III. SEARCH

DATA := initial value

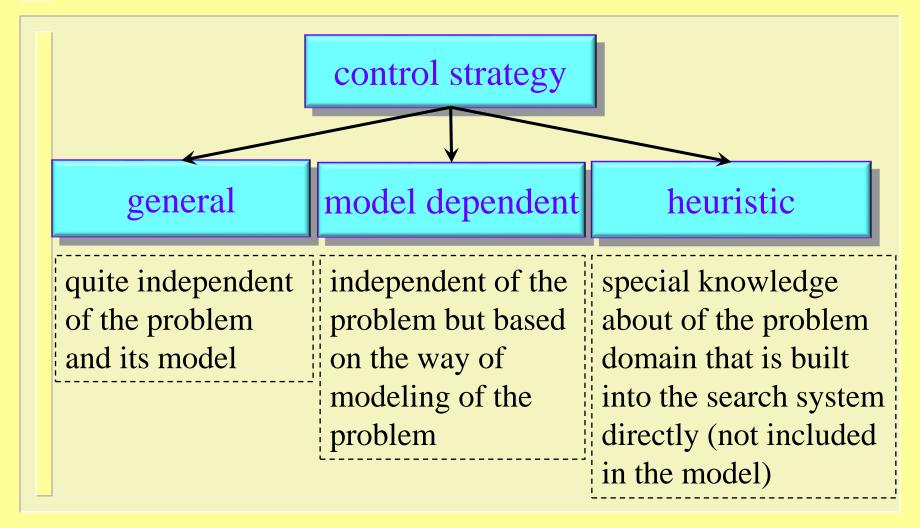
while ¬termination condition(DATA) loop

SELECT R FROM rules that can be applied

DATA := R(DATA)

Levels of control

endloop



General control strategies

general control irrevocable tentative • local search backtracking • graph-search • evolutionary alg. resolution rule-based reasoning

1. Local search

- □ The global workspace of a local search contains only one (current) node of the representation graph with its small environment. Initially this current node is the start node. The search stops if the current node is a goal node or the search could not take the next step.
- □ In each step the current node is exchanged for its better child by a searching rule.
- □ The control strategy uses an evaluation (objective, fitness, heuristic) function to select a better child node. This function tries to estimate to what extent a node promises the achievement of the goal. This function involves some heuristics.

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while ¬termination condition(DATA) loop

SELECT R FROM rules that can be applied

DATA := R(DATA)

endloop

Hill climbing method

- □ It only stores the current node and its parent that is the former current node.
- □ In each step the best child (with the smallest value) of the current node is selected except for the parent.
- 1. current := start
- 2. while $current \notin T$ loop
- 3. $current := \mathbf{opt}_f(\Gamma(current) \pi(current))$
- 4. endloop
- 5. return current

It may be useful to log the sequence of the current nodes as a path driving from the start

The original hill climbing method never makes "uphill" moves (it terminates if it cannot step onward).

