) = getOmniCOMx xs) ∧
(∀ xs v99 v12 v100.
  getOmniCOMx (v12 says v99 lt v100::xs) = getOmniCOMx xs) ∧
(∀ xs v15 v14.
  getOmniCOMx (v14 speaks_for v15::xs) = getOmniCOMx xs) ∧
(∀ xs v17 v16.
  getOmniCOMx (v16 controls v17::xs) = getOmniCOMx xs) ∧

```

$(\forall xs \ v_{20} \ v_{19} \ v_{18}.$
 $\quad \text{getOmniCOMx} (\text{reps } v_{18} \ v_{19} \ v_{20} :: xs) = \text{getOmniCOMx } xs) \wedge$
 $(\forall xs \ v_{22} \ v_{21}.$
 $\quad \text{getOmniCOMx} (v_{21} \text{ domi } v_{22} :: xs) = \text{getOmniCOMx } xs) \wedge$
 $(\forall xs \ v_{24} \ v_{23}.$
 $\quad \text{getOmniCOMx} (v_{23} \text{ eqi } v_{24} :: xs) = \text{getOmniCOMx } xs) \wedge$
 $(\forall xs \ v_{26} \ v_{25}.$
 $\quad \text{getOmniCOMx} (v_{25} \text{ doms } v_{26} :: xs) = \text{getOmniCOMx } xs) \wedge$
 $(\forall xs \ v_{28} \ v_{27}.$
 $\quad \text{getOmniCOMx} (v_{27} \text{ eqs } v_{28} :: xs) = \text{getOmniCOMx } xs) \wedge$
 $(\forall xs \ v_{30} \ v_{29}.$
 $\quad \text{getOmniCOMx} (v_{29} \text{ eqn } v_{30} :: xs) = \text{getOmniCOMx } xs) \wedge$
 $(\forall xs \ v_{32} \ v_{31}.$
 $\quad \text{getOmniCOMx} (v_{31} \text{ lte } v_{32} :: xs) = \text{getOmniCOMx } xs) \wedge$
 $\forall xs \ v_{34} \ v_{33}. \text{getOmniCOMx} (v_{33} \text{ lt } v_{34} :: xs) = \text{getOmniCOMx } xs$

[getOmniCOMx_ind]

$\vdash \forall P.$
 $\quad P \ \square \ \wedge$
 $\quad (\forall cmd \ xs.$
 $\quad \quad P \ (\text{Name Omni says prop (SOME (OmniCOM } cmd)) :: xs)) \wedge$
 $\quad (\forall xs. P \ xs \Rightarrow P \ (\text{TT} :: xs)) \wedge (\forall xs. P \ xs \Rightarrow P \ (\text{FF} :: xs)) \wedge$
 $\quad (\forall v_2 \ xs. P \ xs \Rightarrow P \ (\text{prop } v_2 :: xs)) \wedge$
 $\quad (\forall v_3 \ xs. P \ xs \Rightarrow P \ (\text{notf } v_3 :: xs)) \wedge$
 $\quad (\forall v_4 \ v_5 \ xs. P \ xs \Rightarrow P \ (v_4 \text{ andf } v_5 :: xs)) \wedge$
 $\quad (\forall v_6 \ v_7 \ xs. P \ xs \Rightarrow P \ (v_6 \text{ orf } v_7 :: xs)) \wedge$
 $\quad (\forall v_8 \ v_9 \ xs. P \ xs \Rightarrow P \ (v_8 \text{ impf } v_9 :: xs)) \wedge$
 $\quad (\forall v_{10} \ v_{11} \ xs. P \ xs \Rightarrow P \ (v_{10} \text{ eqf } v_{11} :: xs)) \wedge$
 $\quad (\forall v_{12} \ xs. P \ xs \Rightarrow P \ (v_{12} \text{ says TT} :: xs)) \wedge$
 $\quad (\forall v_{12} \ xs. P \ xs \Rightarrow P \ (v_{12} \text{ says FF} :: xs)) \wedge$
 $\quad (\forall v_{134} \ xs. P \ xs \Rightarrow P \ (\text{Name } v_{134} \text{ says prop NONE} :: xs)) \wedge$
 $\quad (\forall v_{144} \ xs.$
 $\quad \quad P \ xs \Rightarrow$
 $\quad \quad P \ (\text{Name PlatoonLeader says prop (SOME } v_{144}) :: xs)) \wedge$
 $\quad (\forall v_{144} \ xs.$
 $\quad \quad P \ xs \Rightarrow$
 $\quad \quad P \ (\text{Name PlatoonSergeant says prop (SOME } v_{144}) :: xs)) \wedge$
 $\quad (\forall v_{146} \ xs.$
 $\quad \quad P \ xs \Rightarrow$
 $\quad \quad P$
 $\quad \quad (\text{Name Omni says prop (SOME (PlatoonLeaderCOM } v_{146})) ::$
 $\quad \quad \quad xs)) \wedge$
 $\quad (\forall v_{147} \ xs.$
 $\quad \quad P \ xs \Rightarrow$
 $\quad \quad P$
 $\quad \quad (\text{Name Omni says$
 $\quad \quad \quad \text{prop (SOME (PlatoonSergeantCOM } v_{147})) :: xs)) \wedge$
 $\quad (\forall v_{135} \ v_{136} \ v_{68} \ xs.$
 $\quad \quad P \ xs \Rightarrow P \ (v_{135} \text{ meet } v_{136} \text{ says prop } v_{68} :: xs)) \wedge$

$$\begin{aligned}
& (\forall v_{137} v_{138} v_{68} xs. \\
& \quad P xs \Rightarrow P (v_{137} \text{ quoting } v_{138} \text{ says prop } v_{68} :: xs)) \wedge \\
& (\forall v_{12} v_{69} xs. P xs \Rightarrow P (v_{12} \text{ says notf } v_{69} :: xs)) \wedge \\
& (\forall v_{12} v_{70} v_{71} xs. P xs \Rightarrow P (v_{12} \text{ says } (v_{70} \text{ andf } v_{71}) :: xs)) \wedge \\
& (\forall v_{12} v_{72} v_{73} xs. P xs \Rightarrow P (v_{12} \text{ says } (v_{72} \text{ orf } v_{73}) :: xs)) \wedge \\
& (\forall v_{12} v_{74} v_{75} xs. P xs \Rightarrow P (v_{12} \text{ says } (v_{74} \text{ impf } v_{75}) :: xs)) \wedge \\
& (\forall v_{12} v_{76} v_{77} xs. P xs \Rightarrow P (v_{12} \text{ says } (v_{76} \text{ eqf } v_{77}) :: xs)) \wedge \\
& (\forall v_{12} v_{78} v_{79} xs. P xs \Rightarrow P (v_{12} \text{ says } v_{78} \text{ says } v_{79} :: xs)) \wedge \\
& (\forall v_{12} v_{80} v_{81} xs. \\
& \quad P xs \Rightarrow P (v_{12} \text{ says } v_{80} \text{ speaks_for } v_{81} :: xs)) \wedge \\
& (\forall v_{12} v_{82} v_{83} xs. \\
& \quad P xs \Rightarrow P (v_{12} \text{ says } v_{82} \text{ controls } v_{83} :: xs)) \wedge \\
& (\forall v_{12} v_{84} v_{85} v_{86} xs. \\
& \quad P xs \Rightarrow P (v_{12} \text{ says reps } v_{84} v_{85} v_{86} :: xs)) \wedge \\
& (\forall v_{12} v_{87} v_{88} xs. P xs \Rightarrow P (v_{12} \text{ says } v_{87} \text{ domi } v_{88} :: xs)) \wedge \\
& (\forall v_{12} v_{89} v_{90} xs. P xs \Rightarrow P (v_{12} \text{ says } v_{89} \text{ eqi } v_{90} :: xs)) \wedge \\
& (\forall v_{12} v_{91} v_{92} xs. P xs \Rightarrow P (v_{12} \text{ says } v_{91} \text{ doms } v_{92} :: xs)) \wedge \\
& (\forall v_{12} v_{93} v_{94} xs. P xs \Rightarrow P (v_{12} \text{ says } v_{93} \text{ eqs } v_{94} :: xs)) \wedge \\
& (\forall v_{12} v_{95} v_{96} xs. P xs \Rightarrow P (v_{12} \text{ says } v_{95} \text{ eqn } v_{96} :: xs)) \wedge \\
& (\forall v_{12} v_{97} v_{98} xs. P xs \Rightarrow P (v_{12} \text{ says } v_{97} \text{ lte } v_{98} :: xs)) \wedge \\
& (\forall v_{12} v_{99} v_{100} xs. P xs \Rightarrow P (v_{12} \text{ says } v_{99} \text{ lt } v_{100} :: xs)) \wedge \\
& (\forall v_{14} v_{15} xs. P xs \Rightarrow P (v_{14} \text{ speaks_for } v_{15} :: xs)) \wedge \\
& (\forall v_{16} v_{17} xs. P xs \Rightarrow P (v_{16} \text{ controls } v_{17} :: xs)) \wedge \\
& (\forall v_{18} v_{19} v_{20} xs. P xs \Rightarrow P (\text{reps } v_{18} v_{19} v_{20} :: xs)) \wedge \\
& (\forall v_{21} v_{22} xs. P xs \Rightarrow P (v_{21} \text{ domi } v_{22} :: xs)) \wedge \\
& (\forall v_{23} v_{24} xs. P xs \Rightarrow P (v_{23} \text{ eqi } v_{24} :: xs)) \wedge \\
& (\forall v_{25} v_{26} xs. P xs \Rightarrow P (v_{25} \text{ doms } v_{26} :: xs)) \wedge \\
& (\forall v_{27} v_{28} xs. P xs \Rightarrow P (v_{27} \text{ eqs } v_{28} :: xs)) \wedge \\
& (\forall v_{29} v_{30} xs. P xs \Rightarrow P (v_{29} \text{ eqn } v_{30} :: xs)) \wedge \\
& (\forall v_{31} v_{32} xs. P xs \Rightarrow P (v_{31} \text{ lte } v_{32} :: xs)) \wedge \\
& (\forall v_{33} v_{34} xs. P xs \Rightarrow P (v_{33} \text{ lt } v_{34} :: xs)) \Rightarrow \\
& \forall v. P v
\end{aligned}$$

[getPlatoonLeaderCOM_def]

$$\begin{aligned}
& \vdash (\text{getPlatoonLeaderCOM } [] = \text{NONE}) \wedge \\
& (\forall xs \text{ cmd}. \\
& \quad \text{getPlatoonLeaderCOM } (\text{SOME } (\text{PlatoonLeaderCOM } \text{cmd}) :: xs) = \\
& \quad \text{SOME } (\text{PlatoonLeaderCOM } \text{cmd})) \wedge \\
& (\forall xs. \\
& \quad \text{getPlatoonLeaderCOM } (\text{NONE} :: xs) = \text{getPlatoonLeaderCOM } xs) \wedge \\
& (\forall xs \ v_5. \\
& \quad \text{getPlatoonLeaderCOM } (\text{SOME } (\text{PlatoonSergeantCOM } v_5) :: xs) = \\
& \quad \text{getPlatoonLeaderCOM } xs) \wedge \\
& \forall xs \ v_6. \\
& \quad \text{getPlatoonLeaderCOM } (\text{SOME } (\text{OmniCOM } v_6) :: xs) = \\
& \quad \text{getPlatoonLeaderCOM } xs
\end{aligned}$$

[getPlatoonLeaderCOM_ind]

$$\begin{aligned}
& \vdash \forall P. \\
& \quad P [] \wedge (\forall \text{cmd } xs. P (\text{SOME } (\text{PlatoonLeaderCOM } \text{cmd}) :: xs)) \wedge
\end{aligned}$$

$$\begin{aligned}
& (\forall xs. P \ xs \Rightarrow P \ (\text{NONE}::xs)) \wedge \\
& (\forall v_5 \ xs. P \ xs \Rightarrow P \ (\text{SOME} \ (\text{PlatoonSergeantCOM} \ v_5)::xs)) \wedge \\
& (\forall v_6 \ xs. P \ xs \Rightarrow P \ (\text{SOME} \ (\text{OmniCOM} \ v_6)::xs)) \Rightarrow \\
& \forall v. P \ v
\end{aligned}$$

[getPlatoonLeaderCOMx_def]

$$\begin{aligned}
& \vdash (\text{getPlatoonLeaderCOMx} \ [] = \text{NONE}) \wedge \\
& (\forall xs \ cmd. \\
& \quad \text{getPlatoonLeaderCOMx} \\
& \quad \quad (\text{Name PlatoonLeader says} \\
& \quad \quad \quad \text{prop} \ (\text{SOME} \ (\text{PlatoonLeaderCOM} \ cmd))::xs) = \\
& \quad \quad \text{SOME} \ (\text{PlatoonLeaderCOM} \ cmd)) \wedge \\
& (\forall xs. \\
& \quad \text{getPlatoonLeaderCOMx} \ (\text{TT}::xs) = \text{getPlatoonLeaderCOMx} \ xs) \wedge \\
& (\forall xs. \\
& \quad \text{getPlatoonLeaderCOMx} \ (\text{FF}::xs) = \text{getPlatoonLeaderCOMx} \ xs) \wedge \\
& (\forall xs \ v_2. \\
& \quad \text{getPlatoonLeaderCOMx} \ (\text{prop} \ v_2::xs) = \\
& \quad \text{getPlatoonLeaderCOMx} \ xs) \wedge \\
& (\forall xs \ v_3. \\
& \quad \text{getPlatoonLeaderCOMx} \ (\text{notf} \ v_3::xs) = \\
& \quad \text{getPlatoonLeaderCOMx} \ xs) \wedge \\
& (\forall xs \ v_5 \ v_4. \\
& \quad \text{getPlatoonLeaderCOMx} \ (v_4 \ \text{andf} \ v_5::xs) = \\
& \quad \text{getPlatoonLeaderCOMx} \ xs) \wedge \\
& (\forall xs \ v_7 \ v_6. \\
& \quad \text{getPlatoonLeaderCOMx} \ (v_6 \ \text{orf} \ v_7::xs) = \\
& \quad \text{getPlatoonLeaderCOMx} \ xs) \wedge \\
& (\forall xs \ v_9 \ v_8. \\
& \quad \text{getPlatoonLeaderCOMx} \ (v_8 \ \text{impf} \ v_9::xs) = \\
& \quad \text{getPlatoonLeaderCOMx} \ xs) \wedge \\
& (\forall xs \ v_{11} \ v_{10}. \\
& \quad \text{getPlatoonLeaderCOMx} \ (v_{10} \ \text{eqf} \ v_{11}::xs) = \\
& \quad \text{getPlatoonLeaderCOMx} \ xs) \wedge \\
& (\forall xs \ v_{12}. \\
& \quad \text{getPlatoonLeaderCOMx} \ (v_{12} \ \text{says} \ \text{TT}::xs) = \\
& \quad \text{getPlatoonLeaderCOMx} \ xs) \wedge \\
& (\forall xs \ v_{12}. \\
& \quad \text{getPlatoonLeaderCOMx} \ (v_{12} \ \text{says} \ \text{FF}::xs) = \\
& \quad \text{getPlatoonLeaderCOMx} \ xs) \wedge \\
& (\forall xs \ v_{134}. \\
& \quad \text{getPlatoonLeaderCOMx} \ (\text{Name} \ v_{134} \ \text{says} \ \text{prop} \ \text{NONE}::xs) = \\
& \quad \text{getPlatoonLeaderCOMx} \ xs) \wedge \\
& (\forall xs \ v_{147}. \\
& \quad \text{getPlatoonLeaderCOMx} \\
& \quad \quad (\text{Name PlatoonLeader says} \\
& \quad \quad \quad \text{prop} \ (\text{SOME} \ (\text{PlatoonSergeantCOM} \ v_{147}))::xs) = \\
& \quad \quad \text{getPlatoonLeaderCOMx} \ xs) \wedge \\
& (\forall xs \ v_{148}.
\end{aligned}$$

