

CUDA Toolkit 4.1 CUBLAS Library

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Chapter 1 Introduction

The CUBLAS library is an implementation of BLAS (Basic Linear Algebra Subprograms) on top of the NVIDIA®CUDATM runtime. It allows the user to access the computational resources of NVIDIA Graphics Processing Unit (GPU), but does not auto-parallelize across multiple GPUs.

To use the CUBLAS library, the application must allocate the required matrices and vectors in the GPU memory space, fill them with data, call the sequence of desired CUBLAS functions, and then upload the results from the GPU memory space back to the host. The CUBLAS library also provides helper functions for writing and retrieving data from the GPU.

1.1 Data layout

For maximum compatibility with existing Fortran environments, the CUBLAS library uses column-major storage, and 1-based indexing. Since C and C++ use row-major storage, applications written in these languages can not use the native array semantics for two-dimensional arrays. Instead, macros or inline functions should be defined to implement matrices on top of one-dimensional arrays. For Fortran code ported to C in mechanical fashion, one may chose to retain 1-based indexing to avoid the need to transform loops. In this case, the array index of a matrix element in row "i" and column "j" can be computed via the following macro

```
#define IDX2F(i,j,ld) ((((j)-1)*(ld))+((i)-1))
```

Here, ld refers to the leading dimension of the matrix, which in the case of column-major storage is the number of rows of the allocated matrix (even if only a submatrix of it is being used). For natively written C and C++ code, one would most likely choose 0-based indexing, in which case the array index of a matrix element in row "i" and column "j" can be computed via the following macro

```
#define IDX2C(i, j, ld) (((j)*(ld))+(i))
```

1.2 New and Legacy CUBLAS API

Starting with version 4.0, the CUBLAS Library provides a new updated API, in addition to the existing legacy API. This section discusses why a new API is provided, the advantages of using it, and the differences with the existing legacy API.

The new CUBLAS library API can be used by including the header file "cublas_v2.h". It has the following features that the legacy CUBLAS API does not have:

- ▶ the handle to the CUBLAS library context is initialized using the cublasCreate function and is explicitly passed to every subsequent library function call. This allows the user to have more control over the library setup when using multiple host threads and multiple GPUs. This also allows the CUBLAS APIs to be reentrant.
- ▶ the scalars α and β can be passed by reference on the host or the device, instead of only being allowed to be passed by value on the host. This change allows library functions to execute asynchronously using streams even when α and β are generated by a previous kernel.
- ▶ when a library routine returns a scalar result, it can be returned by reference on the host or the device, instead of only being allowed to be returned by value only on the host. This change allows library routines to be called asynchronously when the scalar result is generated and returned by reference on the device resulting in maximum parallelism.
- ▶ the error status cublasStatus_t is returned by all CUBLAS library function calls. This change facilitates debugging and simplifies software development. Note that cublasStatus was renamed cublasStatus_t to be more consistent with other types in the CUBLAS library.
- ▶ the cublasAlloc() and cublasFree() functions have been deprecated. This change removes these unnecessary wrappers around cudaMalloc() and cudaFree(), respectively.
- ▶ the function cublasSetKernelStream() was renamed cublasSetStream() to be more consistent with the other CUDA libraries.

The legacy CUBLAS API, explained in more detail in the Appendix A, can be used by including the header file "cublas.h". Since the legacy API is identical to the previously released CUBLAS library API, existing applications will work out of the box and automatically use this legacy API without any source code changes. In general, new applications should not use the legacy CUBLAS API, and existing existing applications should convert to using the new API if it requires sophisticated and optimal stream parallelism or if it calls CUBLAS routines concurrently from multiple threads. For the rest of the document, the new CUBLAS Library API will simply be referred to as the CUBLAS Library API.

As mentioned earlier the interfaces to the legacy and the CUBLAS library APIs are the header file "cublas.h" and "cublas v2.h", respectively. In addition, applications using the

CUBLAS library need to link against the DSO cublas.so (Linux), the DLL cublas.dll (Windows), or the dynamic library cublas.dylib (Mac OS X). Note: the same dynamic library implements both the new and legacy CUBLAS APIs.

1.3 Example code

For sample code references please see the two examples below. They show an application written in C using the CUBLAS library API with two indexing styles (Example 1. "Application Using C and CUBLAS: 1-based indexing" and Example 2. "Application Using C and CUBLAS: 0-based Indexing").

```
//Example 1. Application Using C and CUBLAS: 1-based indexing
#include <stdio.h>
#include <stdlib.h>
#include <math.h>
#include < cuda_runtime.h>
#include "cublas v2.h'
#define M 6
#define N 5
#define IDX2F(i,j,ld) ((((j)-1)*(ld))+((i)-1))
\verb|cublasSscal| (\verb|handle|, n-p+1|, \&alpha|, \&m[IDX2F(p,q,ldm)]|, ldm|);
    cublasSscal (handle, ldm-p+1, &beta, &m[IDX2F(p,q,ldm)], 1);
int main (void){
   cudaError_t cudaStat;
    cublasStatus_t stat;
    cublasHandle_t handle;
    int i, j;
    float* devPtrA;
    float* a = 0;
    a = (float *)malloc (M * N * sizeof (*a));
    if (!a) {
        printf ("host memory allocation failed");
        return EXIT_FAILURE;
    for (j = 1; j \le N; j++) {
        for (i = 1; i \le M; i++) \{ a[IDX2F(i,j,M)] = (float)((i-1) * M + j); \}
    cudaStat = cudaMalloc ((void**)\&devPtrA, M*N*sizeof(*a));
    if (cudaStat != cudaSuccess) {
        printf ("device memory allocation failed");
        return EXIT_FAILURE;
   stat = cublasCreate(&handle);
   if (stat != CUBLAS_STATUS_SUCCESS) {
        printf ("CUBLAS initialization failed\n");
        return EXIT_FAILURE;
```

```
stat = cublasSetMatrix (M, N, sizeof(*a), a, M, devPtrA, M);
if (stat != CUBLAS_STATUS_SUCCESS) {
     printf ("data download failed");
     cudaFree (devPtrA);
     cublasDestroy(handle);
     return EXIT_FAILURE;
\verb"modify" (handle \,, \ \verb"devPtrA" \,, \ \verb"M" \,, \ \verb"N" \,, \ 2 \,, \ 3 \,, \ 16.0 \, f \,, \ 12.0 \, f \,) \,;
\mathtt{stat} = \mathtt{cublasGetMatrix} \ (\mathtt{M}, \ \mathtt{N}, \ \mathtt{sizeof} \ (\mathtt{*a}) \,, \ \mathtt{devPtrA} \,, \ \mathtt{M}, \ \mathtt{a}, \ \mathtt{M}) \,;
if (stat != CUBLAS_STATUS_SUCCESS) {
     printf ("data upload failed");
     cudaFree (devPtrA);
     cublasDestroy(handle);
     return EXIT_FAILURE;
cudaFree (devPtrA);
cublasDestroy(handle);
for (j = 1; j \le N; j++) {
     for (i = 1; i <= M; i++) {
          printf ("%7.0f", a[IDX2F(i,j,M)]);
     printf ("\n");
return EXIT_SUCCESS;
```

```
//Example 2. Application Using C and CUBLAS: 0-based indexing
#include <stdio.h>
#include <stdlib.h>
#include <math.h>
#include < cuda_runtime.h>
#include "cublas_v2.h"
#define M 6
#define N 5
#define IDX2C(i,j,ld) (((j)*(ld))+(i))
\textbf{static} \ \_\texttt{inline}\_ \ \textbf{void} \ \textbf{modify} \ (\textbf{cublasHandle}\_\textbf{t} \ \textbf{handle}, \ \textbf{float} \ *\textbf{m}, \ \textbf{int} \ \textbf{ldm}, \ \textbf{int} \ \textbf{n}, \ \textbf{int} \ \textbf{m})
                     p, int q, float alpha, float beta) {
                      \texttt{cublasSscal} \hspace{0.2cm} \big( \hspace{0.5mm} \texttt{handle} \hspace{0.2cm}, \hspace{0.2cm} n-p \hspace{0.2cm}, \hspace{0.2cm} \& \texttt{alpha} \hspace{0.2cm}, \hspace{0.2cm} \& \texttt{m} \hspace{0.5mm} \big[ \hspace{0.5mm} \texttt{IDX2C} \hspace{0.2cm} (\hspace{0.5mm} p \hspace{0.2cm}, \hspace{0.2cm} q \hspace{0.2cm}, \hspace{0.2cm} \texttt{ldm} \hspace{0.2cm}) \hspace{0.2cm} \big] \hspace{0.2cm}, \hspace{0.2cm} \hspace{0.2cm} \texttt{ldm} \hspace{0.2cm} \big) \hspace{0.2cm} \big] \hspace{0.2cm}, \hspace{0.2cm} \hspace{0.2cm} \texttt{ldm} \hspace{0.2cm} \big) \hspace{0.2cm} \big] \hspace{0.2cm}, \hspace{0.2cm} \hspace{0.2cm} \hspace{0.2cm} \texttt{ldm} \hspace{0.2cm} \big) \hspace{0.2cm} \big] \hspace{0.2cm}, \hspace{0.2cm} \hspace{0.2cm} \hspace{0.2cm} \texttt{ldm} \hspace{0.2cm} \big) \hspace{0.2cm} \big] \hspace{0.2cm}, \hspace{0.2cm} \hspace{0.2cm} \hspace{0.2cm} \texttt{ldm} \hspace{0.2cm} \big) \hspace{0.2cm} \big] \hspace{0.2cm}, \hspace{0.2cm} \hspace{0.2cm} \hspace{0.2cm} \texttt{ldm} \hspace{0.2cm} \big) \hspace{0.2cm} \big] \hspace{0.2cm}, \hspace{0.2cm} \hspace{0.2cm} \hspace{0.2cm} \texttt{ldm} \hspace{0.2cm} \big) \hspace{0.2cm} \big] \hspace{0.2cm}, \hspace{0.2cm} \hspace{0.2cm} \hspace{0.2cm} \hspace{0.2cm} \texttt{ldm} \hspace{0.2cm} \big) \hspace{0.2cm} \big] \hspace{0.2cm}, \hspace{0.2cm} \hspace{0.2cm} \hspace{0.2cm} \texttt{ldm} \hspace{0.2cm} \big) \hspace{0.2cm} \big] \hspace{0.2cm}, \hspace{0.2cm} \texttt{ldm} \hspace{0.2cm} \big) \hspace{0.2cm} \big] \hspace{0.2cm}, \hspace{0.2cm} \hspace{
                     int main (void){
                      cudaError_t cudaStat;
                      cublasStatus_t stat;
                      cublasHandle_t handle;
                      int i, j;
                      float * devPtrA;
                      float* a = 0;
                      a = (float *)malloc (M * N * sizeof (*a));
                      if (!a) {
                                         printf ("host memory allocation failed");
                                          return EXIT_FAILURE;
                      for (j = 0; j < N; j++) {
                                            for (i = 0; i < M; i++) {
                                                               a[IDX2C(i,j,M)] = (float)(i * M + j + 1);
```

```
cudaStat = cudaMalloc ((void**)&devPtrA, M*N*sizeof(*a));
if (cudaStat != cudaSuccess) {
    printf ("device memory allocation failed");
    return EXIT_FAILURE;
stat = cublasCreate(&handle);
if (stat != CUBLAS_STATUS_SUCCESS) {
   printf ("CUBLAS initialization failed\n");
    return EXIT_FAILURE;
if (stat != CUBLAS_STATUS_SUCCESS) {
   printf ("data download failed");
    cudaFree (devPtrA);
    cublasDestroy(handle);
    return EXIT_FAILURE;
\verb| modify (handle, devPtrA|, M, N, 1, 2, 16.0f, 12.0f); \\
stat = cublasGetMatrix (M, N, sizeof(*a), devPtrA, M, a, M);
if (stat != CUBLAS_STATUS_SUCCESS) {
    printf ("data upload failed");
    cudaFree (devPtrA);
    cublasDestroy(handle);
    return EXIT_FAILURE;
cudaFree (devPtrA);
cublasDestroy(handle);
\quad \  \  \text{for} \ \ (\, \mathtt{j} \, = \, 0\, ; \ \ \mathtt{j} \, < \, \mathtt{N}\, ; \ \ \mathtt{j} + +) \ \{ \,
    for (i = 0; i < M; i++) \{ printf ("%7.0f", a[IDX2C(i,j,M)]); \}
    printf ("\n");
return EXIT_SUCCESS;
```

Chapter 2 Using the CUBLAS API

This section describes how to use the CUBLAS library API. It does not contain a detailed reference for all API datatypes and functions—those are provided in subsequent chapters. The Legacy CUBLAS API is also not covered in this section—that is handled in an Appendix.

2.1 Error status

All CUBLAS library function calls return the error status cublasStatus_t.

2.2 CUBLAS context

The application must initialize the handle to the CUBLAS library context by calling the cublasCreate() function. Then, the handle is explicitly passed to every subsequent library function call. Once the application finishes using the library, it must call the cublasDestroy() function to release the resources associated with the CUBLAS library context.

This approach allows the user to explicitly control the library setup when using multiple host threads and multiple GPUs. For example, the application can use <code>cudaSetDevice()</code> to associate different devices with different host threads and in each of those host threads it can initialize a unique <code>handle</code> to the CUBLAS library context, which will use the particular device associated with that host thread. Then, the CUBLAS library function calls made with different <code>handle</code> will automatically dispatch the computation to different devices.

The device associated with a particular CUBLAS context is assumed to remain unchanged between the corresponding cublasCreate() and cublasDestroy() calls. In order for the CUBLAS library to use a different device in the same host thread, the application must set the new device to be used by calling cudaSetDevice() and then create another CUBLAS context, which will be associated with the new device, by calling cublasCreate().

2.3 Thread Safety

The library is thread safe and its functions can be called from multiple host threads, even with the same handle.

2.4 Scalar Parameters

In the CUBLAS API the scalar parameters α and β can be passed by reference on the host or the device

Also, the few functions that return a scalar result, such as amax(), amin(), asum(), rotg(), rotmg(), dot() and nrm2(), return the resulting value by reference on the host or the device. Notice that even though these functions return immediately, similarly to matrix and vector results, the scalar result is ready only when execution of the routine on the GPU completes. This requires proper synchronization in order to read the result from the host.

These changes allow the library functions to execute completely asynchronously using streams even when α and β are generated by a previous kernel. For example, this situation can arise when iterative methods for solution of linear systems and eigenvalue problems are implemented using the CUBLAS library.

2.5 Parallelism with Streams

If the application uses the results computed by multiple independent tasks, $CUDA^{TM}$ streams can be used to overlap the computation performed in these tasks.

The application can conceptually associate each stream with each task. In order to achieve the overlap of computation between the tasks, the user should create CUDATM streams using the function cudaStreamCreate() and set the stream to be used by each individual CUBLAS library routine by calling cublasSetStream() just before calling the actual CUBLAS routine. Then, the computation performed in separate streams would be overlapped automatically when possible on the GPU. This approach is especially useful when the computation performed by a single task is relatively small and is not enough to fill the GPU with work.

We recommend using the new CUBLAS API with scalar parameters and results passed by reference in the device memory to achieve maximum overlap of the computation when using streams.

A particular application of streams, batching of multiple small kernels, is described below.

2.6 Batching Kernels

In this section we will explain how to use streams to batch the execution of small kernels. For instance, suppose that we have an application where we need to make many small independent matrix-matrix multiplications with dense matrices.

It is clear that even with millions of small independent matrices we will not be able to achieve the same GFLOPS rate as with a one large matrix. For example, a single $n \times n$ large matrix-matrix multiplication performs n^3 operations for n^2 input size, while 1024 $\frac{n}{32} \times \frac{n}{32}$ small matrix-matrix multiplications perform $1024 \left(\frac{n}{32}\right)^3 = \frac{n^3}{32}$ operations for the same input size. However, it is also clear that we can achieve a significantly better performance with many small independent matrices compared with a single small matrix.

The Fermi architecture family of GPUs allows us to execute multiple kernels simultaneously. Hence, in order to batch the execution of independent kernels, we can run each of them in a separate stream. In particular, in the above example we could create 1024 CUDATM streams using the function cudaStreamCreate(), then preface each call to cublas

 cublas

 stream() with a call to cublasSetStream() with a different stream for each of the matrix-matrix multiplications. This will ensure that when possible the different computations will be executed concurrently. Although the user can create many streams, in practice it is not possible to have more than 16 concurrent kernels executing at the same time.

Chapter 3 CUBLAS Datatypes Reference

3.1 cublasHandle_t

The cublasHandle_t type is a pointer type to an opaque structure holding the CUBLAS library context. The CUBLAS library context must be initialized using cublasCreate() and the returned handle must be passed to all subsequent library function calls. The context should be destroyed at the end using cublasDestroy().

3.2 cublasStatus_t

The cublasStatus_t type is used for function status returns. All CUBLAS library functions return their status, which can have the following values.

CUBLAS	STATUS	SUCCESS

The operation completed successfully.

CUBLAS_STATUS_NOT_INITIALIZED

The CUBLAS library was not initialized. This is usually caused by the lack of a prior cublasCreate() call, an error in the CUDA Runtime API called by the CUBLAS routine, or an error in the hardware setup.

To correct: call cublasCreate() prior to the function call; and check that the hardware, an appropriate version of the driver, and the CUBLAS library are correctly installed.

CUBLAS_STATUS_ALLOC_FAILED

Resource allocation failed inside the CUBLAS library. This is usually caused by a cudaMalloc() failure.

To correct: prior to the function call, deallocate previously allocated memory as much as possible.

CUBLAS_STATUS_INVALID_VALUE

An unsupported value or parameter was passed to the function (a negative vector size, for example).

To correct: ensure that all the parameters being passed have valid values.

CUBLAS_STATUS_ARCH_MISMATCH

The function requires a feature absent from the device architecture; usually caused by the lack of support for double precision. **To correct:** compile and run the application on a device with appropriate compute capability, which is 1.3 for double precision.

CUBLAS_STATUS_MAPPING_ERROR

An access to GPU memory space failed, which is usually caused by a failure to bind a texture.

To correct: prior to the function call, unbind any previously bound textures.

CUBLAS_STATUS_EXECUTION_FAILED

The GPU program failed to execute. This is often caused by a launch failure of the kernel on the GPU, which can be caused by multiple reasons.

To correct: check that the hardware, an appropriate version of the driver, and the CUBLAS library are correctly installed.

CUBLAS_STATUS_INTERNAL_ERROR

An internal CUBLAS operation failed. This error is usually caused by a cudaMemcpyAsync() failure.

To correct: check that the hardware, an appropriate version of the driver, and the CUBLAS library are correctly installed. Also, check that the memory passed as a parameter to the routine is not being deallocated prior to the routine's completion.

3.3 cublasOperation_t

The cublasOperation_t type indicates which operation needs to be performed with the dense matrix. Its values correspond to Fortran characters 'N' or 'n' (non-transpose), 'T' or 't' (transpose) and 'C' or 'c' (conjugate transpose) that are often used as parameters to legacy BLAS implementations.

Value	Meaning
CUBLAS_OP_N	the non-transpose operation is selected
CUBLAS_OP_T	the transpose operation is selected
CUBLAS_OP_C	the conjugate transpose operation is selected

3.4 cublasFillMode_t

The cublasFillMode_t type indicates which part (lower or upper) of the dense matrix was filled and consequently should be used by the function. Its values correspond to Fortran characters 'L' or 'l' (lower) and 'U' or 'u' (upper) that are often used as parameters to legacy BLAS implementations.

Value	Meaning
CUBLAS_FILL_MODE_LOWER	the lower part of the matrix is filled
CUBLAS_FILL_MODE_UPPER	the upper part of the matrix is filled

3.5 cublasDiagType_t

The cublasDiagType_t type indicates whether the main diagonal of the dense matrix is unity and consequently should not be touched or modified by the function. Its values correspond to Fortran characters 'N' or 'n' (non-unit) and 'U' or 'u' (unit) that are often used as parameters to legacy BLAS implementations.

Value	Meaning
CUBLAS_DIAG_NON_UNIT	the matrix diagonal has non-unit elements
CUBLAS_DIAG_UNIT	the matrix diagonal has unit elements

3.6 cublasSideMode_t

The cublasSideMode_t type indicates whether the dense matrix is on the left or right side in the matrix equation solved by a particular function. Its values correspond to Fortran characters 'L' or 'l' (left) and 'R' or 'r' (right) that are often used as parameters to legacy BLAS implementations.

Value	Meaning
CUBLAS_SIDE_LEFT	the matrix is on the left side in the equation
CUBLAS_SIDE_RIGHT	the matrix is on the right side in the equation

3.7 cublasPointerMode_t

The cublasPointerMode_t type indicates whether the scalar values are passed by reference on the host or device. It is important to point out that if several scalar values are present in the function call, all of them must conform to the same single pointer mode. The pointer mode can be set and retrieved using cublasSetPointerMode() and cublasGetPointerMode() routines, respectively.

Value	Meaning
CUBLAS_POINTER_MODE_HOST	the scalars are passed by reference on the host
CUBLAS_POINTER_MODE_DEVICE	the scalars are passed by reference on the device

Chapter 4 CUBLAS Helper Function Reference

4.1 cublasCreate()

cublasStatus_t
cublasCreate(cublasHandle_t *handle)

This function initializes the CUBLAS library and creates a handle to an opaque structure holding the CUBLAS library context. It allocates hardware resources on the host and device and must be called prior to making any other CUBLAS library calls.