if $\Gamma(current) = \emptyset$ then

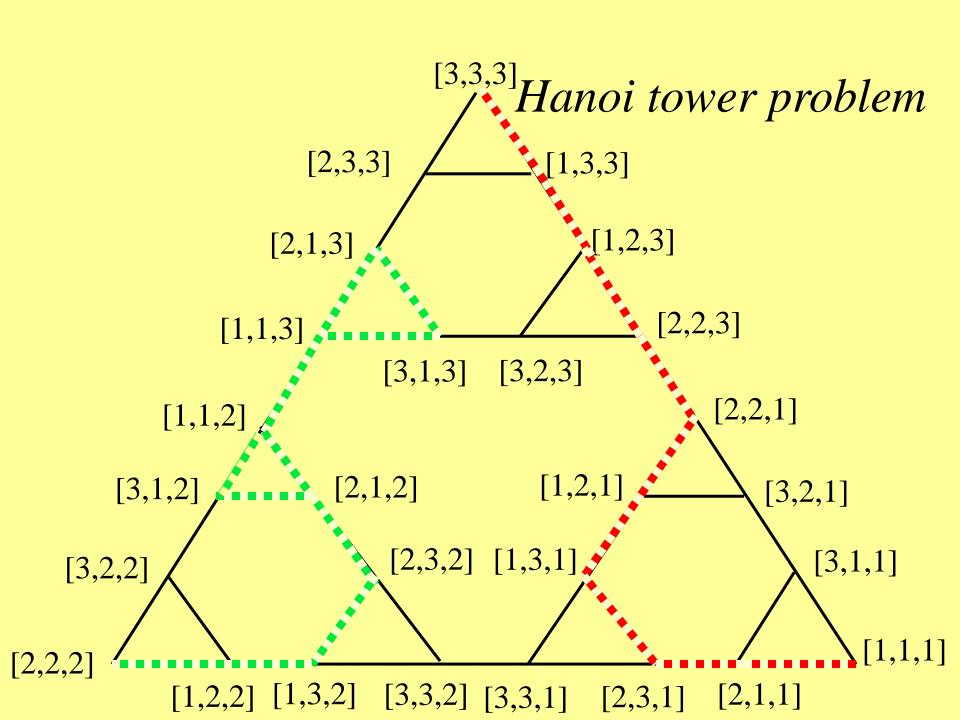
return solution no found

else if $\Gamma(current) - \pi(current) = \emptyset$ then

 $current := \pi(current)$

else *current* :=

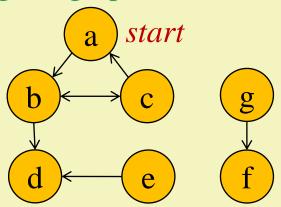
 $\mathbf{opt}_{t}(\Gamma(current) - \pi(current))$



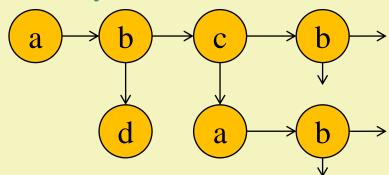
How can a path-finding algorithm perceive the representation graph?

A search discovers the representation graph step by step. Some parts of the graph are never found, and certain parts must be forgotten because of the limited memory. When a node is discovered again but it has been forgotten before, the search registers it as a new node. Thus the search can perceive the graph in a distorted form.

original graph:



distorted graph (tree) when a search can store only one node at a time:



Straightened representation graph

- □ A search that deletes the nodes discovered earlier or ignores checking them works in a tree (that is the straightened version of the original representation graph).
 Advantage: cycles vanish meanwhile each path driving
 - Disadvantage: the same node might occur several, even infinite times in this tree.

from the start node is preserved in this tree.

□ The bidirectional arcs greatly increase the size of this tree. To avoid this it might be useful to ignore the backward arcs from the current node to the previous current node. It needs only little extra memory: it is enough to store the parent node.

Remarks on Hill climbing method

- Advantage: its implementation is easy
- □ Disadvantages:
 - It can rarely find the goal without a strong heuristics because after a wrong decision it can lose itself or even stick in a dead end
 - several current nodes

local beam search

👈 tabu search

several attempts

- random-restart search
- give up the greedy strategy simulated annealing
- It can lose track around a local optimum or on an equidistant surface
 of the evaluation function (where neighboring nodes have identical
 values) if there are cycles in the representation graph (that cannot be
 recognized).
 - recognize smaller cycles

Tabu search

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- Besides the current node it stores
 - the best node (opt) that has ever been met
 - the tabu set (*Tabu*) that contains the last few current nodes
- ☐ In each step
 - the best child of the current node is selected except for the nodes of the *Tabu*
 - if the *current* node is better than *opt* node then *opt* is exchanged for the *current*
 - Tabu must be updated with the current node
- □ Termination conditions:
 - if opt is a goal
 - if the function value of opt has not been changed

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```
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while \neg termination condition(DATA) loop

