CONTENTS

P8106 HW1

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(a) Least Square	10
Fit a linear model using least squares on the training data. Is there any potential disadvantage of this mode	el?
house_training <- read_csv("housing_training.csv") %>% janitor::clean_names()	
## Rows: 1440 Columns: 26 ## Column specification ## Delimiter: ","	
<pre>## Delimiter: "," ## chr (4): Overall_Qual, Kitchen_Qual, Fireplace_Qu, Exter_Qual ## dbl (22): Gr_Liv_Area, First_Flr_SF, Second_Flr_SF, Total_Bsmt_SF, Low_Qual</pre>	
<pre>## ## i Use 'spec()' to retrieve the full column specification for this data. ## i Specify the column types or set 'show col types = FALSE' to quiet this message.</pre>	

Perform 10-folds cross-validation on the full model

There are 25 predictors in total, we want to perform CV to find the best fitted parameters.

```
##
                   (Intercept)
                                                gr_liv_area
                 -4.984628e+06
                                               2.458001e+01
##
##
                  first flr sf
                                              second flr sf
                  4.252481e+01
                                               4.176763e+01
##
##
                 total_bsmt_sf
                                           low_qual_fin_sf
##
                  3.519195e+01
                                                         NA
##
                  wood_deck_sf
                                             open_porch_sf
##
                  1.202429e+01
                                              1.617780e+01
##
                   bsmt_unf_sf
                                              mas_vnr_area
##
                 -2.086972e+01
                                              1.045801e+01
##
                   garage_cars
                                                garage_area
                                               7.769075e+00
##
                  4.228630e+03
##
                    year_built
                                           tot_rms_abv_grd
##
                  3.251188e+02
                                              -3.838101e+03
##
                     full_bath
                                       overall_qualAverage
##
                 -4.340544e+03
                                              -5.013000e+03
                                     overall_qualExcellent
##
    overall_qualBelow_Average
##
                 -1.279921e+04
                                               7.260609e+04
##
             overall_qualFair
                                          overall_qualGood
##
                 -1.114686e+04
                                               1.226308e+04
##
   overall_qualVery_Excellent
                                     overall_qualVery_Good
##
                  1.303770e+05
                                               3.797518e+04
##
             kitchen_qualFair
                                          kitchen_qualGood
##
                 -2.662852e+04
                                              -1.878675e+04
##
          kitchen_qualTypical
                                                 fireplaces
##
                 -2.676512e+04
                                               1.138083e+04
##
             fireplace_quFair
                                          fireplace_quGood
##
                 -7.206510e+03
                                               6.069919e+02
##
     fireplace_quNo_Fireplace
                                          fireplace_quPoor
##
                  3.394267e+03
                                              -5.184597e+03
##
          fireplace_quTypical
                                            exter_qualFair
##
                 -6.397856e+03
                                              -3.854088e+04
##
                exter_qualGood
                                         exter_qualTypical
##
                 -1.993620e+04
                                             -2.436104e+04
##
                  lot_frontage
                                                   lot_area
                  1.024022e+02
                                              6.041670e-01
##
##
                     longitude
                                                   latitude
                 -3.481322e+04
                                              5.874429e+04
##
##
                      misc_val
                                                  year_sold
##
                  9.171290e-01
                                              -6.454655e+02
```

MSE, R-squared values

Check the mean squared error (MSE) and the R-squared value of the model:

```
# The Mean Squared Error is
mean((fit.lm$resample$RMSE)^2)

## [1] 531169999

# The R^2 value is
mean(fit.lm$resample$Rsquared)
```

```
## [1] 0.9029694
```

So the training error for the LS model is 531169999, with R-squared value of 0.9029694.

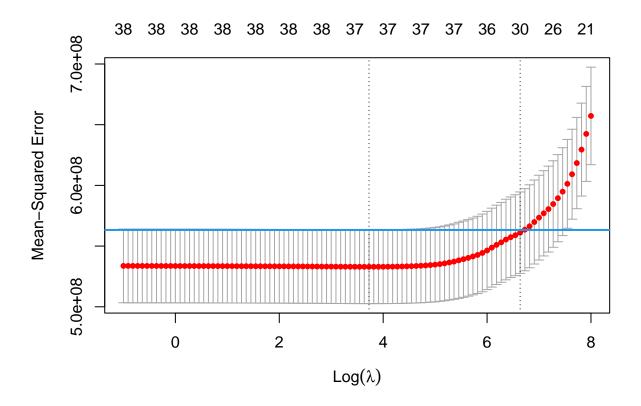
Potential disadvantage: 1. The model has the smallest variance among all the unbiased models, but it has larger variance compared to biased models, but it is not necessarily good enough. It may be better to have a biased estimator with smaller variance/mean squared error. 2. There are many predictors used in this model, and this can cause problem (large variance, colinearity). 3. The model is too complex, a simple model might be better. 4. This model has overfitting problem, meaning that it may perform badly on testing set.

