

## 1. Windows-based E2DISP Model

Figure 1 shows the windows-based E2DISP model that solves the advection-dispersion-reaction equations for BOD (1) and DO (2) using the finite segment method.

$$\frac{d\ell}{dt} = -u \frac{\partial \ell}{\partial x} + E \frac{\partial^2 \ell}{\partial x^2} - k \ell + W_\ell \quad (1)$$

$$\frac{dc}{dt} = -u \frac{\partial c}{\partial x} + E \frac{\partial^2 c}{\partial x^2} - k \ell + \beta(c_s - c) + W_c \quad (2)$$

The FORTRAN coding of the model is given in Koh (2004). The step-by-step instructions on how to run this model are presented below.

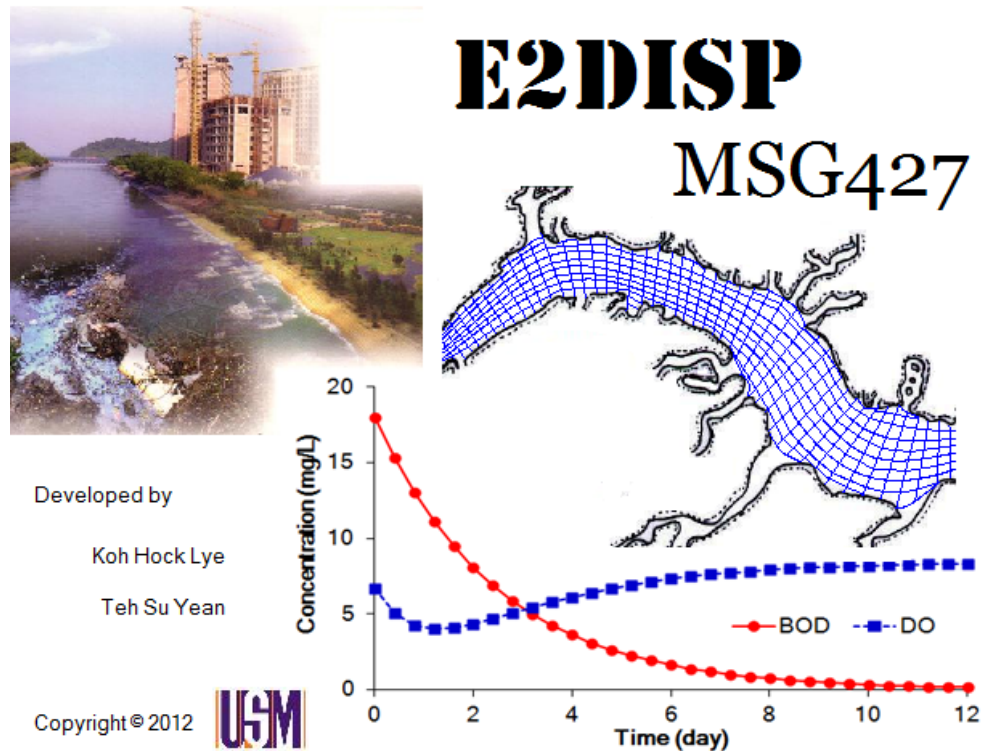


Figure 1: Windows-based E2DISP model

## 2. An Illustrative Example (Example 6.3, Koh 2004)

The river segmentation as shown in Figure 2 is used as an illustrative example. Figure 2 will be displayed when the link [Figure](#) in E2DISP input window (see Figure 3) is clicked.