Return Value	Meaning
CUBLAS_STATUS_SUCCESS	the initialization succeeded
CUBLAS_STATUS_NOT_INITIALIZED	the CUDA TM Runtime initialization failed
CUBLAS_STATUS_ALLOC_FAILED	the resources could not be allocated

4.2 cublasDestroy()

cublasStatus_t
cublasDestroy(cublasHandle_t handle)

This function releases hardware resources used by the CUBLAS library. The release of GPU resources may be deferred until the application exits. This function is usually the last call with a particular handle to the CUBLAS library.

Return Value	Meaning
CUBLAS_STATUS_SUCCESS	the shut down succeeded
CUBLAS_STATUS_NOT_INITIALIZED	the library was not initialized

4.3 cublasGetVersion()

cublasStatus_t
cublasGetVersion(cublasHandle_t handle, int *version)

This function	returns the	version	number	of the	CUBLAS	library.

Return Value	Meaning
CUBLAS_STATUS_SUCCESS	the operation completed successfully
CUBLAS_STATUS_NOT_INITIALIZED	the library was not initialized

4.4 cublasSetStream()

cublasStatus_t

cublasSetStream(cublasHandle_t handle, cudaStream_t streamId)

This function sets the CUBLAS library stream, which will be used to execute all subsequent calls to the CUBLAS library functions. If the CUBLAS library stream is not set, all kernels use the *default* NULL stream. In particular, this routine can be used to change the stream between kernel launches and then to reset the CUBLAS library stream back to NULL.

Return Value	Meaning
CUBLAS_STATUS_SUCCESS	the stream was set successfully
CUBLAS_STATUS_NOT_INITIALIZED	the library was not initialized

4.5 cublasGetStream()

cublasStatus_t

cublasGetStream(cublasHandle_t handle, cudaStream_t *streamId)

This function gets the CUBLAS library stream, which is being used to execute all calls to the CUBLAS library functions. If the CUBLAS library stream is not set, all kernels use the *default* NULL stream.

Return Value	Meaning
CUBLAS_STATUS_SUCCESS	the stream was returned successfully
CUBLAS_STATUS_NOT_INITIALIZED	the library was not initialized

4.6 cublasGetPointerMode()

cublasStatus_t

cublasGetPointerMode(cublasHandle_t handle, cublasPointerMode_t *mode)

This function obtains the pointer mode used by the CUBLAS library. Please see the section on the cublasPointerMode_t type for more details.

Return Value	Meaning
CUBLAS_STATUS_SUCCESS	the pointer mode was obtained successfully
CUBLAS_STATUS_NOT_INITIALIZED	the library was not initialized

4.7 cublasSetPointerMode()

cublasStatus_t
cublasSetPointerMode(cublasHandle_t handle, cublasPointerMode_t mode)

This function sets the pointer mode used by the CUBLAS library. The *default* is for the values to be passed by reference on the host. Please see the section on the cublasPointerMode_t type for more details.

Return Value	Meaning
CUBLAS_STATUS_SUCCESS	the pointer mode was set successfully
CUBLAS_STATUS_NOT_INITIALIZED	the library was not initialized

4.8 cublasSetVector()

This function copies n elements from a vector x in host memory space to a vector y in GPU memory space. Elements in both vectors are assumed to have a size of elemSize bytes. The storage spacing between consecutive elements is given by incx for the source vector x and incy for the destination vector y.

In general, y points to an object, or part of an object, that was allocated via cublasAlloc(). Since column-major format for two-dimensional matrices is assumed, if a vector is part of a matrix, a vector increment equal to 1 accesses a (partial) column of that matrix. Similarly, using an increment equal to the leading dimension of the matrix results in accesses to a (partial) row of that matrix.

Return Value	Meaning
CUBLAS_STATUS_SUCCESS	the operation completed successfully
CUBLAS_STATUS_NOT_INITIALIZED	the library was not initialized
CUBLAS_STATUS_INVALID_VALUE	the parameters incx,incy,elemSize<=0
CUBLAS_STATUS_MAPPING_ERROR	there was an error accessing GPU memory

4.9 cublasGetVector()

This function copies n elements from a vector x in GPU memory space to a vector y in host memory space. Elements in both vectors are assumed to have a size of elemSize

bytes. The storage spacing between consecutive elements is given by incx for the source vector x and incy for the destination vector y.

In general, x points to an object, or part of an object, that was allocated via cublasAlloc(). Since column-major format for two-dimensional matrices is assumed, if a vector is part of a matrix, a vector increment equal to 1 accesses a (partial) column of that matrix. Similarly, using an increment equal to the leading dimension of the matrix results in accesses to a (partial) row of that matrix.

Return Value	Meaning
CUBLAS_STATUS_SUCCESS	the operation completed successfully
CUBLAS_STATUS_NOT_INITIALIZED	the library was not initialized
CUBLAS_STATUS_INVALID_VALUE	the parameters incx,incy,elemSize<=0
CUBLAS_STATUS_MAPPING_ERROR	there was an error accessing GPU memory

4.10 cublasSetMatrix()

This function copies a tile of rows × cols elements from a matrix A in host memory space to a matrix B in GPU memory space. It is assumed that each element requires storage of elemSize bytes and that both matrices are stored in column-major format, with the leading dimension of the source matrix A and destination matrix B given in lda and ldb, respectively. The leading dimension indicates the number of rows of the allocated matrix, even if only a submatrix of it is being used. In general, B is a device pointer that points to an object, or part of an object, that was allocated in GPU memory space via cublasAlloc().

Return Value	Meaning
CUBLAS_STATUS_SUCCESS	the operation completed successfully
CUBLAS_STATUS_NOT_INITIALIZED	the library was not initialized
CUBLAS_STATUS_INVALID_VALUE	the parameters rows,cols<0 or elemSize,lda,ldb<=0
CUBLAS_STATUS_MAPPING_ERROR	there was an error accessing GPU memory

4.11 cublasGetMatrix()

This function copies a tile of rows \times cols elements from a matrix A in GPU memory space to a matrix B in host memory space. It is assumed that each element requires storage of

elemSize bytes and that both matrices are stored in column-major format, with the leading dimension of the source matrix A and destination matrix B given in lda and ldb, respectively. The leading dimension indicates the number of rows of the allocated matrix, even if only a submatrix of it is being used. In general, A is a device pointer that points to an object, or part of an object, that was allocated in GPU memory space via cublasAlloc().

Return Value	Meaning
CUBLAS_STATUS_SUCCESS	the operation completed successfully
CUBLAS_STATUS_NOT_INITIALIZED	the library was not initialized
CUBLAS_STATUS_INVALID_VALUE	the parameters rows,cols<0 or elemSize,lda,ldb<=0
CUBLAS_STATUS_MAPPING_ERROR	there was an error accessing GPU memory

4.12 cublasSetVectorAsync()

cublasStatus_t

This function has the same functionality as cublasSetVector(), with the exception that the data transfer is done asynchronously (with respect to the host) using the given CUDATM stream parameter.

Return Value	Meaning
CUBLAS_STATUS_SUCCESS	the operation completed successfully
CUBLAS_STATUS_NOT_INITIALIZED	the library was not initialized
CUBLAS_STATUS_INVALID_VALUE	the parameters incx,incy,elemSize<=0
CUBLAS_STATUS_MAPPING_ERROR	there was an error accessing GPU memory

4.13 cublasGetVectorAsync()

cublasStatus_t

This function has the same functionality as cublasGetVector(), with the exception that the data transfer is done asynchronously (with respect to the host) using the given CUDATM stream parameter.

Return Value	Meaning
CUBLAS_STATUS_SUCCESS	the operation completed successfully
CUBLAS_STATUS_NOT_INITIALIZED	the library was not initialized
CUBLAS_STATUS_INVALID_VALUE	the parameters incx,incy,elemSize<=0
CUBLAS_STATUS_MAPPING_ERROR	there was an error accessing GPU memory

4.14 cublasSetMatrixAsync()

This function has the same functionality as cublasSetMatrix(), with the exception that the data transfer is done asynchronously (with respect to the host) using the given CUDATM stream parameter.

Return Value	Meaning
CUBLAS_STATUS_SUCCESS	the operation completed successfully
CUBLAS_STATUS_NOT_INITIALIZED	the library was not initialized
CUBLAS_STATUS_INVALID_VALUE	the parameters rows,cols<0 or elemSize,lda,ldb<=0
CUBLAS_STATUS_MAPPING_ERROR	there was an error accessing GPU memory

4.15 cublasGetMatrixAsync()

This function has the same functionality as cublasGetMatrix(), with the exception that the data transfer is done asynchronously (with respect to the host) using the given CUDATM stream parameter.

Return Value	Meaning
CUBLAS_STATUS_SUCCESS	the operation completed successfully
CUBLAS_STATUS_NOT_INITIALIZED	the library was not initialized
CUBLAS_STATUS_INVALID_VALUE	the parameters rows,cols<0 or elemSize,lda,ldb<=0
CUBLAS_STATUS_MAPPING_ERROR	there was an error accessing GPU memory

Chapter 5 CUBLAS Level-1 Function Reference

In this chapter we describe the Level-1 Basic Linear Algebra Subprograms (BLAS1) functions that perform scalar and vector based operations. We will use abbreviations $\langle type \rangle$ for type and $\langle t \rangle$ for the corresponding short type to make a more concise and clear presentation of the implemented functions. Unless otherwise specified $\langle type \rangle$ and $\langle t \rangle$ have the following meanings:

<type $>$	$<$ t $>$	Meaning
float	's' or 'S'	real single-precision
double	'd' or 'D'	real double-precision
cuComplex	'c' or 'C'	complex single-precision
cuDoubleComplex	'z' or 'Z'	complex double-precision

When the parameters and returned values of the function differ, which sometimes happens for complex input, the <t> can also have the following meanings 'Sc', 'Cs', 'Dz' and 'Zd'.

The abbreviation $\mathbf{Re}(.)$ and $\mathbf{Im}(.)$ will stand for the real and imaginary part of a number, respectively. Since imaginary part of a real number does not exist, we will consider it to be zero and can usually simply discard it from the equation where it is being used. Also, the $\bar{\alpha}$ will denote the complex conjugate of α .

In general throughout the documentation, the lower case Greek symbols α and β will denote scalars, lower case English letters in bold type **x** and **y** will denote vectors and capital English letters A, B and C will denote matrices.

5.1 cublasI<t>amax()

This function finds the (smallest) index of the element of the maximum magnitude. Hence, the result is the first i such that $|\mathbf{Im}(\mathbf{x}[j])| + |\mathbf{Re}(\mathbf{x}[j])|$ is maximum for i = 1, ..., n and j = 1 + (i - 1) * incx. Notice that the last equation reflects 1-based indexing used for compatibility with Fortran.

Param.	Memory	In/out	Meaning
handle		input	handle to the CUBLAS library context.
\mathbf{n}		input	number of elements in the vector x .
X	device	input	<type> vector with n elements.</type>
incx		input	stride between consecutive elements of x.
result	host or device	output	the resulting index, which is 0 if n,incx<=0.

The possible error values returned by this function and their meanings are listed below.

Error Values	Meaning
CUBLAS_STATUS_SUCCESS	the operation completed successfully
CUBLAS_STATUS_NOT_INITIALIZED	the library was not initialized
CUBLAS_STATUS_ALLOC_FAILED	the reduction buffer could not be allocated
CUBLAS_STATUS_ARCH_MISMATCH	the device does not support double-precision
CUBLAS_STATUS_EXECUTION_FAILED	the function failed to launch on the GPU

For references please refer to: isamax, idamax, icamax, izamax

5.2 cublasI<t>amin()

This function finds the (smallest) index of the element of the minimum magnitude. Hence, the result is the first i such that $|\mathbf{Im}(\mathbf{x}[j])| + |\mathbf{Re}(\mathbf{x}[j])|$ is minimum for i = 1, ..., n and j = 1 + (i - 1) * incx. Notice that the last equation reflects 1-based indexing used for compatibility with Fortran.

Param.	Memory	In/out	Meaning
handle		input	handle to the CUBLAS library context.
n		input	number of elements in the vector x.
X	device	input	<type> vector with n elements.</type>
incx		input	stride between consecutive elements of x.
result	host or device	output	the resulting index, which is 0 if n,incx<=0.

Error Values	Meaning
CUBLAS_STATUS_SUCCESS	the operation completed successfully
CUBLAS_STATUS_NOT_INITIALIZED	the library was not initialized
CUBLAS_STATUS_ALLOC_FAILED	the reduction buffer could not be allocated
CUBLAS_STATUS_ARCH_MISMATCH	the device does not support double-precision
CUBLAS_STATUS_EXECUTION_FAILED	the function failed to launch on the GPU

The possible error values returned by this function and their meanings are listed below.

For references please refer to: isamin, idamin

5.3 cublas<t>asum()

This function computes the sum of the absolute values of the elements of vector \mathbf{x} . Hence, the result is $\sum_{i=1}^{n} (|\mathbf{Im}(\mathbf{x}[j])| + |\mathbf{Re}(\mathbf{x}[j])|)$ where $j = 1 + (i-1) * \mathrm{incx}$. Notice that the last equation reflects 1-based indexing used for compatibility with Fortran.

Param.	Memory	In/out	Meaning
handle		input	handle to the CUBLAS library context.
n		input	number of elements in the vector \mathbf{x} .
X	device	input	<type> vector with n elements.</type>
incx		input	stride between consecutive elements of x .
result	host or device	output	the resulting sum, which is 0.0 if n,incx<=0.

The possible error values returned by this function and their meanings are listed below.

Error Values	Meaning
CUBLAS_STATUS_SUCCESS	the operation completed successfully
CUBLAS_STATUS_NOT_INITIALIZED	the library was not initialized
CUBLAS_STATUS_ALLOC_FAILED	the reduction buffer could not be allocated
CUBLAS_STATUS_ARCH_MISMATCH	the device does not support double-precision
CUBLAS_STATUS_EXECUTION_FAILED	the function failed to launch on the GPU

For references please refer to: sasum, dasum, scasum, dzasum

5.4 cublas<t>axpy()

```
cublasStatus_t cublasSaxpy(cublasHandle_t handle, int n,
                           const float
                                                  *alpha,
                           const float
                                                  *x, int incx,
                           float
                                                  *y, int incy)
cublasStatus_t cublasDaxpy(cublasHandle_t handle, int n,
                           const double
                                                  *alpha,
                           const double
                                                  *x, int incx,
                           double
                                                  *y, int incy)
cublasStatus_t cublasCaxpy(cublasHandle_t handle, int n,
                           const cuComplex
                                                  *alpha,
                           const cuComplex
                                                  *x, int incx,
                           cuComplex
                                                  *y, int incy)
cublasStatus_t cublasZaxpy(cublasHandle_t handle, int n,
                           const cuDoubleComplex *alpha,
                           const cuDoubleComplex *x, int incx,
                           cuDoubleComplex
                                                  *y, int incy)
```

This function multiplies the vector \mathbf{x} by the scalar α and adds it to the vector \mathbf{y} overwriting the latest vector with the result. Hence, the performed operation is $\mathbf{y}[j] = \alpha \times \mathbf{x}[k] + \mathbf{y}[j]$ for $i = 1, \ldots, n, \ k = 1 + (i-1) * \text{incx}$ and j = 1 + (i-1) * incy. Notice that the last two equations reflect 1-based indexing used for compatibility with Fortran.

Param.	Memory	In/out	Meaning
handle		input	handle to the CUBLAS library context.
alpha	host or device	input	<type> scalar used for multiplication.</type>
n		input	number of elements in the vector \mathbf{x} and \mathbf{y} .
X	device	input	<type> vector with n elements.</type>
incx		input	stride between consecutive elements of x.
У	device	in/out	<type> vector with n elements.</type>
incy		input	stride between consecutive elements of y.

The possible error values returned by this function and their meanings are listed below.

Error Values	Meaning
CUBLAS_STATUS_SUCCESS	the operation completed successfully
CUBLAS_STATUS_NOT_INITIALIZED	the library was not initialized
CUBLAS_STATUS_ARCH_MISMATCH	the device does not support double-precision
CUBLAS_STATUS_EXECUTION_FAILED	the function failed to launch on the GPU

For references please refer to: saxpy, daxpy, caxpy, zaxpy

5.5 cublas<t>copy()

```
cublasStatus_t cublasScopy(cublasHandle_t handle, int n,
                           const float
                                                 *x, int incx,
                           float
                                                 *y, int incy)
cublasStatus_t cublasDcopy(cublasHandle_t handle, int n,
                           const double
                                                *x, int incx,
                                                 *y, int incy)
                           double
cublasStatus_t cublasCcopy(cublasHandle_t handle, int n,
                           const cuComplex
                                                *x, int incx,
                           cuComplex
                                                 *y, int incy)
cublasStatus_t cublasZcopy(cublasHandle_t handle, int n,
                           const cuDoubleComplex *x, int incx,
                           cuDoubleComplex
                                                 *y, int incy)
```

This function copies the vector \mathbf{x} into the vector \mathbf{y} . Hence, the performed operation is $\mathbf{y}[j] = \mathbf{x}[k]$ for $i = 1, \ldots, n, \ k = 1 + (i-1) * \text{incx}$ and j = 1 + (i-1) * incy. Notice that the last two equations reflect 1-based indexing used for compatibility with Fortran.

Param.	Memory	In/out	Meaning
handle		input	handle to the CUBLAS library context.
\mathbf{n}		input	number of elements in the vector \mathbf{x} and \mathbf{y} .
X	device	input	<type> vector with n elements.</type>
incx		input	stride between consecutive elements of x.
\mathbf{y}	device	output	<type> vector with n elements.</type>
incy		input	stride between consecutive elements of y.

The possible error values returned by this function and their meanings are listed below.

Error Values	Meaning
CUBLAS_STATUS_SUCCESS	the operation completed successfully
CUBLAS_STATUS_NOT_INITIALIZED	the library was not initialized
CUBLAS_STATUS_ARCH_MISMATCH	the device does not support double-precision
CUBLAS_STATUS_EXECUTION_FAILED	the function failed to launch on the GPU

For references please refer to: scopy, dcopy, ccopy, zcopy

5.6 cublas<t>dot()

```
const double
                                                  *x, int incx,
                           const double
                                                  *y, int incy,
                           double
                                            *result)
cublasStatus_t cublasCdotu(cublasHandle_t handle, int n,
                           const cuComplex
                                                  *x, int incx,
                           const cuComplex
                                                  *y, int incy,
                           cuComplex
                                           *result)
cublasStatus_t cublasCdotc(cublasHandle_t handle, int n,
                           const cuComplex
                                                 *x, int incx,
                           const cuComplex
                                                  *y, int incy,
                           cuComplex
                                           *result)
cublasStatus_t cublasZdotu(cublasHandle_t handle, int n,
                           const cuDoubleComplex *x, int incx,
                           const cuDoubleComplex *y, int incy,
                           cuDoubleComplex *result)
cublasStatus_t cublasZdotc(cublasHandle_t handle, int n,
                           const cuDoubleComplex *x, int incx,
                           const cuDoubleComplex *y, int incy,
                           cuDoubleComplex *result)
```

This function computes the dot product of vectors \mathbf{x} and \mathbf{y} . Hence, the result is $\sum_{i=1}^{n} (\mathbf{x}[k] \times \mathbf{y}[j])$ where k = 1 + (i-1) * incx and j = 1 + (i-1) * incy. Notice that in the first equation the conjugate of the element of vector \mathbf{x} should be used if the function name ends in character 'c' and that the last two equations reflect 1-based indexing used for compatibility with Fortran.

Param.	Memory	In/out	Meaning
handle		input	handle to the CUBLAS library context.
n		input	number of elements in the vectors x and y .
X	device	input	<type> vector with n elements.</type>
incx		input	stride between consecutive elements of x.
У	device	input	<type> vector with n elements.</type>
incy		input	stride between consecutive elements of y.
result	host or device	output	the resulting dot product, which is 0.0 if n<=0.

The possible error values returned by this function and their meanings are listed below.

Error Values	Meaning
CUBLAS_STATUS_SUCCESS	the operation completed successfully
CUBLAS_STATUS_NOT_INITIALIZED	the library was not initialized
CUBLAS_STATUS_ALLOC_FAILED	the reduction buffer could not be allocated
CUBLAS_STATUS_ARCH_MISMATCH	the device does not support double-precision
CUBLAS_STATUS_EXECUTION_FAILED	the function failed to launch on the GPU

For references please refer to: sdot, ddot, cdotu, cdotc, zdotu, zdotc

5.7 cublas<t>nrm2()

This function computes the Euclidean norm of the vector \mathbf{x} . The code uses a multiphase model of accumulation to avoid intermediate underflow and overflow, with the result being equivalent to $\sqrt{\sum_{i=1}^{n} (\bar{\mathbf{x}}[j] \times \mathbf{x}[j])}$ where j = 1 + (i-1) * incx in exact arithmetic. Notice that the last equation reflects 1-based indexing used for compatibility with Fortran.

Param.	Memory	In/out	Meaning
handle		input	handle to the CUBLAS library context.
\mathbf{n}		input	number of elements in the vector x .
X	device	input	<type> vector with n elements.</type>
incx		input	stride between consecutive elements of x.
result	host or device	output	the resulting norm, which is 0.0 if n,incx<=0.

The possible error values returned by this function and their meanings are listed below.