```

    getPlatoonLeaderCOMx
      (Name PlatoonLeader says prop (SOME (OmniCOM v148))::
        xs) =
    getPlatoonLeaderCOMx xs) ∧
  (∀ xs v144.
    getPlatoonLeaderCOMx
      (Name PlatoonSergeant says prop (SOME v144)::xs) =
    getPlatoonLeaderCOMx xs) ∧
  (∀ xs v144.
    getPlatoonLeaderCOMx
      (Name Omni says prop (SOME v144)::xs) =
    getPlatoonLeaderCOMx xs) ∧
  (∀ xs v68 v136 v135.
    getPlatoonLeaderCOMx (v135 meet v136 says prop v68::xs) =
    getPlatoonLeaderCOMx xs) ∧
  (∀ xs v68 v138 v137.
    getPlatoonLeaderCOMx
      (v137 quoting v138 says prop v68::xs) =
    getPlatoonLeaderCOMx xs) ∧
  (∀ xs v69 v12.
    getPlatoonLeaderCOMx (v12 says notf v69::xs) =
    getPlatoonLeaderCOMx xs) ∧
  (∀ xs v71 v70 v12.
    getPlatoonLeaderCOMx (v12 says (v70 andf v71)::xs) =
    getPlatoonLeaderCOMx xs) ∧
  (∀ xs v73 v72 v12.
    getPlatoonLeaderCOMx (v12 says (v72 orf v73)::xs) =
    getPlatoonLeaderCOMx xs) ∧
  (∀ xs v75 v74 v12.
    getPlatoonLeaderCOMx (v12 says (v74 impf v75)::xs) =
    getPlatoonLeaderCOMx xs) ∧
  (∀ xs v77 v76 v12.
    getPlatoonLeaderCOMx (v12 says (v76 eqf v77)::xs) =
    getPlatoonLeaderCOMx xs) ∧
  (∀ xs v79 v78 v12.
    getPlatoonLeaderCOMx (v12 says v78 says v79::xs) =
    getPlatoonLeaderCOMx xs) ∧
  (∀ xs v81 v80 v12.
    getPlatoonLeaderCOMx (v12 says v80 speaks_for v81::xs) =
    getPlatoonLeaderCOMx xs) ∧
  (∀ xs v83 v82 v12.
    getPlatoonLeaderCOMx (v12 says v82 controls v83::xs) =
    getPlatoonLeaderCOMx xs) ∧
  (∀ xs v86 v85 v84 v12.
    getPlatoonLeaderCOMx (v12 says reps v84 v85 v86::xs) =
    getPlatoonLeaderCOMx xs) ∧
  (∀ xs v88 v87 v12.
    getPlatoonLeaderCOMx (v12 says v87 domi v88::xs) =
    getPlatoonLeaderCOMx xs) ∧

```

$$\begin{aligned}
& (\forall xs \ v_{90} \ v_{89} \ v_{12}. \\
& \quad \text{getPlatoonLeaderCOMx } (v_{12} \text{ says } v_{89} \text{ eqi } v_{90}::xs) = \\
& \quad \text{getPlatoonLeaderCOMx } xs) \wedge \\
& (\forall xs \ v_{92} \ v_{91} \ v_{12}. \\
& \quad \text{getPlatoonLeaderCOMx } (v_{12} \text{ says } v_{91} \text{ doms } v_{92}::xs) = \\
& \quad \text{getPlatoonLeaderCOMx } xs) \wedge \\
& (\forall xs \ v_{94} \ v_{93} \ v_{12}. \\
& \quad \text{getPlatoonLeaderCOMx } (v_{12} \text{ says } v_{93} \text{ eqs } v_{94}::xs) = \\
& \quad \text{getPlatoonLeaderCOMx } xs) \wedge \\
& (\forall xs \ v_{96} \ v_{95} \ v_{12}. \\
& \quad \text{getPlatoonLeaderCOMx } (v_{12} \text{ says } v_{95} \text{ eqn } v_{96}::xs) = \\
& \quad \text{getPlatoonLeaderCOMx } xs) \wedge \\
& (\forall xs \ v_{98} \ v_{97} \ v_{12}. \\
& \quad \text{getPlatoonLeaderCOMx } (v_{12} \text{ says } v_{97} \text{ lte } v_{98}::xs) = \\
& \quad \text{getPlatoonLeaderCOMx } xs) \wedge \\
& (\forall xs \ v_{99} \ v_{12} \ v_{100}. \\
& \quad \text{getPlatoonLeaderCOMx } (v_{12} \text{ says } v_{99} \text{ lt } v_{100}::xs) = \\
& \quad \text{getPlatoonLeaderCOMx } xs) \wedge \\
& (\forall xs \ v_{15} \ v_{14}. \\
& \quad \text{getPlatoonLeaderCOMx } (v_{14} \text{ speaks_for } v_{15}::xs) = \\
& \quad \text{getPlatoonLeaderCOMx } xs) \wedge \\
& (\forall xs \ v_{17} \ v_{16}. \\
& \quad \text{getPlatoonLeaderCOMx } (v_{16} \text{ controls } v_{17}::xs) = \\
& \quad \text{getPlatoonLeaderCOMx } xs) \wedge \\
& (\forall xs \ v_{20} \ v_{19} \ v_{18}. \\
& \quad \text{getPlatoonLeaderCOMx } (\text{reps } v_{18} \ v_{19} \ v_{20}::xs) = \\
& \quad \text{getPlatoonLeaderCOMx } xs) \wedge \\
& (\forall xs \ v_{22} \ v_{21}. \\
& \quad \text{getPlatoonLeaderCOMx } (v_{21} \text{ domi } v_{22}::xs) = \\
& \quad \text{getPlatoonLeaderCOMx } xs) \wedge \\
& (\forall xs \ v_{24} \ v_{23}. \\
& \quad \text{getPlatoonLeaderCOMx } (v_{23} \text{ eqi } v_{24}::xs) = \\
& \quad \text{getPlatoonLeaderCOMx } xs) \wedge \\
& (\forall xs \ v_{26} \ v_{25}. \\
& \quad \text{getPlatoonLeaderCOMx } (v_{25} \text{ doms } v_{26}::xs) = \\
& \quad \text{getPlatoonLeaderCOMx } xs) \wedge \\
& (\forall xs \ v_{28} \ v_{27}. \\
& \quad \text{getPlatoonLeaderCOMx } (v_{27} \text{ eqs } v_{28}::xs) = \\
& \quad \text{getPlatoonLeaderCOMx } xs) \wedge \\
& (\forall xs \ v_{30} \ v_{29}. \\
& \quad \text{getPlatoonLeaderCOMx } (v_{29} \text{ eqn } v_{30}::xs) = \\
& \quad \text{getPlatoonLeaderCOMx } xs) \wedge \\
& (\forall xs \ v_{32} \ v_{31}. \\
& \quad \text{getPlatoonLeaderCOMx } (v_{31} \text{ lte } v_{32}::xs) = \\
& \quad \text{getPlatoonLeaderCOMx } xs) \wedge \\
& \forall xs \ v_{34} \ v_{33}. \\
& \quad \text{getPlatoonLeaderCOMx } (v_{33} \text{ lt } v_{34}::xs) = \\
& \quad \text{getPlatoonLeaderCOMx } xs
\end{aligned}$$

[getPlatoonLeaderCOMx_ind]

$$\begin{aligned}
& \vdash \forall P. \\
& \quad P \square \wedge \\
& \quad (\forall cmd \ xs. \\
& \quad \quad P \\
& \quad \quad \quad (\text{Name PlatoonLeader says} \\
& \quad \quad \quad \quad \text{prop (SOME (PlatoonLeaderCOM cmd))}::xs)) \wedge \\
& \quad (\forall xs. P \ xs \Rightarrow P \ (\text{TT}::xs)) \wedge (\forall xs. P \ xs \Rightarrow P \ (\text{FF}::xs)) \wedge \\
& \quad (\forall v_2 \ xs. P \ xs \Rightarrow P \ (\text{prop } v_2::xs)) \wedge \\
& \quad (\forall v_3 \ xs. P \ xs \Rightarrow P \ (\text{notf } v_3::xs)) \wedge \\
& \quad (\forall v_4 \ v_5 \ xs. P \ xs \Rightarrow P \ (v_4 \ \text{andf } v_5::xs)) \wedge \\
& \quad (\forall v_6 \ v_7 \ xs. P \ xs \Rightarrow P \ (v_6 \ \text{orf } v_7::xs)) \wedge \\
& \quad (\forall v_8 \ v_9 \ xs. P \ xs \Rightarrow P \ (v_8 \ \text{impf } v_9::xs)) \wedge \\
& \quad (\forall v_{10} \ v_{11} \ xs. P \ xs \Rightarrow P \ (v_{10} \ \text{eqf } v_{11}::xs)) \wedge \\
& \quad (\forall v_{12} \ xs. P \ xs \Rightarrow P \ (v_{12} \ \text{says TT}::xs)) \wedge \\
& \quad (\forall v_{12} \ xs. P \ xs \Rightarrow P \ (v_{12} \ \text{says FF}::xs)) \wedge \\
& \quad (\forall v_{134} \ xs. P \ xs \Rightarrow P \ (\text{Name } v_{134} \ \text{says prop NONE}::xs)) \wedge \\
& \quad (\forall v_{147} \ xs. \\
& \quad \quad P \ xs \Rightarrow \\
& \quad \quad \quad P \\
