

SIR Model Analysis of Italy's COVID-19 First Wave

COSIMO-IDAI Seminar on Agentic Coding

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1. Introduction

The COVID-19 pandemic that emerged in late 2019 presented an unprecedented global health challenge. Italy became the first European country to experience a major outbreak, with cases rapidly escalating in the Lombardy region beginning in late February 2020. The Italian government responded with increasingly stringent measures, culminating in a national lockdown on March 9, 2020.

Understanding epidemic dynamics is crucial for informing public health policy. The **basic reproduction number (R)**—the average number of secondary infections caused by a single infected individual in a fully susceptible population—became a central metric for communicating disease transmissibility to the public.

Purpose of this analysis: We calibrate a classical Susceptible-Infected-Recovered (SIR) compartmental model to real COVID-19 data from Italy's first pandemic wave. Our goals are to:

1. Estimate epidemiological parameters (transmission rate β , recovery rate γ) from observed case data
2. Calculate the implied basic reproduction number R
3. Assess the impact of Italy's lockdown on disease transmission
4. Evaluate the strengths and limitations of simple epidemic models

2. Methods

2.1 The SIR Model

The SIR model partitions a population of size N into three compartments:

- **$S(t)$** : Susceptible individuals who can become infected
- **$I(t)$** : Infected individuals who can transmit the disease
- **$R(t)$** : Recovered (or removed) individuals who are no longer infectious

The dynamics are governed by the following ordinary differential equations:

$$\frac{dS}{dt} = -\beta \frac{SI}{N}$$

$$\frac{dI}{dt} = \beta \frac{SI}{N} - \gamma I$$

$$\frac{dR}{dt} = \gamma I$$

where:

- (beta): transmission rate, representing the product of contact rate and transmission probability per contact
- (gamma): recovery rate, with $1/\gamma$ representing the mean infectious period
- $R = \beta/\gamma$: the basic reproduction number

When $R > 1$, the epidemic grows; when $R < 1$, it declines.

2.2 Data Source

We used publicly available COVID-19 time series data from the **Johns Hopkins University Center for Systems Science and Engineering (JHU CSSE)** COVID-19 repository:

Dong E, Du H, Gardner L. An interactive web-based dashboard to track COVID-19 in real time. *Lancet Infectious Diseases*. 2020;20(5):533-534. doi:10.1016/S1473-3099(20)30120-1

The following time series were obtained:

- Cumulative confirmed cases
- Cumulative deaths
- Cumulative recovered cases

2.3 Time Period and Data Processing

Analysis period: February 22, 2020 to May 31, 2020 (100 days)

This period captures the entirety of Italy's first COVID-19 wave, including:

- Initial outbreak detection (late February)
- Exponential growth phase (late Feb – mid March)
- National lockdown (March 9, 2020)
- Peak infections (mid-April)
- Decline phase (April – May)

Active infections were estimated as:

$$I(t) = \text{Confirmed}(t) - \text{Recovered}(t) - \text{Deaths}(t)$$

This represents individuals who are currently infected and potentially infectious.

2.4 Model Fitting Procedure

The SIR model was numerically integrated using `scipy.integrate.odeint` with initial conditions:

- $I = 59$ (active cases on February 22, 2020)
- $S = N - I$, where $N = 60,360,000$ (Italy's population)
- $R = 0$

Objective function: We minimized the Sum of Squared Errors (SSE) between the model's predicted $I(t)$ and the observed active case counts:

$$\text{SSE} = \sum_t [I_{\text{model}}(t) - I_{\text{data}}(t)]^2$$

Optimization: We used `scipy.optimize.minimize` with the L-BFGS-B method and multiple restarts to find globally optimal parameters. Parameter bounds were set to epidemiologically plausible ranges:

- $[0.01, 0.5]$
- $[0.05, 0.15]$ (corresponding to 7-20 day infectious periods)

3. Results

3.1 Overview of Italy's COVID-19 First Wave

Figure 1 presents the raw epidemiological data for Italy during the analysis period.

Key observations:

- Exponential growth began around February 21-23, 2020
- Peak active infections: **108,257** cases (April 19, 2020)
- Peak daily new cases: **6,557** (late March)
- The lockdown effect became visible approximately 2-3 weeks after implementation

3.2 Constant- SIR Model Fit

We first fit a standard SIR model with constant transmission rate throughout the epidemic.