(b) Lasso

```
x_train <- model.matrix(sale_price ~ ., house_training)[ ,-1]
y_train <- house_training$sale_price</pre>
```

Fit the model using Lasso Regression

```
plot(cv.lasso)
abline(h = (cv.lasso$cvm + cv.lasso$cvsd)[which.min(cv.lasso$cvm)], col = 4, lwd = 2)
```



When 1se rule is applied, there are total 30 predictors in the model.

The coefficient of LASSO regression model is:

```
predict(cv.lasso, s = cv.lasso$lambda.1se, type = "coefficient")
```

```
## 40 x 1 sparse Matrix of class "dgCMatrix"
##
## (Intercept)
                               -2.535481e+06
## gr_liv_area
                                5.723258e+01
## first_flr_sf
                                1.066538e+00
## second_flr_sf
                                3.678078e+01
## total_bsmt_sf
## low_qual_fin_sf
                               -2.724627e+01
## wood_deck_sf
                                8.467731e+00
                                8.403562e+00
## open_porch_sf
## bsmt_unf_sf
                               -1.971379e+01
## mas vnr area
                                1.414590e+01
## garage_cars
                                3.078143e+03
## garage_area
                                1.115981e+01
## year_built
                                3.123467e+02
## tot_rms_abv_grd
                               -1.439453e+03
## full_bath
## overall_qualAverage
                               -3.158907e+03
## overall_qualBelow_Average
                              -9.303478e+03
## overall_qualExcellent
                                9.066941e+04
```

```
## overall_qualFair
                             -6.610047e+03
## overall_qualGood
                              1.002368e+04
## overall_qualVery_Excellent 1.606478e+05
## overall_qualVery_Good
                            3.636198e+04
## kitchen_qualFair
                             -5.480630e+03
## kitchen_qualGood
## kitchen_qualTypical
                             -9.580041e+03
## fireplaces
                              6.514237e+03
## fireplace_quFair
## fireplace_quGood
                              4.630463e+03
## fireplace_quNo_Fireplace
## fireplace_quPoor
## fireplace_quTypical
                             -3.377484e+02
## exter_qualFair
                             -1.481214e+04
## exter_qualGood
## exter_qualTypical
                             -5.036385e+03
## lot_frontage
                             7.261206e+01
## lot area
                             5.648507e-01
                             -1.213699e+04
## longitude
## latitude
                              1.973031e+04
## misc_val
## year_sold
```

Training and Testing Error

Calculate the MSE of the test set

```
housing_testing <- read_csv("housing_test.csv") %>%
    janitor::clean_names()
x_test <- model.matrix(sale_price ~ ., housing_testing)[ ,-1]
y_test <- housing_testing$sale_price

# Training Error
y_pred_t <- predict(cv.lasso, newx = x_train, s = "lambda.1se", type = "response")
mean(RMSE(y_pred_t, y_train)^2)</pre>
```

[1] 515636300

The training error (MSE) is 515636300 for lasso model.

```
y_pred <- predict(cv.lasso, newx = x_test, s = "lambda.1se", type = "response")
lasso_te <- mean(RMSE(y_pred, y_test)^2)
lasso_te</pre>
```

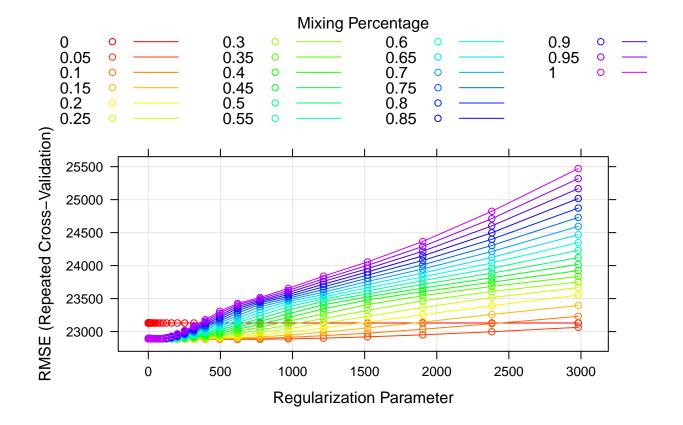
```
## [1] 420354616
```

The test error (MSE) is 420354616 for lasso regression model when the 1SE rule is applied.