& \quad \quad \quad \quad (\text{Name PlatoonLeader says} \\
& \quad \quad \quad \quad \quad \text{prop (SOME (PlatoonSergeantCOM } v_{147}))}::xs)) \wedge \\
& \quad (\forall v_{148} \ xs. \\
& \quad \quad P \ xs \Rightarrow \\
& \quad \quad \quad P \\
& \quad \quad \quad \quad (\text{Name PlatoonLeader says prop (SOME (OmniCOM } v_{148}))}:: \\
& \quad \quad \quad \quad \quad xs)) \wedge \\
& \quad (\forall v_{144} \ xs. \\
& \quad \quad P \ xs \Rightarrow \\
& \quad \quad \quad P \ (\text{Name PlatoonSergeant says prop (SOME } v_{144})}::xs)) \wedge \\
& \quad (\forall v_{144} \ xs. \\
& \quad \quad P \ xs \Rightarrow P \ (\text{Name Omni says prop (SOME } v_{144})}::xs)) \wedge \\
& \quad (\forall v_{135} \ v_{136} \ v_{68} \ xs. \\
& \quad \quad P \ xs \Rightarrow P \ (v_{135} \ \text{meet } v_{136} \ \text{says prop } v_{68}::xs)) \wedge \\
& \quad (\forall v_{137} \ v_{138} \ v_{68} \ xs. \\
& \quad \quad P \ xs \Rightarrow P \ (v_{137} \ \text{quoting } v_{138} \ \text{says prop } v_{68}::xs)) \wedge \\
& \quad (\forall v_{12} \ v_{69} \ xs. P \ xs \Rightarrow P \ (v_{12} \ \text{says notf } v_{69}::xs)) \wedge \\
& \quad (\forall v_{12} \ v_{70} \ v_{71} \ xs. P \ xs \Rightarrow P \ (v_{12} \ \text{says (} v_{70} \ \text{andf } v_{71})}::xs)) \wedge \\
& \quad (\forall v_{12} \ v_{72} \ v_{73} \ xs. P \ xs \Rightarrow P \ (v_{12} \ \text{says (} v_{72} \ \text{orf } v_{73})}::xs)) \wedge \\
& \quad (\forall v_{12} \ v_{74} \ v_{75} \ xs. P \ xs \Rightarrow P \ (v_{12} \ \text{says (} v_{74} \ \text{impf } v_{75})}::xs)) \wedge \\
& \quad (\forall v_{12} \ v_{76} \ v_{77} \ xs. P \ xs \Rightarrow P \ (v_{12} \ \text{says (} v_{76} \ \text{eqf } v_{77})}::xs)) \wedge \\
& \quad (\forall v_{12} \ v_{78} \ v_{79} \ xs. P \ xs \Rightarrow P \ (v_{12} \ \text{says } v_{78} \ \text{says } v_{79}::xs)) \wedge \\
& \quad (\forall v_{12} \ v_{80} \ v_{81} \ xs. \\
& \quad \quad P \ xs \Rightarrow P \ (v_{12} \ \text{says } v_{80} \ \text{speaks_for } v_{81}::xs)) \wedge \\
& \quad (\forall v_{12} \ v_{82} \ v_{83} \ xs. \\
& \quad \quad P \ xs \Rightarrow P \ (v_{12} \ \text{says } v_{82} \ \text{controls } v_{83}::xs)) \wedge \\
& \quad (\forall v_{12} \ v_{84} \ v_{85} \ v_{86} \ xs. \\
& \quad \quad P \ xs \Rightarrow P \ (v_{12} \ \text{says reps } v_{84} \ v_{85} \ v_{86}::xs)) \wedge \\
& \quad (\forall v_{12} \ v_{87} \ v_{88} \ xs. P \ xs \Rightarrow P \ (v_{12} \ \text{says } v_{87} \ \text{domi } v_{88}::xs)) \wedge
\end{aligned}$$

$$\begin{aligned}
& (\forall v_{12} v_{89} v_{90} xs. P xs \Rightarrow P (v_{12} \text{ says } v_{89} \text{ eqi } v_{90} :: xs)) \wedge \\
& (\forall v_{12} v_{91} v_{92} xs. P xs \Rightarrow P (v_{12} \text{ says } v_{91} \text{ doms } v_{92} :: xs)) \wedge \\
& (\forall v_{12} v_{93} v_{94} xs. P xs \Rightarrow P (v_{12} \text{ says } v_{93} \text{ eqs } v_{94} :: xs)) \wedge \\
& (\forall v_{12} v_{95} v_{96} xs. P xs \Rightarrow P (v_{12} \text{ says } v_{95} \text{ eqn } v_{96} :: xs)) \wedge \\
& (\forall v_{12} v_{97} v_{98} xs. P xs \Rightarrow P (v_{12} \text{ says } v_{97} \text{ lte } v_{98} :: xs)) \wedge \\
& (\forall v_{12} v_{99} v_{100} xs. P xs \Rightarrow P (v_{12} \text{ says } v_{99} \text{ lt } v_{100} :: xs)) \wedge \\
& (\forall v_{14} v_{15} xs. P xs \Rightarrow P (v_{14} \text{ speaks_for } v_{15} :: xs)) \wedge \\
& (\forall v_{16} v_{17} xs. P xs \Rightarrow P (v_{16} \text{ controls } v_{17} :: xs)) \wedge \\
& (\forall v_{18} v_{19} v_{20} xs. P xs \Rightarrow P (\text{reps } v_{18} v_{19} v_{20} :: xs)) \wedge \\
& (\forall v_{21} v_{22} xs. P xs \Rightarrow P (v_{21} \text{ domi } v_{22} :: xs)) \wedge \\
& (\forall v_{23} v_{24} xs. P xs \Rightarrow P (v_{23} \text{ eqi } v_{24} :: xs)) \wedge \\
& (\forall v_{25} v_{26} xs. P xs \Rightarrow P (v_{25} \text{ doms } v_{26} :: xs)) \wedge \\
& (\forall v_{27} v_{28} xs. P xs \Rightarrow P (v_{27} \text{ eqs } v_{28} :: xs)) \wedge \\
& (\forall v_{29} v_{30} xs. P xs \Rightarrow P (v_{29} \text{ eqn } v_{30} :: xs)) \wedge \\
& (\forall v_{31} v_{32} xs. P xs \Rightarrow P (v_{31} \text{ lte } v_{32} :: xs)) \wedge \\
& (\forall v_{33} v_{34} xs. P xs \Rightarrow P (v_{33} \text{ lt } v_{34} :: xs)) \Rightarrow \\
& \forall v. P v
\end{aligned}$$

[getPlatoonSergeantCOM_def]

$$\begin{aligned}
& \vdash (\text{getPlatoonSergeantCOM } [] = \text{NONE}) \wedge \\
& (\forall xs \text{ cmd}. \\
& \quad \text{getPlatoonSergeantCOM} \\
& \quad \quad (\text{SOME } (\text{PlatoonSergeantCOM } \text{cmd}) :: xs) = \\
& \quad \quad \text{SOME } (\text{PlatoonSergeantCOM } \text{cmd})) \wedge \\
& (\forall xs. \\
& \quad \text{getPlatoonSergeantCOM } (\text{NONE} :: xs) = \\
& \quad \text{getPlatoonSergeantCOM } xs) \wedge \\
& (\forall xs \ v_4. \\
& \quad \text{getPlatoonSergeantCOM } (\text{SOME } (\text{PlatoonLeaderCOM } v_4) :: xs) = \\
& \quad \text{getPlatoonSergeantCOM } xs) \wedge \\
& \forall xs \ v_6. \\
& \quad \text{getPlatoonSergeantCOM } (\text{SOME } (\text{OmniCOM } v_6) :: xs) = \\
& \quad \text{getPlatoonSergeantCOM } xs
\end{aligned}$$

[getPlatoonSergeantCOM_ind]

$$\begin{aligned}
& \vdash \forall P. \\
& \quad P [] \wedge (\forall \text{cmd } xs. P (\text{SOME } (\text{PlatoonSergeantCOM } \text{cmd}) :: xs)) \wedge \\
& \quad (\forall xs. P xs \Rightarrow P (\text{NONE} :: xs)) \wedge \\
& \quad (\forall v_4 \ xs. P xs \Rightarrow P (\text{SOME } (\text{PlatoonLeaderCOM } v_4) :: xs)) \wedge \\
& \quad (\forall v_6 \ xs. P xs \Rightarrow P (\text{SOME } (\text{OmniCOM } v_6) :: xs)) \Rightarrow \\
& \quad \forall v. P v
\end{aligned}$$

[getPlatoonSergeantCOMx_def]

$$\begin{aligned}
& \vdash (\text{getPlatoonSergeantCOMx } [] = \text{NONE}) \wedge \\
& (\forall xs \text{ cmd}. \\
& \quad \text{getPlatoonSergeantCOMx} \\
& \quad \quad (\text{Name PlatoonSergeant says} \\
& \quad \quad \text{prop } (\text{SOME } (\text{PlatoonSergeantCOM } \text{cmd}) :: xs) =
\end{aligned}$$