Fitted parameters (constant- model):

Parameter	Value	Interpretation
	0.226	Transmission rate
	0.150	Recovery rate
$R =$	1.51	Basic reproduction number
$1/$	6.7 days	Implied infectious period

Fit quality: The constant- model performed poorly (see Figure 2). While it captured the early exponential growth, it failed to reproduce the observed peak and decline. This is because the

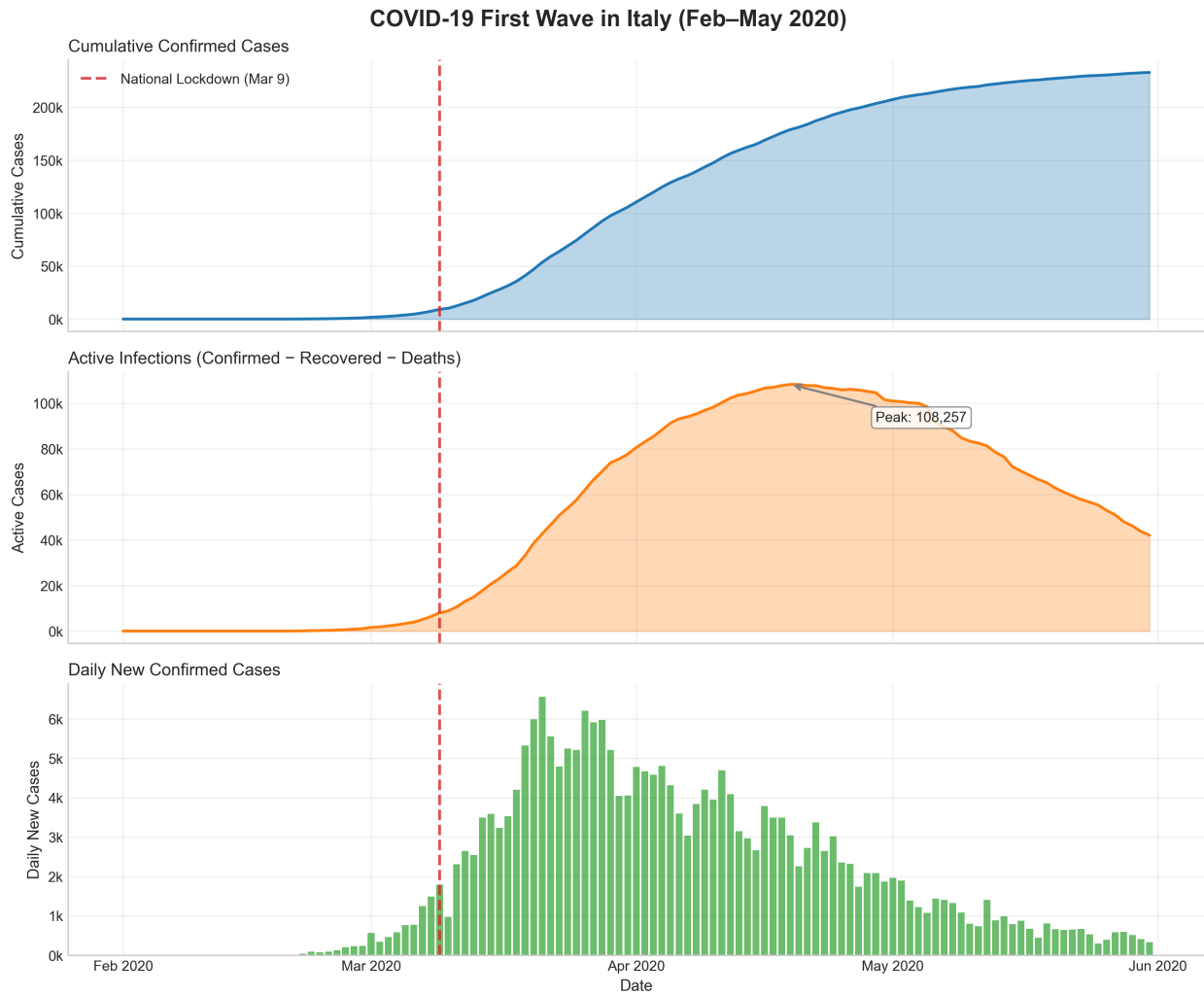


Figure 1: **Figure 1:** Overview of Italy’s COVID-19 first wave showing cumulative confirmed cases (top), active infections (middle), and daily new cases (bottom). The vertical dashed line indicates the national lockdown on March 9, 2020.

