

# **Εργασία 2η Ειδικων Κεραιων-Συνθεση Κεραιων**

**Μελετη BeamForming και  
DoA(Directional of Arriving)**

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**ΚΩΔΙΚΕΣ ΤΟΥ MATLAB**

## Μερος 1<sup>ο</sup> :Υλοποίηση MVDR BeamFormer

```
% Implementation of MVDR
Beamformer

fileId=fopen('resultsMVDR.txt','w+'); %delete if
results.txt has data
fclose(fileId);
AoANb=0; %Counter For change AoAdev SINR.txt to save
the data

%Calculate Results for different SNRdb,delta
for SNRdb=0:5:20
    for delta=2:2:10
        AoANb=AoANb+1;
        CalcAoA(delta,SNRdb,AoANb);
        CalcRes(AoANb);
    end
end

%function to make AoAdev_SINR.txt
function CalcAoA(delta,SNRdb,AoANb)

N=5; %Number of Incoming Signals
signals_DoA=zeros(1,N); %Initialization for incoming
angles
M=16; %Number Of elementaries in antenna
Pg=1; %Power for our Signals
Psd=Pg; %Power of desirable signal
SNR=10^(SNRdb/10); %SNR
Pn=Pg/SNR; %Power of Noise.From
SNR=Pdesirable/Pnoise
AoANb=int2str(AoANb); %Parameter to take different
txt for AoAdev
fileName=strcat('AoAdev_SINR',AoANb,'.txt');
fileID=fopen(fileName,'w+');

%Loop for all theta
for polar_angle=30:1:150
```

```

        %Make angles for signals in a vector
        for i=1:1:N
            signals_DoA(1,i)=polar_angle+(i-1)*delta;
        end
        if (polar_angle+4*delta)>150 %Check For
Maximum_Angle=150 The worst case in every scenario
            break; %If an angle
exceed 150 then break the loop
        end

        %Take in every loop one desirable and others
interference
        for desirable=1:1:size(signals_DoA,2)

            theta_0=signals_DoA(desirable);
%Desirable Signal
            fprintf(fileID,'%d',theta_0);
            theta_i=zeros(1,N-1); %Initialization
for Interference Signals
                counter=0;

                %Seperate desirable angle from the
interference angles
                for i=1:1:N %Loop for take
Interference Signals
                    if i==desirable
                        continue;
                    else
                        counter=counter+1;
                        fprintf(fileID,'
%d',signals_DoA(i));

theta_i(1,counter)=signals_DoA(i); %Interference
Signal
                    end
                end
            end

            %Calculate A,ad vectors
            ad_vector=zeros(M,1); %Initialization of
steering vector
            A_vector=zeros(M,N); %Initialization of
steering incoming vector
            for signal=0:1:(N-1) %Calculate Vectors
                for pos_elem=1:1:M
                    if signal==0

```

```

ad_vector(pos_elem,signal+1)=exp((1j)*pi*(pos_elem-
1)*cosd(theta_0));

A_vector(pos_elem,signal+1)=exp((1j)*pi*(pos_elem-
1)*cosd(theta_0));
        else

A_vector(pos_elem,signal+1)=exp((1j)*pi*(pos_elem-
1)*cosd(theta_i(1,signal)));
        end

    end

end

    %Calculate SINR
    Rgg=Pg*eye(N,N); %Correletion Matrix of
incoming signals modulation gi
    %Irrelevant with each_other
    Rnn=Pn*eye(M,M); %Correletion Matrix of
noise in every element of antenna
    Rxx=A_vector*Rgg*(A_vector')+Rnn;
%Correletion Matrix of incoming signals Xi in every
element of antenna

    Wmvdr=(inv(Rxx))*ad_vector; %Weight
vector

    Ai=A_vector(:,2:end); %Steering Vector
for interference signals
    Rgigi=Rgg(2:end,2:end); %Correletion of
incoming interference signals modulation

SINR=(Psd*(Wmvdr')*ad_vector*(ad_vector')*Wmvdr)/((Wm
vdr')*Ai*Rgigi*(Ai')*Wmvdr+(Wmvdr')*Rnn*Wmvdr);
    SINRdb=10*log10(abs(SINR)); %SINR (Db)

    %Plot Radiation Diagram

    thetav=(0:0.1:180); %Initialization for
scanning angle in AF
    a=zeros(M,size(thetav,2));
%Initialization for variable a vector
    for pos_elem=1:1:M
        b=exp((1j)*pi*(pos_elem-
1)*cosd(thetav));