```

    SOME (PlatoonSergeantCOM cmd)) ∧
  (∀ xs.
    getPlatoonSergeantCOMx (TT::xs) =
    getPlatoonSergeantCOMx xs) ∧
  (∀ xs.
    getPlatoonSergeantCOMx (FF::xs) =
    getPlatoonSergeantCOMx xs) ∧
  (∀ xs v2.
    getPlatoonSergeantCOMx (prop v2::xs) =
    getPlatoonSergeantCOMx xs) ∧
  (∀ xs v3.
    getPlatoonSergeantCOMx (notf v3::xs) =
    getPlatoonSergeantCOMx xs) ∧
  (∀ xs v5 v4.
    getPlatoonSergeantCOMx (v4 andf v5::xs) =
    getPlatoonSergeantCOMx xs) ∧
  (∀ xs v7 v6.
    getPlatoonSergeantCOMx (v6 orf v7::xs) =
    getPlatoonSergeantCOMx xs) ∧
  (∀ xs v9 v8.
    getPlatoonSergeantCOMx (v8 impf v9::xs) =
    getPlatoonSergeantCOMx xs) ∧
  (∀ xs v11 v10.
    getPlatoonSergeantCOMx (v10 eqf v11::xs) =
    getPlatoonSergeantCOMx xs) ∧
  (∀ xs v12.
    getPlatoonSergeantCOMx (v12 says TT::xs) =
    getPlatoonSergeantCOMx xs) ∧
  (∀ xs v12.
    getPlatoonSergeantCOMx (v12 says FF::xs) =
    getPlatoonSergeantCOMx xs) ∧
  (∀ xs v134.
    getPlatoonSergeantCOMx (Name v134 says prop NONE::xs) =
    getPlatoonSergeantCOMx xs) ∧
  (∀ xs v144.
    getPlatoonSergeantCOMx
      (Name PlatoonLeader says prop (SOME v144)::xs) =
    getPlatoonSergeantCOMx xs) ∧
  (∀ xs v146.
    getPlatoonSergeantCOMx
      (Name PlatoonSergeant says
        prop (SOME (PlatoonLeaderCOM v146))::xs) =
    getPlatoonSergeantCOMx xs) ∧
  (∀ xs v148.
    getPlatoonSergeantCOMx
      (Name PlatoonSergeant says prop (SOME (OmniCOM v148))::
        xs) =
    getPlatoonSergeantCOMx xs) ∧
  (∀ xs v144.

```

```

    getPlatoonSergeantCOMx
      (Name Omni says prop (SOME v144)::xs) =
    getPlatoonSergeantCOMx xs) ∧
  (∀ xs v68 v136 v135.
    getPlatoonSergeantCOMx
      (v135 meet v136 says prop v68::xs) =
    getPlatoonSergeantCOMx xs) ∧
  (∀ xs v68 v138 v137.
    getPlatoonSergeantCOMx
      (v137 quoting v138 says prop v68::xs) =
    getPlatoonSergeantCOMx xs) ∧
  (∀ xs v69 v12.
    getPlatoonSergeantCOMx (v12 says notf v69::xs) =
    getPlatoonSergeantCOMx xs) ∧
  (∀ xs v71 v70 v12.
    getPlatoonSergeantCOMx (v12 says (v70 andf v71)::xs) =
    getPlatoonSergeantCOMx xs) ∧
  (∀ xs v73 v72 v12.
    getPlatoonSergeantCOMx (v12 says (v72 orf v73)::xs) =
    getPlatoonSergeantCOMx xs) ∧
  (∀ xs v75 v74 v12.
    getPlatoonSergeantCOMx (v12 says (v74 impf v75)::xs) =
    getPlatoonSergeantCOMx xs) ∧
  (∀ xs v77 v76 v12.
    getPlatoonSergeantCOMx (v12 says (v76 eqf v77)::xs) =
    getPlatoonSergeantCOMx xs) ∧
  (∀ xs v79 v78 v12.
    getPlatoonSergeantCOMx (v12 says v78 says v79::xs) =
    getPlatoonSergeantCOMx xs) ∧
  (∀ xs v81 v80 v12.
    getPlatoonSergeantCOMx (v12 says v80 speaks_for v81::xs) =
    getPlatoonSergeantCOMx xs) ∧
  (∀ xs v83 v82 v12.
    getPlatoonSergeantCOMx (v12 says v82 controls v83::xs) =
    getPlatoonSergeantCOMx xs) ∧
  (∀ xs v86 v85 v84 v12.
    getPlatoonSergeantCOMx (v12 says reps v84 v85 v86::xs) =
    getPlatoonSergeantCOMx xs) ∧
  (∀ xs v88 v87 v12.
    getPlatoonSergeantCOMx (v12 says v87 domi v88::xs) =
    getPlatoonSergeantCOMx xs) ∧
  (∀ xs v90 v89 v12.
    getPlatoonSergeantCOMx (v12 says v89 eqi v90::xs) =
    getPlatoonSergeantCOMx xs) ∧
  (∀ xs v92 v91 v12.
    getPlatoonSergeantCOMx (v12 says v91 doms v92::xs) =
    getPlatoonSergeantCOMx xs) ∧
  (∀ xs v94 v93 v12.
    getPlatoonSergeantCOMx (v12 says v93 eqs v94::xs) =

```

```

    getPlatoonSergeantCOMx xs) ∧
  (∀ xs v96 v95 v12.
    getPlatoonSergeantCOMx (v12 says v95 eqn v96::xs) =
    getPlatoonSergeantCOMx xs) ∧
  (∀ xs v98 v97 v12.
    getPlatoonSergeantCOMx (v12 says v97 lte v98::xs) =
    getPlatoonSergeantCOMx xs) ∧
  (∀ xs v99 v12 v100.
    getPlatoonSergeantCOMx (v12 says v99 lt v100::xs) =
    getPlatoonSergeantCOMx xs) ∧
  (∀ xs v15 v14.
    getPlatoonSergeantCOMx (v14 speaks_for v15::xs) =
    getPlatoonSergeantCOMx xs) ∧
  (∀ xs v17 v16.
    getPlatoonSergeantCOMx (v16 controls v17::xs) =
    getPlatoonSergeantCOMx xs) ∧
  (∀ xs v20 v19 v18.
    getPlatoonSergeantCOMx (reps v18 v19 v20::xs) =
    getPlatoonSergeantCOMx xs) ∧
  (∀ xs v22 v21.
    getPlatoonSergeantCOMx (v21 domi v22::xs) =
    getPlatoonSergeantCOMx xs) ∧
  (∀ xs v24 v23.
    getPlatoonSergeantCOMx (v23 eqi v24::xs) =
    getPlatoonSergeantCOMx xs) ∧
  (∀ xs v26 v25.
    getPlatoonSergeantCOMx (v25 doms v26::xs) =
    getPlatoonSergeantCOMx xs) ∧
  (∀ xs v28 v27.
    getPlatoonSergeantCOMx (v27 eqs v28::xs) =
    getPlatoonSergeantCOMx xs) ∧
  (∀ xs v30 v29.
    getPlatoonSergeantCOMx (v29 eqn v30::xs) =
    getPlatoonSergeantCOMx xs) ∧
  (∀ xs v32 v31.
    getPlatoonSergeantCOMx (v31 lte v32::xs) =
    getPlatoonSergeantCOMx xs) ∧
  ∀ xs v34 v33.
    getPlatoonSergeantCOMx (v33 lt v34::xs) =
    getPlatoonSergeantCOMx xs

```

[getPlatoonSergeantCOMx_ind]