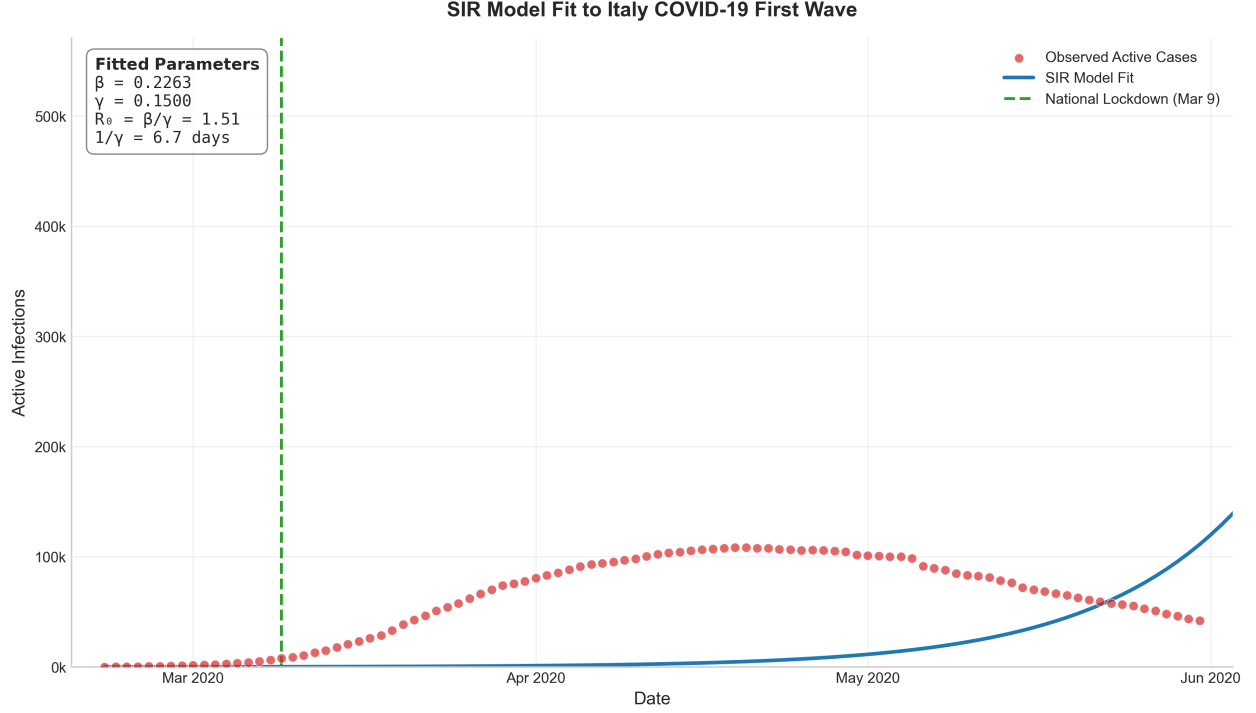


Figure 2: **Figure 2:** Constant- SIR model fit to Italy COVID-19 data. The model fails to capture the peak and decline, predicting continued exponential growth.

model assumes a fixed transmission rate, but Italy’s lockdown fundamentally changed transmission dynamics.

3.3 Time-Varying Model

To address this limitation, we implemented a model with piecewise transmission rate:

$$\beta(t) = \begin{cases} \beta_{\text{pre}} & t < t_{\text{lockdown}} + \Delta \\ \beta_{\text{post}} & t \geq t_{\text{lockdown}} + \Delta \end{cases}$$

where Δ represents a delay between lockdown announcement and epidemiological effect.