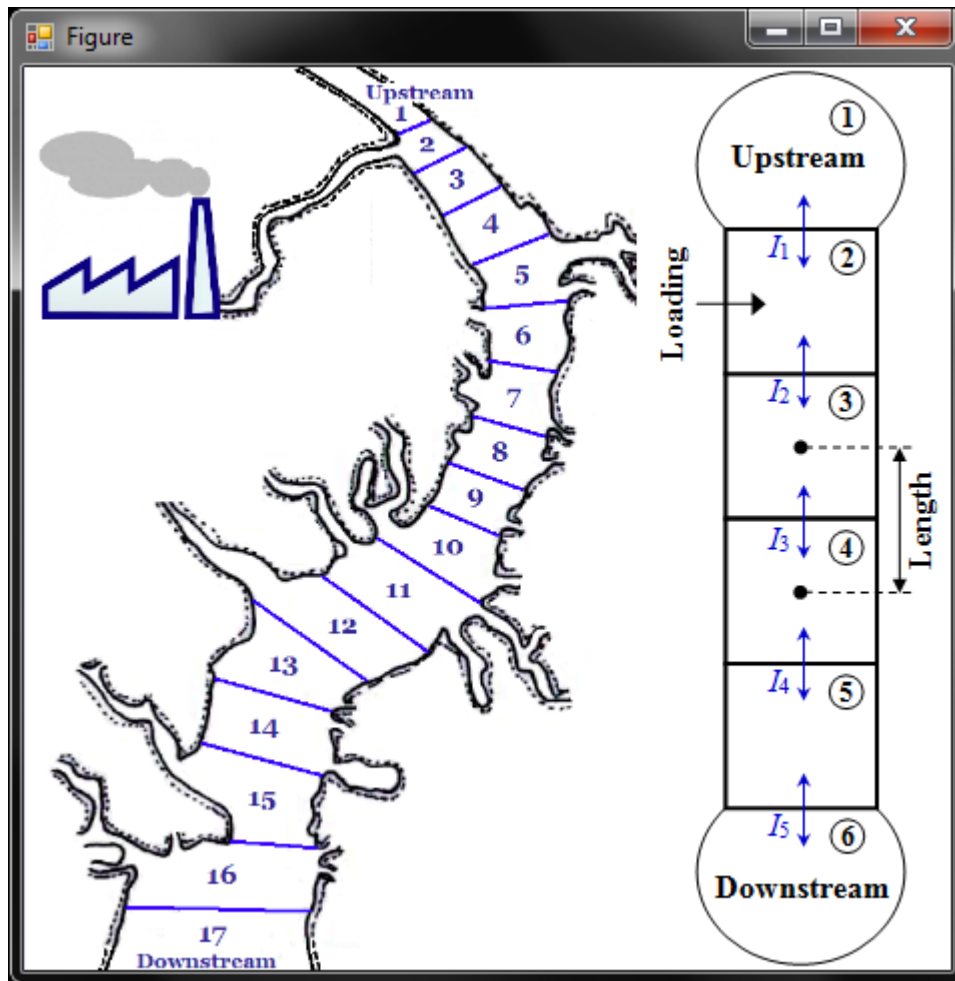


Figure 2: An illustrative river example

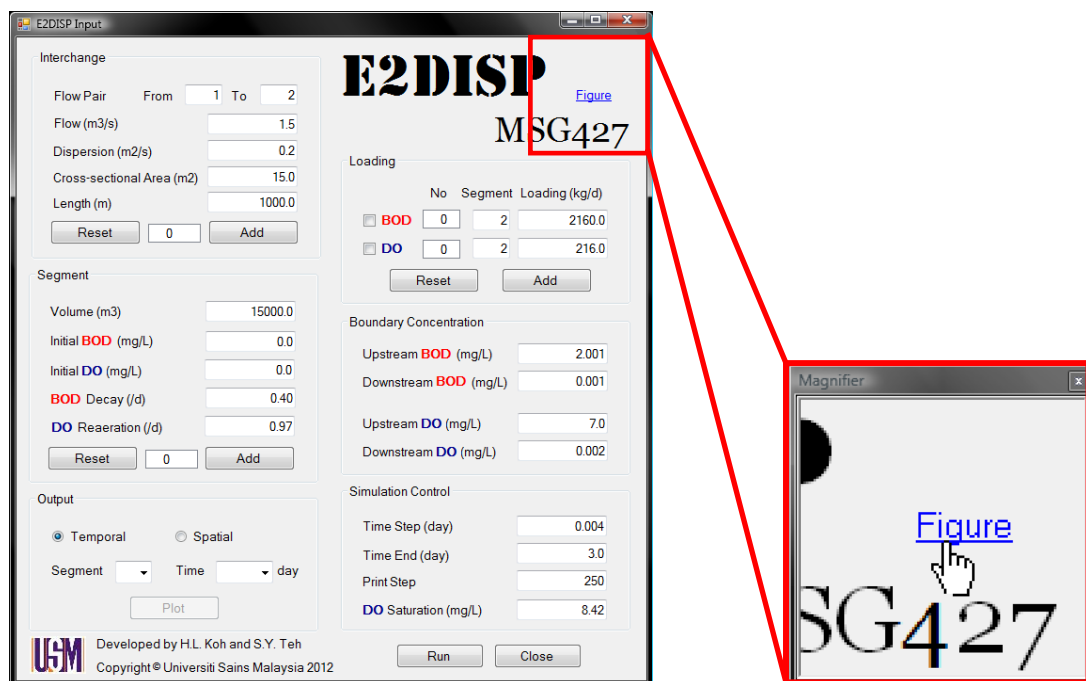


Figure 3: The link Figure in E2DISP input window

## 2.1 *Description of River*

For convenience of initialization, we treat this river as a uniform river with constant cross-sectional area and constant flow. In reality, the cross-sectional area and flow will increase in the downstream direction. There is a small factory and a small farm releasing wastewater into this river at an upstream location. We want to simulate how this wastewater will change BOD and DO concentrations as it moves downstream. We divide this river into several segments. In Figure 2 (left), we have 17 segments with segment 1 as the upstream segment and segment 17 as the downstream segment. Segment 2 is located at the upstream and segment 16 is located at the downstream end. The length of each and every segment is 1000.0 m with a constant cross-sectional area of 15.0 m<sup>2</sup>. The volume of water contained in each segment is 15000.0 m<sup>3</sup>. We assume that the flow in this river is 1.5 m<sup>3</sup>/s through the entire stretch, which implies a river velocity of 0.1 m/s. We further assume that the wastewater from the factory/farm containing 50 mg/L BOD and 5 mg/L of DO is discharged into segment 2 at the flow rate of 0.5 m<sup>3</sup>/s. The decay rate for BOD is 8.64 d<sup>-1</sup> while the DO reaeration rate is 0.97 d<sup>-1</sup> and DO saturation level is 8.42 mg/L. Initial BOD and DO concentrations