```

⊢ ∀ P.
  P [] ∧
  (∀ cmd xs.
    P
      (Name PlatoonSergeant says
        prop (SOME (PlatoonSergeantCOM cmd))::xs)) ∧
  (∀ xs. P xs ⇒ P (TT::xs)) ∧ (∀ xs. P xs ⇒ P (FF::xs)) ∧

```


$$\begin{aligned}
& (\forall v_2 \text{ } xs. P \text{ } xs \Rightarrow P \text{ } (\text{prop } v_2::xs)) \wedge \\
& (\forall v_3 \text{ } xs. P \text{ } xs \Rightarrow P \text{ } (\text{notf } v_3::xs)) \wedge \\
& (\forall v_4 \text{ } v_5 \text{ } xs. P \text{ } xs \Rightarrow P \text{ } (v_4 \text{ } \text{andf } v_5::xs)) \wedge \\
& (\forall v_6 \text{ } v_7 \text{ } xs. P \text{ } xs \Rightarrow P \text{ } (v_6 \text{ } \text{orf } v_7::xs)) \wedge \\
& (\forall v_8 \text{ } v_9 \text{ } xs. P \text{ } xs \Rightarrow P \text{ } (v_8 \text{ } \text{impf } v_9::xs)) \wedge \\
& (\forall v_{10} \text{ } v_{11} \text{ } xs. P \text{ } xs \Rightarrow P \text{ } (v_{10} \text{ } \text{eqf } v_{11}::xs)) \wedge \\
& (\forall v_{12} \text{ } xs. P \text{ } xs \Rightarrow P \text{ } (v_{12} \text{ } \text{says TT}::xs)) \wedge \\
& (\forall v_{12} \text{ } xs. P \text{ } xs \Rightarrow P \text{ } (v_{12} \text{ } \text{says FF}::xs)) \wedge \\
& (\forall v_{134} \text{ } xs. P \text{ } xs \Rightarrow P \text{ } (\text{Name } v_{134} \text{ } \text{says prop NONE}::xs)) \wedge \\
& (\forall v_{144} \text{ } xs. \\
& \quad P \text{ } xs \Rightarrow \\
& \quad P \text{ } (\text{Name PlatoonLeader says prop (SOME } v_{144})::xs)) \wedge \\
& (\forall v_{146} \text{ } xs. \\
& \quad P \text{ } xs \Rightarrow \\
& \quad P \\
& \quad (\text{Name PlatoonSergeant says} \\
& \quad \quad \text{prop (SOME (PlatoonLeaderCOM } v_{146}))::xs)) \wedge \\
& (\forall v_{148} \text{ } xs. \\
& \quad P \text{ } xs \Rightarrow \\
& \quad P \\
& \quad (\text{Name PlatoonSergeant says} \\
& \quad \quad \text{prop (SOME (OmniCOM } v_{148}))::xs)) \wedge \\
& (\forall v_{144} \text{ } xs. \\
& \quad P \text{ } xs \Rightarrow P \text{ } (\text{Name Omni says prop (SOME } v_{144})::xs)) \wedge \\
& (\forall v_{135} \text{ } v_{136} \text{ } v_{68} \text{ } xs. \\
& \quad P \text{ } xs \Rightarrow P \text{ } (v_{135} \text{ } \text{meet } v_{136} \text{ } \text{says prop } v_{68}::xs)) \wedge \\
& (\forall v_{137} \text{ } v_{138} \text{ } v_{68} \text{ } xs. \\
& \quad P \text{ } xs \Rightarrow P \text{ } (v_{137} \text{ } \text{quoting } v_{138} \text{ } \text{says prop } v_{68}::xs)) \wedge \\
& (\forall v_{12} \text{ } v_{69} \text{ } xs. P \text{ } xs \Rightarrow P \text{ } (v_{12} \text{ } \text{says notf } v_{69}::xs)) \wedge \\
& (\forall v_{12} \text{ } v_{70} \text{ } v_{71} \text{ } xs. P \text{ } xs \Rightarrow P \text{ } (v_{12} \text{ } \text{says (} v_{70} \text{ } \text{andf } v_{71})::xs)) \wedge \\
& (\forall v_{12} \text{ } v_{72} \text{ } v_{73} \text{ } xs. P \text{ } xs \Rightarrow P \text{ } (v_{12} \text{ } \text{says (} v_{72} \text{ } \text{orf } v_{73})::xs)) \wedge \\
& (\forall v_{12} \text{ } v_{74} \text{ } v_{75} \text{ } xs. P \text{ } xs \Rightarrow P \text{ } (v_{12} \text{ } \text{says (} v_{74} \text{ } \text{impf } v_{75})::xs)) \wedge \\
& (\forall v_{12} \text{ } v_{76} \text{ } v_{77} \text{ } xs. P \text{ } xs \Rightarrow P \text{ } (v_{12} \text{ } \text{says (} v_{76} \text{ } \text{eqf } v_{77})::xs)) \wedge \\
& (\forall v_{12} \text{ } v_{78} \text{ } v_{79} \text{ } xs. P \text{ } xs \Rightarrow P \text{ } (v_{12} \text{ } \text{says } v_{78} \text{ } \text{says } v_{79}::xs)) \wedge \\
& (\forall v_{12} \text{ } v_{80} \text{ } v_{81} \text{ } xs. \\
& \quad P \text{ } xs \Rightarrow P \text{ } (v_{12} \text{ } \text{says } v_{80} \text{ } \text{speaks_for } v_{81}::xs)) \wedge \\
& (\forall v_{12} \text{ } v_{82} \text{ } v_{83} \text{ } xs. \\
& \quad P \text{ } xs \Rightarrow P \text{ } (v_{12} \text{ } \text{says } v_{82} \text{ } \text{controls } v_{83}::xs)) \wedge \\
& (\forall v_{12} \text{ } v_{84} \text{ } v_{85} \text{ } v_{86} \text{ } xs. \\
& \quad P \text{ } xs \Rightarrow P \text{ } (v_{12} \text{ } \text{says reps } v_{84} \text{ } v_{85} \text{ } v_{86}::xs)) \wedge \\
& (\forall v_{12} \text{ } v_{87} \text{ } v_{88} \text{ } xs. P \text{ } xs \Rightarrow P \text{ } (v_{12} \text{ } \text{says } v_{87} \text{ } \text{domi } v_{88}::xs)) \wedge \\
& (\forall v_{12} \text{ } v_{89} \text{ } v_{90} \text{ } xs. P \text{ } xs \Rightarrow P \text{ } (v_{12} \text{ } \text{says } v_{89} \text{ } \text{eqi } v_{90}::xs)) \wedge \\
& (\forall v_{12} \text{ } v_{91} \text{ } v_{92} \text{ } xs. P \text{ } xs \Rightarrow P \text{ } (v_{12} \text{ } \text{says } v_{91} \text{ } \text{doms } v_{92}::xs)) \wedge \\
& (\forall v_{12} \text{ } v_{93} \text{ } v_{94} \text{ } xs. P \text{ } xs \Rightarrow P \text{ } (v_{12} \text{ } \text{says } v_{93} \text{ } \text{eqs } v_{94}::xs)) \wedge \\
& (\forall v_{12} \text{ } v_{95} \text{ } v_{96} \text{ } xs. P \text{ } xs \Rightarrow P \text{ } (v_{12} \text{ } \text{says } v_{95} \text{ } \text{eqn } v_{96}::xs)) \wedge \\
& (\forall v_{12} \text{ } v_{97} \text{ } v_{98} \text{ } xs. P \text{ } xs \Rightarrow P \text{ } (v_{12} \text{ } \text{says } v_{97} \text{ } \text{lte } v_{98}::xs)) \wedge \\
& (\forall v_{12} \text{ } v_{99} \text{ } v_{100} \text{ } xs. P \text{ } xs \Rightarrow P \text{ } (v_{12} \text{ } \text{says } v_{99} \text{ } \text{lt } v_{100}::xs)) \wedge \\
& (\forall v_{14} \text{ } v_{15} \text{ } xs. P \text{ } xs \Rightarrow P \text{ } (v_{14} \text{ } \text{speaks_for } v_{15}::xs)) \wedge \\
& (\forall v_{16} \text{ } v_{17} \text{ } xs. P \text{ } xs \Rightarrow P \text{ } (v_{16} \text{ } \text{controls } v_{17}::xs)) \wedge
\end{aligned}$$

$$\begin{aligned}
& (\forall v_{18} v_{19} v_{20} xs. P xs \Rightarrow P (\text{reps } v_{18} v_{19} v_{20} :: xs)) \wedge \\
& (\forall v_{21} v_{22} xs. P xs \Rightarrow P (v_{21} \text{ domi } v_{22} :: xs)) \wedge \\
& (\forall v_{23} v_{24} xs. P xs \Rightarrow P (v_{23} \text{ eqi } v_{24} :: xs)) \wedge \\
& (\forall v_{25} v_{26} xs. P xs \Rightarrow P (v_{25} \text{ doms } v_{26} :: xs)) \wedge \\
& (\forall v_{27} v_{28} xs. P xs \Rightarrow P (v_{27} \text{ eqs } v_{28} :: xs)) \wedge \\
& (\forall v_{29} v_{30} xs. P xs \Rightarrow P (v_{29} \text{ eqn } v_{30} :: xs)) \wedge \\
& (\forall v_{31} v_{32} xs. P xs \Rightarrow P (v_{31} \text{ lte } v_{32} :: xs)) \wedge \\
& (\forall v_{33} v_{34} xs. P xs \Rightarrow P (v_{33} \text{ lt } v_{34} :: xs)) \Rightarrow \\
& \forall v. P v
\end{aligned}$$

3 projectSM Theory

Built: 27 December 2018

Parent Theories: projectUtilities, ssm

3.1 Theorems

[NOut_def]