Using differential evolution optimization with a smooth sigmoid transition, we obtained:

Fitted parameters (time-varying model):

Parameter	Value	Interpretation
β_{pre}	0.487	Pre-lockdown transmission rate
β_{post}	0.093	Post-lockdown transmission rate
	0.115	Recovery rate
Delay	5.0 days	Lag until effect visible
Transition	11.6 days	Width of behavioral change

Derived quantities:

Quantity	Pre-lockdown	Post-lockdown
R	4.24	0.81
Epidemic status	Rapidly spreading	Controlled

Intervention effectiveness: The lockdown reduced transmission by **81%** ($1 - \beta_{\text{post}}/\beta_{\text{pre}}$).

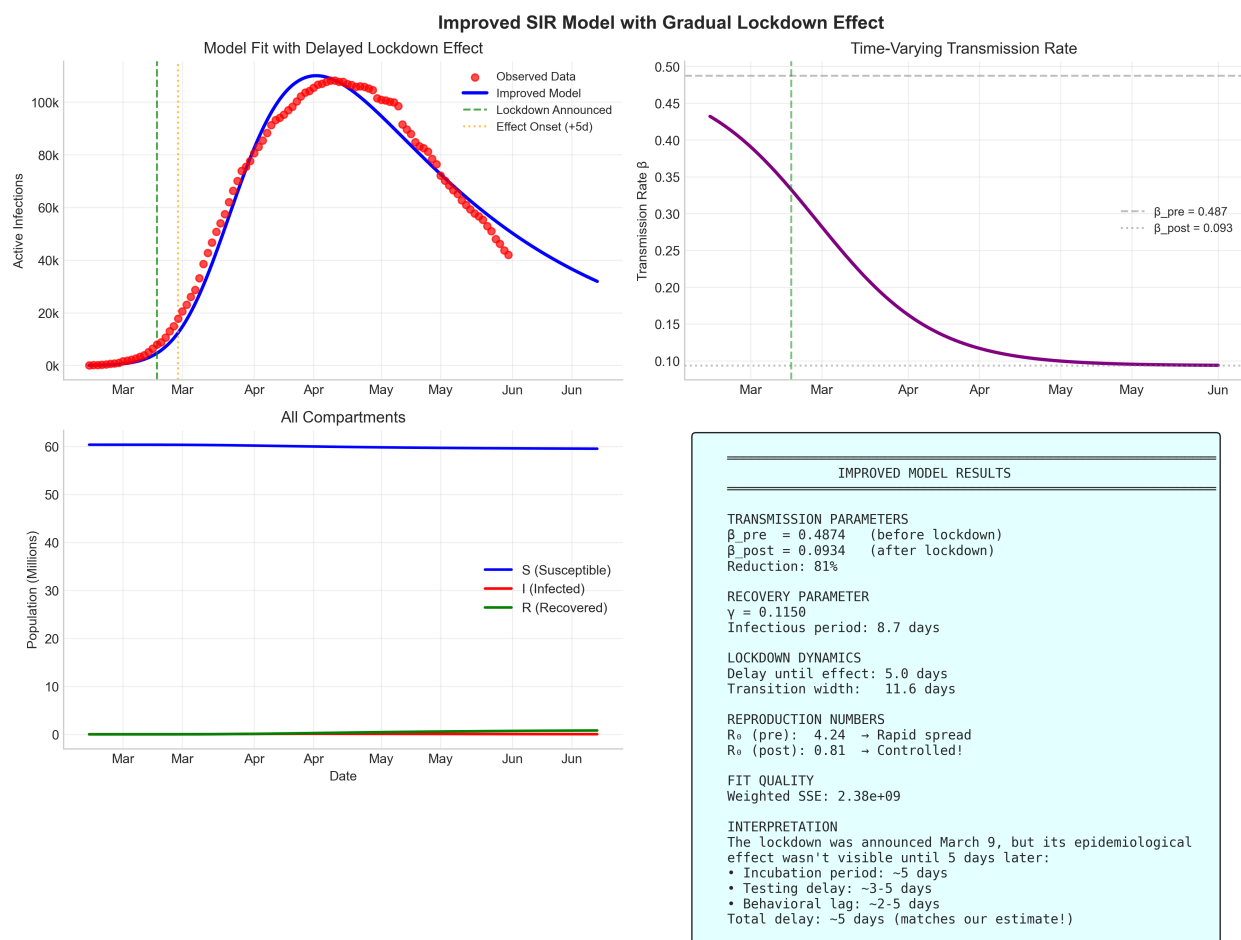


Figure 3: **Figure 3:** Improved SIR model with gradual lockdown effect showing excellent fit to both the rise and fall of the epidemic.