c) Fit an elastic net model on the training data

Report the selected tuning parameters

```
set.seed(2)
enet.fit <- train(x_train, y_train,</pre>
                  method = "glmnet",
                   tuneGrid = expand.grid(alpha = seq(0, 1, length = 21),
                                           lambda = exp(seq(8, -3, length = 50))),
                   trControl = trainControl(method = "repeatedcv", number = 10, repeats = 5))
enet.fit$bestTune
      alpha
##
              lambda
      0.05 619.2886
# Set rainbow color
myCol<- rainbow(25)</pre>
myPar <- list(superpose.symbol = list(col = myCol),</pre>
                     superpose.line = list(col = myCol))
plot(enet.fit, par.settings = myPar)
```



Test error 7

coef(enet.fit\$finalModel, enet.fit\$bestTune\$lambda)

```
## 40 x 1 sparse Matrix of class "dgCMatrix"
## (Intercept)
                              -5.119099e+06
## gr liv area
                               3.871803e+01
## first_flr_sf
                               2.667284e+01
## second_flr_sf
                               2.539870e+01
## total_bsmt_sf
                               3.492629e+01
## low_qual_fin_sf
                              -1.586669e+01
## wood_deck_sf
                               1.234466e+01
## open_porch_sf
                               1.692220e+01
## bsmt_unf_sf
                              -2.071319e+01
## mas_vnr_area
                               1.172260e+01
## garage_cars
                               4.041408e+03
                               8.948237e+00
## garage_area
## year built
                               3.188394e+02
## tot_rms_abv_grd
                              -3.419303e+03
## full bath
                              -3.659651e+03
## overall_qualAverage
                              -5.119003e+03
## overall_qualBelow_Average -1.269888e+04
## overall_qualExcellent
                               7.592629e+04
## overall_qualFair
                              -1.148475e+04
## overall_qualGood
                               1.195840e+04
## overall_qualVery_Excellent 1.365876e+05
## overall_qualVery_Good
                               3.762260e+04
## kitchen_qualFair
                              -2.354051e+04
## kitchen_qualGood
                              -1.597423e+04
## kitchen_qualTypical
                              -2.402780e+04
## fireplaces
                               1.079788e+04
## fireplace_quFair
                              -7.863526e+03
## fireplace_quGood
                               1.474300e+02
## fireplace_quNo_Fireplace
                               1.757694e+03
## fireplace quPoor
                              -5.809405e+03
                              -6.964071e+03
## fireplace_quTypical
## exter qualFair
                              -3.276755e+04
## exter_qualGood
                              -1.436584e+04
## exter_qualTypical
                              -1.897822e+04
## lot_frontage
                               1.000357e+02
## lot area
                               6.030183e-01
## longitude
                              -3.517964e+04
## latitude
                               5.769405e+04
## misc_val
                               8.652364e-01
## year_sold
                              -5.712351e+02
```

The tunning parameter λ is 619.2886. The parameter α is 0.05.

Test error

```
enet.pred <- predict(enet.fit, newdata = x_test)
# test error</pre>
```

```
enet_te <- mean(RMSE(enet.pred, y_test)^2)
enet_te</pre>
```

[1] 438209306

The test error (MSE) is 438209306 for elastic net model.