```

⊢ (NOut CONDUCT_PB (exec x) =
  if
    getPlatoonLeaderCOM x = SOME (PlatoonLeaderCOM secure)
  then
    Secure
  else NoActionTaken) ∧
(NOut SECURE (exec x) =
  if
    getPlatoonSergeantCOM x =
      SOME (PlatoonSergeantCOM actionsIn)
  then
    ActionsIn
  else NoActionTaken) ∧
(NOut ACTIONS_IN (exec x) =
  if
    getPlatoonLeaderCOM x = SOME (PlatoonLeaderCOM withdraw)
  then
    Withdraw
  else NoActionTaken) ∧
(NOut WITHDRAW (exec x) =
  if
    getPlatoonLeaderCOM x = SOME (PlatoonLeaderCOM complete)
  then
    Complete
  else NoActionTaken) ∧ (NOut s (trap v0) = Unauthorized) ∧
(NOut s (discard v1) = UnAuthenticated)

```

[NOut_ind]

$$\vdash \forall P. \\
(\forall x. P \text{ CONDUCT_PB } (\text{exec } x)) \wedge (\forall x. P \text{ SECURE } (\text{exec } x)) \wedge \\
(\forall x. P \text{ ACTIONS_IN } (\text{exec } x)) \wedge (\forall x. P \text{ WITHDRAW } (\text{exec } x)) \wedge \\
(\forall s \ v_0. P \ s \ (\text{trap } v_0)) \wedge (\forall s \ v_1. P \ s \ (\text{discard } v_1)) \wedge \\
(\forall v_6. P \text{ COMPLETE } (\text{exec } v_6)) \Rightarrow \\
\forall v \ v_1. P \ v \ v_1$$

[NS_def]

$$\vdash (\text{NS CONDUCT_PB } (\text{exec } x) = \\
\text{if} \\
\quad \text{getPlatoonLeaderCOM } x = \text{SOME } (\text{PlatoonLeaderCOM secure}) \\
\quad \text{then} \\
\quad \quad \text{SECURE} \\
\quad \text{else CONDUCT_PB}) \wedge \\
(\text{NS SECURE } (\text{exec } x) = \\
\text{if} \\
\quad \text{getPlatoonSergeantCOM } x = \\
\quad \quad \text{SOME } (\text{PlatoonSergeantCOM actionsIn}) \\
\quad \text{then} \\
\quad \quad \text{ACTIONS_IN} \\
\quad \text{else SECURE}) \wedge \\
(\text{NS ACTIONS_IN } (\text{exec } x) = \\
\text{if} \\
\quad \text{getPlatoonLeaderCOM } x = \text{SOME } (\text{PlatoonLeaderCOM withdraw}) \\
\quad \text{then} \\
\quad \quad \text{WITHDRAW} \\
\quad \text{else ACTIONS_IN}) \wedge \\
(\text{NS WITHDRAW } (\text{exec } x) = \\
\text{if} \\
\quad \text{getPlatoonLeaderCOM } x = \text{SOME } (\text{PlatoonLeaderCOM complete}) \\
\quad \text{then} \\
\quad \quad \text{COMPLETE} \\
\quad \text{else WITHDRAW}) \wedge (\text{NS } s \ (\text{trap } v_0) = s) \wedge \\
(\text{NS } s \ (\text{discard } v_1) = s)$$

[NS_ind]

$$\vdash \forall P. \\
(\forall x. P \text{ CONDUCT_PB } (\text{exec } x)) \wedge (\forall x. P \text{ SECURE } (\text{exec } x)) \wedge \\
(\forall x. P \text{ ACTIONS_IN } (\text{exec } x)) \wedge (\forall x. P \text{ WITHDRAW } (\text{exec } x)) \wedge \\
(\forall s \ v_0. P \ s \ (\text{trap } v_0)) \wedge (\forall s \ v_1. P \ s \ (\text{discard } v_1)) \wedge \\
(\forall v_6. P \text{ COMPLETE } (\text{exec } v_6)) \Rightarrow \\
\forall v \ v_1. P \ v \ v_1$$

4 projectSecurity Theory

Built: 27 December 2018

Parent Theories: projectUtilities, ssm

4.1 Definitions

[globalAuth_def]

$\vdash \forall x. \text{globalAuth } x = [\text{TT}]$

[stateAuth_def]

$\vdash \forall s \ x.$
 $\text{stateAuth } s \ x =$
if $s = \text{CONDUCT_PB}$ **then**
 if
 $\text{getPlatoonLeaderCOMx } x = \text{SOME } (\text{PlatoonLeaderCOM } \text{secure})$
 then
 $[\text{Name } \text{PlatoonLeader } \text{controls}$
 $\text{prop } (\text{SOME } (\text{PlatoonLeaderCOM } \text{secure}))]$
 else $[\text{prop NONE}]$
else if $s = \text{SECURE}$ **then**
 if
 $\text{getPlatoonSergeantCOMx } x =$
 $\text{SOME } (\text{PlatoonSergeantCOM } \text{actionsIn})$
 then
 $[\text{Name } \text{PlatoonSergeant } \text{controls}$
 $\text{prop } (\text{SOME } (\text{PlatoonSergeantCOM } \text{actionsIn}))]$
 else $[\text{prop NONE}]$
else if $s = \text{ACTIONS_IN}$ **then**
 if
 $\text{getPlatoonLeaderCOMx } x =$
 $\text{SOME } (\text{PlatoonLeaderCOM } \text{withdraw})$
 then
 $[\text{Name } \text{PlatoonLeader } \text{controls}$
 $\text{prop } (\text{SOME } (\text{PlatoonLeaderCOM } \text{withdraw}))]$
 else $[\text{prop NONE}]$
else if $s = \text{WITHDRAW}$ **then**
 if
 $\text{getPlatoonLeaderCOMx } x =$
 $\text{SOME } (\text{PlatoonLeaderCOM } \text{complete})$
 then
 $[\text{Name } \text{PlatoonLeader } \text{controls}$
 $\text{prop } (\text{SOME } (\text{PlatoonLeaderCOM } \text{complete}))]$
 else $[\text{prop NONE}]$
else $[\text{prop NONE}]$

4.2 Theorems

[authentication_def]

$\vdash (\text{authentication}$
 $(\text{Name } \text{PlatoonLeader } \text{says}$
 $\text{prop } (\text{SOME } (\text{PlatoonLeaderCOM } x'')))) \iff T) \wedge$
 $(\text{authentication}$

```

(Name PlatoonSergeant says
  prop (SOME (PlatoonSergeantCOM x'))))  $\iff$  T)  $\wedge$ 
(authentication (Name Omni says prop (SOME (OmniCOM x)))  $\iff$ 
  T)  $\wedge$  (authentication TT  $\iff$  F)  $\wedge$  (authentication FF  $\iff$  F)  $\wedge$ 
(authentication (prop v)  $\iff$  F)  $\wedge$ 
(authentication (notf v1)  $\iff$  F)  $\wedge$ 
(authentication (v2 andf v3)  $\iff$  F)  $\wedge$ 
(authentication (v4 orf v5)  $\iff$  F)  $\wedge$ 
(authentication (v6 impf v7)  $\iff$  F)  $\wedge$ 
(authentication (v8 eqf v9)  $\iff$  F)  $\wedge$ 
(authentication (Name v66 says TT)  $\iff$  F)  $\wedge$ 
(authentication (Name v66 says FF)  $\iff$  F)  $\wedge$ 
(authentication (Name v66 says prop NONE)  $\iff$  F)  $\wedge$ 
(authentication
  (Name PlatoonSergeant says
    prop (SOME (PlatoonLeaderCOM v144))))  $\iff$  F)  $\wedge$ 
(authentication
  (Name Omni says prop (SOME (PlatoonLeaderCOM v144))))  $\iff$ 
  F)  $\wedge$ 
(authentication
  (Name PlatoonLeader says
    prop (SOME (PlatoonSergeantCOM v145))))  $\iff$  F)  $\wedge$ 
(authentication
  (Name Omni says prop (SOME (PlatoonSergeantCOM v145))))  $\iff$ 
  F)  $\wedge$ 
(authentication
  (Name PlatoonLeader says prop (SOME (OmniCOM v146))))  $\iff$ 
  F)  $\wedge$ 
(authentication
  (Name PlatoonSergeant says prop (SOME (OmniCOM v146))))  $\iff$ 
  F)  $\wedge$  (authentication (Name v66 says notf v77)  $\iff$  F)  $\wedge$ 
(authentication (Name v66 says (v78 andf v79))  $\iff$  F)  $\wedge$ 
(authentication (Name v66 says (v80 orf v81))  $\iff$  F)  $\wedge$ 
(authentication (Name v66 says (v82 impf v83))  $\iff$  F)  $\wedge$ 
(authentication (Name v66 says (v84 eqf v85))  $\iff$  F)  $\wedge$ 
(authentication (Name v66 says v86 says v87)  $\iff$  F)  $\wedge$ 
(authentication (Name v66 says v88 speaks_for v89)  $\iff$  F)  $\wedge$ 
(authentication (Name v66 says v90 controls v91)  $\iff$  F)  $\wedge$ 
(authentication (Name v66 says reps v92 v93 v94)  $\iff$  F)  $\wedge$ 
(authentication (Name v66 says v95 domi v96)  $\iff$  F)  $\wedge$ 
(authentication (Name v66 says v97 eqi v98)  $\iff$  F)  $\wedge$ 
(authentication (Name v66 says v99 doms v100)  $\iff$  F)  $\wedge$ 
(authentication (Name v66 says v101 eqs v102)  $\iff$  F)  $\wedge$ 
(authentication (Name v66 says v103 eqn v104)  $\iff$  F)  $\wedge$ 
(authentication (Name v66 says v105 lte v106)  $\iff$  F)  $\wedge$ 
(authentication (Name v66 says v107 lt v108)  $\iff$  F)  $\wedge$ 
(authentication (v67 meet v68 says v11)  $\iff$  F)  $\wedge$ 
(authentication (v69 quoting v70 says v11)  $\iff$  F)  $\wedge$ 
(authentication (v12 speaks_for v13)  $\iff$  F)  $\wedge$ 

```

(authentication (v_{14} controls v_{15}) \iff F) \wedge
 (authentication (reps v_{16} v_{17} v_{18}) \iff F) \wedge
 (authentication (v_{19} domi v_{20}) \iff F) \wedge
 (authentication (v_{21} eqi v_{22}) \iff F) \wedge
 (authentication (v_{23} doms v_{24}) \iff F) \wedge
 (authentication (v_{25} eqs v_{26}) \iff F) \wedge
 (authentication (v_{27} eqn v_{28}) \iff F) \wedge
 (authentication (v_{29} lte v_{30}) \iff F) \wedge
 (authentication (v_{31} lt v_{32}) \iff F)

[authentication_ind]

$\vdash \forall P.$
 $(\forall x.$
 $\quad P$
 $\quad (\text{Name PlatoonLeader says}$
 $\quad \quad \text{prop (SOME (PlatoonLeaderCOM } x))) \wedge$
 $(\forall x.$
 $\quad P$
 $\quad (\text{Name PlatoonSergeant says}$
 $\quad \quad \text{prop (SOME (PlatoonSergeantCOM } x))) \wedge$
 $(\forall x. P (\text{Name Omni says prop (SOME (OmniCOM } x)))) \wedge P \text{ TT} \wedge$
 $P \text{ FF} \wedge (\forall v. P (\text{prop } v)) \wedge (\forall v_1. P (\text{notf } v_1)) \wedge$
 $(\forall v_2 v_3. P (v_2 \text{ andf } v_3)) \wedge (\forall v_4 v_5. P (v_4 \text{ orf } v_5)) \wedge$
 $(\forall v_6 v_7. P (v_6 \text{ impf } v_7)) \wedge (\forall v_8 v_9. P (v_8 \text{ eqf } v_9)) \wedge$
 $(\forall v_{66}. P (\text{Name } v_{66} \text{ says TT})) \wedge$
 $(\forall v_{66}. P (\text{Name } v_{66} \text{ says FF})) \wedge$
 $(\forall v_{66}. P (\text{Name } v_{66} \text{ says prop NONE})) \wedge$
 $(\forall v_{144}.$
 $\quad P$
 $\quad (\text{Name PlatoonSergeant says}$
 $\quad \quad \text{prop (SOME (PlatoonLeaderCOM } v_{144}))) \wedge$
 $(\forall v_{144}.$
 $\quad P$
 $\quad (\text{Name Omni says}$
 $\quad \quad \text{prop (SOME (PlatoonLeaderCOM } v_{144}))) \wedge$
 $(\forall v_{145}.$
 $\quad P$
 $\quad (\text{Name PlatoonLeader says}$
 $\quad \quad \text{prop (SOME (PlatoonSergeantCOM } v_{145}))) \wedge$
 $(\forall v_{145}.$
 $\quad P$
 $\quad (\text{Name Omni says}$
 $\quad \quad \text{prop (SOME (PlatoonSergeantCOM } v_{145}))) \wedge$
 $(\forall v_{146}.$
 $\quad P$
 $\quad (\text{Name PlatoonLeader says}$
 $\quad \quad \text{prop (SOME (OmniCOM } v_{146}))) \wedge$
 $(\forall v_{146}.$
 $\quad P$

