

Stack Machine Specification

$$\begin{aligned}
\mathbf{nop:} \quad & (PC_p, PC'_p, w_p, \rho, \xi)_\sigma \xrightarrow{\langle \mathbf{nop} \ 0 \rangle}_{(p,N)} (PC_p + 1, PC_p, w_p, \rho, \xi)_\sigma \\
\mathbf{ipush:} \quad & (PC_p, PC'_p, w_p, \rho, \xi)_\sigma \xrightarrow{\langle \mathbf{ipush} \ z \rangle}_{(p,N)} (PC_p + 1, PC_p, zw_p, \rho, \xi)_\sigma \\
\mathbf{load:} \quad & (PC_p, PC'_p, w_p, \rho, \xi)_\sigma \xrightarrow{\langle \mathbf{load} \ v \rangle}_{(p,N)} (PC_p + 1, PC_p, \sigma(v)w_p, \rho, \xi)_\sigma \\
\mathbf{store:} \quad & (PC_p, PC'_p, zw_p, \rho, \xi)_\sigma \xrightarrow{\langle \mathbf{store} \ v \rangle}_{(p,N)} (PC_p + 1, PC_p, w_p, \rho, \langle p, z \rangle \xi)_\sigma [v \mapsto z] \\
\mathbf{jpc:} \quad & (PC_p, PC'_p, zw_p, \rho, \xi)_\sigma \xrightarrow{\langle \mathbf{jpc} \ a \rangle}_{(p,N)} \begin{cases} (a, PC_p, w_p, \rho, \xi)_\sigma & \text{if } z \neq 0 \\ (PC_p + 1, PC_p, w_p, \rho, \xi)_\sigma & \text{if } z = 0 \end{cases} \\
\mathbf{jmp:} \quad & (PC_p, PC'_p, w_p, \rho, \xi)_\sigma \xrightarrow{\langle \mathbf{jmp} \ a \rangle}_{(p,N)} (a, PC_p, w_p, \rho, \xi)_\sigma \\
\mathbf{op:} \quad & (PC_p, PC'_p, z_1 z_2 w_p, \rho, \xi)_\sigma \xrightarrow{\langle \mathbf{op} \ k \rangle}_{(p,N)} (PC_p + 1, PC_p, \mathbf{op}_k(z_1, z_2)w_p, \rho, \xi)_\sigma \\
& \text{where } \mathbf{op}_1 \equiv +, \mathbf{op}_2 \equiv \times, \mathbf{op}_3 \equiv -, \mathbf{op}_4 \equiv <, \mathbf{op}_5 \equiv ==. \\
& z_1 < z_2 \text{ and } z_1 == z_2 \text{ are 1 when the relations hold and 0 otherwise.} \\
\mathbf{label:} \quad & (PC_p, PC'_p, w, \rho, \xi)_\sigma \xrightarrow{\langle \mathbf{label} \ n \rangle}_{(p,N)} (PC_p + 1, PC_p, \langle n + 1 - PC'_p, p \rangle \rho, \xi) \\
\mathbf{rjmp:} \quad & (PC_p, PC'_p, w, \langle a, N + 1 - p \rangle \rho, \xi)_\sigma \xrightarrow{\langle \mathbf{rjmp} \ 0 \rangle}_{(p,N)} (a, PC_p, w, \rho, \xi)_\sigma \\
\mathbf{restore:} \quad & (PC_p, PC'_p, w, \rho, \langle z, N + 1 - p \rangle \xi)_\sigma \\
& \xrightarrow{\langle \mathbf{restore} \ v \rangle}_{(p,N)} (PC_p + 1, PC_p, w, \rho, \xi)_\sigma [v \mapsto z] \\
\mathbf{alloc:} \quad & (PC_p, PC'_p, w_p, \rho, \xi)_\sigma \xrightarrow{\langle \mathbf{alloc} \ v \rangle}_{(p,N)} (PC_p + 1, PC_p, 0w_p, \rho, \xi)_\sigma [v \mapsto 0] \\
\mathbf{free:} \quad & (PC_p, PC'_p, zw_p, \rho, \xi)_\sigma \xrightarrow{\langle \mathbf{free} \ v \rangle}_{(p,N)} (PC_p + 1, PC_p, w_p, \rho, \xi)_\sigma \setminus v
\end{aligned}$$