are zero for all segments. We need to impose the upstream and downstream boundary conditions for BOD and DO. The upstream BOD is 2.001 mg/L while the downstream BOD is 0.001 mg/L. The upstream DO is 7.0 while the downstream DO is 0.002 mg/L. The dispersion coefficient is 0.2 m<sup>2</sup>/s. We have chosen the numbers so that no same number will appear twice in the input screen.

## 2.2 *How to Start Simulation*

As a start, we suggest that you consider a simulation with only 4 segments (2-5) and two boundary segments (1 and 6) as shown in Figure 2 (right). There will be five interfaces ( $I_1 - I_5$ ) which we call interchange or exchange pairs. The first interchange is the interface between the upstream segment 1 and segment 2. In the same way, interchange 5 is the interface between segment 4 and the downstream segment 6. When you double click on E2DISP.exe, the E2DISP input window (Figure 4) will be displayed with default numbers that reflect the river that we have chosen to simulate. There are FIVE groups of input data: (a) **Interchange** (Figure 5), (b) **Segment** (Figure 6), (c) **Loading** (Figure 7), (d) **Boundary Concentration** (Figure 8), (e) **Simulation Control** (Figure 9)

and one group of output data: (f) **Output** (Figure 10). The default values and their respective units will be displayed on the input window, prompting you to either use them as is OR modify them as you wish. Note that the button <Plot> in the Output group will remain deactivated until the model is run successfully.