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endloop

Algorithm of tabu search
```

- 1. current, opt, Tabu := start, start, Ø
- 2. while not $(opt \in T or$

opt has not been changing for a long time) loop

- 3. $current_{\cdot} = \mathbf{opt}_{f}(\Gamma(current) Tabu)$
- 4. Tabu := Update(current, Tabu)
- 5. **if** f(current) < f(opt) **then** opt := current
- 6. endloop
- 7. return current

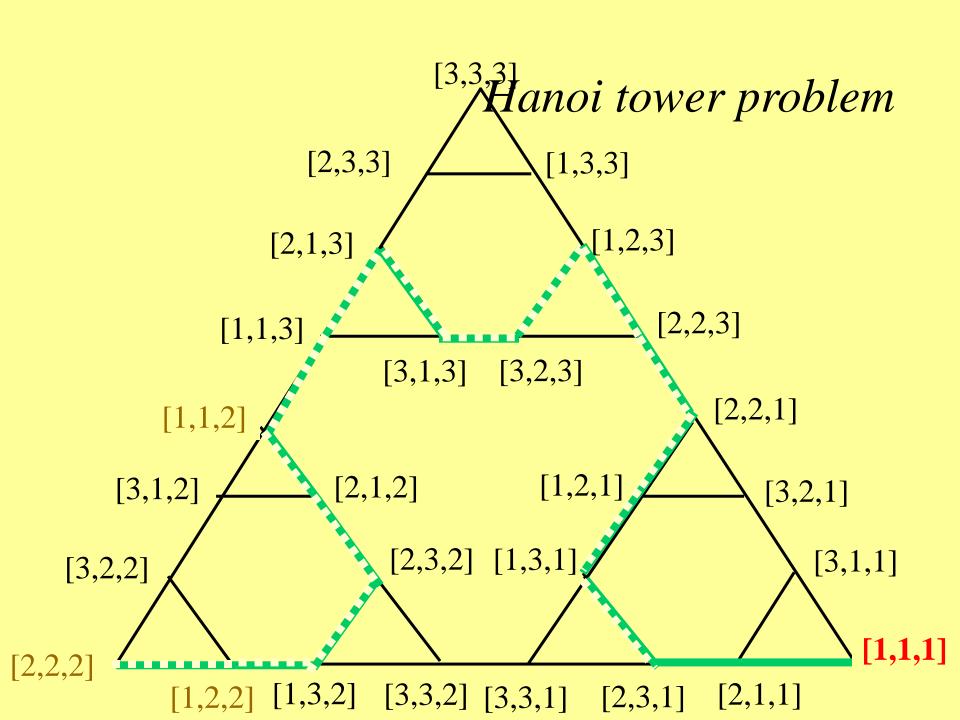
 Γ if $\Gamma(current) = \emptyset$ then return solution no found

else if $\Gamma(current)$ – $Tabu = \emptyset$

then $current := \mathbf{opt}_f(\Gamma(current))$

else $current := \mathbf{opt}_t(\Gamma(current) - Tabu)$

The original tabu search can get stuck on a node if all its children are in the tabu set.



Remarks on Tabu search

■ Advantages:

 Tabu search can recognize the smaller cycles which is shorter than the size of the tabu set so it can dominate the local optimums and the equidistant surfaces.

□ Disadvantages:

- The size of the tabu set can be set only a posteriori.
- Without a strong heuristics it can rarely find the goal,
 after wrong decisions it can lose itself or even stick in a dead end.

Simulated annealing

- □ Instead of selecting the best child of the current node, the *new* node is picked randomly from among the children of the current node.
- □ If the value of this new node is not worse than the value of the current node $(f(new) \le f(current))$, then the new node is accepted as the newer current one.