```

```

        a(pos_elem,:)=b;
    end

    AF=(Wmvdr')*a;    %radiation Diagram
    titleId=['Radiation Diagram MVDR Delta='
num2str(delta) ' SNR(Db)=' num2str(SNRdb)];

    %Normalize
    AFN=abs(AF)/max(abs(AF));
    %If we want all the figures just delete %
down from %figure
    %figure
    plot(thetav,AFN);
    ylabel('|AF|/|AFmax|');
    xlabel('theta');
    title(titleId);
    legend('|AF|')

    Dtheta=zeros(1,N); %Initialization for
Deviation for interference angles and |AF| zeros

    %Calculate Direction Deviations for
Desirable
    [~,locs] = findpeaks(abs(AF)); %take the
peaks from |AF| and their index in matrix
    Peaks=thetav(1,locs(1,1:end)); %Angles
for the peaks
    Dtheta(1,1)=min(abs(Peaks-theta_0)); %Min
Deviation Of Peak and incoming desirable angle
    fprintf(fileID,' %f',Dtheta(1,1));

    %Calculate Direction Deviations for
Interference
    [~,locs] = findpeaks(-abs(AF));
    zeroes=thetav(1,locs(1,1:end)); %Angles
for the zeros
    for i=2:1:N
        Dtheta(1,i)=min(abs(zeroes-
theta_i(1,(i-1))))); %Min Deviation Of Zero and
incoming interference angle
    end
    for i=2:size(Dtheta,2)
        fprintf(fileID,' %f',Dtheta(1,i));
    end
    fprintf(fileID,' %f\n',SINRdb);

```

```

end
end
fclose(fileID);
end
%function to make results.txt
function CalcRes(AoANb)
N=5; %Number of signals

%Read Data From AoAdev_SINR.txt
AoANb=int2str(AoANb);
fileName=strcat('AoAdev_SINR',AoANb, '.txt');
fileID=fopen(fileName, 'r');
sizeA=[11 Inf];
A=fscanf(fileID, '%d %d %d %d %d %f %f %f %f %f %f \n', sizeA);
A=A'; %Transpose array to take the data like in txt
fclose(fileID);

%Calculate min,max,mean std deviation for
Dtheta_0(desirable)
vector=A(:, (N+1)); %Take all Dtheta_0 from the array
Dtheta_0max=max(vector);
Dtheta_0min=min(vector);
Dtheta_0mean=mean(vector);
Dtheta_0std=std(vector);

%Calculate min,max,mean std deviation for
Dtheta_i(interference signals)

vector=reshape(A(:, (N+2):2*N), [], 1); % convert
matrix to column vector every column stuck under the
first column
Dtheta_imax=max(vector);
Dtheta_imin=min(vector);
Dtheta_imean=mean(vector);
Dtheta_istd=std(vector);

%Calculate min,max,mean std deviation for SINR(db)
vector=A(:, (2*N+1));
SINRdbmax=max(vector);
SINRdbmin=min(vector);
SINRdbmean=mean(vector);
SINRdbstd=std(vector);

fileID=fopen('resultsMVDR.txt', 'a+');

```

```

fprintf(fileId, '%.3f %.3f %.3f %.3f %.3f %.3f %.3f
%.3f %.3f %.3f %.3f %.3f
\n', Dtheta_0min, Dtheta_0max, Dtheta_0mean, Dtheta_0std,
Dtheta_imin, Dtheta_imax, Dtheta_imean, Dtheta_istd, SINR
dbmin, SINRdbmax, SINRdbmean, SINRdbstd);
fclose(fileID);
end

```

## Μερος 2° Υλοποίηση RLS Beamformer

```

% RLS BeamFormer

RLSbeamformer();

function RLSbeamformer()
M=16; %Number Of elementaries in antenna
N=6; %Number of Incoming Signals
Pg=1; %Power of Incoming Signals
Pn=sqrt(0.1); %Power of Noise
%Incoming signals(polar_angle
theta=50:20:150; %Incoming Signals

%Calculate A teering incoming vector
A_vector=zeros(M,N); %Initialization of steering
incoming vector
for signal=0:1:(N-1) %Calculate Vectors
    for pos_elem=1:1:M

A_vector(pos_elem,signal+1)=exp((1j)*pi*(pos_elem-
1)*cosd(theta(1,(signal+1))));
    end
end
end