**E2DISP** [Figure](#)  
**MSG427**

**Interchange**

Flow Pair From  To

Flow (m3/s)

Dispersion (m2/s)

Cross-sectional Area (m2)

Length (m)

**Segment**

Volume (m3)

Initial **BOD** (mg/L)

Initial **DO** (mg/L)

**BOD** Decay (/d)

**DO** Reaeration (/d)

**Loading**

	No	Segment	Loading (kg/d)
<input type="checkbox"/> <b>BOD</b>	<input type="text" value="0"/>	<input type="text" value="2"/>	<input type="text" value="2160.0"/>
<input type="checkbox"/> <b>DO</b>	<input type="text" value="0"/>	<input type="text" value="2"/>	<input type="text" value="216.0"/>

**Boundary Concentration**

Upstream **BOD** (mg/L)

Downstream **BOD** (mg/L)

Upstream **DO** (mg/L)

Downstream **DO** (mg/L)

**Simulation Control**

Time Step (day)

Time End (day)

Print Step

**DO** Saturation (mg/L)

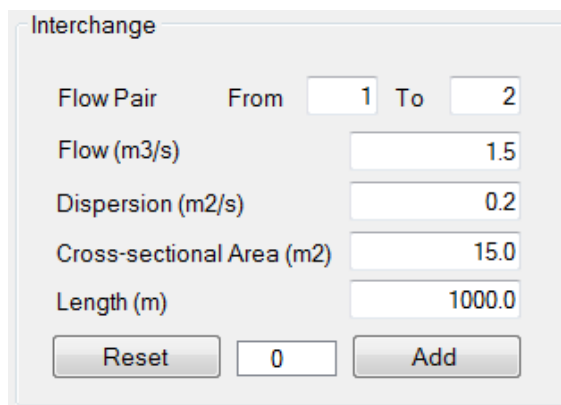
**Output**

☒ Temporal ☐ Spatial

Segment  Time  day

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Figure 4: Windows-based E2DISP input window



Interchange

Flow Pair From  To

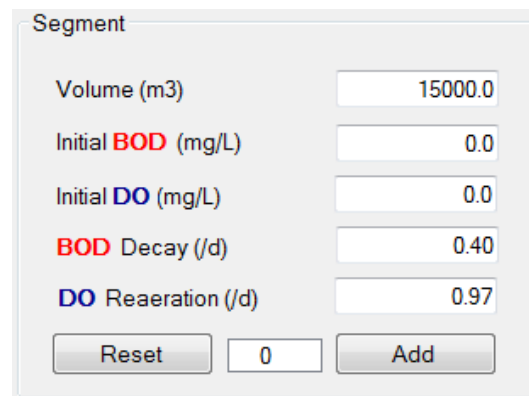
Flow (m3/s)

Dispersion (m2/s)

Cross-sectional Area (m2)

Length (m)

Figure 5: Interchange input data



Segment

Volume (m3)

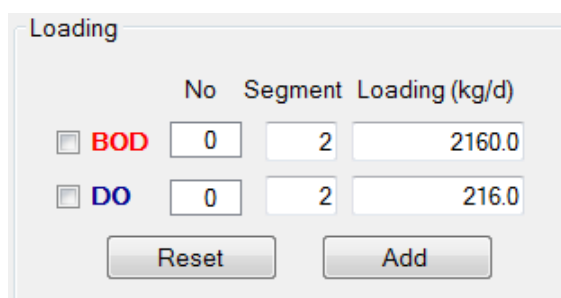
Initial **BOD** (mg/L)

Initial **DO** (mg/L)

**BOD** Decay (/d)

**DO** Reaeration (/d)

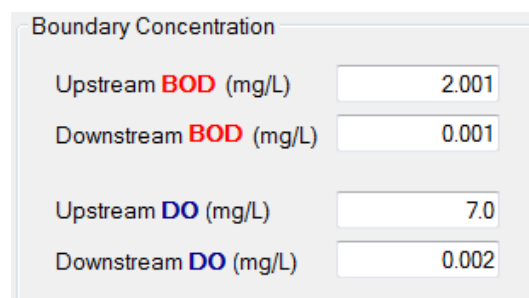
Figure 6: Segment input data



Loading

	No	Segment	Loading (kg/d)
<input type="checkbox"/> <b>BOD</b>	<input type="text" value="0"/>	<input type="text" value="2"/>	<input type="text" value="2160.0"/>
<input type="checkbox"/> <b>DO</b>	<input type="text" value="0"/>	<input type="text" value="2"/>	<input type="text" value="216.0"/>