(d) Fit a partial least squares model

Fit model using plsr

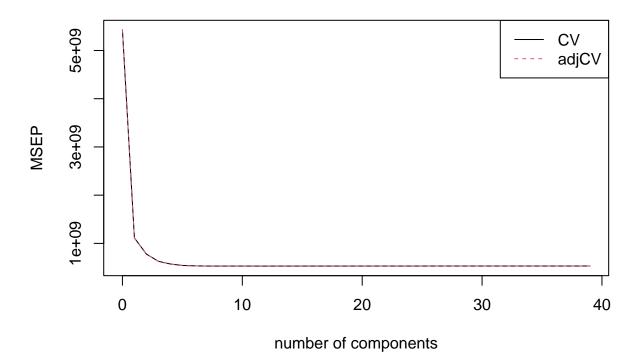
```
## Data:
            X dimension: 1440 39
## Y dimension: 1440 1
## Fit method: kernelpls
## Number of components considered: 39
## VALIDATION: RMSEP
## Cross-validated using 10 random segments.
##
          (Intercept) 1 comps 2 comps 3 comps 4 comps
                                                              5 comps
                                                                        6 comps
## CV
                 73685
                          33357
                                    27895
                                             25075
                                                       23920
                                                                23294
                                                                          23114
## adiCV
                 73685
                          33354
                                    27863
                                             25006
                                                       23858
                                                                23233
                                                                          23061
##
          7 comps 8 comps
                            9 comps 10 comps 11 comps 12 comps
                                                                      13 comps
            23020
                      23007
                               23021
                                          23022
                                                     23011
                                                               23011
## CV
                                                                          23013
            22968
                      22954
## adjCV
                               22965
                                          22964
                                                    22953
                                                               22952
                                                                          22953
##
          14 comps
                    15 comps
                               16 comps
                                          17 comps
                                                    18 comps
                                                               19 comps
                                                                          20 comps
             23010
                        23016
                                   23014
                                             23014
                                                        23019
                                                                  23022
                                                                             23024
## CV
                                                                  22961
## adjCV
             22951
                        22956
                                   22954
                                             22954
                                                        22959
                                                                             22964
                                                               26 comps
##
          21 comps
                    22 comps
                               23 comps
                                          24 comps
                                                    25 comps
                                                                          27 comps
                                                                  23032
## CV
             23027
                        23031
                                   23029
                                             23030
                                                        23030
                                                                             23033
## adjCV
             22967
                        22970
                                   22968
                                             22969
                                                        22969
                                                                   22971
                                                                             22972
##
          28 comps
                    29 comps
                               30 comps
                                         31 comps
                                                    32 comps
                                                               33 comps
                                                                          34 comps
## CV
             23034
                        23034
                                   23034
                                             23034
                                                        23034
                                                                  23034
                                                                             23034
## adjCV
             22973
                        22973
                                   22972
                                             22973
                                                        22973
                                                                  22973
                                                                             22973
##
          35 comps
                    36 comps
                               37 comps
                                          38 comps
                                                    39 comps
             23034
                        23034
                                                        23052
## CV
                                   23034
                                             23034
## adjCV
             22973
                        22973
                                   22973
                                             22973
                                                        22990
##
## TRAINING: % variance explained
##
               1 comps 2 comps 3 comps
                                            4 comps 5 comps
                                                               6 comps
                                                                        7 comps
## X
                  20.02
                           25.93
                                     29.67
                                              33.59
                                                        37.01
                                                                 40.03
                                                                           42.49
## sale_price
                 79.73
                           86.35
                                     89.36
                                              90.37
                                                        90.87
                                                                 90.99
                                                                           91.06
```

Fit model using plsr 9

```
##
                8 comps
                         9 comps
                                  10 comps
                                             11 comps
                                                       12 comps 13 comps
                                                                             14 comps
## X
                  45.53
                           47.97
                                      50.15
                                                 52.01
                                                           53.69
                                                                      55.35
                                                                                 56.86
                                      91.13
                                                           91.15
## sale_price
                  91.08
                           91.10
                                                 91.15
                                                                      91.16
                                                                                 91.16
##
                                                                     20 comps
                15 comps
                          16 comps
                                     17 comps
                                               18 comps
                                                          19 comps
## X
                   58.64
                             60.01
                                        62.18
                                                   63.87
                                                             65.26
                                                                        67.10
                   91.16
                             91.16
                                        91.16
                                                   91.16
                                                             91.16
                                                                        91.16
## sale_price
##
                21 comps
                          22 comps
                                     23 comps
                                               24 comps
                                                          25 comps
                                                                     26 comps
                                        71.72
                             70.12
                                                   73.35
                                                             75.20
                                                                        77.27
## X
                   68.44
## sale_price
                   91.16
                             91.16
                                        91.16
                                                   91.16
                                                             91.16
                                                                        91.16
##
                27 comps
                          28 comps
                                     29 comps
                                               30 comps
                                                          31 comps
                                                                     32 comps
## X
                   78.97
                             80.10
                                        81.83
                                                   83.55
                                                             84.39
                                                                        86.34
                             91.16
                                        91.16
## sale_price
                   91.16
                                                   91.16
                                                             91.16
                                                                        91.16
##
                33 comps
                          34 comps
                                     35 comps
                                               36 comps
                                                          37 comps
                                                                     38 comps
## X
                   88.63
                             90.79
                                        92.79
                                                   95.45
                                                             97.49
                                                                       100.00
## sale_price
                   91.16
                             91.16
                                        91.16
                                                   91.16
                                                             91.16
                                                                        91.16
##
                39 comps
## X
                  100.67
## sale_price
                   91.16
```

validationplot(pls.mod, val.type="MSEP", legendpos = "topright")

sale_price



Training Error and Testing Error

```
# training error
cv.mse <- RMSEP(pls.mod)
mean(min(cv.mse$val[1,,])^2)</pre>
```

[1] 529300397

[1] 440217938

The model with 8 components yields the minimum training error (MSE) 529300397. The testing error (MSE) is 440217938.

e) Select Model

```
#compute the testing error of LS regression first
y_pred <- predict(fit.lm, newdata = housing_testing)
ls_te <- mean(RMSE(y_pred, y_test)^2)
ls_te</pre>
```

[1] 447287652

The test error of LS model is 447287652.

For response predicting, we want to choose the model with the smallest test error. The test error (MSE) is 420354616 for lasso regression model, 438209306 for elastic net model, and 440217938 for the PLS model. Therefore, we should choose the lasso regression model for predicting the response.