Error Values	Meaning
CUBLAS_STATUS_SUCCESS	the operation completed successfully
CUBLAS_STATUS_NOT_INITIALIZED	the library was not initialized
CUBLAS_STATUS_ALLOC_FAILED	the reduction buffer could not be allocated
CUBLAS_STATUS_ARCH_MISMATCH	the device does not support double-precision
CUBLAS_STATUS_EXECUTION_FAILED	the function failed to launch on the GPU

For references please refer to:

snrm2, snrm2, dnrm2, dnrm2, scnrm2, scnrm2, dznrm2

5.8 cublas<t>rot()

This function applies Givens rotation matrix

$$G = \left(\begin{array}{cc} c & s \\ -s & c \end{array}\right)$$

to vectors \mathbf{x} and \mathbf{y} .

Hence, the result is $\mathbf{x}[k] = c \times \mathbf{x}[k] + s \times \mathbf{y}[j]$ and $\mathbf{y}[j] = -s \times \mathbf{x}[k] + c \times \mathbf{y}[j]$ where k = 1 + (i - 1) * incx and j = 1 + (i - 1) * incy. Notice that the last two equations reflect 1-based indexing used for compatibility with Fortran.

Param.	Memory	In/out	Meaning
handle		input	handle to the CUBLAS library context.
\mathbf{n}		input	number of elements in the vectors \mathbf{x} and \mathbf{y} .
X	device	in/out	<type> vector with n elements.</type>
incx		input	stride between consecutive elements of x.
y	device	in/out	<type> vector with n elements.</type>
incy		input	stride between consecutive elements of y.
\mathbf{c}	host or device	input	cosine element of the rotation matrix.
s	host or device	input	sine element of the rotation matrix.

The possible error values returned by this function and their meanings are listed below.

Error Values	Meaning
CUBLAS_STATUS_SUCCESS	the operation completed successfully
CUBLAS_STATUS_NOT_INITIALIZED	the library was not initialized
CUBLAS_STATUS_ARCH_MISMATCH	the device does not support double-precision
CUBLAS_STATUS_EXECUTION_FAILED	the function failed to launch on the GPU

For references please refer to: srot, drot, crot, csrot, zrot, zdrot

5.9 cublas<t>rotg()

cublasStatus_t cublasSrotg(cublasHandle_t handle,

float *c, float *s)

cublasStatus_t cublasDrotg(cublasHandle_t handle,

double *c, double *s)

cublasStatus_t cublasCrotg(cublasHandle_t handle,

cublasStatus_t cublasZrotg(cublasHandle_t handle,

This function constructs the Givens rotation matrix

$$G = \left(\begin{array}{cc} c & s \\ -s & c \end{array}\right)$$

that zeros out the second entry of a 2×1 vector $(a, b)^T$.

Then, for real numbers we can write

$$\left(\begin{array}{cc}c&s\\-s&c\end{array}\right)\left(\begin{array}{c}a\\b\end{array}\right)=\left(\begin{array}{c}r\\0\end{array}\right)$$

where $c^2 + s^2 = 1$ and $r = a^2 + b^2$. The parameters a and b are overwritten with r and z, respectively. The value of z is such that c and s may be recovered using the following rules:

$$(c,s) = \begin{cases} (\sqrt{1-z^2}, z) & \text{if } |z| < 1\\ (0.0, 1.0) & \text{if } |z| = 1\\ (1/z, \sqrt{1-z^2}) & \text{if } |z| > 1 \end{cases}$$

For complex numbers we can write

$$\left(\begin{array}{cc} c & s \\ -\bar{s} & c \end{array}\right) \left(\begin{array}{c} a \\ b \end{array}\right) = \left(\begin{array}{c} r \\ 0 \end{array}\right)$$

where $c^2 + (\bar{s} \times s) = 1$ and $r = \frac{a}{|a|} \times ||(a,b)^T||_2$ with $||(a,b)^T||_2 = \sqrt{|a|^2 + |b|^2}$ for $a \neq 0$ and r = b for a = 0. Finally, the parameter a is overwritten with r on exit.

Param.	Memory	In/out	Meaning
handle		input	handle to the CUBLAS library context.
a	host or device	in/out	$\langle \text{type} \rangle$ scalar that is overwritten with r .
b	host or device	in/out	$\langle \text{type} \rangle$ scalar that is overwritten with z.
c	host or device	output	cosine element of the rotation matrix.
S	host or device	output	sine element of the rotation matrix.

The possible error values returned by this function and their meanings are listed below.

Error Values	Meaning
CUBLAS_STATUS_SUCCESS	the operation completed successfully
CUBLAS_STATUS_NOT_INITIALIZED	the library was not initialized
CUBLAS_STATUS_ARCH_MISMATCH	the device does not support double-precision
CUBLAS_STATUS_EXECUTION_FAILED	the function failed to launch on the GPU

For references please refer to: srotg, drotg, crotg, zrotg

5.10 cublas<t>rotm()

This function applies the modified Givens transformation

$$H = \left(\begin{array}{cc} h_{11} & h_{12} \\ h_{21} & h_{22} \end{array}\right)$$

to vectors \mathbf{x} and \mathbf{y} .

Hence, the result is $\mathbf{x}[k] = h_{11} \times \mathbf{x}[k] + h_{12} \times \mathbf{y}[j]$ and $\mathbf{y}[j] = h_{21} \times \mathbf{x}[k] + h_{22} \times \mathbf{y}[j]$ where k = 1 + (i - 1) * incx and j = 1 + (i - 1) * incy. Notice that the last two equations reflect 1-based indexing used for compatibility with Fortran.

The elements h_{11} , h_{21} , h_{12} and h_{22} of 2×2 matrix H are stored in param[1], param[2], param[3] and param[4], respectively. The flag = param[0] defines the following predefined values for the matrix H entries

Notice that the values -1.0, 0.0 and 1.0 implied by the flag are not stored in param.

Param.	Memory	In/out	Meaning
handle		input	handle to the CUBLAS library context.
n		input	number of elements in the vectors x and y .
X	device	in/out	<type> vector with n elements.</type>
incx		input	stride between consecutive elements of x.
У	device	in/out	<type> vector with n elements.</type>
incy		input	stride between consecutive elements of y.
param	host or device	input	<pre><type> vector of 5 elements, where param[0]</type></pre>
			and $param[1-4]$ contain the flag and matrix H .

The possible error values returned by this function and their meanings are listed below.

Error Values	Meaning
CUBLAS_STATUS_SUCCESS	the operation completed successfully
CUBLAS_STATUS_NOT_INITIALIZED	the library was not initialized
CUBLAS_STATUS_ARCH_MISMATCH	the device does not support double-precision
CUBLAS_STATUS_EXECUTION_FAILED	the function failed to launch on the GPU

For references please refer to: srotm, drotm

5.11 cublas<t>rotmg()

This function constructs the modified Givens transformation

$$H = \left(\begin{array}{cc} h_{11} & h_{12} \\ h_{21} & h_{22} \end{array} \right)$$

that zeros out the second entry of a 2×1 vector $(\sqrt{d1} * x1, \sqrt{d2} * y1)^T$.

The flag = param[0] defines the following predefined values for the matrix H entries

Notice that the values -1.0, 0.0 and 1.0 implied by the flag are not stored in param.

Param.	Memory	In/out	Meaning
handle		input	handle to the CUBLAS library context.
d1	host or device	in/out	<pre><type> scalar that is overwritten on exit.</type></pre>
d2	host or device	in/out	<pre><type> scalar that is overwritten on exit.</type></pre>
x1	host or device	in/out	<pre><type> scalar that is overwritten on exit.</type></pre>
y1	host or device	input	<type> scalar.</type>
param	host or device	output	<pre><type> vector of 5 elements, where param[0]</type></pre>
			and $param[1-4]$ contain the flag and matrix H .

Error Values	Meaning
CUBLAS_STATUS_SUCCESS	the operation completed successfully
CUBLAS_STATUS_NOT_INITIALIZED	the library was not initialized
CUBLAS_STATUS_ARCH_MISMATCH	the device does not support double-precision
CUBLAS_STATUS_EXECUTION_FAILED	the function failed to launch on the GPU

For references please refer to: srotmg, drotmg

5.12 cublas<t>scal()

```
cublasStatus_t cublasSscal (cublasHandle_t handle, int n,
                            const float
                                                   *alpha,
                            float
                                             *x, int incx)
cublasStatus_t cublasDscal (cublasHandle_t handle, int n,
                            const double
                                                   *alpha,
                                             *x, int incx)
                            double
cublasStatus_t cublasCscal (cublasHandle_t handle, int n,
                            const cuComplex
                                                   *alpha,
                            cuComplex
                                             *x, int incx)
cublasStatus_t cublasCsscal(cublasHandle_t handle, int n,
                            const float
                                                   *alpha,
                                            *x, int incx)
                            cuComplex
cublasStatus_t cublasZscal (cublasHandle_t handle, int n,
                            const cuDoubleComplex *alpha,
                            cuDoubleComplex *x, int incx)
cublasStatus_t cublasZdscal(cublasHandle_t handle, int n,
                            const double
                                                   *alpha,
                            cuDoubleComplex *x, int incx)
```

This function scales the vector \mathbf{x} by the scalar α and overwrites it with the result. Hence, the performed operation is $\mathbf{x}[j] = \alpha \times \mathbf{x}[j]$ for i = 1, ..., n and j = 1 + (i - 1) * incx. Notice that the last two equations reflect 1-based indexing used for compatibility with Fortran.

Param.	Memory	In/out	Meaning
handle		input	handle to the CUBLAS library context.
alpha	host or device	input	<type> scalar used for multiplication.</type>
n		input	number of elements in the vector x .
X	device	in/out	<type> vector with n elements.</type>
incx		input	stride between consecutive elements of x.

Error Values	Meaning
CUBLAS_STATUS_SUCCESS	the operation completed successfully
CUBLAS_STATUS_NOT_INITIALIZED	the library was not initialized
CUBLAS_STATUS_ARCH_MISMATCH	the device does not support double-precision
CUBLAS_STATUS_EXECUTION_FAILED	the function failed to launch on the GPU

For references please refer to: sscal, dscal, cscal, cscal, zdscal, zdscal, zdscal, zdscal

5.13 cublas<t>swap()

This function interchanges the elements of vector \mathbf{x} and \mathbf{y} . Hence, the performed operation is $\mathbf{y}[j] \Leftrightarrow \mathbf{x}[k]$ for i = 1, ..., n, k = 1 + (i - 1) * incx and j = 1 + (i - 1) * incy. Notice that the last two equations reflect 1-based indexing used for compatibility with Fortran.

Param.	Memory	In/out	Meaning
handle		input	handle to the CUBLAS library context.
\mathbf{n}		input	number of elements in the vector \mathbf{x} and \mathbf{y} .
X	device	in/out	<type> vector with n elements.</type>
incx		input	stride between consecutive elements of x.
y	device	in/out	<type> vector with n elements.</type>
incy		input	stride between consecutive elements of y.

The possible error values returned by this function and their meanings are listed below.

Error Values	Meaning
CUBLAS_STATUS_SUCCESS	the operation completed successfully
CUBLAS_STATUS_NOT_INITIALIZED	the library was not initialized
CUBLAS_STATUS_ARCH_MISMATCH	the device does not support double-precision
CUBLAS_STATUS_EXECUTION_FAILED	the function failed to launch on the GPU

For references please refer to: sswap, dswap, cswap, zswap

Chapter 6 CUBLAS Level-2 Function Reference

In this chapter we describe the Level-2 Basic Linear Algebra Subprograms (BLAS2) functions that perform matrix-vector operations.

6.1 cublas<t>gbmv()

```
cublasStatus_t cublasSgbmv(cublasHandle_t handle, cublasOperation_t trans,
                           int m, int n, int kl, int ku,
                           const float
                                                  *alpha,
                           const float
                                                  *A, int lda,
                           const float
                                                  *x, int incx,
                           const float
                                                  *beta,
                           float
                                            *y, int incy)
cublasStatus_t cublasDgbmv(cublasHandle_t handle, cublasOperation_t trans,
                           int m, int n, int kl, int ku,
                           const double
                                                  *alpha,
                           const double
                                                  *A, int lda,
                           const double
                                                  *x, int incx,
                           const double
                                                  *beta,
                                            *y, int incy)
                           double
cublasStatus_t cublasCgbmv(cublasHandle_t handle, cublasOperation_t trans,
                           int m, int n, int kl, int ku,
                           const cuComplex
                                                  *alpha,
                           const cuComplex
                                                  *A, int lda,
                           const cuComplex
                                                  *x, int incx,
                           const cuComplex
                                                  *beta,
                                            *y, int incy)
                           cuComplex
cublasStatus_t cublasZgbmv(cublasHandle_t handle, cublasOperation_t trans,
                           int m, int n, int kl, int ku,
                           const cuDoubleComplex *alpha,
                           const cuDoubleComplex *A, int lda,
                           const cuDoubleComplex *x, int incx,
```

This function performs the banded matrix-vector multiplication

$$\mathbf{y} = \alpha \operatorname{op}(A)\mathbf{x} + \beta \mathbf{y}$$

where A is a $m \times n$ banded matrix with kl subdiagonals and ku superdiagonals, \mathbf{x} and \mathbf{y} are vectors, and α and β are scalars. Also, for matrix A

$$\mathrm{op}(A) = \begin{cases} A & \text{if transa} == \texttt{CUBLAS_OP_N} \\ A^T & \text{if transa} == \texttt{CUBLAS_OP_T} \\ A^H & \text{if transa} == \texttt{CUBLAS_OP_C} \end{cases}$$

The banded matrix A is stored column by column, with the main diagonal stored in row ku+1 (starting in first position), the first superdiagonal stored in row ku (starting in second position), the first subdiagonal stored in row ku+2 (starting in first position), etc. So that in general, the element A(i,j) is stored in the memory location A(ku+1+i-j,j) for $j=1,\ldots,n$ and $i\in [\max(1,j-ku),\min(m,j+kl)]$. Also, the elements in the array A that do not conceptually correspond to the elements in the banded matrix (the top left $ku\times ku$ and bottom right $kl\times kl$ triangles) are not referenced.

Param.	Memory	In/out	Meaning
handle		input	handle to the CUBLAS library context.
trans		input	operation op(A) that is non- or (conj.) transpose.
m		input	number of rows of matrix A.
n		input	number of columns of matrix A.
kl		input	number of subdiagonals of matrix A.
ku		input	number of superdiagonals of matrix A.
alpha	host or device	input	<type> scalar used for multiplication.</type>
A	device	input	$<$ type $>$ array of dimension lda \times n
			with $lda \ge kl+ku+1$.
lda		input	leading dimension of two-dimensional array used
			to store matrix A.
X	device	input	<type> vector with n elements if</type>
			transa == CUBLAS_OP_N and m elements otherwise.
incx		input	stride between consecutive elements of x.
beta	host or device	input	<pre><type> scalar used for multiplication, if beta==0</type></pre>
			then y does not have to be a valid input.
У	device	in/out	<type> vector with m elements if</type>
			transa == CUBLAS_OP_N and n elements otherwise.
incy		input	stride between consecutive elements of y.

The possible error values returned by this function and their meanings are listed below.

Error Values	Meaning
CUBLAS_STATUS_SUCCESS	the operation completed successfully
CUBLAS_STATUS_NOT_INITIALIZED	the library was not initialized
CUBLAS_STATUS_INVALID_VALUE	the parameters m,n,kl,ku<0 or incx,incy=0
CUBLAS_STATUS_ARCH_MISMATCH	the device does not support double-precision
CUBLAS_STATUS_EXECUTION_FAILED	the function failed to launch on the GPU

For references please refer to: sgbmv, dgbmv, cgbmv, zgbmv

6.2 cublas<t>gemv()

```
cublasStatus_t cublasSgemv(cublasHandle_t handle, cublasOperation_t trans,
                           int m, int n,
                           const float
                                                 *alpha,
                           const float
                                                 *A, int lda,
                           const float
                                                 *x, int incx,
                           const float
                                                  *beta,
                           float
                                           *y, int incy)
cublasStatus_t cublasDgemv(cublasHandle_t handle, cublasOperation_t trans,
                           int m, int n,
                           const double
                                                 *alpha,
                           const double
                                                 *A, int lda,
                           const double
                                                  *x, int incx,
                           const double
                                                  *beta,
                           double
                                           *y, int incy)
cublasStatus_t cublasCgemv(cublasHandle_t handle, cublasOperation_t trans,
                           int m, int n,
                           const cuComplex
                                                  *alpha,
                           const cuComplex
                                                  *A, int lda,
                           const cuComplex
                                                 *x, int incx,
                           const cuComplex
                                                 *beta,
                           cuComplex
                                           *y, int incy)
cublasStatus_t cublasZgemv(cublasHandle_t handle, cublasOperation_t trans,
                           int m, int n,
                           const cuDoubleComplex *alpha,
                           const cuDoubleComplex *A, int lda,
                           const cuDoubleComplex *x, int incx,
                           const cuDoubleComplex *beta,
                           cuDoubleComplex *y, int incy)
```

This function performs the matrix-vector multiplication

$$\mathbf{y} = \alpha \operatorname{op}(A)\mathbf{x} + \beta \mathbf{y}$$

where A is a $m \times n$ matrix stored in column-major format, \mathbf{x} and \mathbf{y} are vectors, and α and β are scalars. Also, for matrix A

$$\mathrm{op}(A) = \begin{cases} A & \text{if transa} == \texttt{CUBLAS_OP_N} \\ A^T & \text{if transa} == \texttt{CUBLAS_OP_T} \\ A^H & \text{if transa} == \texttt{CUBLAS_OP_C} \end{cases}$$

Param.	Memory	In/out	Meaning
handle		input	handle to the CUBLAS library context.
trans		input	operation op(A) that is non- or (conj.) transpose.
m		input	number of rows of matrix A.
n		input	number of columns of matrix A.
alpha	host or device	input	<type> scalar used for multiplication.</type>
A	device	input	$<$ type $>$ array of dimension lda \times n
			with $lda \ge max(1,m)$ if transa==CUBLAS_OP_N
		input	and $1da \times m$ with $1da \ge max(1,n)$ otherwise.
lda		input	leading dimension of two-dimensional array
			used to store matrix A.
X	device	input	<type> vector with n elements if</type>
		input	transa==CUBLAS_OP_N and m elements otherwise.
incx		input	stride between consecutive elements of x.
beta	host or device	input	<pre><type> scalar used for multiplication, if beta==0</type></pre>
		input	then y does not have to be a valid input.
У	device	input	<type> vector with m elements if</type>
		in/out	transa==CUBLAS_OP_N and n elements otherwise.
incy		input	stride between consecutive elements of y.

The possible error values returned by this function and their meanings are listed below.

Error Values	Meaning
CUBLAS_STATUS_SUCCESS	the operation completed successfully
CUBLAS_STATUS_NOT_INITIALIZED	the library was not initialized
CUBLAS_STATUS_INVALID_VALUE	the parameters m,n<0 or incx,incy=0
CUBLAS_STATUS_ARCH_MISMATCH	the device does not support double-precision
CUBLAS_STATUS_EXECUTION_FAILED	the function failed to launch on the GPU

For references please refer to: sgemv, dgemv, cgemv, zgemv

6.3 cublas<t>ger()

```
const float
                                                 *x, int incx,
                           const float
                                                 *y, int incy,
                           float
                                           *A, int lda)
cublasStatus_t cublasDger (cublasHandle_t handle, int m, int n,
                          const double
                                                 *alpha,
                          const double
                                                 *x, int incx,
                          const double
                                                 *y, int incy,
                                           *A, int lda)
                          double
cublasStatus_t cublasCgeru(cublasHandle_t handle, int m, int n,
                           const cuComplex
                                                 *alpha,
                           const cuComplex
                                                *x, int incx,
                           const cuComplex
                                                *y, int incy,
                                           *A, int lda)
                           cuComplex
cublasStatus_t cublasCgerc(cublasHandle_t handle, int m, int n,
                           const cuComplex
                                                *alpha,
                           const cuComplex
                                                *x, int incx,
                           const cuComplex
                                                 *y, int incy,
                           cuComplex
                                           *A, int lda)
cublasStatus_t cublasZgeru(cublasHandle_t handle, int m, int n,
                           const cuDoubleComplex *alpha,
                           const cuDoubleComplex *x, int incx,
                           const cuDoubleComplex *y, int incy,
                           cuDoubleComplex *A, int lda)
cublasStatus_t cublasZgerc(cublasHandle_t handle, int m, int n,
                           const cuDoubleComplex *alpha,
                           const cuDoubleComplex *x, int incx,
                           const cuDoubleComplex *y, int incy,
                           cuDoubleComplex *A, int lda)
```

This function performs the rank-1 update

$$A = \begin{cases} \alpha \mathbf{x} \mathbf{y}^T + A & \text{if ger(),geru() is called} \\ \alpha \mathbf{x} \mathbf{y}^H + A & \text{if gerc() is called} \end{cases}$$

where A is a $m \times n$ matrix stored in column-major format, **x** and **y** are vectors, and α is a scalar.

Param.	Memory	In/out	Meaning
handle		input	handle to the CUBLAS library context.
m		input	number of rows of matrix A.
n		input	number of columns of matrix A.
alpha	host or device	input	<type> scalar used for multiplication.</type>
X	device	input	<type> vector with m elements.</type>
incx		input	stride between consecutive elements of x.
У	device	input	<type> vector with n elements.</type>
incy		input	stride between consecutive elements of y.
A	device	in/out	$<$ type $>$ array of dimension lda \times n
			with $lda \ge max(1,m)$.
lda		input	leading dimension of two-dimensional array used
			to store matrix A.