- Otherwise (f(new) > f(current)), the probability of the acceptance of the new node is inversely proportional to the difference of the values of the new and the current node (|f(current) f(new)|). $e^{\frac{f(current) f(new)}{T}} > rand[0,1]$

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Annealing schedule

- \Box The algorithm continuously changes the coefficient T of the acceptance formula.
- The changing of the coefficient is based on an annealing schedule (T_k, L_k) k=1,2,... that rules that the coefficient be T_1 during L_1 steps, then be T_2 at the next L_2 steps, etc.

 $e^{\frac{f(current)-f(new)}{T_k}} > rand[0,1]$

•	•	
	T	exp(-13/T)
	10^{10}	0.9999
	50	0.77
	20	0.52
	10	0.2725
	5	0.0743
	1	0.000002

f(new)=120, f(current)=107

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$$e^{\frac{f(current)-f(new)}{T_k}} > rand[0,1]$$

□ If T_1 , T_2 , ... is given in a decreasing order, then the probability of the acceptance of the same "bad" node is greater at the start than later.

	T	exp(-13/T)
	10^{10}	0.9999
7	50	0.77
	20	0.52
	10	0.2725
	5	0.0743
	1	0.000002

f(new)=120, f(current)=107

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endloop

Of simulated annealing

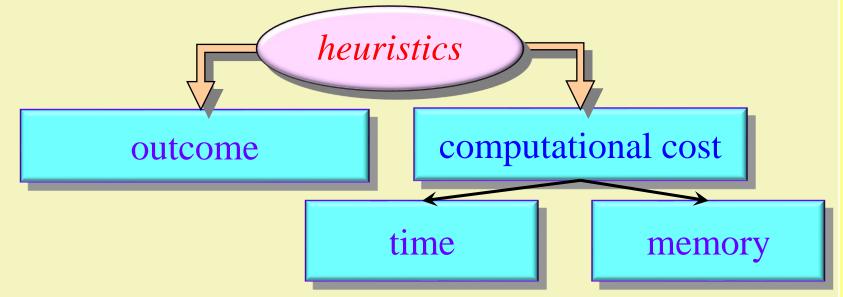
```
1. current := start; k := 1; i := 1
2. while not(current \in T \text{ or } f(current)) has not been changing) loop
3.
     if i > L_k then k := k + 1; i := 1
     new := \mathbf{select}(\Gamma(current) - \pi(current))
    if f(new) \leq f(current) or
                                     f(current)-f(new)
                                             T_k
                                                       > rand[0,1]
