Assignment 3: Population Dynamics

- 1. To find the age distribution, birth rate, and morality rates for the Canadian population, I gathered data from Statistics Canada's website where time t_0 was set to the year 2020, as this is the most recent year for which data is available for all three of these variables. In order to create 100 bin vectors, I assumed that the distribution of the data was uniform over each of the defined age groups. For example, the population of age group 0 4 was 1,918,870 people, and therefore, each bin should have a value of 1,918,870 / 5 = 383,774 people. Calculations for the birth and mortality rates follow similarly.
- 2. How do I 'specify' my 100*100 transition matrix in a one page report? Similarly to the discrete dynamical model described by Boyd and Vandenberghe, the birth rate was given by a 100-vector b where b_i is the average births per person with age i-1. The mortality rate is given by a 100-vector d, where d_i is the portion of people aged i-1 who die in the current year. Then the transition matrix is given by A where the first row is b_0 to b_{99} and subsequent rows are given by $1-d_i$ along the diagonal.
- 3. Using the initial population vector given by my 2020 age distribution, and the transition matrix given by my birth and mortality rates, I projected the population of Canada for the years 2028, 2033, and 2038. These results were found by repeatingly multiplying the population vector by the transition matrix in a for loop 8, 13, and 18 times respectively. The results are as shown in Figure 1.
- 4. I gathered immigration rates from Statistics Canada 'Estimates of the components of international migration, by age and sex, annual' for the 2021/2022 year and created a 100 component vector similar to the population distribution. I treated this immigration factor as an exogenous variable, adding it to the results of each iteration in the procedure described in question 3. In these projections, I assumed that the immigration rates through to 2038 would remain constant at the 2021/2022 rate. The results are as shown in Figure 2.
- 5. To increase accuracy of this model, I recommend to account for the fact that population numbers are not evenly distributed across age groups. Furthermore, we could also take into account the fact that fertility, mortality, and immigration rates are not constant over time and vary based on external factors.

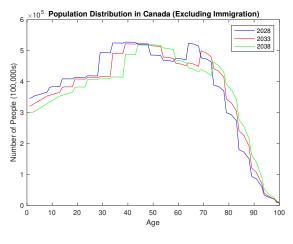


Figure 1

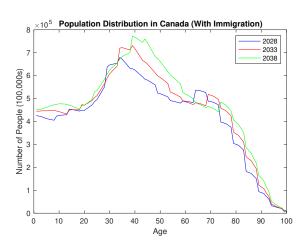


Figure 2