Error Values	Meaning
CUBLAS_STATUS_SUCCESS	the operation completed successfully
CUBLAS_STATUS_NOT_INITIALIZED	the library was not initialized
CUBLAS_STATUS_INVALID_VALUE	the parameters m,n<0 or incx,incy=0
CUBLAS_STATUS_ARCH_MISMATCH	the device does not support double-precision
CUBLAS_STATUS_EXECUTION_FAILED	the function failed to launch on the GPU

For references please refer to:

sger, dger, cgeru, cgerc, zgeru, zgerc

6.4 cublas<t>sbmv()

This function performs the symmetric banded matrix-vector multiplication

$$\mathbf{y} = \alpha A \mathbf{x} + \beta \mathbf{y}$$

where A is a $n \times n$ symmetric banded matrix with k subdiagonals and superdiagonals, **x** and **y** are vectors, and α and β are scalars.

If uplo == CUBLAS_FILL_MODE_LOWER then the symmetric banded matrix A is stored column by column, with the main diagonal of the matrix stored in row 1, the first subdiagonal in row 2 (starting at first position), the second subdiagonal in row 3 (starting at first position), etc. So that in general, the element A(i,j) is stored in the memory location A(1+i-j,j) for $j=1,\ldots,n$ and $i\in[j,\min(m,j+k)]$. Also, the elements in the array A that do not conceptually correspond to the elements in the banded matrix (the bottom right $k \times k$ triangle) are not referenced.

If uplo == CUBLAS_FILL_MODE_UPPER then the symmetric banded matrix A is stored column by column, with the main diagonal of the matrix stored in row k+1, the first superdiagonal in row k (starting at second position), the second superdiagonal in row k-1 (starting at third position), etc. So that in general, the element A(i,j) is stored in the memory location A(1+k+i-j,j) for $j=1,\ldots,n$ and $i\in[\max(1,j-k),j]$. Also, the elements in the array A that do not conceptually correspond to the elements in the banded matrix (the top left $k \times k$ triangle) are not referenced.

Param.	Memory	In/out	Meaning
handle		input	handle to the CUBLAS library context.
uplo		input	indicates if matrix A lower or upper part
			is stored, the other symmetric part is not referen-
			ced and is inferred from the stored elements.
n		input	number of rows and columns of matrix A.
k		input	number of sub- and super-diagonals of matrix A.
alpha	host or device	input	<type> scalar used for multiplication.</type>
A	device	input	$<$ type $>$ array of dimension lda \times n
			with $lda \ge k+1$.
lda		input	leading dimension of two-dimensional array used
			to store matrix A.
X	device	input	<type> vector with n elements.</type>
incx		input	stride between consecutive elements of x.
beta	host or device	input	<pre><type> scalar used for multiplication, if beta==0</type></pre>
			then y does not have to be a valid input.
У	device	in/out	<type> vector with n elements.</type>
incy		input	stride between consecutive elements of y.

The possible error values returned by this function and their meanings are listed below.

Error Values	Meaning
CUBLAS_STATUS_SUCCESS	the operation completed successfully
CUBLAS_STATUS_NOT_INITIALIZED	the library was not initialized
CUBLAS_STATUS_INVALID_VALUE	the parameters n,k<0 or incx,incy=0
CUBLAS_STATUS_ARCH_MISMATCH	the device does not support double-precision
CUBLAS_STATUS_EXECUTION_FAILED	the function failed to launch on the GPU

For references please refer to: ssbmv, dsbmv

6.5 cublas<t>spmv()

This function performs the symmetric packed matrix-vector multiplication

$$\mathbf{y} = \alpha A \mathbf{x} + \beta \mathbf{y}$$

where A is a $n \times n$ symmetric matrix stored in packed format, **x** and **y** are vectors, and α and β are scalars.

If uplo == CUBLAS_FILL_MODE_LOWER then the elements in the lower triangular part of the symmetric matrix A are packed together column by column without gaps, so that the element A(i,j) is stored in the memory location AP[i+((2*n-j+1)*j)/2] for $j=1,\ldots,n$ and $i\geq j$. Consequently, the packed format requires only $\frac{n(n+1)}{2}$ elements for storage.

If uplo == CUBLAS_FILL_MODE_UPPER then the elements in the upper triangular part of the symmetric matrix A are packed together column by column without gaps, so that the element A(i,j) is stored in the memory location AP[i+(j*(j+1))/2] for $j=1,\ldots,n$ and $i \leq j$. Consequently, the packed format requires only $\frac{n(n+1)}{2}$ elements for storage.

Param.	Memory	In/out	Meaning
handle		input	handle to the CUBLAS library context.
uplo		input	indicates if matrix A lower or upper part
			is stored, the other symmetric part is not referen-
			ced and is inferred from the stored elements.
n		input	number of rows and columns of matrix A .
k		input	number of sub- and super-diagonals of matrix A .
alpha	host or device	input	<type> scalar used for multiplication.</type>
AP	device	input	$\langle \text{type} \rangle$ array with A stored in packed format.
X	device	input	<type> vector with n elements.</type>
incx		input	stride between consecutive elements of x.
beta	host or device	input	<pre><type> scalar used for multiplication, if beta==0</type></pre>
			then y does not have to be a valid input.
у	device	input	<type> vector with n elements.</type>
incy		input	stride between consecutive elements of y.

The possible error values returned by this function and their meanings are listed below.

Error Values	Meaning
CUBLAS_STATUS_SUCCESS	the operation completed successfully
CUBLAS_STATUS_NOT_INITIALIZED	the library was not initialized
CUBLAS_STATUS_INVALID_VALUE	the parameters n<0 or incx,incy=0
CUBLAS_STATUS_ARCH_MISMATCH	the device does not support double-precision
CUBLAS_STATUS_EXECUTION_FAILED	the function failed to launch on the GPU

For references please refer to: sspmv, dspmv

6.6 cublas<t>spr()

This function performs the packed symmetric rank-1 update

$$A = \alpha \mathbf{x} \mathbf{x}^T + A$$

where A is a $n \times n$ symmetric matrix stored in packed format, \mathbf{x} is a vector, and α is a scalar.

If uplo == CUBLAS_FILL_MODE_LOWER then the elements in the lower triangular part of the symmetric matrix A are packed together column by column without gaps, so that the element A(i,j) is stored in the memory location AP[i+((2*n-j+1)*j)/2] for $j=1,\ldots,n$ and $i\geq j$. Consequently, the packed format requires only $\frac{n(n+1)}{2}$ elements for storage.

If uplo == CUBLAS_FILL_MODE_UPPER then the elements in the upper triangular part of the symmetric matrix A are packed together column by column without gaps, so that the element A(i,j) is stored in the memory location AP[i+(j*(j+1))/2] for $j=1,\ldots,n$ and $i \leq j$. Consequently, the packed format requires only $\frac{n(n+1)}{2}$ elements for storage.

Param.	Memory	In/out	Meaning
handle		input	handle to the CUBLAS library context.
uplo		input	indicates if matrix A lower or upper part
			is stored, the other symmetric part is not referen-
			ced and is inferred from the stored elements.
n		input	number of rows and columns of matrix A .
alpha	host or device	input	<type> scalar used for multiplication.</type>
X	device	input	<type> vector with n elements.</type>
incx		input	stride between consecutive elements of x.
AP	device	in/out	$\langle \text{type} \rangle$ array with A stored in packed format.

Error Values	Meaning
CUBLAS_STATUS_SUCCESS	the operation completed successfully
CUBLAS_STATUS_NOT_INITIALIZED	the library was not initialized
CUBLAS_STATUS_INVALID_VALUE	the parameters n<0 or incx,incy=0
CUBLAS_STATUS_ARCH_MISMATCH	the device does not support double-precision
CUBLAS_STATUS_EXECUTION_FAILED	the function failed to launch on the GPU

For references please refer to: sspr, dspr

6.7 cublas<t>spr2()

This function performs the packed symmetric rank-2 update

$$A = \alpha \left(\mathbf{x} \mathbf{y}^T + \mathbf{y} \mathbf{x}^T \right) + A$$

where A is a $n \times n$ symmetric matrix stored in packed format, **x** and **y** are vectors, and α is a scalar.

If uplo == CUBLAS_FILL_MODE_LOWER then the elements in the lower triangular part of the symmetric matrix A are packed together column by column without gaps, so that the element A(i,j) is stored in the memory location AP[i+((2*n-j+1)*j)/2] for $j=1,\ldots,n$ and $i\geq j$. Consequently, the packed format requires only $\frac{n(n+1)}{2}$ elements for storage.

If uplo == CUBLAS_FILL_MODE_UPPER then the elements in the upper triangular part of the symmetric matrix A are packed together column by column without gaps, so that the element A(i,j) is stored in the memory location AP[i+(j*(j+1))/2] for $j=1,\ldots,n$ and $i \leq j$. Consequently, the packed format requires only $\frac{n(n+1)}{2}$ elements for storage.

Param.	Memory	In/out	Meaning
handle		input	handle to the CUBLAS library context.
uplo		input	indicates if matrix A lower or upper part
			is stored, the other symmetric part is not referen-
			ced and is inferred from the stored elements.
n		input	number of rows and columns of matrix A .
alpha	host or device	input	<type> scalar used for multiplication.</type>
X	device	input	<type> vector with n elements.</type>
incx		input	stride between consecutive elements of x.
У	device	input	<type> vector with n elements.</type>
incy		input	stride between consecutive elements of y.
AP	device	in/out	$\langle \text{type} \rangle$ array with A stored in packed format.

Error Values	Meaning
CUBLAS_STATUS_SUCCESS	the operation completed successfully
CUBLAS_STATUS_NOT_INITIALIZED	the library was not initialized
CUBLAS_STATUS_INVALID_VALUE	the parameters n<0 or incx,incy=0
CUBLAS_STATUS_ARCH_MISMATCH	the device does not support double-precision
CUBLAS_STATUS_EXECUTION_FAILED	the function failed to launch on the GPU

For references please refer to: sspr2, dspr2

6.8 cublas<t>symv()

This function performs the symmetric matrix-vector multiplication

$$\mathbf{y} = \alpha A \mathbf{x} + \beta \mathbf{y}$$

where A is a $n \times n$ symmetric matrix stored in lower or upper mode, **x** and **y** are vectors, and α and β are scalars.

Param.	Memory	In/out	Meaning
handle		input	handle to the CUBLAS library context.
uplo		input	indicates if matrix A lower or upper part
			is stored, the other symmetric part is not referen-
			ced and is inferred from the stored elements.
n		input	number of rows and columns of matrix A.
alpha	host or device	input	<type> scalar used for multiplication.</type>
A	device	input	$<$ type $>$ array of dimension lda \times n
			with $lda \ge max(1,n)$.
lda		input	leading dimension of two-dimensional array used
			to store matrix A.
X	device	input	<type> vector with n elements.</type>
incx		input	stride between consecutive elements of x.
beta	host or device	input	<pre><type> scalar used for multiplication, if beta==0</type></pre>
			then y does not have to be a valid input.
У	device	in/out	<type> vector with n elements.</type>
incy		input	stride between consecutive elements of y.

Error Values	Meaning
CUBLAS_STATUS_SUCCESS	the operation completed successfully
CUBLAS_STATUS_NOT_INITIALIZED	the library was not initialized
CUBLAS_STATUS_INVALID_VALUE	the parameters n<0 or incx,incy=0
CUBLAS_STATUS_ARCH_MISMATCH	the device does not support double-precision
CUBLAS_STATUS_EXECUTION_FAILED	the function failed to launch on the GPU

For references please refer to: ssymv, dsymv

6.9 cublas<t>syr()

This function performs the symmetric rank-1 update

$$A = \alpha \mathbf{x} \mathbf{x}^T + A$$

where A is a $n \times n$ symmetric matrix stored in column-major format, **x** is a vector, and α is a scalar.

Param.	Memory	In/out	Meaning
handle		input	handle to the CUBLAS library context.
uplo		input	indicates if matrix A lower or upper part,
			is stored, the other symmetric part is not referen-
		input	ced and is inferred from the stored elements.
n		input	number of rows and columns of matrix A.
alpha	host or device	input	<type> scalar used for multiplication.</type>
X	device	input	<type> vector with n elements.</type>
incx		input	stride between consecutive elements of x.
A	device	in/out	$<$ type $>$ array of dimensions lda \times n,
			with $lda \ge max(1,n)$.
lda		input	leading dimension of two-dimensional array used
			to store matrix A.

Error Values	Meaning
CUBLAS_STATUS_SUCCESS	the operation completed successfully
CUBLAS_STATUS_NOT_INITIALIZED	the library was not initialized
CUBLAS_STATUS_INVALID_VALUE	the parameters n<0 or incx=0
CUBLAS_STATUS_ARCH_MISMATCH	the device does not support double-precision
CUBLAS_STATUS_EXECUTION_FAILED	the function failed to launch on the GPU

For references please refer to:

ssyr, dsyr

6.10 cublas<t>syr2()

This function performs the symmetric rank-2 update

$$A = \alpha \left(\mathbf{x} \mathbf{y}^T + \mathbf{y} \mathbf{x}^T \right) + A$$

where A is a $n \times n$ symmetric matrix stored in column-major format, **x** and **y** are vectors, and α is a scalar.

Param.	Memory	In/out	Meaning
handle		input	handle to the CUBLAS library context.
uplo		input	indicates if matrix A lower or upper part
			is stored, the other symmetric part is not referen-
			ced and is inferred from the stored elements.
n		input	number of rows and columns of matrix A.
alpha	host or device	input	<type> scalar used for multiplication.</type>
X	device	input	<type> vector with n elements.</type>
incx		input	stride between consecutive elements of x.
У	device	input	<type> vector with n elements.</type>
incy		input	stride between consecutive elements of y.
A	device	in/out	$<$ type $>$ array of dimensions lda \times n,
			with $lda \ge max(1,n)$.
lda		input	leading dimension of two-dimensional array used
			to store matrix A.

Error Values	Meaning
CUBLAS_STATUS_SUCCESS	the operation completed successfully
CUBLAS_STATUS_NOT_INITIALIZED	the library was not initialized
CUBLAS_STATUS_INVALID_VALUE	the parameters n<0 or incx,incy=0
CUBLAS_STATUS_ARCH_MISMATCH	the device does not support double-precision
CUBLAS_STATUS_EXECUTION_FAILED	the function failed to launch on the GPU

For references please refer to: ssyr2, dsyr2

6.11 cublas<t>tbmv()

```
cublasStatus_t cublasStbmv(cublasHandle_t handle, cublasFillMode_t uplo,
                           cublasOperation_t trans, cublasDiagType_t diag,
                           int n, int k, const float
                                                                *A, int lda,
                           float
                                           *x, int incx)
cublasStatus_t cublasDtbmv(cublasHandle_t handle, cublasFillMode_t uplo,
                           cublasOperation_t trans, cublasDiagType_t diag,
                           int n, int k, const double
                                                                *A, int lda,
                           double
                                           *x, int incx)
cublasStatus_t cublasCtbmv(cublasHandle_t handle, cublasFillMode_t uplo,
                           cublasOperation_t trans, cublasDiagType_t diag,
                           int n, int k, const cuComplex
                                                                *A, int lda,
                           cuComplex
                                           *x, int incx)
cublasStatus_t cublasZtbmv(cublasHandle_t handle, cublasFillMode_t uplo,
                           cublasOperation_t trans, cublasDiagType_t diag,
```

int n, int k, const cuDoubleComplex *A, int lda,
cuDoubleComplex *x, int incx)

This function performs the triangular banded matrix-vector multiplication

$$\mathbf{x} = \operatorname{op}(A)\mathbf{x}$$

where A is a triangular banded matrix, and \mathbf{x} is a vector. Also, for matrix A

$$\mathrm{op}(A) = \begin{cases} A & \text{if trans} == \texttt{CUBLAS_OP_N} \\ A^T & \text{if trans} == \texttt{CUBLAS_OP_T} \\ A^H & \text{if trans} == \texttt{CUBLAS_OP_C} \end{cases}$$

If uplo == CUBLAS_FILL_MODE_LOWER then the triangular banded matrix A is stored column by column, with the main diagonal of the matrix stored in row 1, the first subdiagonal in row 2 (starting at first position), the second subdiagonal in row 3 (starting at first position), etc. So that in general, the element A(i,j) is stored in the memory location A(1+i-j,j) for $j=1,\ldots,n$ and $i\in[j,\min(m,j+k)]$. Also, the elements in the array A that do not conceptually correspond to the elements in the banded matrix (the bottom right $k \times k$ triangle) are not referenced.

If uplo == CUBLAS_FILL_MODE_UPPER then the triangular banded matrix A is stored column by column, with the main diagonal of the matrix stored in row k+1, the first superdiagonal in row k (starting at second position), the second superdiagonal in row k-1 (starting at third position), etc. So that in general, the element A(i,j) is stored in the memory location A(1+k+i-j,j) for $j=1,\ldots,n$ and $i\in[\max(1,j-k),j]$. Also, the elements in the array A that do not conceptually correspond to the elements in the banded matrix (the top left $k \times k$ triangle) are not referenced.

Param.	Memory	In/out	Meaning
handle		input	handle to the CUBLAS library context.
uplo		input	indicates if matrix A lower or upper part
			is stored, the other part is not referen-
			ced and is inferred from the stored elements.
trans		input	operation op(A) that is non- or (conj.) transpose.
diag		input	indicates if the elements on the main diagonal of
			matrix A are unity and should not be accessed.
n			number of rows and columns of matrix A.
k		input	number of sub- and super-diagonals of matrix A.
A	device	input	$\langle \text{type} \rangle$ array of dimension $\mathtt{lda} \times \mathtt{n}$,
			with $1da \ge k+1$.
lda		input	leading dimension of two-dimensional array used
		_	to store matrix A.
X	device	in/out	<type> vector with n elements.</type>
incx		input	stride between consecutive elements of x.

Error Values	Meaning
CUBLAS_STATUS_SUCCESS	the operation completed successfully
CUBLAS_STATUS_NOT_INITIALIZED	the library was not initialized
CUBLAS_STATUS_INVALID_VALUE	the parameters n,k<0 or incx=0
CUBLAS_STATUS_ARCH_MISMATCH	the device does not support double-precision
CUBLAS_STATUS_ALLOC_FAILED	the allocation of internal scratch memory failed
CUBLAS_STATUS_EXECUTION_FAILED	the function failed to launch on the GPU

For references please refer to: stbmv, dtbmv, ctbmv, ztbmv

6.12 cublas<t>tbsv()

```
cublasStatus_t cublasStbsv(cublasHandle_t handle, cublasFillMode_t uplo,
                           cublasOperation_t trans, cublasDiagType_t diag,
                           int n, int k, const float
                                                                *A, int lda,
                           float
                                           *x, int incx)
cublasStatus_t cublasDtbsv(cublasHandle_t handle, cublasFillMode_t uplo,
                           cublasOperation_t trans, cublasDiagType_t diag,
                           int n, int k, const double
                                                               *A, int lda,
                           double
                                           *x, int incx)
cublasStatus_t cublasCtbsv(cublasHandle_t handle, cublasFillMode_t uplo,
                           cublasOperation_t trans, cublasDiagType_t diag,
                           int n, int k, const cuComplex
                                                               *A, int lda,
                           cuComplex
                                           *x, int incx)
cublasStatus_t cublasZtbsv(cublasHandle_t handle, cublasFillMode_t uplo,
                           cublasOperation_t trans, cublasDiagType_t diag,
                           int n, int k, const cuDoubleComplex *A, int lda,
                           cuDoubleComplex *x, int incx)
```

This function solves the triangular banded linear system with a single right-hand-side

$$op(A)\mathbf{x} = \mathbf{b}$$

where A is a triangular banded matrix, and \mathbf{x} and \mathbf{b} are vectors. Also, for matrix A

$$\mathrm{op}(A) = \begin{cases} A & \text{if trans == CUBLAS_OP_N} \\ A^T & \text{if trans == CUBLAS_OP_T} \\ A^H & \text{if trans == CUBLAS_OP_C} \end{cases}$$

The solution \mathbf{x} overwrites the right-hand-sides \mathbf{b} on exit.

No test for singularity or near-singularity is included in this function.

If uplo == CUBLAS_FILL_MODE_LOWER then the triangular banded matrix A is stored column by column, with the main diagonal of the matrix stored in row 1, the first subdiagonal in row 2 (starting at first position), the second subdiagonal in row 3 (starting at first position), etc. So that in general, the element A(i,j) is stored in the memory location A(1+i-j,j) for $j=1,\ldots,n$ and $i\in[j,\min(m,j+k)]$. Also, the elements in the array A that do not conceptually correspond to the elements in the banded matrix (the bottom right $k \times k$ triangle) are not referenced.

If uplo == CUBLAS_FILL_MODE_UPPER then the triangular banded matrix A is stored column by column, with the main diagonal of the matrix stored in row k+1, the first superdiagonal in row k (starting at second position), the second superdiagonal in row k-1 (starting at third position), etc. So that in general, the element A(i,j) is stored in the memory location A(1+k+i-j,j) for $j=1,\ldots,n$ and $i\in[\max(1,j-k),j]$. Also, the elements in the array A that do not conceptually correspond to the elements in the banded matrix (the top left $k \times k$ triangle) are not referenced.

Param.	Memory	In/out	Meaning
handle		input	handle to the CUBLAS library context.
uplo		input	indicates if matrix A lower or upper part
			is stored, the other part is not referen-
			ced and is inferred from the stored elements.
trans		input	operation op(A) that is non- or (conj.) transpose.
diag		input	indicates if the elements on the main diagonal of
			matrix A are unity and should not be accessed.
n			number of rows and columns of matrix A.
k		input	number of sub- and super-diagonals of matrix A.
A	device	input	$\langle \text{type} \rangle$ array of dimension $\texttt{lda} \times \texttt{n}$,
			with $1da \ge k+1$.
lda			leading dimension of two-dimensional array used
			to store matrix A.
X	device	in/out	<type> vector with n elements.</type>
incx		input	stride between consecutive elements of x.