Figure 7: Loading input data



Boundary Concentration

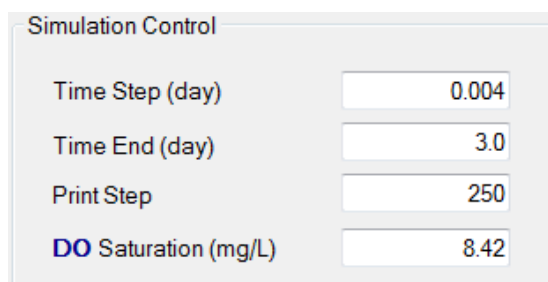
Upstream **BOD** (mg/L)

Downstream **BOD** (mg/L)

Upstream **DO** (mg/L)

Downstream **DO** (mg/L)

Figure 8: Boundary input data



Simulation Control

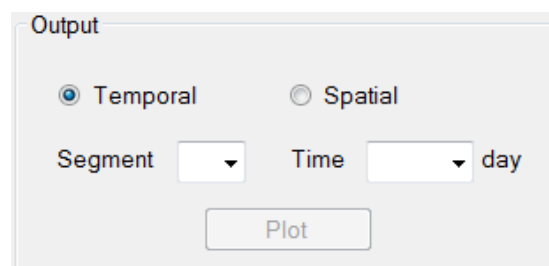
Time Step (day)

Time End (day)

Print Step

**DO** Saturation (mg/L)

Figure 9: Simulation control input



Output

☒ Temporal ☐ Spatial

Segment  Time  day

Figure 10: Output Graph Control

## Interchange

We have decided to simulate with 5 interchanges, with each and every interchange taking the same values as appeared on the screen. To input the first interchange between the upstream segment 1 and segment 2, you click the <Add> button once. Then the displayed values will be assumed for the FIRST interchange in the internal input file, and the number [ 1 ] will appear between <Reset> and <Add>. To input the second interchange between the segment 2 and segment 3, change the numbering in Flow Pair (From 2 To 3) and then click <Add> a second time with the SAME values displayed to input SECOND interchange values into the input file. Then [ 2 ] will appear between

<Reset> and <Add>. Repeat this process a total of 5 times in order to input the pre-set values for the 5 interchanges. This completes the input of the interchange (total of 5).

### **Segment**

Click <Add> just once to input the preset values of segments into the input files for segments. Then [ 1 ] will appear between <Reset> and <Add>. This means that segment 2 has been assigned the values as indicated on the segment screen. Then you click <Add> second time to input values for segment 3. You continue to click <Add> for the third and fourth times to complete input for segments (total of 4, segments 2 – 5).

### **Boundary**

You accept the preset values of upstream and downstream boundary conditions. You may change the preset values as you wish.

### **Loading**

Unless specified here in this segment, all segments have zero loadings. For this example, the BOD and DO loadings are discharge into segment 2, i.e. the first segment immediately after the upstream segment. Select the BOD and DO checkboxes and click <Add> to add the BOD loading of 2160.0 kg/d and DO loading of 216.0 kg/d to segment 2. You may add loading to other segments as you wish.

### **Simulation Control**

The Time Step  $\Delta t$ , Time End and Print Step for the numerical calculation should be input in this section. Further, the DO saturation of 8.42 mg/L is specified here. The time step is chosen depending on the characteristics of the problem. A larger time step can be used when the solution varies slowly while smaller time steps are used where the solution varies rapidly. The value for Time End determines when the numerical simulation will end. Print Step controls the interval of output being displayed. For this example, Time Step = 0.004 day, Time End = 3.0 day and Print Step = 250. This means the numerical calculation is performed for  $\frac{\text{Time End}}{\text{Time Step}} = \frac{3.0}{0.004} = 750$  iterations. The output will be printed for every 125 (Print Step) iterations, i.e. every 1.0 day.