```

(Name PlatoonSergeant says
  prop (SOME (OmniCOM v146)))) ∧
(∀ v66 v77. P (Name v66 says notif v77)) ∧
(∀ v66 v78 v79. P (Name v66 says (v78 andf v79))) ∧
(∀ v66 v80 v81. P (Name v66 says (v80 orf v81))) ∧
(∀ v66 v82 v83. P (Name v66 says (v82 impf v83))) ∧
(∀ v66 v84 v85. P (Name v66 says (v84 eqf v85))) ∧
(∀ v66 v86 v87. P (Name v66 says v86 says v87)) ∧
(∀ v66 v88 v89. P (Name v66 says v88 speaks_for v89)) ∧
(∀ v66 v90 v91. P (Name v66 says v90 controls v91)) ∧
(∀ v66 v92 v93 v94. P (Name v66 says reps v92 v93 v94)) ∧
(∀ v66 v95 v96. P (Name v66 says v95 domi v96)) ∧
(∀ v66 v97 v98. P (Name v66 says v97 eqi v98)) ∧
(∀ v66 v99 v100. P (Name v66 says v99 doms v100)) ∧
(∀ v66 v101 v102. P (Name v66 says v101 eqs v102)) ∧
(∀ v66 v103 v104. P (Name v66 says v103 eqn v104)) ∧
(∀ v66 v105 v106. P (Name v66 says v105 lte v106)) ∧
(∀ v66 v107 v108. P (Name v66 says v107 lt v108)) ∧
(∀ v67 v68 v11. P (v67 meet v68 says v11)) ∧
(∀ v69 v70 v11. P (v69 quoting v70 says v11)) ∧
(∀ v12 v13. P (v12 speaks_for v13)) ∧
(∀ v14 v15. P (v14 controls v15)) ∧
(∀ v16 v17 v18. P (reps v16 v17 v18)) ∧
(∀ v19 v20. P (v19 domi v20)) ∧
(∀ v21 v22. P (v21 eqi v22)) ∧
(∀ v23 v24. P (v23 doms v24)) ∧
(∀ v25 v26. P (v25 eqs v26)) ∧ (∀ v27 v28. P (v27 eqn v28)) ∧
(∀ v29 v30. P (v29 lte v30)) ∧ (∀ v31 v32. P (v31 lt v32)) ⇒
∀ v. P v

```

5 projectAssuranceExec Theory

Built: 27 December 2018

Parent Theories: projectSecurity

5.1 Theorems

[ACTIONS_IN_exec_withdraw_lemma1]

```

⊢ ∀ M Oi Os.
  CFGInterpret (M, Oi, Os)
    (CFG authentication stateAuth globalAuth
      ([Name PlatoonLeader says
        prop (SOME (PlatoonLeaderCOM withdraw))]::ins)
        ACTIONS_IN outs) ⇒
  (M, Oi, Os) satList
  propCommandList
    [Name PlatoonLeader says
      prop (SOME (PlatoonLeaderCOM withdraw))]

```

[ACTIONS_IN_exec_withdraw_lemma2]

$\vdash \forall NS \text{ Out } M \text{ } Oi \text{ } Os.$
 $TR (M, Oi, Os)$
 $(exec$
 $(inputList$
 $([Name \text{ PlatoonLeader says}$
 $\text{prop (SOME (PlatoonLeaderCOM withdraw))]))$
 $(CFG \text{ authentication stateAuth globalAuth}$
 $([Name \text{ PlatoonLeader says}$
 $\text{prop (SOME (PlatoonLeaderCOM withdraw))}]::ins)$
 $ACTIONS_IN \text{ outs})$
 $(CFG \text{ authentication stateAuth globalAuth ins}$
 $(NS \text{ ACTIONS_IN}$
 $(exec$
 $(inputList$
 $([Name \text{ PlatoonLeader says}$
 $\text{prop (SOME (PlatoonLeaderCOM withdraw))]))$
 $(Out \text{ ACTIONS_IN}$
 $(exec$
 $(inputList$
 $([Name \text{ PlatoonLeader says}$
 $\text{prop (SOME (PlatoonLeaderCOM withdraw))}]::$
 $\text{outs})) \iff$
 $authenticationTest \text{ authentication}$
 $([Name \text{ PlatoonLeader says}$
 $\text{prop (SOME (PlatoonLeaderCOM withdraw))}] \wedge$
 $CFGInterpret (M, Oi, Os)$
 $(CFG \text{ authentication stateAuth globalAuth}$
 $([Name \text{ PlatoonLeader says}$
 $\text{prop (SOME (PlatoonLeaderCOM withdraw))}]::ins)$
 $ACTIONS_IN \text{ outs}) \wedge$
 $(M, Oi, Os) \text{ satList}$
 $propCommandList$
 $([Name \text{ PlatoonLeader says}$
 $\text{prop (SOME (PlatoonLeaderCOM withdraw))}]$

[ACTIONS_IN_exec_withdraw_thm]

$\vdash \forall NS \text{ Out } M \text{ } Oi \text{ } Os.$
 $TR (M, Oi, Os) (exec [SOME (PlatoonLeaderCOM withdraw)])$
 $(CFG \text{ authentication stateAuth globalAuth}$
 $([Name \text{ PlatoonLeader says}$
 $\text{prop (SOME (PlatoonLeaderCOM withdraw))}]::ins)$
 $ACTIONS_IN \text{ outs})$
 $(CFG \text{ authentication stateAuth globalAuth ins}$
 $(NS \text{ ACTIONS_IN}$
 $(exec [SOME (PlatoonLeaderCOM withdraw)]))$
 $(Out \text{ ACTIONS_IN}$
 $(exec [SOME (PlatoonLeaderCOM withdraw)]))::$
 $\text{outs})) \iff$


```

authenticationTest authentication
  [Name PlatoonLeader says
    prop (SOME (PlatoonLeaderCOM withdraw))]] ∧
CFGInterpret (M, Oi, Os)
  (CFG authentication stateAuth globalAuth
    ([Name PlatoonLeader says
      prop (SOME (PlatoonLeaderCOM withdraw))]]::ins)
    ACTIONS_IN outs) ∧
(M, Oi, Os) satList [prop (SOME (PlatoonLeaderCOM withdraw))]

```

[CONDUCT_PB_exec_secure_lemma1]

```

⊢ ∀ M Oi Os.
  CFGInterpret (M, Oi, Os)
    (CFG authentication stateAuth globalAuth
      ([Name PlatoonLeader says
        prop (SOME (PlatoonLeaderCOM secure))]]::ins)
      CONDUCT_PB outs) ⇒
(M, Oi, Os) satList
propCommandList
  [Name PlatoonLeader says
    prop (SOME (PlatoonLeaderCOM secure))]

```

[CONDUCT_PB_exec_secure_lemma2]