        f(new) > f(current) and e
      then current := new
6.
7. i := i+1 '-- if \Gamma(current) = \emptyset then return solution no found
                      else if \Gamma(current) - \pi(current) = \emptyset then new := \pi(current)
8. endloop
                      else new := select(\Gamma(current) - \pi(current))
9. return current
```

When is local search worth using?

- □ There is no chance to find a solution without strong heuristics.
 - A wrong decision can cause a fatal error.
 - An evaluation function using good heuristics can avoid dead-ends and traversing cycles.
- □ There are no dead-ends in a strongly connected representation graph.
 - Opposite to this, in a directed tree almost each branch is a dead-end. In this case only the perfect evaluation function (that never misses the appropriate path) can find solution.

Heuristics in search systems

Heuristics is an idea (special extra information) derived from the problem. It must be built directly into the algorithm (not into the model) in order to get better solution or any solution and to improve the computational cost of the algorithm, but there is no guarantee to achieve these aims.

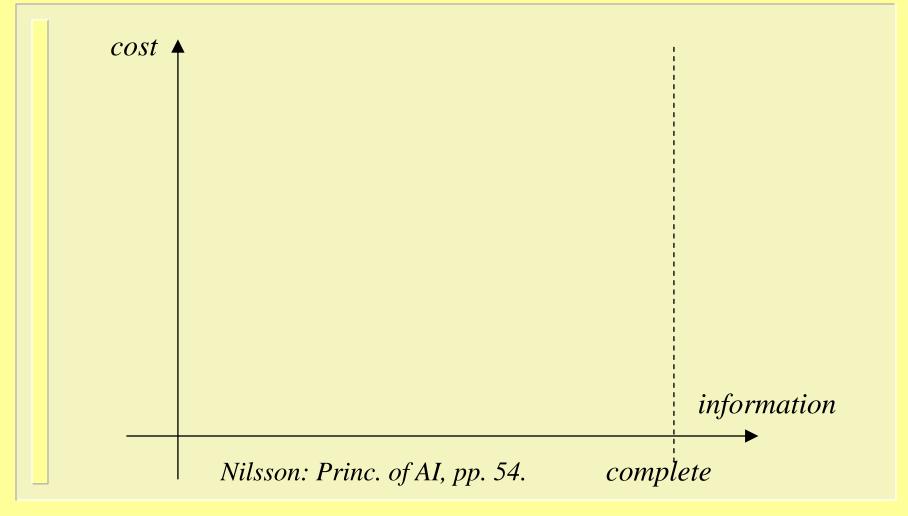


DATA \leftarrow initial value (start node)

while \neg termination condition(DATA) loop
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endloop

the computation complexity



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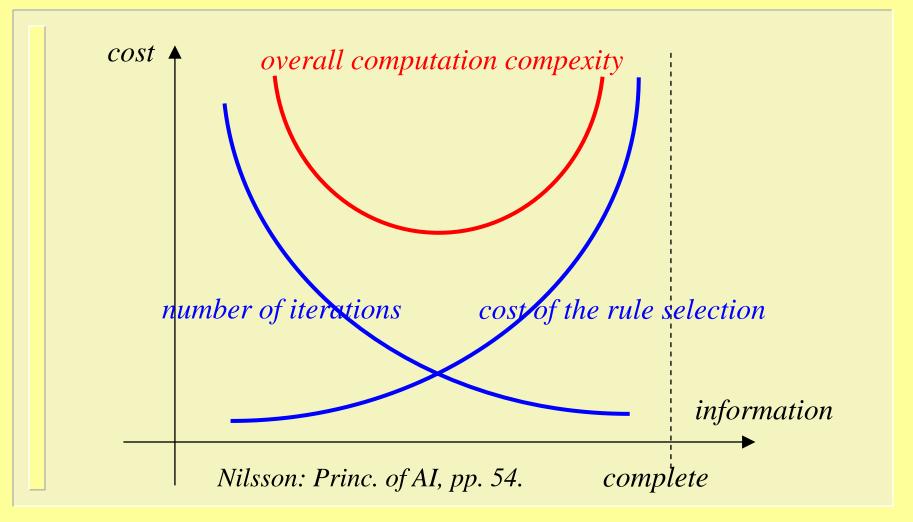
Artificial intelligence

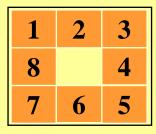
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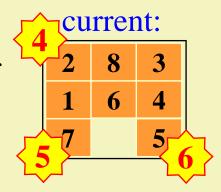