### You are Ready to RUN.

Click <Run> once to execute the model simulation (Figure 11). If all are set up properly then the simulation results as shown in Figure 12 will appear in a pop up window. The output is also saved in a text file named “answer.txt” (Figure 13) to enable plotting by other software such as Excel. If the model is executed successfully, the <Plot> button in the Output group will be activated. You may select to plot temporal (concentration vs. time) or spatial (concentration vs. segment) plots. For example, selecting Temporal plot and Segment 2 in the drop down box (Figure 14) will display the concentration time series for segment 2 when the button <Plot> is clicked. If Spatial plot and Time = 2.0 day are selected (Figure 15), the spatial concentration for 2.0 day will be displayed when the button <Plot> is clicked. Good Luck.

**E2DISP** Figure  
**MSG427**

**Interchange**

Flow Pair From  To

Flow (m3/s)

Dispersion (m2/s)

Cross-sectional Area (m2)

Length (m)

**Segment**

Volume (m3)

Initial **BOD** (mg/L)

Initial **DO** (mg/L)

**BOD** Decay (/d)

**DO** Reaeration (/d)

**Output**

☒ Temporal ☐ Spatial

Segment  Time  day

**Loading**

	No	Segment	Loading (kg/d)
<input checked="" type="checkbox"/> <b>BOD</b>	<input type="text" value="1"/>	<input type="text" value="2"/>	<input type="text" value="2160.0"/>
<input checked="" type="checkbox"/> <b>DO</b>	<input type="text" value="1"/>	<input type="text" value="2"/>	<input type="text" value="216.0"/>

**Boundary Concentration**

Upstream **BOD** (mg/L)

Downstream **BOD** (mg/L)

Upstream **DO** (mg/L)

Downstream **DO** (mg/L)

**Simulation Control**

Time Step (day)

Time End (day)

Print Step

**DO** Saturation (mg/L)

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Figure 11: Setup model ready to run

BOD							DO					
Time	Segment 1	Segment 2	Segment 3	Segment 4	Segment 5	Segment 6	Segment 1	Segment 2	Segment 3	Segment 4	Segment 5	Segment 6
0.000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000
1.000	2.0010	17.7730	16.9686	16.1381	15.1716	0.0010	7.0000	7.7894	7.1491	6.6064	6.1488	0.0020
2.000	2.0010	17.7753	16.9894	16.2376	15.4913	0.0010	7.0000	7.7893	7.1479	6.6006	6.1295	0.0020
3.000	2.0010	17.7753	16.9894	16.2377	15.4915	0.0010	7.0000	7.7893	7.1479	6.6005	6.1294	0.0020

Figure 12: Simulated concentrations for each segment at selected times

The result is saved in answer.txt.  
Please use Wordpad to open the file.

OK

Time	BOD1	BOD2	BOD3	BOD4	BOD5	BOD6	DO1	DO2	DO3	DO4	DO5	DO6
0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000
1.000	2.001	17.773	16.969	16.138	15.172	0.001	7.000	7.789	7.149	6.606	6.149	0.002
2.000	2.001	17.775	16.989	16.238	15.491	0.001	7.000	7.789	7.148	6.601	6.130	0.002
3.000	2.001	17.775	16.989	16.238	15.492	0.001	7.000	7.789	7.148	6.601	6.129	0.002

For Help, press F1

Figure 13: Simulation results saved in “answer.txt”