The possible error values returned by this function and their meanings are listed below.

Error Values	Meaning
CUBLAS_STATUS_SUCCESS	the operation completed successfully
CUBLAS_STATUS_NOT_INITIALIZED	the library was not initialized
CUBLAS_STATUS_INVALID_VALUE	the parameters n<0 or incx=0
CUBLAS_STATUS_ARCH_MISMATCH	the device does not support double-precision
CUBLAS_STATUS_EXECUTION_FAILED	the function failed to launch on the GPU

For references please refer to: stbsv, dtbsv, ctbsv, ztbsv

6.13 cublas<t>tpmv()

cublasStatus_t cublasStpmv(cublasHandle_t handle, cublasFillMode_t uplo, cublasOperation_t trans, cublasDiagType_t diag, int n, const float *AP, float *x, int incx) cublasStatus_t cublasDtpmv(cublasHandle_t handle, cublasFillMode_t uplo, cublasOperation_t trans, cublasDiagType_t diag, int n, const double *x, int incx) double cublasStatus_t cublasCtpmv(cublasHandle_t handle, cublasFillMode_t uplo, cublasOperation_t trans, cublasDiagType_t diag, int n, const cuComplex *AP, cuComplex *x, int incx) cublasStatus_t cublasZtpmv(cublasHandle_t handle, cublasFillMode_t uplo, cublasOperation_t trans, cublasDiagType_t diag, int n, const cuDoubleComplex *AP, cuDoubleComplex *x, int incx)

This function performs the triangular packed matrix-vector multiplication

$$\mathbf{x} = \operatorname{op}(A)\mathbf{x}$$

where A is a triangular matrix stored in packed format, and ${\bf x}$ is a vector. Also, for matrix A

$$\mathrm{op}(A) = \begin{cases} A & \text{if trans} == \texttt{CUBLAS_OP_N} \\ A^T & \text{if trans} == \texttt{CUBLAS_OP_T} \\ A^H & \text{if trans} == \texttt{CUBLAS_OP_C} \end{cases}$$

If uplo == CUBLAS_FILL_MODE_LOWER then the elements in the lower triangular part of the triangular matrix A are packed together column by column without gaps, so that the element A(i,j) is stored in the memory location AP[i+((2*n-j+1)*j)/2] for $j=1,\ldots,n$ and $i\geq j$. Consequently, the packed format requires only $\frac{n(n+1)}{2}$ elements for storage.

If uplo == CUBLAS_FILL_MODE_UPPER then the elements in the upper triangular part of the triangular matrix A are packed together column by column without gaps, so that the element A(i,j) is stored in the memory location AP[i+(j*(j+1))/2] for $j=1,\ldots,n$ and $i \leq j$. Consequently, the packed format requires only $\frac{n(n+1)}{2}$ elements for storage.

Param.	Memory	In/out	Meaning
handle		input	handle to the CUBLAS library context.
uplo		input	indicates if matrix A lower or upper part
			is stored, the other part is not referen-
			ced and is inferred from the stored elements.
trans		input	operation op(A) that is non- or (conj.) transpose.
diag		input	indicates if the elements on the main diagonal of
			matrix A are unity and should not be accessed.
n		input	number of rows and columns of matrix A.
AP	device	input	$\langle \text{type} \rangle$ array with A stored in packed format.
X	device	in/out	<type> vector with n elements.</type>
incx		input	stride between consecutive elements of x.

Meaning
the operation completed successfully
the library was not initialized
the parameters n<0 or incx=0
the device does not support double-precision
the allocation of internal scratch memory failed
the function failed to launch on the GPU

For references please refer to: stpmv, dtpmv, ctpmv, ztpmv

6.14 cublas<t>tpsv()

```
cublasStatus_t cublasStpsv(cublasHandle_t handle, cublasFillMode_t uplo,
                           cublasOperation_t trans, cublasDiagType_t diag,
                           int n, const float
                                                         *AP,
                           float
                                           *x, int incx)
cublasStatus_t cublasDtpsv(cublasHandle_t handle, cublasFillMode_t uplo,
                           cublasOperation_t trans, cublasDiagType_t diag,
                           int n, const double
                                                         *AP,
                           double
                                           *x, int incx)
cublasStatus_t cublasCtpsv(cublasHandle_t handle, cublasFillMode_t uplo,
                           cublasOperation_t trans, cublasDiagType_t diag,
                           int n, const cuComplex
                                                         *AP,
                           cuComplex
                                           *x, int incx)
cublasStatus_t cublasZtpsv(cublasHandle_t handle, cublasFillMode_t uplo,
                           cublasOperation_t trans, cublasDiagType_t diag,
                           int n, const cuDoubleComplex *AP,
                           cuDoubleComplex *x, int incx)
```

This function solves the packed triangular linear system with a single right-hand-side

$$op(A)\mathbf{x} = \mathbf{b}$$

where A is a triangular matrix stored in packed format, and ${\bf x}$ and ${\bf b}$ are vectors. Also, for matrix A

$$\mathrm{op}(A) = \begin{cases} A & \text{if trans} == \texttt{CUBLAS_OP_N} \\ A^T & \text{if trans} == \texttt{CUBLAS_OP_T} \\ A^H & \text{if trans} == \texttt{CUBLAS_OP_C} \end{cases}$$

The solution \mathbf{x} overwrites the right-hand-sides \mathbf{b} on exit

No test for singularity or near-singularity is included in this function.

If uplo == CUBLAS_FILL_MODE_LOWER then the elements in the lower triangular part of the triangular matrix A are packed together column by column without gaps, so that the element A(i,j) is stored in the memory location AP[i+((2*n-j+1)*j)/2] for $j=1,\ldots,n$ and $i \geq j$. Consequently, the packed format requires only $\frac{n(n+1)}{2}$ elements for storage.

If uplo == CUBLAS_FILL_MODE_UPPER then the elements in the upper triangular part of the triangular matrix A are packed together column by column without gaps, so that the element A(i,j) is stored in the memory location AP[i+(j*(j+1))/2] for $j=1,\ldots,n$ and $i \leq j$. Consequently, the packed format requires only $\frac{n(n+1)}{2}$ elements for storage.

Param.	Memory	In/out	Meaning
handle		input	handle to the CUBLAS library context.
uplo		input	indicates if matrix A lower or upper part
			is stored, the other part is not referen-
			ced and is inferred from the stored elements.
trans		input	operation op(A) that is non- or (conj.) transpose.
diag		input	indicates if the elements on the main diagonal of
		input	matrix A are unity and should not be accessed.
n		input	number of rows and columns of matrix A.
AP	device	input	$\langle \text{type} \rangle$ array with A stored in packed format.
X	device	in/out	<type> vector with n elements.</type>
incx		input	stride between consecutive elements of x.

The possible error values returned by this function and their meanings are listed below.

Error Values	Meaning
CUBLAS_STATUS_SUCCESS	the operation completed successfully
CUBLAS_STATUS_NOT_INITIALIZED	the library was not initialized
CUBLAS_STATUS_INVALID_VALUE	the parameters n<0 or incx=0
CUBLAS_STATUS_ARCH_MISMATCH	the device does not support double-precision
CUBLAS_STATUS_EXECUTION_FAILED	the function failed to launch on the GPU

For references please refer to: stpsv, dtpsv, ctpsv, ztpsv

6.15 cublas<t>trmv()

cublasStatus_t cublasCtrmv(cublasHandle_t handle, cublasFillMode_t uplo, cublasOperation_t trans, cublasDiagType_t diag, int n, const cuComplex *A, int lda, cuComplex *x, int incx)

This function performs the triangular matrix-vector multiplication

$$\mathbf{x} = \operatorname{op}(A)\mathbf{x}$$

where A is a triangular matrix stored in lower or upper mode with or without the main diagonal, and \mathbf{x} is a vector. Also, for matrix A

$$\mathrm{op}(A) = egin{cases} A & ext{if trans} == \mathtt{CUBLAS_OP_N} \ A^T & ext{if trans} == \mathtt{CUBLAS_OP_T} \ A^H & ext{if trans} == \mathtt{CUBLAS_OP_C} \end{cases}$$

Param.	Memory	In/out	Meaning
handle		input	handle to the CUBLAS library context.
uplo		input	indicates if matrix A lower or upper part
			is stored, the other part is not referen-
			ced and is inferred from the stored elements.
trans		input	operation op(A) that is non- or (conj.) transpose.
diag		input	indicates if the elements on the main diagonal of
			matrix A are unity and should not be accessed.
n		input	number of rows and columns of matrix A.
A	device	input	$\langle \text{type} \rangle$ array of dimensions $\mathtt{lda} \times \mathtt{n}$,
			with $lda \ge max(1,n)$.
lda		input	leading dimension of two-dimensional array used
			to store matrix A.
X	device	in/out	<type> vector with n elements.</type>
incx		input	stride between consecutive elements of x.

Error Values	Meaning
CUBLAS_STATUS_SUCCESS	the operation completed successfully
CUBLAS_STATUS_NOT_INITIALIZED	the library was not initialized
CUBLAS_STATUS_INVALID_VALUE	the parameters n<0 or incx=0
CUBLAS_STATUS_ARCH_MISMATCH	the device does not support double-precision
CUBLAS_STATUS_ALLOC_FAILED	the allocation of internal scratch memory failed
CUBLAS_STATUS_EXECUTION_FAILED	the function failed to launch on the GPU

For references please refer to: strmy, dtrmy, ctrmy, ztrmy

6.16 cublas<t>trsv()

```
cublasStatus_t cublasStrsv(cublasHandle_t handle, cublasFillMode_t uplo,
                           cublasOperation_t trans, cublasDiagType_t diag,
                           int n, const float
                                                         *A, int lda,
                           float
                                           *x, int incx)
cublasStatus_t cublasDtrsv(cublasHandle_t handle, cublasFillMode_t uplo,
                           cublasOperation_t trans, cublasDiagType_t diag,
                           int n, const double
                                                         *A, int lda,
                           double
                                           *x, int incx)
cublasStatus_t cublasCtrsv(cublasHandle_t handle, cublasFillMode_t uplo,
                           cublasOperation_t trans, cublasDiagType_t diag,
                           int n, const cuComplex
                                                         *A, int lda,
                           cuComplex
                                           *x, int incx)
cublasStatus_t cublasZtrsv(cublasHandle_t handle, cublasFillMode_t uplo,
                           cublasOperation_t trans, cublasDiagType_t diag,
                           int n, const cuDoubleComplex *A, int lda,
                           cuDoubleComplex *x, int incx)
```

This function solves the triangular linear system with a single right-hand-side

$$op(A)\mathbf{x} = \mathbf{b}$$

where A is a triangular matrix stored in lower or upper mode with or without the main diagonal, and \mathbf{x} and \mathbf{b} are vectors. Also, for matrix A

$$\mathrm{op}(A) = \begin{cases} A & \text{if trans} == \texttt{CUBLAS_OP_N} \\ A^T & \text{if trans} == \texttt{CUBLAS_OP_T} \\ A^H & \text{if trans} == \texttt{CUBLAS_OP_C} \end{cases}$$

The solution \mathbf{x} overwrites the right-hand-sides \mathbf{b} on exit.

Param.	Memory	In/out	Meaning
handle		input	handle to the CUBLAS library context.
uplo		input	indicates if matrix A lower or upper part
			is stored, the other part is not referen-
			ced and is inferred from the stored elements.
trans		input	operation op(A) that is non- or (conj.) transpose.
diag		input	indicates if the elements on the main diagonal of
			matrix A are unity and should not be accessed.
n		input	number of rows and columns of matrix A.
A	device	input	$\langle \text{type} \rangle$ array of dimension $\texttt{lda} \times \texttt{n}$,
			with $lda \ge max(1,n)$.
lda		input	leading dimension of two-dimensional array used
			to store matrix A.
X	device	in/out	<type> vector with n elements.</type>
incx		input	stride between consecutive elements of x.

No test for singularity or near-singularity is included in this function.

The possible error values returned by this function and their meanings are listed below.

Error Values	Meaning
CUBLAS_STATUS_SUCCESS	the operation completed successfully
CUBLAS_STATUS_NOT_INITIALIZED	the library was not initialized
CUBLAS_STATUS_INVALID_VALUE	the parameters n<0 or incx=0
CUBLAS_STATUS_ARCH_MISMATCH	the device does not support double-precision
CUBLAS_STATUS_EXECUTION_FAILED	the function failed to launch on the GPU

For references please refer to:

strsv, dtrsv, ctrsv, ztrsv

6.17 cublas<t>hemv()

```
cublasStatus_t cublasChemv(cublasHandle_t handle, cublasFillMode_t uplo,
                           int n, const cuComplex
                           const cuComplex
                                                 *A, int lda,
                           const cuComplex
                                                 *x, int incx,
                           const cuComplex
                                                 *beta,
                           cuComplex
                                           *y, int incy)
cublasStatus_t cublasZhemv(cublasHandle_t handle, cublasFillMode_t uplo,
                           int n, const cuDoubleComplex *alpha,
                           const cuDoubleComplex *A, int lda,
                           const cuDoubleComplex *x, int incx,
                           const cuDoubleComplex *beta,
                           cuDoubleComplex *y, int incy)
```

This function performs the Hermitian matrix-vector multiplication

$$\mathbf{y} = \alpha A \mathbf{x} + \beta \mathbf{y}$$

where A is a $n \times n$ Hermitian matrix stored in lower or upper mode, **x** and **y** are vectors, and α and β are scalars.

Param.	Memory	In/out	Meaning
handle		input	handle to the CUBLAS library context.
uplo		input	indicates if matrix A lower or upper part
			is stored, the other Hermitian part is not referen-
			ced and is inferred from the stored elements.
n		input	number of rows and columns of matrix A.
alpha	host or device	input	<type> scalar used for multiplication.</type>
A	device	input	$\langle \text{type} \rangle$ array of dimension $\mathtt{lda} \times \mathtt{n}$, with
			$lda \ge max(1,n)$ The imaginary parts of the
			diagonal elements are assumed to be zero.
lda		input	leading dimension of two-dimensional array used
			to store matrix A.
X	device	input	<type> vector with n elements.</type>
incx		input	stride between consecutive elements of x.
beta	host or device	input	<pre><type> scalar used for multiplication, if beta==0</type></pre>
			then y does not have to be a valid input.
У	device	in/out	<type> vector with n elements.</type>
incy		input	stride between consecutive elements of y.

The possible error values returned by this function and their meanings are listed below.

Error Values	Meaning
CUBLAS_STATUS_SUCCESS	the operation completed successfully
CUBLAS_STATUS_NOT_INITIALIZED	the library was not initialized
CUBLAS_STATUS_INVALID_VALUE	the parameters n<0 or incx,incy=0
CUBLAS_STATUS_ARCH_MISMATCH	the device does not support double-precision
CUBLAS_STATUS_EXECUTION_FAILED	the function failed to launch on the GPU

For references please refer to: chemy, zhemy

6.18 cublas<t>hbmv()

This function performs the Hermitian banded matrix-vector multiplication

$$\mathbf{y} = \alpha A \mathbf{x} + \beta \mathbf{y}$$

where A is a $n \times n$ Hermitian banded matrix with k subdiagonals and superdiagonals, **x** and **y** are vectors, and α and β are scalars.

If uplo == CUBLAS_FILL_MODE_LOWER then the Hermitian banded matrix A is stored column by column, with the main diagonal of the matrix stored in row 1, the first subdiagonal in row 2 (starting at first position), the second subdiagonal in row 3 (starting at first position), etc. So that in general, the element A(i,j) is stored in the memory location A(1+i-j,j) for $j=1,\ldots,n$ and $i\in[j,\min(m,j+k)]$. Also, the elements in the array A that do not conceptually correspond to the elements in the banded matrix (the bottom right $k \times k$ triangle) are not referenced.

If uplo == CUBLAS_FILL_MODE_UPPER then the Hermitian banded matrix A is stored column by column, with the main diagonal of the matrix stored in row k+1, the first superdiagonal in row k (starting at second position), the second superdiagonal in row k-1 (starting at third position), etc. So that in general, the element A(i,j) is stored in the memory location A(1+k+i-j,j) for $j=1,\ldots,n$ and $i\in[\max(1,j-k),j]$. Also, the elements in the array A that do not conceptually correspond to the elements in the banded matrix (the top left $k \times k$ triangle) are not referenced.

Param.	Memory	In/out	Meaning
handle		input	handle to the CUBLAS library context.
uplo		input	indicates if matrix A lower or upper part
			is stored, the other Hermitian part is not referen-
			ced and is inferred from the stored elements.
n		input	number of rows and columns of matrix A.
k		input	number of sub- and super-diagonals of matrix A.
alpha	host or device	input	<type> scalar used for multiplication.</type>
A	device	input	$\langle \text{type} \rangle$ array of dimensions $\mathtt{lda} \times \mathtt{n}$, with
			$lda \ge k+1$. The imaginary parts of the
			diagonal elements are assumed to be zero.
lda		input	leading dimension of two-dimensional array used
			to store matrix A.
X	device	input	<type> vector with n elements.</type>
incx		input	stride between consecutive elements of x.
beta	host or device	input	<pre><type> scalar used for multiplication, if beta==0</type></pre>
			then y does not have to be a valid input.
У	device	in/out	<type> vector with n elements.</type>
incy		input	stride between consecutive elements of y.

Error Values	Meaning
CUBLAS_STATUS_SUCCESS	the operation completed successfully
CUBLAS_STATUS_NOT_INITIALIZED	the library was not initialized
CUBLAS_STATUS_INVALID_VALUE	the parameters n,k<0 or incx,incy=0
CUBLAS_STATUS_ARCH_MISMATCH	the device does not support double-precision
CUBLAS_STATUS_EXECUTION_FAILED	the function failed to launch on the GPU

For references please refer to: chbmv, zhbmv

6.19 cublas<t>hpmv()

const cuDoubleComplex *beta, cuDoubleComplex *y, int incy)

This function performs the Hermitian packed matrix-vector multiplication

$$\mathbf{y} = \alpha A \mathbf{x} + \beta \mathbf{y}$$

where A is a $n \times n$ Hermitian matrix stored in packed format, **x** and **y** are vectors, and α and β are scalars.

If uplo == CUBLAS_FILL_MODE_LOWER then the elements in the lower triangular part of the Hermitian matrix A are packed together column by column without gaps, so that the element A(i,j) is stored in the memory location AP[i+((2*n-j+1)*j)/2] for $j=1,\ldots,n$ and $i\geq j$. Consequently, the packed format requires only $\frac{n(n+1)}{2}$ elements for storage.

If uplo == CUBLAS_FILL_MODE_UPPER then the elements in the upper triangular part of the Hermitian matrix A are packed together column by column without gaps, so that the element A(i,j) is stored in the memory location AP[i+(j*(j+1))/2] for $j=1,\ldots,n$ and $i \leq j$. Consequently, the packed format requires only $\frac{n(n+1)}{2}$ elements for storage.

Param.	Memory	In/out	Meaning
handle		input	handle to the CUBLAS library context.
uplo		input	indicates if matrix A lower or upper part
			is stored, the other Hermitian part is not referen-
			ced and is inferred from the stored elements.
n		input	number of rows and columns of matrix A .
k		input	number of sub- and super-diagonals of matrix A .
alpha	host or device	input	<type> scalar used for multiplication.</type>
AP	device	input	$\langle \text{type} \rangle$ array with A stored in packed format
			The imaginary parts of the diagonal elements
			are assumed to be zero.
X	device	input	<type> vector with n elements.</type>
incx		input	stride between consecutive elements of x.
beta	host or device	input	<type> scalar used for multiplication, if beta==0</type>
			then y does not have to be a valid input.
У	device	in/out	<type> vector with n elements.</type>
incy		input	stride between consecutive elements of y.

The possible error values returned by this function and their meanings are listed below.

Error Values	Meaning
CUBLAS_STATUS_SUCCESS	the operation completed successfully
CUBLAS_STATUS_NOT_INITIALIZED	the library was not initialized
CUBLAS_STATUS_INVALID_VALUE	the parameters n<0 or incx,incy=0
CUBLAS_STATUS_ARCH_MISMATCH	the device does not support double-precision
CUBLAS_STATUS_EXECUTION_FAILED	the function failed to launch on the GPU

For references please refer to:

chpmv, zhpmv

6.20 cublas<t>her()

This function performs the Hermitian rank-1 update

$$A = \alpha \mathbf{x} \mathbf{x}^H + A$$

where A is a $n \times n$ Hermitian matrix stored in column-major format, **x** is a vector, and α is a scalar.

Param.	Memory	In/out	Meaning
handle		input	handle to the CUBLAS library context.
uplo		input	indicates if matrix A lower or upper part
			is stored, the other Hermitian part is not referen-
			ced and is inferred from the stored elements.
n		input	number of rows and columns of matrix A.
alpha	host or device	input	<type> scalar used for multiplication.</type>
X	device	input	<type> vector with n elements.</type>
incx		input	stride between consecutive elements of x.
A	device	in/out	$\langle \text{type} \rangle$ array of dimensions $\mathtt{lda} \times \mathtt{n}$, with
			$1da \ge max(1,n)$. The imaginary parts of the
			diagonal elements are assumed and set to zero.
lda		input	leading dimension of two-dimensional array used
			to store matrix A.

The possible error values returned by this function and their meanings are listed below.

