



Random values and Random Number Generators

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Overview

- Seminar (PV181 Masaryk Uni, Brno, Czech)
 - Preparation for testing
 - Example how courses look like at Masaryk Uni.
- Random number generators theory
- Installation of the environment (Windows)
 - Copy repository
 - Installation python packages and JN
- Tasks
 - Example how to solve first task
 - Your work on the next tasks (hands on)

You will learn

- What types of RNG you can find in libraries.
- What RNGs are (in)apropriate for crypto.
- How to generate secure random values:
 - in python, C
- Why standard rand() and others (e.g. Mersenne Twister) are insecure.

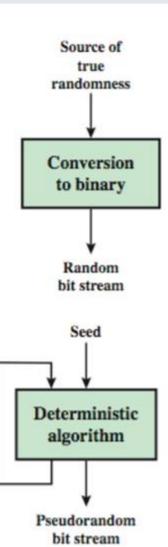
RNG types

True random (TRNG)

- Source: physical device (noise) radio decay, thermal noise, ...
- non-deterministic, aperiodic, slow

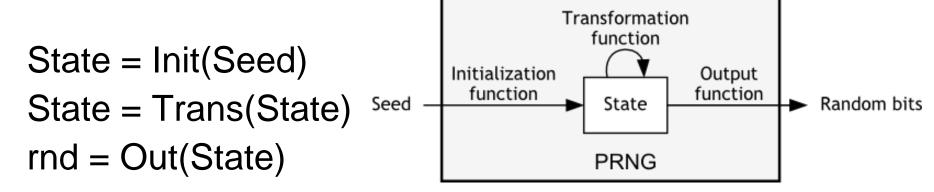
Pseudo random (PRNG)

- Source: software function
- **deterministic**, periodic, very fast



PRNG

defined by 3 functions: Init, Transform, Output



Cryptographically secure PRNG (CSPRNG)

 generated data leaks no information about next or previous values ⇒ no info about Seed, State

Tasks

- Determinism of PRNG (Tasks 1-7)
 - Seed or internal determine entire sequence
- Standard PRNG
 - Implement standard ANSI C generator (Task 8)
 - Verify your implementation (Task 9)
 - Generate from different starting point (Task 10)
 - Invert the generation process (Task 11)
- Small state attack
 - Generate key, encrypt and decrypt message (Task 12,13)
 - Find the key and decrypt the message (Task 14)

Example ANSI C portable functions

```
static unsigned long int next = 1;
int rand(void) // RAND_MAX assumed to be 32767
      next = next * 1103515245 + 12345;
      return (unsigned int)(next/65536) % 32768;
void srand(unsigned int seed)
      next = seed;
```

Standard library functions

ANSI C(rand), Java(java.util.random),...

- very fast but very insecure LCG generator
 Linear Congruential Generator(LCG)
- $s_{n+1}=a^*s_n+b \mod m$ (fixed constants a,b,c)
- 1. rnd value = State ⇒ next rnd easily computed
- 2. Trans is simple: s_{n+1} is *linear func of* $s_n \Rightarrow$ previous states (hence rnd values) easily computed $s_n = (s_{n+1} b)/a \mod m$ (/a is inverse modulo!)

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Practice

CSPRNG:

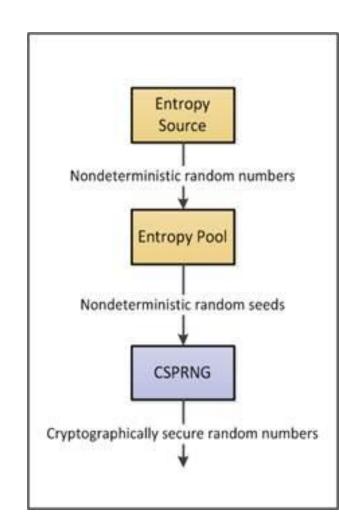
seeded from entropy pool

Entropy pool:

- stores entropy
- usage decreases entropy in pool

TRNG (entropy source):

repeatedly adds entropy to pool



TRNG and pools

Linux: two entropy pools (files) dev/(u)random

- keyboard timings, mouse movements, IDE timings
- /dev/random
 - always produces some entropy but,
 - blocking can block the caller until entropy available (entropy estimation)
- /dev/urandom
 - amount of entropy not guaranteed
 - always returns quickly (non blocking)

Windows: similar to Linux

binary register HKEY_LOCAL_MACHINE\SYSTEM\RNG\Seed

Unix: methods and quality

Good sources(C):

- initialized random/urandom
- <u>getrandom()</u> + flags:
 - source: random or urandom
 - blocking or non-blocking (also blocks until initialized)
- get_random_bytes() kernel space
- similar in Python: <u>os.urandom()</u>, <u>os.getrandom()</u>, secrets.token_bytes()

Weak sources:

 rand, time(rdtsc instruction, clock func,...), uninitialized urandom

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Practice (python)

- Clone the repository
 - git clone <u>https://github.com/sysox/Maputo_Workshop.git</u>
- Open powershell and go to repository
- Install
 - pip install -r .\requirements.txt
- Execute the jupyter notebook
 - python -m notebook
- Open JN with tasks
 - PV181_RNG_python.ipynb
- Solve the tasks:
 - If stacked 1. ask me 2. use JN with the solution