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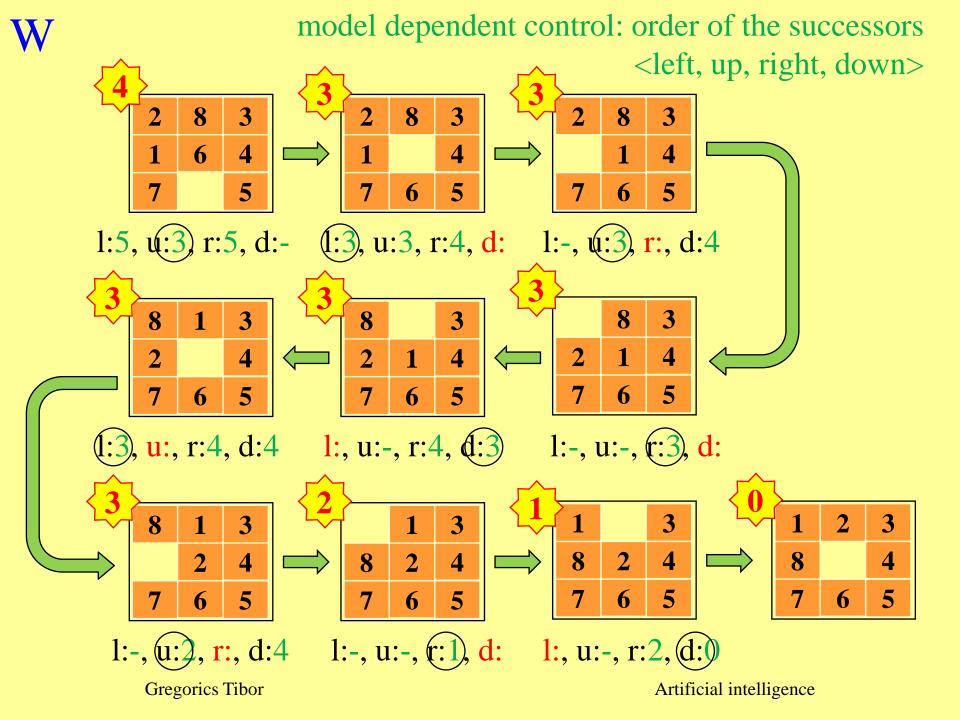


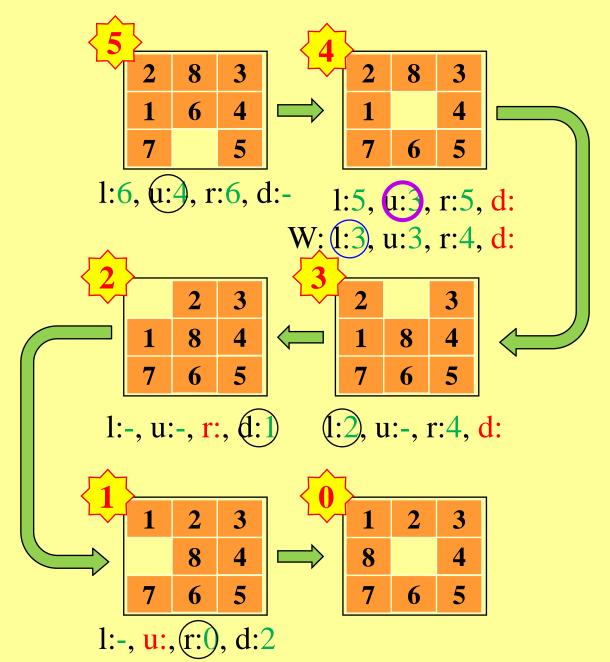
Heuristics for the 8-puzzle

- Misplaced (W): the number of the misplaced tiles
- Manhattan (P): the sum of the distances (number of horizontal and vertical moves) of the tiles from their final position



- □ Frame (F) or Edge: It uses penalty scores
 - + 1 score for each tile that is not followed by its corresponding successor according to the final state on the edges in the clockwise direction
 - + 2 scores for each corner that does not contain the corresponding tile according to the final state

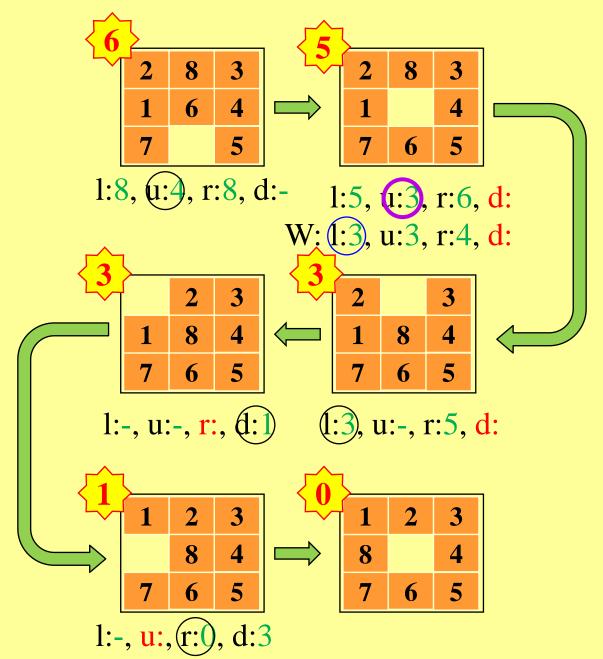




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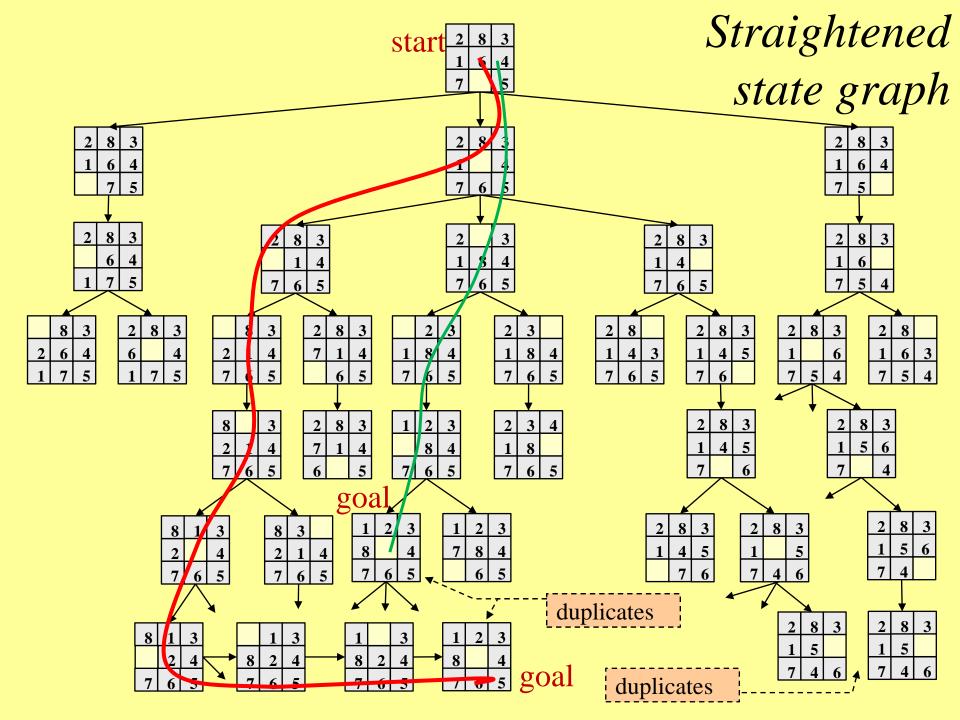
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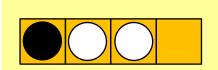
F



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Heuristics for Black&White puzzle

There are n black and m white stones and one empty place in a linear frame with n+m+1 length. A stone can be slid to the adjacent empty place or it can be jumped over another stone onto an empty place. Initially all black stones are on the left of the white stones and the empty is the last. Let's reverse the order of black and white stones!

- □ Inversion number of the permutation: *I(this)*how many swaps must be taken to achieve the goal permutation (where all white stones precede all black ones)
- Modified inversion number:

$$M(this) = 2*I(this) - (1 if this has)$$



part)