Error Values	Meaning
CUBLAS_STATUS_SUCCESS	the operation completed successfully
CUBLAS_STATUS_NOT_INITIALIZED	the library was not initialized
CUBLAS_STATUS_INVALID_VALUE	the parameters n<0 or incx=0
CUBLAS_STATUS_ARCH_MISMATCH	the device does not support double-precision
CUBLAS_STATUS_EXECUTION_FAILED	the function failed to launch on the GPU

For references please refer to: cher, zher

6.21 cublas<t>her2()

This function performs the Hermitian rank-2 update

$$A = \alpha \mathbf{x} \mathbf{y}^H + \bar{\alpha} \mathbf{y} \mathbf{x}^H + A$$

where A is a $n \times n$ Hermitian matrix stored in column-major format, **x** and **y** are vectors, and α is a scalar.

Param.	Memory	In/out	Meaning
handle		input	handle to the CUBLAS library context.
uplo		input	indicates if matrix A lower or upper part
			is stored, the other Hermitian part is not referen-
			ced and is inferred from the stored elements.
n		input	number of rows and columns of matrix A.
alpha	host or device	input	<type> scalar used for multiplication.</type>
X	device	input	<type> vector with n elements.</type>
incx		input	stride between consecutive elements of x.
У	device	input	<type> vector with n elements.</type>
incy		input	stride between consecutive elements of y.
A	device	in/out	$\langle \text{type} \rangle$ array of dimension $\mathtt{lda} \times \mathtt{n}$ with
			$lda \ge max(1,n)$. The imaginary parts of the
			diagonal elements are assumed and set to zero.
lda		input	leading dimension of two-dimensional array used
			to store matrix A.

The possible error values returned by this function and their meanings are listed below.

Error Values	Meaning
CUBLAS_STATUS_SUCCESS	the operation completed successfully
CUBLAS_STATUS_NOT_INITIALIZED	the library was not initialized
CUBLAS_STATUS_INVALID_VALUE	the parameters n<0 or incx,incy=0
CUBLAS_STATUS_ARCH_MISMATCH	the device does not support double-precision
CUBLAS_STATUS_EXECUTION_FAILED	the function failed to launch on the GPU

For references please refer to:

cher2, zher2

6.22 cublas<t>hpr()

This function performs the packed Hermitian rank-1 update

$$A = \alpha \mathbf{x} \mathbf{x}^H + A$$

where A is a $n \times n$ Hermitian matrix stored in packed format, \mathbf{x} is a vector, and α is a scalar.

If uplo == CUBLAS_FILL_MODE_LOWER then the elements in the lower triangular part of the Hermitian matrix A are packed together column by column without gaps, so that the element A(i,j) is stored in the memory location AP[i+((2*n-j+1)*j)/2] for $j=1,\ldots,n$ and $i\geq j$. Consequently, the packed format requires only $\frac{n(n+1)}{2}$ elements for storage.

If uplo == CUBLAS_FILL_MODE_UPPER then the elements in the upper triangular part of the Hermitian matrix A are packed together column by column without gaps, so that the element A(i,j) is stored in the memory location AP[i+(j*(j+1))/2] for $j=1,\ldots,n$ and $i \leq j$. Consequently, the packed format requires only $\frac{n(n+1)}{2}$ elements for storage.

Param.	Memory	In/out	Meaning
handle		input	handle to the CUBLAS library context.
uplo		input	indicates if matrix A lower or upper part
			is stored, the other Hermitian part is not referen-
			ced and is inferred from the stored elements.
\mathbf{n}		input	number of rows and columns of matrix A .
alpha	host or device	input	<type> scalar used for multiplication.</type>
X	device	input	<type> vector with n elements.</type>
incx		input	stride between consecutive elements of x.
AP	device	in/out	$\langle \text{type} \rangle$ array with A stored in packed format
			The imaginary parts of the diagonal elements
			are assumed and set to zero.

The possible error values returned by this function and their meanings are listed below.

Error Values	Meaning
CUBLAS_STATUS_SUCCESS	the operation completed successfully
CUBLAS_STATUS_NOT_INITIALIZED	the library was not initialized
CUBLAS_STATUS_INVALID_VALUE	the parameters n<0 or incx=0
CUBLAS_STATUS_ARCH_MISMATCH	the device does not support double-precision
CUBLAS_STATUS_EXECUTION_FAILED	the function failed to launch on the GPU

For references please refer to: chpr, zhpr

6.23 cublas<t>hpr2()

This function performs the packed Hermitian rank-2 update

$$A = \alpha \mathbf{x} \mathbf{y}^H + \bar{\alpha} \mathbf{y} \mathbf{x}^H + A$$

where A is a $n \times n$ Hermitian matrix stored in packed format, **x** and **y** are vectors, and α is a scalar.

If uplo == CUBLAS_FILL_MODE_LOWER then the elements in the lower triangular part of the Hermitian matrix A are packed together column by column without gaps, so that the element A(i,j) is stored in the memory location AP[i+((2*n-j+1)*j)/2] for $j=1,\ldots,n$ and $i\geq j$. Consequently, the packed format requires only $\frac{n(n+1)}{2}$ elements for storage.

If uplo == CUBLAS_FILL_MODE_UPPER then the elements in the upper triangular part of the Hermitian matrix A are packed together column by column without gaps, so that the element A(i,j) is stored in the memory location AP[i+(j*(j+1))/2] for $j=1,\ldots,n$ and $i \leq j$. Consequently, the packed format requires only $\frac{n(n+1)}{2}$ elements for storage.

Param.	Memory	In/out	Meaning
handle		input	handle to the CUBLAS library context.
uplo		input	indicates if matrix A lower or upper part
			is stored, the other Hermitian part is not referen-
			ced and is inferred from the stored elements.
n		input	number of rows and columns of matrix A .
alpha	host or device	input	<type> scalar used for multiplication.</type>
X	device	input	<type> vector with n elements.</type>
incx		input	stride between consecutive elements of x.
У	device	input	<type> vector with n elements.</type>
incy		input	stride between consecutive elements of y.
AP	device	in/out	$\langle \text{type} \rangle$ array with A stored in packed format
			The imaginary parts of the diagonal elements
			are assumed and set to zero.

Error Values	Meaning
CUBLAS_STATUS_SUCCESS	the operation completed successfully
CUBLAS_STATUS_NOT_INITIALIZED	the library was not initialized
CUBLAS_STATUS_INVALID_VALUE	the parameters n<0 or incx,incy=0
CUBLAS_STATUS_ARCH_MISMATCH	the device does not support double-precision
CUBLAS_STATUS_EXECUTION_FAILED	the function failed to launch on the GPU

For references please refer to: chpr2, zhpr2

Chapter 7 CUBLAS Level-3 Function Reference

In this chapter we describe the Level-3 Basic Linear Algebra Subprograms (BLAS3) functions that perform matrix-matrix operations.

7.1 cublas<t>gemm()

```
cublasStatus_t cublasSgemm(cublasHandle_t handle,
                           cublasOperation_t transa, cublasOperation_t transb,
                           int m, int n, int k,
                           const float
                                                  *alpha,
                           const float
                                                  *A, int lda,
                           const float
                                                  *B, int ldb,
                           const float
                                                  *beta,
                           float
                                            *C, int ldc)
cublasStatus_t cublasDgemm(cublasHandle_t handle,
                           cublasOperation_t transa, cublasOperation_t transb,
                           int m, int n, int k,
                           const double
                                                  *alpha,
                           const double
                                                  *A, int lda,
                           const double
                                                  *B, int ldb,
                           const double
                                                  *beta,
                           double
                                            *C, int ldc)
cublasStatus_t cublasCgemm(cublasHandle_t handle,
                           cublasOperation_t transa, cublasOperation_t transb,
                           int m, int n, int k,
                           const cuComplex
                                                  *alpha,
                           const cuComplex
                                                  *A, int lda,
                           const cuComplex
                                                  *B, int ldb,
                           const cuComplex
                                                  *beta,
                           cuComplex
                                            *C, int ldc)
cublasStatus_t cublasZgemm(cublasHandle_t handle,
                           cublasOperation_t transa, cublasOperation_t transb,
```

```
int m, int n, int k,
const cuDoubleComplex *alpha,
const cuDoubleComplex *A, int lda,
const cuDoubleComplex *B, int ldb,
const cuDoubleComplex *beta,
cuDoubleComplex *C, int ldc)
```

This function performs the matrix-matrix multiplication

$$C = \alpha \operatorname{op}(A)\operatorname{op}(B) + \beta C$$

where α and β are scalars, and A, B and C are matrices stored in column-major format with dimensions op(A) $m \times k$, op(B) $k \times n$ and C $m \times n$, respectively. Also, for matrix A

$$\mathrm{op}(A) = \begin{cases} A & \text{if transa == CUBLAS_OP_N} \\ A^T & \text{if transa == CUBLAS_OP_T} \\ A^H & \text{if transa == CUBLAS_OP_C} \end{cases}$$

and op(B) is defined similarly for matrix B.

Param.	Memory	In/out	Meaning
handle		input	handle to the CUBLAS library context.
transa		input	operation op(A) that is non- or (conj.) transpose.
transb		input	operation op(B) that is non- or (conj.) transpose.
\mathbf{m}		input	number of rows of matrix op(A) and C.
\mathbf{n}		input	number of columns of matrix op(B) and C.
k		input	number of columns of $op(A)$ and rows of $op(B)$.
alpha	host or device	input	<type> scalar used for multiplication.</type>
A	device	input	$\langle \text{type} \rangle$ array of dimensions $lda \times k$ with
			$lda \ge max(1,m)$ if transa == CUBLAS_OP_N
			and $\mathtt{lda} \times \mathtt{m}$ with $\mathtt{lda} \geq \max(1,\mathtt{k})$ otherwise.
lda		input	leading dimension of two-dimensional array used
			to store the matrix A .
В	device	input	$\langle \text{type} \rangle$ array of dimension $\mathtt{ldb} \times \mathtt{n}$ with
			$ldb \ge \max(1,k)$ if transa == CUBLAS_OP_N
			and $ldb \times k$ with $ldb \ge max(1,n)$ otherwise.
ldb		input	leading dimension of two-dimensional array used
			to store matrix B.
beta	host or device	input	<type> scalar used for multiplication.</type>
			If beta == 0, C does not have to be a valid input.
С	device	in/out	$<$ type $>$ array of dimensions $1dc \times n$
			with $1dc \ge max(1,m)$.
ldc		input	leading dimension of a two-dimensional array used
			to store the matrix C.

The possible error values returned by this function and their meanings are listed below.

Error Values	Meaning
CUBLAS_STATUS_SUCCESS	the operation completed successfully
CUBLAS_STATUS_NOT_INITIALIZED	the library was not initialized
CUBLAS_STATUS_INVALID_VALUE	the parameters m,n,k<0
CUBLAS_STATUS_ARCH_MISMATCH	the device does not support double-precision
CUBLAS_STATUS_EXECUTION_FAILED	the function failed to launch on the GPU

For references please refer to: sgemm, dgemm, cgemm, zgemm

7.2 cublas<t>gemmBatched()

```
cublasStatus_t cublasSgemmBatched(cublasHandle_t handle,
                           cublasOperation_t transa, cublasOperation_t transb,
                           int m, int n, int k,
                           const float
                                                 *alpha,
                           const float
                                                 *Aarray[], int lda,
                           const float
                                                 *Barray[], int ldb,
                           const float
                                                 *beta,
                                           *Carray[], int ldc, int batchCount)
                           float
cublasStatus_t cublasDgemmBatched(cublasHandle_t handle,
                           cublasOperation_t transa, cublasOperation_t transb,
                           int m, int n, int k,
                           const double
                                                 *alpha,
                           const double
                                                 *Aarray[], int lda,
                                                 *Barray[], int ldb,
                           const double
                           const double
                                                 *beta,
                                           *Carray[], int ldc, int batchCount)
                           double
cublasStatus_t cublasCgemmBatched(cublasHandle_t handle,
                           cublasOperation_t transa, cublasOperation_t transb,
                           int m, int n, int k,
                           const cuComplex
                                                 *alpha,
                                                 *Aarray[], int lda,
                           const cuComplex
                                                 *Barray[], int ldb,
                           const cuComplex
                           const cuComplex
                                                 *beta,
                           cuComplex
                                           *Carray[], int ldc, int batchCount)
cublasStatus_t cublasZgemmBatched(cublasHandle_t handle,
                           cublasOperation_t transa, cublasOperation_t transb,
                           int m, int n, int k,
                           const cuDoubleComplex *alpha,
                           const cuDoubleComplex *Aarray[], int lda,
                           const cuDoubleComplex *Barray[], int ldb,
```

const cuDoubleComplex *beta,
cuDoubleComplex *Carray[], int ldc, int batchCount)

This function performs the matrix-matrix multiplications of an array of matrices.

$$C[i] = \alpha \operatorname{op}(A[i])\operatorname{op}(B[i]) + \beta C[i], \text{ for } i \in [0, batchCount - 1]$$

where α and β are scalars, and A, B and C are arrays of pointers to matrices stored in column-major format with dimensions op(A[i]) $m \times k$, op(B[i]) $k \times n$ and C[i] $m \times n$, respectively. Also, for matrix A[i]

$$\mathrm{op}(A[i]) = \begin{cases} A[i] & \text{if transa} == \texttt{CUBLAS_OP_N} \\ A^T[i] & \text{if transa} == \texttt{CUBLAS_OP_T} \\ A^H[i] & \text{if transa} == \texttt{CUBLAS_OP_C} \end{cases}$$

and op(B[i]) is defined similarly for matrix B[i].

This function is intended to be used for matrices of small sizes where the launch overhead is a significant factor.

Param.	Memory	In/out	Meaning
handle		input	handle to the CUBLAS library context.
transa		input	operation op(A[i]) that is non- or (conj.) transpose.
transb		input	operation op(B[i]) that is non- or (conj.) transpose.
m		input	number of rows of matrix op(A[i]) and C[i].
n		input	number of columns of op(B[i]) and C[i].
k		input	number of columns of op(A[i]) and rows of op(B[i]).
alpha	host or device	input	<type> scalar used for multiplication.</type>
A	device	input	array of pointers to <type> array, with each array of</type>
			dim. $lda \times k$ with $lda \ge max(1,m)$ if transa==CUBLAS_OP_N
			and $lda \times m$ with $lda \ge max(1,k)$ otherwise.
lda		input	leading dimension of two-dimensional array used
			to store each matrix $A[i]$.
В	device	input	array of pointers to <type> array, with each array of</type>
			dim. $ldb \times n$ with $ldb \ge max(1,k)$ if transa==CUBLAS_OP_N
			and $ldb \times k$ with $ldb \ge max(1,n)$ otherwise.
ldb		input	leading dimension of two-dimensional array used
			to store each matrix B[i].
beta	host or device	input	<pre><type> scalar used for multiplication</type></pre>
			If beta == 0, C does not have to be a valid input.
С	device	in/out	array of pointers to <type> array</type>
			It has dimensions $1dc \times n$ with $1dc \ge max(1,m)$.
ldc		input	leading dimension of two-dimensional array used
			to store each matrix C[i].
batchCount		input	number of pointers contained in A, B and C.

The possible error values returned by this function and their meanings are listed below.

Error Values	Meaning
CUBLAS_STATUS_SUCCESS	the operation completed successfully
CUBLAS_STATUS_NOT_INITIALIZED	the library was not initialized
CUBLAS_STATUS_INVALID_VALUE	the parameters m,n,k, batchCount<0
CUBLAS_STATUS_ARCH_MISMATCH	the device does not support double-precision
CUBLAS_STATUS_EXECUTION_FAILED	the function failed to launch on the GPU

7.3 cublas<t>symm()

```
cublasStatus_t cublasSsymm(cublasHandle_t handle,
                           cublasSideMode_t side, cublasFillMode_t uplo,
                           int m, int n,
                           const float
                                                  *alpha,
                           const float
                                                 *A, int lda,
                           const float
                                                 *B, int ldb,
                           const float
                                                  *beta,
                                           *C, int ldc)
                           float
cublasStatus_t cublasDsymm(cublasHandle_t handle,
                           cublasSideMode_t side, cublasFillMode_t uplo,
                           int m, int n,
                           const double
                                                 *alpha,
                                                *A, int lda,
                           const double
                           const double
                                                 *B, int ldb,
                           const double
                                                 *beta,
                                           *C, int ldc)
                           double
cublasStatus_t cublasCsymm(cublasHandle_t handle,
                           cublasSideMode_t side, cublasFillMode_t uplo,
                           int m, int n,
                           const cuComplex
                                                 *alpha,
                           const cuComplex
                                                 *A, int lda,
                           const cuComplex
                                                 *B, int ldb,
                           const cuComplex
                                                 *beta,
                           cuComplex
                                           *C, int ldc)
cublasStatus_t cublasZsymm(cublasHandle_t handle,
                           cublasSideMode_t side, cublasFillMode_t uplo,
                           int m, int n,
                           const cuDoubleComplex *alpha,
                           const cuDoubleComplex *A, int lda,
                           const cuDoubleComplex *B, int ldb,
                           const cuDoubleComplex *beta,
                           cuDoubleComplex *C, int ldc)
```

This function performs the symmetric matrix-matrix multiplication

$$C = \begin{cases} \alpha AB + \beta C & \text{if side == CUBLAS_SIDE_LEFT} \\ \alpha BA + \beta C & \text{if side == CUBLAS_SIDE_RIGHT} \end{cases}$$

where A is a symmetric matrix stored in lower or upper mode, B and C are $m \times n$ matrices, and α and β are scalars.

Param.	Memory	In/out	Meaning
handle		input	handle to the CUBLAS library context.
side		input	indicates if matrix A is on the left or right of B.
uplo		input	indicates if matrix A lower or upper part is
			stored, the other symmetric part is not referen-
			ced and is inferred from the stored elements.
m		input	number of rows of matrix C and B, with
			matrix A sized accordingly.
n		input	number of columns of matrix C and B, with
			matrix A sized accordingly.
alpha	host or device	input	<type> scalar used for multiplication.</type>
A	device	input	$<$ type $>$ array of dimension lda \times m with
			$ exttt{lda} \geq \max(1, exttt{m}) ext{ if side} == exttt{CUBLAS_SIDE_LEFT}$
			and $1da \times n$ with $1da \ge max(1,n)$ otherwise.
lda			leading dimension of two-dimensional array used
			to store matrix A.
В	device		$<$ type $>$ array of dimension ldb \times n
			with $ldb \ge max(1,m)$.
ldb			leading dimension of two-dimensional array used
			to store matrix B.
beta	host or device	input	<pre><type> scalar used for multiplication, if beta==0</type></pre>
			then C does not have to be a valid input.
\mathbf{C}	device	in/out	$<$ type $>$ array of dimension $1dc \times n$
			with $1dc \ge \max(1,m)$.
ldc		input	leading dimension of two-dimensional array used
			to store matrix C.

The possible error values returned by this function and their meanings are listed below.

Error Values	Meaning
CUBLAS_STATUS_SUCCESS	the operation completed successfully
CUBLAS_STATUS_NOT_INITIALIZED	the library was not initialized
CUBLAS_STATUS_INVALID_VALUE	the parameters m,n<0
CUBLAS_STATUS_ARCH_MISMATCH	the device does not support double-precision
CUBLAS_STATUS_EXECUTION_FAILED	the function failed to launch on the GPU

For references please refer to: ssymm, dsymm, csymm, zsymm

7.4 cublas<t>syrk()

```
cublasStatus_t cublasSsyrk(cublasHandle_t handle,
                           cublasFillMode_t uplo, cublasOperation_t trans,
                           int n, int k,
                           const float
                                                 *alpha,
                           const float
                                                 *A, int lda,
                           const float
                                                 *beta.
                          float
                                         *C, int ldc)
cublasStatus_t cublasDsyrk(cublasHandle_t handle,
                           cublasFillMode_t uplo, cublasOperation_t trans,
                           int n, int k,
                           const double
                                                 *alpha,
                           const double
                                               *A, int lda,
                           const double
                                               *beta,
                          double
                                          *C, int ldc)
cublasStatus_t cublasCsyrk(cublasHandle_t handle,
                           cublasFillMode_t uplo, cublasOperation_t trans,
                           int n, int k,
                           const cuComplex
                                               *alpha,
                           const cuComplex
                                               *A, int lda,
                           const cuComplex
                                                 *beta,
                           cuComplex
                                          *C, int ldc)
cublasStatus_t cublasZsyrk(cublasHandle_t handle,
                          cublasFillMode_t uplo, cublasOperation_t trans,
                           int n, int k,
                           const cuDoubleComplex *alpha,
                           const cuDoubleComplex *A, int lda,
                           const cuDoubleComplex *beta,
                           cuDoubleComplex *C, int ldc)
```

This function performs the symmetric rank-k update

$$C = \alpha \operatorname{op}(A)\operatorname{op}(A)^T + \beta C$$

where α and β are scalars, C is a symmetric matrix stored in lower or upper mode, and A is a matrix with dimensions op(A) $n \times k$. Also, for matrix A

$$\mathrm{op}(A) = \begin{cases} A & \text{if trans == CUBLAS_OP_N} \\ A^T & \text{if trans == CUBLAS_OP_T} \end{cases}$$

Param.	Memory	In/out	Meaning
handle		input	handle to the CUBLAS library context.
uplo		input	indicates if matrix A lower or upper part is
			stored, the other symmetric part is not referen-
			ced and is inferred from the stored elements.
trans		input	operation op(A) that is non- or transpose.
n		input	number of rows of matrix op(A) and C.
k		input	number of columns of matrix op(A).
alpha	host or device	input	<type> scalar used for multiplication.</type>
A	device	input	$<$ type $>$ array of dimension lda \times k with
			$\mathtt{lda} \geq \max(\mathtt{1,n}) \; if \; \mathtt{transa} == \mathtt{CUBLAS_OP_N}$
			and $1da \times n$ with $1da \ge max(1,k)$ otherwise.
lda		input	leading dimension of two-dimensional array used
			to store matrix A.
beta	host or device	input	<pre><type> scalar used for multiplication, if beta==0</type></pre>
			then C does not have to be a valid input.
\mathbf{C}	device	in/out	$<$ type $>$ array of dimension $1dc \times n$,
			with $1dc \ge \max(1,n)$.
ldc		input	leading dimension of two-dimensional array used
			to store matrix C.