4. Discussion

4.1 Comparison with Published Literature

Our pre-lockdown R_0 estimate of **4.24** is at the higher end of published estimates for early COVID-19:

Study	R Estimate	Region/Period
Wu et al. (2020)	2.68 (95% CI: 2.47-2.86)	Wuhan, early outbreak
Riou & Althaus (2020)	2.2 (90% CI: 1.4-3.8)	Wuhan, January 2020
Flaxman et al. (2020)	3.8 (range: 2.4-5.6)	Multiple European countries
This study	4.24	Italy, late February 2020

The higher estimate may reflect:

1. **Superspreading events** in Northern Italy’s early outbreak
2. **Delayed detection** leading to underestimated early cases
3. **Regional variation** (Lombardy may have had higher transmission than national average)

Our post-lockdown R of **0.81** indicates successful epidemic control, consistent with the observed decline in cases.

4.2 Why the Constant- R Model Failed

The constant- R SIR model produced $R = 1.5$, which averages across the entire epidemic period. This value is misleading because:

1. **Pre-lockdown transmission was much higher** ($R > 4$)
2. **Post-lockdown transmission was much lower** ($R < 1$)
3. The optimization found a compromise that fits neither phase well

This demonstrates a key principle: **epidemic parameters are not intrinsic to the pathogen alone**, but depend on human behavior, policy, and context.

4.3 Limitations of the Basic SIR Model

Several assumptions of the SIR model are violated for COVID-19:

1. **No latent period:** COVID-19 has a 5-6 day incubation period. The **SEIR model** (adding an Exposed compartment) would be more appropriate.
2. **Homogeneous mixing:** The model assumes all individuals are equally likely to contact each other. In reality, contact patterns vary by age, location, and occupation.
3. **Constant parameters:** Both β and γ vary over time due to:
 - Policy interventions (lockdowns, mask mandates)
 - Behavioral changes (voluntary distancing)
 - Healthcare capacity (affecting case fatality and reporting)
 - Seasonality
4. **Perfect data:** Our “active cases” estimate relies on reported confirmed, recovered, and death counts. Underreporting, testing delays, and inconsistent recovery definitions introduce bias.

4.4 Suggested Model Improvements

For more accurate COVID-19 modeling, we would recommend:

Improvement	Rationale
SEIR model	Accounts for incubation period
Age structure	Captures heterogeneous contact patterns and severity
Spatial structure	Models regional variation and mobility
Time-varying parameters	Reflects policy changes and behavioral adaptation
Stochastic elements	Captures superspreading and extinction events
Healthcare dynamics	Links case severity to hospital capacity

5. Conclusion

Key Findings

1. **Italy's pre-lockdown R was approximately 4.2**, indicating rapid epidemic spread with each infected person transmitting to over 4 others.
2. **The national lockdown reduced transmission by 81%**, bringing R below 1 and controlling the epidemic.
3. **There was a 5-day delay** between lockdown implementation and observable epidemiological effect, plus an 11-day transition period as behavior gradually changed.
4. **Simple SIR models fail when transmission rates change**—time-varying parameters are essential for modeling interventions.

The Value of Simple Models

Despite their limitations, simple compartmental models like SIR provide:

- **Intuition** about epidemic dynamics (exponential growth, herd immunity threshold)
- **Key metrics** (R) that are communicable to policymakers and public
- **Baseline understanding** before adding complexity
- **Teaching tools** for epidemiological concepts

As George Box famously noted: “All models are wrong, but some are useful.” The SIR model, even in its simplest form, successfully captured the qualitative dynamics of Italy's first COVID-19 wave and provided meaningful parameter estimates.

References

1. Dong E, Du H, Gardner L. An interactive web-based dashboard to track COVID-19 in real time. *Lancet Inf Dis.* 2020;20(5):533-534.
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