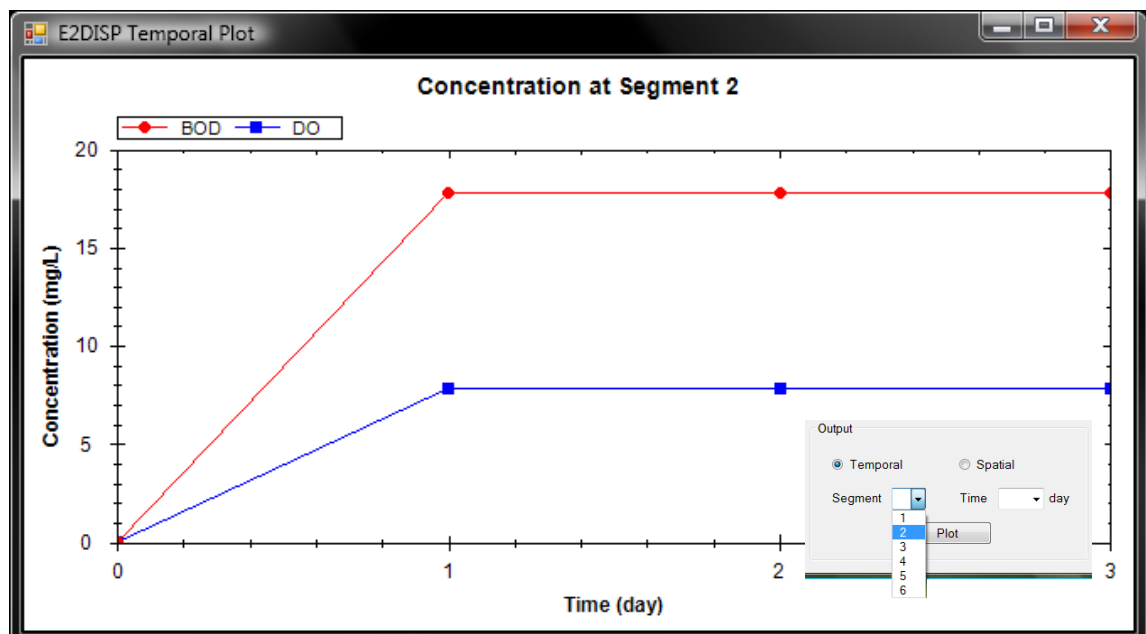


Figure 14: Graph of simulated concentration vs. time for Segment 2



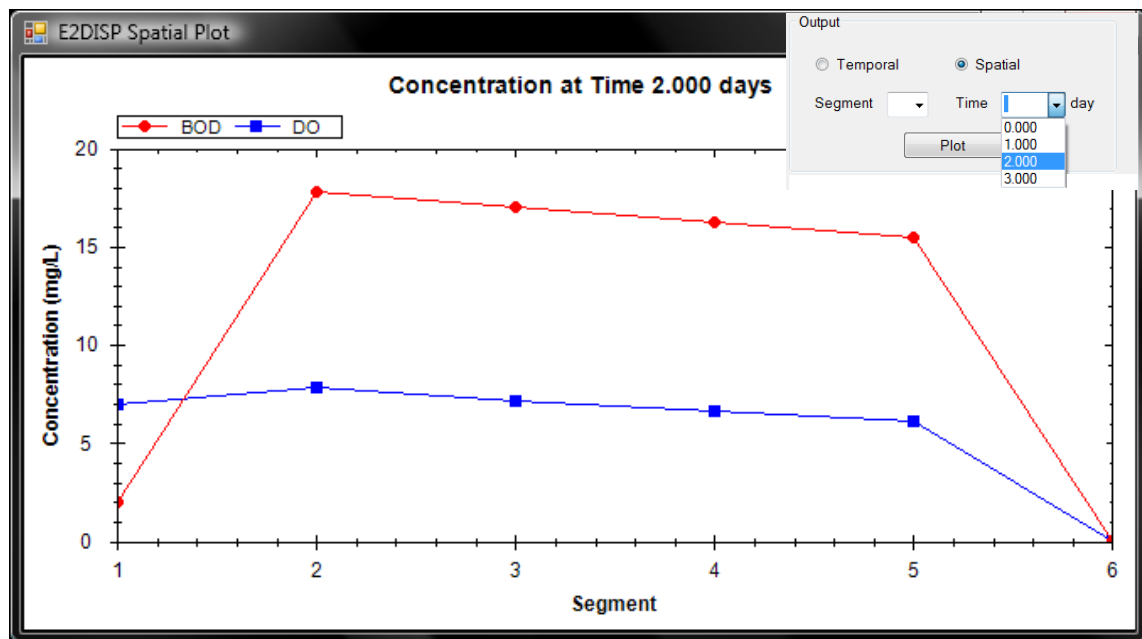


Figure 14: Graph of simulated concentration vs. segment at time  $t = 2.0$  day