The possible error values returned by this function and their meanings are listed below.

Error Values	Meaning
CUBLAS_STATUS_SUCCESS	the operation completed successfully
CUBLAS_STATUS_NOT_INITIALIZED	the library was not initialized
CUBLAS_STATUS_INVALID_VALUE	the parameters n,k<0
CUBLAS_STATUS_ARCH_MISMATCH	the device does not support double-precision
CUBLAS_STATUS_EXECUTION_FAILED	the function failed to launch on the GPU

For references please refer to: ssyrk, dsyrk, csyrk, zsyrk

7.5 cublas<t>syr2k()

cublasStatus_t cublasDsyr2k(cublasHandle_t handle,

```
cublasFillMode_t uplo, cublasOperation_t trans,
                            int n, int k,
                            const double
                                                  *alpha,
                            const double
                                                  *A, int lda,
                            const double
                                                  *B, int ldb,
                            const double
                                                  *beta,
                            double
                                            *C, int ldc)
cublasStatus_t cublasCsyr2k(cublasHandle_t handle,
                            cublasFillMode_t uplo, cublasOperation_t trans,
                            int n, int k,
                            const cuComplex
                                                *alpha,
                            const cuComplex
                                                  *A, int lda,
                                                *B, int ldb,
                            const cuComplex
                                              *beta,
                            const cuComplex
                                           *C, int ldc)
                            cuComplex
cublasStatus_t cublasZsyr2k(cublasHandle_t handle,
                            cublasFillMode_t uplo, cublasOperation_t trans,
                            int n, int k,
                            const cuDoubleComplex *alpha,
                            const cuDoubleComplex *A, int lda,
                            const cuDoubleComplex *B, int ldb,
                            const cuDoubleComplex *beta,
                            cuDoubleComplex *C, int ldc)
```

This function performs the symmetric rank-2k update

$$C = \alpha \left(op(A)op(B)^T + op(B)op(A)^T \right) + \beta C$$

where α and β are scalars, C is a symmetric matrix stored in lower or upper mode, and A and B are matrices with dimensions op(A) $n \times k$ and op(B) $n \times k$, respectively. Also, for matrix A and B

$$\mathrm{op}(A) \text{ and } \mathrm{op}(B) = \begin{cases} A \text{ and } B & \text{if trans == CUBLAS_OP_N} \\ A^T \text{ and } B^T & \text{if trans == CUBLAS_OP_T} \end{cases}$$

Param.	Memory	In/out	Meaning
handle		input	handle to the CUBLAS library context.
uplo		input	indicates if matrix A lower or upper part, is
			stored, the other symmetric part is not referen-
			ced and is inferred from the stored elements.
trans		input	operation op(A) that is non- or transpose.
n		input	number of rows of matrix op(A), op(B) and C.
k		input	number of columns of matrix op(A) and op(B).
alpha	host or device	input	<type> scalar used for multiplication.</type>
A	device	input	<type> array of dimension lda × k</type>
			with $lda \ge max(1,n)$ if transa == CUBLAS_OP_N
			and $\mathtt{lda} \times \mathtt{n}$ with $\mathtt{lda} \geq \max(1,\mathtt{k})$ otherwise.
lda		input	leading dimension of two-dimensional array used
			to store matrix A.
В	device	input	$\langle \text{type} \rangle$ array of dimensions 1db \times k
			with $ldb \ge max(1,n)$ if transa == CUBLAS_OP_N
			and $ldb \times n$ with $ldb \ge max(1,k)$ otherwise.
ldb		input	leading dimension of two-dimensional array used
			to store matrix B.
beta	host or device	input	<pre><type> scalar used for multiplication, if beta==0,</type></pre>
			then C does not have to be a valid input.
\mathbf{C}	device	in/out	$\langle \text{type} \rangle$ array of dimensions $\mathtt{ldc} \times \mathtt{n}$
			with $1dc \ge max(1,n)$.
ldc		input	leading dimension of two-dimensional array used
			to store matrix C.

The possible error values returned by this function and their meanings are listed below.

Error Values	Meaning
CUBLAS_STATUS_SUCCESS	the operation completed successfully
CUBLAS_STATUS_NOT_INITIALIZED	the library was not initialized
CUBLAS_STATUS_INVALID_VALUE	the parameters n,k<0
CUBLAS_STATUS_ARCH_MISMATCH	the device does not support double-precision
CUBLAS_STATUS_EXECUTION_FAILED	the function failed to launch on the GPU

For references please refer to: ssyr2k, dsyr2k, csyr2k, zsyr2k

7.6 cublas<t>trmm()

```
const float
                                            *alpha,
                           const float
                                                  *A, int lda,
                           const float
                                                  *B, int ldb,
                           float
                                                  *C, int ldc)
cublasStatus_t cublasDtrmm(cublasHandle_t handle,
                           cublasSideMode_t side, cublasFillMode_t uplo,
                           cublasOperation_t trans, cublasDiagType_t diag,
                           int m, int n,
                           const double
                                            *alpha,
                           const double
                                                  *A, int lda,
                           const double
                                                  *B, int ldb,
                                                  *C, int ldc)
                           double
cublasStatus_t cublasCtrmm(cublasHandle_t handle,
                           cublasSideMode_t side, cublasFillMode_t uplo,
                           cublasOperation_t trans, cublasDiagType_t diag,
                           int m, int n,
                           const cuComplex *alpha,
                           const cuComplex
                                                  *A, int lda,
                                                  *B, int ldb,
                           const cuComplex
                                                  *C, int ldc)
                           cuComplex
cublasStatus_t cublasZtrmm(cublasHandle_t handle,
                           cublasSideMode_t side, cublasFillMode_t uplo,
                           cublasOperation_t trans, cublasDiagType_t diag,
                           int m, int n, const
                           cuDoubleComplex *alpha,
                           const cuDoubleComplex *A, int lda,
                           const cuDoubleComplex *B, int ldb,
                           cuDoubleComplex
                                                  *C, int ldc)
```

This function performs the triangular matrix-matrix multiplication

$$C = \begin{cases} \alpha \operatorname{op}(A)B & \text{if side == CUBLAS_SIDE_LEFT} \\ \alpha B \operatorname{op}(A) & \text{if side == CUBLAS_SIDE_RIGHT} \end{cases}$$

where A is a triangular matrix stored in lower or upper mode with or without the main diagonal, B and C are $m \times n$ matrix, and α is a scalar. Also, for matrix A

$$\mathrm{op}(A) = \begin{cases} A & \text{if trans == CUBLAS_OP_N} \\ A^T & \text{if trans == CUBLAS_OP_T} \\ A^H & \text{if trans == CUBLAS_OP_C} \end{cases}$$

Notice that in order to achieve better parallelism CUBLAS differs from the BLAS API only for this routine. The BLAS API assumes an in-place implementation (with results written back to B), while the CUBLAS API assumes an out-of-place implementation (with

results written into C). The application can obtain the in-place functionality of BLAS in the CUBLAS API by passing the address of the matrix B in place of the matrix C. No other overlapping in the input parameters is supported.

Param.	Memory	In/out	Meaning
handle		input	handle to the CUBLAS library context.
side		input	indicates if matrix A is on the left or right of B.
uplo		input	indicates if matrix A lower or upper part
			is stored, the other part is not referen-
			ced and is inferred from the stored elements.
trans		input	operation op(A) that is non- or (conj.) transpose.
diag		input	indicates if the elements on the main diagonal of
			matrix A are unity and should not be accessed.
\mathbf{m}		input	number of rows of matrix B, with
			matrix A sized accordingly.
n		input	number of columns of matrix B, with
			matrix A sized accordingly.
alpha	host or device	input	<pre><type> scalar used for multiplication, if alpha==0</type></pre>
			then A is not referenced and B does not have to be
			a valid input.
A	device	input	$<$ type $>$ array of dimension lda \times m with
			${ t lda} \geq \max(1,{ t m}) ext{ if side == CUBLAS_SIDE_LEFT}$
			and $\mathtt{lda} \times \mathtt{n}$ with $\mathtt{lda} \geq \max(1,\mathtt{n})$ otherwise.
lda		input	leading dimension of two-dimensional array used
			to store matrix A.
В	device	input	$<$ type $>$ array of dimension ldb \times n
			with $ldb \ge max(1,m)$.
ldb		input	leading dimension of two-dimensional array used
			to store matrix B.
С	device	in/out	$<$ type $>$ array of dimension $1dc \times n$
			with $1dc \ge \max(1,m)$.
ldc		input	leading dimension of two-dimensional array used
			to store matrix C.

The possible error values returned by this function and their meanings are listed below.

Error Values	Meaning
CUBLAS_STATUS_SUCCESS	the operation completed successfully
CUBLAS_STATUS_NOT_INITIALIZED	the library was not initialized
CUBLAS_STATUS_INVALID_VALUE	the parameters m,n<0
CUBLAS_STATUS_ARCH_MISMATCH	the device does not support double-precision
CUBLAS_STATUS_EXECUTION_FAILED	the function failed to launch on the GPU

For references please refer to: strmm, dtrmm, ctrmm, ztrmm

7.7 cublas<t>trsm()

```
cublasStatus_t cublasStrsm(cublasHandle_t handle,
                           cublasSideMode_t side, cublasFillMode_t uplo,
                           cublasOperation_t trans, cublasDiagType_t diag,
                           int m, int n,
                           const float
                                                 *alpha,
                           const float
                                                 *A, int lda,
                           float
                                          *B, int ldb)
cublasStatus_t cublasDtrsm(cublasHandle_t handle,
                           cublasSideMode_t side, cublasFillMode_t uplo,
                           cublasOperation_t trans, cublasDiagType_t diag,
                           int m, int n,
                           const double
                                                *alpha,
                           const double
                                                *A, int lda,
                           double
                                           *B, int ldb)
cublasStatus_t cublasCtrsm(cublasHandle_t handle,
                           cublasSideMode_t side, cublasFillMode_t uplo,
                           cublasOperation_t trans, cublasDiagType_t diag,
                           int m, int n,
                           const cuComplex
                                                 *alpha,
                                                 *A, int lda,
                           const cuComplex
                           cuComplex
                                           *B, int ldb)
cublasStatus_t cublasZtrsm(cublasHandle_t handle,
                           cublasSideMode_t side, cublasFillMode_t uplo,
                           cublasOperation_t trans, cublasDiagType_t diag,
                           int m, int n,
                           const cuDoubleComplex *alpha,
                           const cuDoubleComplex *A, int lda,
                           cuDoubleComplex *B, int ldb)
```

This function solves the triangular linear system with multiple right-hand-sides

$$\begin{cases} \operatorname{op}(A)X = \alpha B & \text{if side == CUBLAS_SIDE_LEFT} \\ X\operatorname{op}(A) = \alpha B & \text{if side == CUBLAS_SIDE_RIGHT} \end{cases}$$

where A is a triangular matrix stored in lower or upper mode with or without the main diagonal, X and B are $m \times n$ matrices, and α is a scalar. Also, for matrix A

$$\mathrm{op}(A) = \begin{cases} A & \text{if trans} == \texttt{CUBLAS_OP_N} \\ A^T & \text{if trans} == \texttt{CUBLAS_OP_T} \\ A^H & \text{if trans} == \texttt{CUBLAS_OP_C} \end{cases}$$

The solution X overwrites the right-hand-sides B on exit.

Param.	Memory	In/out	Meaning
handle		input	handle to the CUBLAS library context.
side		input	indicates if matrix A is on the left or right of X .
uplo		input	indicates if matrix A lower or upper part
			is stored, the other part is not referen-
			ced and is inferred from the stored elements.
trans		input	operation op(A) that is non- or (conj.) transpose.
diag		input	indicates if the elements on the main diagonal of
			matrix A are unity and should not be accessed.
m		input	number of rows of matrix B, with
			matrix A sized accordingly.
n		input	number of columns of matrix B, with
		_	matrix A is sized accordingly.
alpha	host or device	input	<pre><type> scalar used for multiplication, if alpha==0</type></pre>
			then A is not referenced and B does not have to be
			a valid input.
A	device	input	$\langle \text{type} \rangle$ array of dimension $\texttt{lda} \times \texttt{m}$ with
			$ exttt{lda} \geq \max(1, exttt{m}) ext{ if side} == exttt{CUBLAS_SIDE_LEFT}$
			and $\mathtt{lda} \times \mathtt{n}$ with $\mathtt{lda} \geq \max(1,\mathtt{n})$ otherwise.
lda		input	leading dimension of two-dimensional array used
			to store matrix A.
В	device	in/out	<type> array</type>
		·	It has dimensions $ldb \times n$ with $ldb \ge max(1,m)$.
ldb		input	leading dimension of two-dimensional array used
			to store matrix B.

No test for singularity or near-singularity is included in this function.

The possible error values returned by this function and their meanings are listed below.

Error Values	Meaning
CUBLAS_STATUS_SUCCESS	the operation completed successfully
CUBLAS_STATUS_NOT_INITIALIZED	the library was not initialized
CUBLAS_STATUS_INVALID_VALUE	the parameters m,n<0
CUBLAS_STATUS_ARCH_MISMATCH	the device does not support double-precision
CUBLAS_STATUS_EXECUTION_FAILED	the function failed to launch on the GPU

For references please refer to: strsm, dtrsm, ctrsm, ztrsm

7.8 cublas<t>hemm()

```
const cuComplex
                                                 *alpha,
                           const cuComplex
                                                *A, int lda,
                           const cuComplex
                                                *B, int ldb,
                           const cuComplex
                                                *beta,
                           cuComplex
                                           *C, int ldc)
cublasStatus_t cublasZhemm(cublasHandle_t handle,
                           cublasSideMode_t side, cublasFillMode_t uplo,
                           int m, int n,
                           const cuDoubleComplex *alpha,
                           const cuDoubleComplex *A, int lda,
                           const cuDoubleComplex *B, int ldb,
                           const cuDoubleComplex *beta,
                           cuDoubleComplex *C, int ldc)
```

This function performs the Hermitian matrix-matrix multiplication

$$C = \begin{cases} \alpha AB + \beta C & \text{if side == CUBLAS_SIDE_LEFT} \\ \alpha BA + \beta C & \text{if side == CUBLAS_SIDE_RIGHT} \end{cases}$$

where A is a Hermitian matrix stored in lower or upper mode, B and C are $m \times n$ matrices, and α and β are scalars.

Param.	Memory	In/out	Meaning
handle		input	handle to the CUBLAS library context.
side		input	indicates if matrix A is on the left or right of B.
uplo		input	indicates if matrix A lower or upper part is
			stored, the other Hermitian part is not referen-
			ced and is inferred from the stored elements.
\mathbf{m}		input	number of rows of matrix C and B,
			with matrix A sized accordingly.
\mathbf{n}		input	number of columns of matrix C and B,
			with matrix A sized accordingly.
alpha	host or device	input	<pre><type> scalar used for multiplication.</type></pre>
A	device	input	$<$ type $>$ array of dimension lda \times m
			with $\mathtt{lda} \geq \max(1,\mathtt{m})$ if $\mathtt{side} = \mathtt{CUBLAS_SIDE_LEFT}$
			and $\mathtt{lda} \times \mathtt{n}$ with $\mathtt{lda} \geq \max(1,\mathtt{n})$ otherwise.
			The imaginary parts of the diagonal elements are
			assumed to be zero.
lda		input	leading dimension of two-dimensional array used
			to store matrix A.
В	device	input	$<$ type $>$ array of dimension ldb \times n
			with $ldb \ge max(1,m)$.
ldb		input	leading dimension of two-dimensional array used
			to store matrix B.
beta		input	<pre><type> scalar used for multiplication, if beta==0</type></pre>
			then C does not have to be a valid input.
С	device	in/out	$<$ type $>$ array of dimensions $1dc \times n$
			with $1dc \ge max(1,m)$.
ldc		input	leading dimension of two-dimensional array used
			to store matrix C.

The possible error values returned by this function and their meanings are listed below.

Error Values	Meaning
CUBLAS_STATUS_SUCCESS	the operation completed successfully
CUBLAS_STATUS_NOT_INITIALIZED	the library was not initialized
CUBLAS_STATUS_INVALID_VALUE	the parameters m,n<0
CUBLAS_STATUS_ARCH_MISMATCH	the device does not support double-precision
CUBLAS_STATUS_EXECUTION_FAILED	the function failed to launch on the GPU

For references please refer to: chemm, zhemm

7.9 cublas<t>herk()

```
cublasStatus_t cublasCherk(cublasHandle_t handle,
                           cublasFillMode_t uplo, cublasOperation_t trans,
                           int n, int k,
                           const float *alpha,
                           const cuComplex
                                                *A, int lda,
                           const float *beta,
                           cuComplex
                                           *C, int ldc)
cublasStatus_t cublasZherk(cublasHandle_t handle,
                           cublasFillMode_t uplo, cublasOperation_t trans,
                           int n, int k,
                           const double *alpha,
                           const cuDoubleComplex *A, int lda,
                           const double *beta,
                           cuDoubleComplex *C, int ldc)
```

This function performs the Hermitian rank-k update

$$C = \alpha \operatorname{op}(A)\operatorname{op}(A)^H + \beta C$$

where α and β are scalars, C is a Hermitian matrix stored in lower or upper mode, and A is a matrix with dimensions op(A) $n \times k$. Also, for matrix A

$$\mathrm{op}(A) = \begin{cases} A & \text{if trans} == \texttt{CUBLAS_OP_N} \\ A^H & \text{if trans} == \texttt{CUBLAS_OP_C} \end{cases}$$

Param.	Memory	In/out	Meaning
handle		input	handle to the CUBLAS library context.
uplo		input	indicates if matrix A lower or upper part is
			stored, the other Hermitian part is not referen-
			ced and is inferred from the stored elements.
trans		input	operation op(A) that is non- or (conj.) transpose.
n		input	number of rows of matrix op(A) and C.
k		input	number of columns of matrix op(A).
alpha	host or device	input	<type> scalar used for multiplication.</type>
A	device	input	$<$ type $>$ array of dimension lda \times k
			with $lda \ge max(1,n)$ if transa == CUBLAS_OP_N
			and $\mathtt{lda} \times \mathtt{n}$ with $\mathtt{lda} \geq \max(1,\mathtt{k})$ otherwise.
lda		input	leading dimension of two-dimensional array used
			to store matrix A.
beta		input	<pre><type> scalar used for multiplication, if beta==0</type></pre>
			then C does not have to be a valid input.
С	device	in/out	$\langle \text{type} \rangle$ array of dimension $\mathtt{ldc} \times \mathtt{n}$, with
			$1dc \ge max(1,n)$. The imaginary parts of the
			diagonal elements are assumed and set to zero.
ldc		input	leading dimension of two-dimensional array used
			to store matrix C.

The possible error values returned by this function and their meanings are listed below.

Error Values	Meaning
CUBLAS_STATUS_SUCCESS	the operation completed successfully
CUBLAS_STATUS_NOT_INITIALIZED	the library was not initialized
CUBLAS_STATUS_INVALID_VALUE	the parameters n,k<0
CUBLAS_STATUS_ARCH_MISMATCH	the device does not support double-precision
CUBLAS_STATUS_EXECUTION_FAILED	the function failed to launch on the GPU

For references please refer to: cherk, zherk

7.10 cublas<t>her2k()

This function performs the Hermitian rank-2k update

$$C = \alpha \operatorname{op}(A)\operatorname{op}(B)^{H} + \bar{\alpha}\operatorname{op}(B)\operatorname{op}(A)^{H} + \beta C$$

where α and β are scalars, C is a Hermitian matrix stored in lower or upper mode, and A and B are matrices with dimensions op(A) $n \times k$ and op(B) $n \times k$, respectively. Also, for matrix A and B

$$\mathrm{op}(A) \text{ and } \mathrm{op}(B) = \begin{cases} A \text{ and } B & \text{if trans == CUBLAS_OP_N} \\ A^H \text{ and } B^H & \text{if trans == CUBLAS_OP_C} \end{cases}$$

handle uplo input indicates if matrix A lower or upper part is stored, the other Hermitian part is not referenced and is inferred from the stored elements. trans input operation op(A) that is non- or (conj.) transpos number of rows of matrix op(A), op(B) and C. k input number of columns of matrix op(A) and op(B).	
stored, the other Hermitian part is not referenced and is inferred from the stored elements. trans input operation op(A) that is non- or (conj.) transpos n input number of rows of matrix op(A), op(B) and C.	
trans input operation op(A) that is non- or (conj.) transpos number of rows of matrix op(A), op(B) and C.	
trans input operation $op(A)$ that is non- or $(conj.)$ transpos number of rows of matrix $op(A)$, $op(B)$ and C .).GO
n input number of rows of matrix $op(A)$, $op(B)$ and C .	\CO
	DSE.
k input number of columns of matrix $op(A)$ and $op(B)$.	
=	
alpha host or device input <type> scalar used for multiplication.</type>	
A device input $\langle \text{type} \rangle$ array of dimension lda \times k	
with $1da \ge max(1,n)$ if transa == CUBLAS_OP_	_N
and $\mathtt{lda} \times \mathtt{n}$ with $\mathtt{lda} \geq \max(1,\mathtt{k})$ otherwise.	
lda input leading dimension of two-dimensional array used	ed
to store matrix A.	
B device input $\langle \text{type} \rangle$ array of dimension $\mathtt{ldb} \times \mathtt{k}$	
	J
and $\mathtt{ldb} \times \mathtt{n}$ with $\mathtt{ldb} \geq \max(1,\mathtt{k})$ otherwise.	
ldb input leading dimension of two-dimensional array used	ed
to store matrix B.	
beta host or device input <type> scalar used for multiplication, if beta=</type>	==0
then C does not have to be a valid input.	
C device in/out $<$ type $>$ array of dimension $1dc \times n$, with	
$1dc \ge \max(1,n)$. The imaginary parts of the	
diagonal elements are assumed and set to zero.).
ldc input leading dimension of two-dimensional array used	
to store matrix C.	