```

⊢ ∀ NS Out M Oi Os.
  TR (M, Oi, Os)
    (exec
      (inputList
        [Name PlatoonLeader says
          prop (SOME (PlatoonLeaderCOM secure))]))
    (CFG authentication stateAuth globalAuth
      ([Name PlatoonLeader says
        prop (SOME (PlatoonLeaderCOM secure))]]::ins)
      CONDUCT_PB outs)
    (CFG authentication stateAuth globalAuth ins
      (NS CONDUCT_PB
        (exec
          (inputList
            [Name PlatoonLeader says
              prop (SOME (PlatoonLeaderCOM secure))]))))
    (Out CONDUCT_PB
      (exec
        (inputList
          [Name PlatoonLeader says
            prop (SOME (PlatoonLeaderCOM secure))]]))::
      outs)) ⇔
authenticationTest authentication
  [Name PlatoonLeader says
    prop (SOME (PlatoonLeaderCOM secure))] ∧
CFGInterpret (M, Oi, Os)

```

```

(CFG authentication stateAuth globalAuth
  ([Name PlatoonLeader says
    prop (SOME (PlatoonLeaderCOM secure))]::ins)
  CONDUCT_PB outs) ∧
(M, Oi, Os) satList
propCommandList
[Name PlatoonLeader says
  prop (SOME (PlatoonLeaderCOM secure))]]

[CONDUCT_PB_exec_secure_thm]
⊢ ∀ NS Out M Oi Os.
  TR (M, Oi, Os) (exec [SOME (PlatoonLeaderCOM secure)])
  (CFG authentication stateAuth globalAuth
    ([Name PlatoonLeader says
      prop (SOME (PlatoonLeaderCOM secure))]::ins)
    CONDUCT_PB outs)
  (CFG authentication stateAuth globalAuth ins
    (NS CONDUCT_PB
      (exec [SOME (PlatoonLeaderCOM secure)])))
  (Out CONDUCT_PB
    (exec [SOME (PlatoonLeaderCOM secure)])::outs)) ⇔
authenticationTest authentication
[Name PlatoonLeader says
  prop (SOME (PlatoonLeaderCOM secure))]] ∧
CFGInterpret (M, Oi, Os)
  (CFG authentication stateAuth globalAuth
    ([Name PlatoonLeader says
      prop (SOME (PlatoonLeaderCOM secure))]::ins)
    CONDUCT_PB outs) ∧
(M, Oi, Os) satList [prop (SOME (PlatoonLeaderCOM secure))]]

[SECURE_exec_actionsIn_lemma1]
⊢ ∀ M Oi Os.
  CFGInterpret (M, Oi, Os)
  (CFG authentication stateAuth globalAuth
    ([Name PlatoonSergeant says
      prop (SOME (PlatoonSergeantCOM actionsIn))]::ins)
    SECURE outs) ⇒
(M, Oi, Os) satList
propCommandList
[Name PlatoonSergeant says
  prop (SOME (PlatoonSergeantCOM actionsIn))]]

[SECURE_exec_actionsIn_lemma2]
⊢ ∀ NS Out M Oi Os.
  TR (M, Oi, Os)
  (exec
    (inputList

```

```

      [Name PlatoonSergeant says
        prop (SOME (PlatoonSergeantCOM actionsIn))]]))
(CFG authentication stateAuth globalAuth
  ([Name PlatoonSergeant says
    prop (SOME (PlatoonSergeantCOM actionsIn))]::ins)
  SECURE outs)
(CFG authentication stateAuth globalAuth ins
  (NS SECURE
    (exec
      (inputList
        [Name PlatoonSergeant says
          prop
            (SOME (PlatoonSergeantCOM actionsIn))]))))
(Out SECURE
  (exec
    (inputList
      [Name PlatoonSergeant says
        prop
          (SOME (PlatoonSergeantCOM actionsIn))]::
            outs)))  $\iff$ 
authenticationTest authentication
  [Name PlatoonSergeant says
    prop (SOME (PlatoonSergeantCOM actionsIn))]  $\wedge$ 
CFGInterpret (M, Oi, Os)
  (CFG authentication stateAuth globalAuth
    ([Name PlatoonSergeant says
      prop (SOME (PlatoonSergeantCOM actionsIn))]::ins)
    SECURE outs)  $\wedge$ 
  (M, Oi, Os) satList
propCommandList
  [Name PlatoonSergeant says
    prop (SOME (PlatoonSergeantCOM actionsIn))]

```

[SECURE_exec_actionsIn_thm]

```

 $\vdash \forall NS \text{ Out } M \text{ Oi } Os.$ 
TR (M, Oi, Os) (exec [SOME (PlatoonSergeantCOM actionsIn)])
(CFG authentication stateAuth globalAuth
  ([Name PlatoonSergeant says
    prop (SOME (PlatoonSergeantCOM actionsIn))]::ins)
  SECURE outs)
(CFG authentication stateAuth globalAuth ins
  (NS SECURE
    (exec [SOME (PlatoonSergeantCOM actionsIn)]))
  (Out SECURE
    (exec [SOME (PlatoonSergeantCOM actionsIn)]::
      outs)))  $\iff$ 
authenticationTest authentication
  [Name PlatoonSergeant says
    prop (SOME (PlatoonSergeantCOM actionsIn))]  $\wedge$ 

```

```

CFGInterpret (M, Oi, Os)
  (CFG authentication stateAuth globalAuth
    ([Name PlatoonSergeant says
      prop (SOME (PlatoonSergeantCOM actionsIn))]::ins)
    SECURE outs) ∧
(M, Oi, Os) satList
[prop (SOME (PlatoonSergeantCOM actionsIn))]

[WITHDRAW_exec_complete_lemma1]
⊢ ∀ M Oi Os.
  CFGInterpret (M, Oi, Os)
    (CFG authentication stateAuth globalAuth
      ([Name PlatoonLeader says
        prop (SOME (PlatoonLeaderCOM complete))]::ins)
      WITHDRAW outs) ⇒
(M, Oi, Os) satList
propCommandList
  [Name PlatoonLeader says
    prop (SOME (PlatoonLeaderCOM complete))]

[WITHDRAW_exec_complete_lemma2]
⊢ ∀ NS Out M Oi Os.
  TR (M, Oi, Os)
    (exec
      (inputList
        [Name PlatoonLeader says
          prop (SOME (PlatoonLeaderCOM complete))]))
  (CFG authentication stateAuth globalAuth
    ([Name PlatoonLeader says
      prop (SOME (PlatoonLeaderCOM complete))]::ins)
    WITHDRAW outs)
  (CFG authentication stateAuth globalAuth ins
    (NS WITHDRAW
      (exec
        (inputList
          [Name PlatoonLeader says
            prop (SOME (PlatoonLeaderCOM complete))]))))
  (Out WITHDRAW
    (exec
      (inputList
        [Name PlatoonLeader says
          prop (SOME (PlatoonLeaderCOM complete))]))))::
outs)) ⇔
authenticationTest authentication
  [Name PlatoonLeader says
    prop (SOME (PlatoonLeaderCOM complete))] ∧
CFGInterpret (M, Oi, Os)
  (CFG authentication stateAuth globalAuth
    ([Name PlatoonLeader says

```

```

      prop (SOME (PlatoonLeaderCOM complete))]]::ins)
    WITHDRAW outs) ∧
  (M, Oi, Os) satList
  propCommandList
  [Name PlatoonLeader says
   prop (SOME (PlatoonLeaderCOM complete))]]
[WITHDRAW_exec_complete_thm]
⊢ ∀ NS Out M Oi Os.
  TR (M, Oi, Os) (exec [SOME (PlatoonLeaderCOM complete)])
  (CFG authentication stateAuth globalAuth
   ([Name PlatoonLeader says
    prop (SOME (PlatoonLeaderCOM complete))]]::ins)
   WITHDRAW outs)
  (CFG authentication stateAuth globalAuth ins
   (NS WITHDRAW
    (exec [SOME (PlatoonLeaderCOM complete)])))
  (Out WITHDRAW
   (exec [SOME (PlatoonLeaderCOM complete)]))::
   outs)) ⇔
authenticationTest authentication
  [Name PlatoonLeader says
   prop (SOME (PlatoonLeaderCOM complete))]] ∧
CFGInterpret (M, Oi, Os)
  (CFG authentication stateAuth globalAuth
   ([Name PlatoonLeader says
    prop (SOME (PlatoonLeaderCOM complete))]]::ins)
   WITHDRAW outs) ∧
  (M, Oi, Os) satList [prop (SOME (PlatoonLeaderCOM complete))]]

```


Index

projectAssuranceExec Theory, 23

Theorems, 23

ACTIONS_IN_exec_withdraw_lemma1,
23

ACTIONS_IN_exec_withdraw_lemma2,
24

ACTIONS_IN_exec_withdraw_thm, 24

CONDUCT_PB_exec_secure_lemma1,
25

CONDUCT_PB_exec_secure_lemma2,
25

CONDUCT_PB_exec_secure_thm, 26

SECURE_exec_actionsIn_lemma1, 26

SECURE_exec_actionsIn_lemma2, 26

SECURE_exec_actionsIn_thm, 27

WITHDRAW_exec_complete_lemma1,
28

WITHDRAW_exec_complete_lemma2,
28

WITHDRAW_exec_complete_thm, 29

projectSecurity Theory, 19

Definitions, 20

globalAuth_def, 20

stateAuth_def, 20

Theorems, 20

authentication_def, 20

authentication_ind, 22

projectSM Theory, 18

Theorems, 18

NOut_def, 18

NOut_ind, 18

NS_def, 19

NS_ind, 19

projectTypes Theory, 3

Datatypes, 3

Theorems, 3

commands_distinct_clauses, 3

commands_one_one, 3

omniCom_distinct_clauses, 3

output_distinct_clauses, 4

platoonLeaderCom_distinct_clauses, 4

platoonSergeantCom_distinct_clauses,
4

principal_distinct_clauses, 4

state_distinct_clauses, 4

projectUtilities Theory, 4

Theorems, 4

getOmniCOM_def, 4

getOmniCOM_ind, 5

getOmniCOMx_def, 5

getOmniCOMx_ind, 7

getPlatoonLeaderCOM_def, 8

getPlatoonLeaderCOM_ind, 8

getPlatoonLeaderCOMx_def, 9

getPlatoonLeaderCOMx_ind, 12

getPlatoonSergeantCOM_def, 13

getPlatoonSergeantCOM_ind, 13

getPlatoonSergeantCOMx_def, 13

getPlatoonSergeantCOMx_ind, 16