```

```

        %Initialize Algorithm
        %q=1
a=0.9; %forgetting factor
Q=50; %NumberOfSamples
Wrls=zeros(M,1); %Initialize weight-vector
delta=10^6;
invRxx=delta*eye(M,M); %Initialize Rxx^(-1)

        %Repetition Of RLS Algorithm
for q=2:1:Q
    g=Pg*randn(N,1); %Calculate Signals_modulation
    from normal Distribution
    n=Pn*randn(M,1); %Calculate noise From normal
    Distribution
    r0=g(1,1); %Reference Signal = Desirable
    Signal
    x=A_vector*g+n; %Calculate x_vector
    h=(a^(-1)*invRxx*x)/(1+a^(-1)*(x')*invRxx*x);
    %calculate h
    invRxx=(q/(q-1))*(a^(-1)*invRxx-a^(-
    1)*h*(x')*invRxx); %Calculate Rxx^(-1)
    Wrls(:,1)=Wrls(:,1)+h*(conj(r0)-(x')*Wrls(:,1));
    %Calculate Weight lifting

end

%Display Weight Vector after 50 repetitions
disp(Wrls(:,1));

%Plot Radiation Diagram

thetav=(0:0.1:180); %Initialization for scanning
angle in AF
a=zeros(M,size(thetav,2)); %Initialization for
variable a vector

for pos_elem=1:1:M
    b=exp((1j)*pi*(pos_elem-1)*cosd(thetav));
    a(pos_elem,:)=b;
end

AF=(Wrls(:,1)')*a; %radiation Diagram

```



```

%Normalize
AFN=abs (AF) /max (abs (AF) );

%if we want all the figures just delete % down from
%figure
%figure
plot (thetav,AFN);
ylabel ('|AF|/|AFmax|');
xlabel ('theta');
titleId=('Radiation Diagram RLS Q=50 repetitions');
title(titleId);
legend ('|AF|')

Dtheta=zeros (1,N); %Initialization for Deviation for
angles and |AF| max,zeros

%Calculate Direction Deviations for Desirable
[~,locs] = findpeaks(abs(AF)); %take the peaks from
|AF| and their index in matrix

Peaks=thetav(1,locs(1,1:end)); %Angles for the peaks
Dtheta(1,1)=min(abs(Peaks-theta(1,1))); %Min
Deviation Of Peak and incoming desirable angle

%Calculate Direction Deviations for Interference
[~,locs] = findpeaks(-abs(AF));
zeroes=thetav(1,locs(1,1:end)); %Angles for the
zeros
for i=2:1:N
    Dtheta(1,i)=min(abs(zeroes-theta(1,i))); %Min
Deviation Of Zero and incoming interference angle
end
%Display Deviations for every signal
disp(Dtheta);

%save results in a txt

fileId=fopen('resultsRLS.txt','w+');
for i=1:1:size(Dtheta,2)
    fprintf(fileId, ' %f',Dtheta(1,i));

end
fclose(fileId);
end

```

### Μερος 3<sup>ο</sup> (A) Υλοποίηση MUSIC Beamformer

```
%DoA MUSIC
MusicDoA()

function MusicDoA()
%Known Data
M=16; %Number Of elementaries in antenna
N=8; %Number of Incoming Signals
Pg=1; %Power for our Signals
SNRdb=10; %SNR in Db
SNR=10^(SNRdb/10); %SNR
Pn=Pg/SNR; %Power of Noise.From
SNR=Pdesirable/Pnoise
theta=50:10:120; %Angle of Signals

%Calculate A
A_vector=zeros(M,N); %Initialization of steering
incoming vector

for signal=1:1:N %Calculate steering incoming
vector
    for pos_elem=1:1:M

A_vector(pos_elem,signal)=exp((1j)*pi*(pos_elem-
1)*cosd(theta(1,signal)));
    end
end
Rgg=Pg*eye(N,N); %Correletion Matrix of incoming
signals modulation gi
%Irrelevant with each_other
Rnn=Pn*eye(M,M); %Correletion Matrix of noise in
every element of antenna
Rxx=A_vector*Rgg*(A_vector')+Rnn;
%Correletion Matrix of incoming signals Xi in every
element of antenna
[V , ~]=eig(Rxx); %Take eigen values In Diagonal
Matrix from Rxx Matrix,Sorted from Minimum to Maximum
by default from Matlab
%Take eigen vectors thats satisfy
A*V = V*D Sorted by
%default from Matlab V(:,1) goes to
eig D(1,1) which is the
%minimum and goes on
U=V(:,1:(M-N)); %Construct U Noise Vector
```

```

%Initialization for plotting Power Diagram
thetav=(0:0.1:180); %Initialization for scanning
angle in P
a=zeros(M,size(thetav,2)); %Initialization variable
a_vector
for pos_elem=1:1:M
b=exp((1j)*pi*(pos_elem-1)*cosd(thetav));
a(pos_elem,:)=b;
end

P=zeros(1,size(thetav,2));
for i=1:1:size(thetav,2)
    P(1,i)=1/((a(:,i)')*U*(U')*a(:,i)); %Calculate P
Power
end
Pdb=10*log10(abs(P)); %Convert to Db
PdbN=Pdb/max(Pdb); %Normalize from Pmax(Db)

%Plot P power
figure
plot(thetav,PdbN);
ylabel('P/Pmax');
xlabel('theta');
titleId=('Power Diagram MUSIC DoA');
title(titleId);
legend('P/Pmax(Db)')

    %Calculate Direction Deviations for Signals
    [~,locs] = findpeaks(abs(PdbN)); %take the peaks
from |P| and their index in matrix
    Dtheta=zeros(1,N); %Initialization for Deviation for
angles of incoming signals
    Peaks=thetav(1,locs(1,1:end));
for i=1:1:N
    Dtheta(1,i)=min(abs(Peaks-theta(i)));
end
    %Display Results
    disp(Dtheta)

    %save results in a txt

fileId=fopen('resultsMUSICa.txt','w+');
for i=1:1:size(Dtheta,2)
    fprintf(fileId, ' %f',Dtheta(1,i));

end
fclose(fileId);