The possible error values returned by this function and their meanings are listed below.

Error Values	Meaning
CUBLAS_STATUS_SUCCESS	the operation completed successfully
CUBLAS_STATUS_NOT_INITIALIZED	the library was not initialized
CUBLAS_STATUS_INVALID_VALUE	the parameters n,k<0
CUBLAS_STATUS_ARCH_MISMATCH	the device does not support double-precision
CUBLAS_STATUS_EXECUTION_FAILED	the function failed to launch on the GPU

For references please refer to: cher2k, zher2k

Chapter 8

Appendix A: Using the CUBLAS Legacy API

This appendix does not provide a full reference of each Legacy API datatype and entry point. Instead, it describes how to use the API, especially where this is different from the regular CUBLAS API.

Note that in this section, all references to the "CUBLAS Library" refer to the Legacy CUBLAS API only.

8.1 Error Status

The cublasStatus type is used for function status returns. The CUBLAS Library helper functions return status directly, while the status of core functions can be retrieved using cublasGetError(). Notice that reading the error status via cublasGetError(), resets the internal error state to CUBLAS_STATUS_SUCCESS. Currently, the following values for cublasStatus are defined:

Value	Meaning
CUBLAS_STATUS_SUCCESS	the operation completed successfully
CUBLAS_STATUS_NOT_INITIALIZED	the library was not initialized
CUBLAS_STATUS_ALLOC_FAILED	the resource allocation failed
CUBLAS_STATUS_INVALID_VALUE	an invalid numerical value was used as an argument
CUBLAS_STATUS_ARCH_MISMATCH	an absent device architectural feature is required
CUBLAS_STATUS_MAPPING_ERROR	an access to GPU memory space failed
CUBLAS_STATUS_EXECUTION_FAILED	the GPU program failed to execute
CUBLAS_STATUS_INTERNAL_ERROR	an internal operation failed

This legacy type corresponds to type cublasStatus_t in the CUBLAS library API.

8.2 Initialization and Shutdown

The functions cublasInit() and cublasShutdown() are used to initialize and shutdown the CUBLAS library. It is recommended for cublasInit() to be called before any other

function is invoked. It allocates hardware resources on the GPU device that is currently bound to the host thread from which it was invoked.

The legacy initialization and shutdown functions are similar to the CUBLAS library API routines cublasCreate() and cublasDestroy().

8.3 Thread Safety

The legacy API is not thread safe when used with multiple host threads and devices. It is recommended to be used only when utmost compatibility with Fortran is required and when a single host thread is used to setup the library and make all the functions calls.

8.4 Memory Management

The memory used by the legacy CUBLAS library API is allocated and released using functions cublasAlloc() and cublasFree(), respectively. These functions create and destroy an object in the GPU memory space capable of holding an array of n elements, where each element requires elemSize bytes of storage. Please see the legacy CUBLAS API header file "cublas.h" for the prototypes of these functions.

The function cublasAlloc() is a wrapper around the function cudaMalloc(), therefore device pointers returned by cublasAlloc() can be passed to any CUDATM device kernel functions. However, these device pointers can not be dereferenced in the host code. The function cublasFree() is a wrapper around the function cudaFree().

8.5 Scalar Parameters

In the legacy CUBLAS API, scalar parameters are passed by value from the host. Also, the few functions that do return a scalar result, such as dot() and nrm2(), return the resulting value on the host, and hence these routines will wait for kernel execution on the device to complete before returning, which makes parallelism with streams impractical. However, the majority of functions do not return any value, in order to be more compatible with Fortran and the existing BLAS libraries.

8.6 Helper Functions

In this section we list the helper functions provided by the legacy CUBLAS API and their functionality. For the exact prototypes of these functions please refer to the legacy CUBLAS API header file "cublas.h".

Helper function	Meaning
cublasInit()	initialize the library
cublasShutdown()	shuts down the library
cublasGetError()	retrieves the error status of the library
cublasSetKernelStream()	sets the stream to be used by the library
cublasAlloc()	allocates the device memory for the library
cublasFree()	releases the device memory allocated for the library
cublasSetVector()	copies a vector x on the host to a vector y on the GPU
<pre>cublasGetVector()</pre>	copies a vector x on the GPU to a vector y on the host
<pre>cublasSetMatrix()</pre>	copies a $m \times n$ tile from a matrix on the host to the GPU
<pre>cublasGetMatrix()</pre>	copies a $m \times n$ tile from a matrix on the GPU to the host
<pre>cublasSetVectorAsync()</pre>	similar to cublasSetVector(), but the copy is asynchronous
<pre>cublasGetVectorAsync()</pre>	similar to cublasGetVector(), but the copy is asynchronous
<pre>cublasSetMatrixAsync()</pre>	similar to cublasSetMatrix(), but the copy is asynchronous
<pre>cublasGetMatrixAsync()</pre>	similar to cublasGetMatrix(), but the copy is asynchronous

8.7 Level-1,2,3 Functions

The Level-1,2,3 CUBLAS functions (also called core functions) have the same name and behavior as the ones listed in the chapters 3, 4 and 5 in this document. Please refer to the legacy CUBLAS API header file "cublas.h" for their exact prototype. Also, the next section talks a bit more about the differences between the legacy and the CUBLAS API prototypes, more specifically how to convert the function calls from one API to another.

8.8 Converting Legacy to the CUBLAS API

There are a few general rules that can be used to convert from legacy to the CUBLAS API.

- 1. Exchange the header file "cublas.h" for "cublas v2.h".
- 2. Exchange the type cublasStatus for cublasStatus_t.
- 3. Exchange the function cublasSetKernelStream() for cublasSetStream().
- 4. Exchange the function cublasAlloc() and cublasFree() for cudaMalloc() and cudaFree(), respectively. Notice that cudaMalloc() expects the size of the allocated memory to be provided in bytes (usually simply provide n × elemSize to allocate n elements, each of size elemSize bytes).
- 5. Declare the cublasHandle_t CUBLAS library handle.
- 6. Initialize the handle using cublasCreate(). Also, release the handle once finished using cublasDestroy().
- 7. Add the handle as the first parameter to all the CUBLAS library function calls.

- 8. Change the scalar parameters to be passed by reference, instead of by value (usually simply adding "&" symbol in C/C++ is enough, because the parameters are passed by reference on the host by default). However, note that if the routine is running asynchronously, then the variable holding the scalar parameter cannot be changed until the kernels that the routine dispatches are completed. See the CUDA C Programming Guide for a detailed discussion of how to use streams.
- Change the parameter characters 'N' or 'n' (non-transpose operation), 'T' or 't' (transpose operation) and 'C' or 'c' (conjugate transpose operation) to CUBLAS_OP_N, CUBLAS_OP_T and CUBLAS_OP_C, respectively.
- 10. Change the parameter characters 'L' or 'l' (lower part filled) and 'U' or 'u' (upper part filled) to CUBLAS_FILL_MODE_LOWER and CUBLAS_FILL_MODE_UPPER, respectively.
- 11. Change the parameter characters 'N' or 'n' (non-unit diagonal) and 'U' or 'u' (unit diagonal) to CUBLAS_DIAG_NON_UNIT and CUBLAS_DIAG_UNIT, respectively.
- 12. Change the parameter characters 'L' or 'l' (left side) and 'R' or 'r' (right side) to CUBLAS_SIDE_LEFT and CUBLAS_SIDE_RIGHT, respectively.
- 13. If the legacy API function returns a scalar value, add an extra scalar parameter of the same type passed by reference, as the last parameter to the same function.
- 14. Instead of using cublasGetError(), use the return value of the function itself to check for errors.

Finally, please use the function prototypes in the header files "cublas.h" and "cublas_v2.h" to check the code for correctness.

8.9 Examples

For sample code references that use the legacy CUBLAS API please see the two examples below. They show an application written in C using the legacy CUBLAS library API with two indexing styles (Example A.1. "Application Using C and CUBLAS: 1-based indexing" and Example A.2. "Application Using C and CUBLAS: 0-based Indexing"). This application is analogous to the one using the CUBLAS library API that is shown in the Introduction chapter.

```
//Example A.1. Application Using C and CUBLAS: 1-based indexing
//
#include <stdio.h>
#include <stdlib.h>
#include <math.h>
#include "cublas.h"
#define M 6
#define N 5
#define IDX2F(i,j,ld) ((((j)-1)*(ld))+((i)-1))
```

```
static __inline__ void modify (float *m, int ldm, int n, int p, int q, float alpha, ←
    float beta){
    \verb|cublasSscal| (n-p+1, alpha|, &m[IDX2F(p,q,ldm)]|, ldm|;
    cublasSscal (1dm-p+1, beta, &m[IDX2F(p,q,1dm)], 1);
int main (void){
   int i, j;
    cublasStatus stat;
    float* devPtrA;
    float* a = 0;
   a = (float *)malloc (M * N * sizeof (*a));
   if (!a) {
       printf ("host memory allocation failed");
       return EXIT_FAILURE;
    for (j = 1; j \le N; j++) {
        for (i = 1; i \le M; i++) {
           a[IDX2F(i,j,M)] = (float)((i-1) * M + j);
   cublasInit();
    stat = cublasAlloc (M*N, sizeof(*a), (void**)&devPtrA);
    if (stat != CUBLAS_STATUS_SUCCESS) {
        printf ("device memory allocation failed");
        cublasShutdown();
       return EXIT_FAILURE;
    stat = cublasSetMatrix (M, N, sizeof(*a), a, M, devPtrA, M);
    if (stat != CUBLAS_STATUS_SUCCESS) {
       printf ("data download failed");
       cublasFree (devPtrA);
        cublasShutdown();
       return EXIT_FAILURE;
   modify (devPtrA, M, N, 2, 3, 16.0f, 12.0f);
   stat = cublasGetMatrix (M, N, sizeof(*a), devPtrA, M, a, M);
    if (stat != CUBLAS_STATUS_SUCCESS) {
       printf ("data upload failed");
        cublasFree (devPtrA);
        cublasShutdown();
       return EXIT_FAILURE;
    cublasFree (devPtrA);
    cublasShutdown();
    for (j = 1; j \le N; j++) {
        for (i = 1; i \le M; i++) {
           printf ("\n");
    return EXIT_SUCCESS;
```

```
//Example A.2. Application Using C and CUBLAS: 0-based indexing
//-
#include <stdio.h>
#include <stdlib.h>
#include <math.h>
#include "cublas.h"
```

```
#define M 6
#define N 5
#define IDX2C(i,j,ld) (((j)*(ld))+(i))
static \ \_\texttt{inline}\_\texttt{void} \ \texttt{modify} \ ( \ \texttt{float} \ *\texttt{m}, \ \texttt{int} \ \texttt{ldm}, \ \texttt{int} \ \texttt{n}, \ \texttt{int} \ \texttt{p}, \ \texttt{int} \ \texttt{q}, \ \texttt{float} \ \texttt{alpha}, \hookleftarrow
      float beta){
     \verb|cublasSscal| (n-p, alpha, &m[IDX2C(p,q,ldm)], ldm); \\
     cublasSscal (ldm-p, beta, &m[IDX2C(p,q,ldm)], 1);
int main (void) {
    int i, j;
     cublasStatus stat;
     float* devPtrA;
     float* a = 0;
     a = (float *)malloc (M * N * sizeof (*a));
     if (!a) {
         printf ("host memory allocation failed");
         return EXIT_FAILURE;
     for (j = 0; j < N; j++) {
         for (i = 0; i < M; i++) {
              a[IDX2C(i,j,M)] = (float)(i * M + j + 1);
     cublasInit();
     \mathtt{stat} \, = \, \mathtt{cublasAlloc} \, \, \left( \, \mathtt{M*N} \, , \, \, \, \, \mathbf{sizeof} \, (\, \mathtt{*a}) \, , \, \, \, (\, \mathtt{void} \, \mathtt{**}) \& \mathtt{devPtrA} \, \right);
     if (stat != CUBLAS_STATUS_SUCCESS) {
         printf ("device memory allocation failed");
          cublasShutdown();
          return EXIT_FAILURE;
    }
     stat = cublasSetMatrix (M, N, sizeof(*a), a, M, devPtrA, M);
     if (stat != CUBLAS_STATUS_SUCCESS) {
         printf ("data download failed");
         cublasFree (devPtrA);
         cublasShutdown();
         return EXIT_FAILURE;
    if (stat != CUBLAS_STATUS_SUCCESS) {
         printf ("data upload failed");
         cublasFree (devPtrA);
          cublasShutdown();
         return EXIT_FAILURE;
     cublasFree (devPtrA);
    cublasShutdown();
     for (j = 0; j < N; j++) {
          for (i = 0; i < M; i++) {
              printf ("%7.0f", a[IDX2C(i,j,M)]);
         printf ("\n");
     return EXIT_SUCCESS;
```

Chapter 9

Appendix B: CUBLAS Fortran Bindings

The CUBLAS library is implemented using the C-based CUDA toolchain, and thus provides a C-style API. This makes interfacing to applications written in C and C++ trivial, but the library can also be used by applications written in Fortran. In particular, the CUBLAS library uses 1-based indexing and Fortran-style column-major storage for multidimensional data to simplify interfacing to Fortran applications. Unfortunately, Fortran-to-C calling conventions are not standardized and differ by platform and toolchain. In particular, differences may exist in the following areas:

- ▶ symbol names (capitalization, name decoration)
- ▶ argument passing (by value or reference)
- ▶ passing of string arguments (length information)
- ▶ passing of pointer arguments (size of the pointer)
- ► returning floating-point or compound data types (for example single-precision or complex data types)

To provide maximum flexibility in addressing those differences, the CUBLAS Fortran interface is provided in the form of wrapper functions. These wrapper functions, written in C, are provided in two forms:

- 1. the thunking wrapper interface located in the file fortran thunking.c
- 2. the direct wrapper interface located in the file fortran.c

The code of one of those 2 files needs to be compiled into an application for it to call the CUBLAS API functions. Providing source code allows users to make any changes necessary for a particular platform and toolchain.

The code in those two C files has been used to demonstrate interoperability with the compilers $g77\ 3.2.3$ and $g95\ 0.91$ on 32-bit Linux, $g77\ 3.4.5$ and $g95\ 0.91$ on 64-bit Linux, Intel Fortran 9.0 and Intel Fortran 10.0 on 32-bit and 64-bit Microsoft Windows XP, and $g77\ 3.4.0$ and $g95\ 0.92$ on Mac OS X.

Note that for g77, use of the compiler flag -fno-second-underscore is required to use these wrappers as provided. Also, the use of the default calling conventions with regard to

argument and return value passing is expected. Using the flag -fno-f2c changes the default calling convention with respect to these two items.

The thunking wrappers allow interfacing to existing Fortran applications without any changes to the application. During each call, the wrappers allocate GPU memory, copy source data from CPU memory space to GPU memory space, call CUBLAS, and finally copy back the results to CPU memory space and deallocate the GPU memory. As this process causes very significant call overhead, these wrappers are intended for light testing, not for production code. To use the thunking wrappers, the application needs to be compiled with the file fortran—thunking.c

The direct wrappers, intended for production code, substitute device pointers for vector and matrix arguments in all BLAS functions. To use these interfaces, existing applications need to be modified slightly to allocate and deallocate data structures in GPU memory space (using CUBLAS_ALLOC and CUBLAS_FREE) and to copy data between GPU and CPU memory spaces (using CUBLAS_SET_VECTOR, CUBLAS_GET_VECTOR, CUBLAS_SET_MATRIX, and CUBLAS_GET_MATRIX). The sample wrappers provided in fortran.c map device pointers to the OS-dependent type size_t, which is 32-bit wide on 32-bit platforms and 64-bit wide on a 64-bit platforms.

```
Example B.1. Fortran 77 Application Executing on the Host
      subroutine modify (m, ldm, n, p, q, alpha, beta)
     implicit none
     integer ldm, n, p, q
     real*4 m(1dm,*), alpha, beta
      external cublas_sscal
      call cublas_sscal (n-p+1, alpha, m(p,q), ldm)
      call cublas_sscal (ldm-p+1, beta, m(p,q), 1)
      return
     end
     program matrixmod
     implicit none
     integer M, N
     parameter (M=6, N=5)
      real*4 a(M,N)
      integer i, j
     external cublas_init
     external cublas_shutdown
     do j = 1, N
       doi=1, M
         \mathtt{a}(\mathtt{i},\mathtt{j}) = (\mathtt{i} \mathtt{-} 1) * \mathtt{M} + \mathtt{j}
        enddo
      enddo
      call cublas_init
      call modify (a, M, N, 2, 3, 16.0, 12.0)
      call cublas_shutdown
     do j = 1, N
        do i = 1, M
          write(*,"(F7.0$)") a(i,j)
        enddo
        write (*,*) ""
      enddo
```

```
stop
end
```

One approach to deal with index arithmetic on device pointers in Fortran code is to use C-style macros, and use the C preprocessor to expand these, as shown in the example below. On Linux and Mac OS X, one way of pre-processing is to use the option '-E -x f77-cpp-input' when using g77 compiler, or simply the option '-cpp' when using g95 or gfortran. On Windows platforms with Microsoft Visual C/C++, using 'cl -EP' achieves similar results.

When traditional fixed-form Fortran 77 code is ported to use the CUBLAS library, line length often increases when the BLAS calls are exchanged for CUBLAS calls. Longer function names and possible macro expansion are contributing factors. Inadvertently exceeding the maximum line length can lead to run-time errors that are difficult to find, so care should be taken not to exceed the 72-column limit if fixed form is retained.

The examples in this chapter show a small application implemented in Fortran 77 on the host and the same application with the non-thunking wrappers after it has been ported to use the CUBLAS library.

The second example should be compiled with ARCH_64 defined as 1 on 64-bit OS system and as 0 on 32-bit OS system. For example for g95 or gfortran, this can be done directly on the command line by using the option '-cpp -DARCH 64=1'.

```
!Example B.2. Same Application Using Non-thunking CUBLAS Calls
\# 	exttt{define IDX2F(i,j,ld)} \ ((((j)-1)*(ld))+((i)-1))
       subroutine modify (devPtrM, ldm, n, p, q, alpha, beta)
       implicit none
       integer sizeof_real
       parameter (sizeof_real=4)
       integer ldm, n, p, q
#if ARCH_64
       integer *8 devPtrM
#else
       integer *4 devPtrM
#endif
       real *4 alpha, beta
       call cublas_sscal (n-p+1, alpha,
      1
                             devPtrM+IDX2F(p,q,ldm)*sizeof\_real,
      2
                             ldm)
       call cublas_sscal (1dm-p+1, beta,
      1
                             {\tt devPtrM} + {\tt IDX2F} \, (\, p \, , q \, , {\tt ldm} \,) * {\tt sizeof\_real} \; ,
      2
       return
       program matrixmod
       implicit none
       integer M, N, sizeof_real
#if ARCH_64
       integer *8 devPtrA
#else
```

```
integer *4 devPtrA
#endif
      parameter (M=6, N=5, sizeof_real=4)
       real*4 a(M,N)
      integer i, j, stat
      external cublas_init, cublas_set_matrix, cublas_get_matrix
       {\tt external \ cublas\_shutdown}\ ,\ {\tt cublas\_alloc}
      integer cublas_alloc, cublas_set_matrix, cublas_get_matrix
      do j = 1, N
        do i = 1, M
          \mathtt{a}(\mathtt{i},\mathtt{j}) = (\mathtt{i} - 1) * \mathtt{M} + \mathtt{j}
        enddo
      enddo
       call cublas_init
       stat = cublas_alloc(M*N, sizeof_real, devPtrA)
       if (stat .NE. 0) then
        write(*,*) "device memory allocation failed"
        call cublas_shutdown
        stop
       endif
       stat = cublas_set_matrix (M, N, sizeof_real, a, M, devPtrA, M)
       if (stat .NE. 0) then
        call cublas_free (devPtrA)
         write (*,*) "data download failed"
        call cublas_shutdown
        stop
       endif
       call modify (devPtrA, M, N, 2, 3, 16.0, 12.0)
       {\tt stat} = {\tt cublas\_get\_matrix} \ ({\tt M},\ {\tt N},\ {\tt sizeof\_real}\,,\ {\tt devPtrA}\,,\ {\tt M},\ {\tt a},\ {\tt M})
       if (stat .NE. 0) then
        call cublas_free (devPtrA)
        write(*,*) "data upload failed"
        call cublas_shutdown
        stop
       endif
       call cublas_free (devPtrA)
       call cublas_shutdown
      do j = 1, N
        do i = 1, M
           write(*,"(F7.0\$)") a(i,j)
        enddo
         write (*,*) ""
       enddo
       stop
       end
```

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