```

end

### Μερος 3<sup>ο</sup> (B) Διακριτική Ικανότητα MUSIC Beamformer

```
%DoA MUSIC Find distinctive ability
MusicDistinctive();
function MusicDistinctive ()
%Loop for check smaller and smaller delta until we
have a same peak for 2
%different signals
for delta=2:(-0.01):0

    %Known Data
    M=16; %Number Of elementaries in antenna
    N=8; %Number of Incoming Signals
    Pg=1; %Power for our Signals
    SNRdb=10; %SNR in Db
    SNR=10^(SNRdb/10); %SNR
    Pn=Pg/SNR; %Power of Noise.From
    SNR=Pdesirable/Pnoise

    %Initialize Angles of Incoming Signals
    theta=zeros(1,N);
    for i=1:1:N
        theta(1,i)=50+(i-1)*delta;
    end

    %Calculate A
    A_vector=zeros(M,N); %Initialization of steering
incoming vector

    for signal=1:1:N %Calculate steering incoming
vector
        for pos_elem=1:1:M

            A_vector(pos_elem,signal)=exp((1j)*pi*(pos_elem-
1)*cosd(theta(1,signal)));
        end
    end

    Rgg=Pg*eye(N,N); %Correletion Matrix of incoming
signals modulation gi
    %Irrelevant with each_other
    Rnn=Pn*eye(M,M); %Correletion Matrix of noise in
every element of antenna
```

```

    Rxx=A_vector*Rgg*(A_vector')+Rnn;
%Correletion Matrix of incoming signals Xi in every
element of antenna
    [V , ~]=eig(Rxx); %Take eigen values In
Diagonal Matrix from Rxx Matrix,Sorted from Minimum
to Maximum by default from Matlab
    %Take eigen vectors thats satisfy
A*V = V*D Sorted by
    %default from Matlab V(:,1) goes to
eig D(1,1) which is the
    %minimum and goes on
    U=V(:,1:(M-N)); %Construct U Noise Vector

    thetav=(0:0.01:180); %Initialization for scanning
angle in P
    a=zeros(M,size(thetav,2)); %Initialization
variable a_vector
    for pos_elem=1:1:M
        b=exp((1j)*pi*(pos_elem-1)*cosd(thetav));
        a(pos_elem,:)=b;
    end

    P=zeros(1,size(thetav,2));
    for i=1:1:size(thetav,2)
        P(1,i)=1/((a(:,i)')*U*(U')*a(:,i));
%Calculate P Power
    end
    Pdb=10*log10(abs(P)); %Convert to Db
    PdbN=Pdb/max(Pdb); %Normalize from Pmax

    %Plot P power
    %?f we want all the figures just delete % down
from %figure
    %figure
    plot(thetav,PdbN);
    ylabel('P/Pmax(Db)');
    xlabel('theta');
    titleId=['Power Diagram Music DoA Delta='
num2str(delta) 'SNR(Db)=' num2str(SNRdb)];
    title(titleId);
    legend('P/Pmax(Db)');

    %Check for Peaks
    pk=findpeaks(PdbN);
    Lowest_Threshold=0.3; %In Normalized Db of
radiation Diagram

```

```

        sizeOfRealPeaks=0; %Initialize conter
        for i=1:1:size(pk,2) %Cut Low peaks to keep only
from incoming signals
            if pk(i)>=Lowest_Threshold
                sizeOfRealPeaks=sizeOfRealPeaks+1; %Peaks
that have a high peak in radiation diagram
            end
        end
        if sizeOfRealPeaks<N %if we have less peaks than
Number of Signals then Display delta and break

            %Display Results
            disp(delta);

            %save results in a txt

            fileId=fopen('resultsMUSICb.txt','w+');
            fprintf(fileId,'%f',delta);
            fclose(fileId);
            break;
        end
    end
end
end

```