Paweł Jaworski

Luxoft/Akademia Górniczo Hutnicza

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Outline

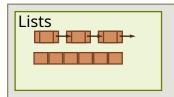
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 - Complexity calculation and nomenclature
- 3 List
 - ArrayList
 - Generics
 - LinkedList
- 4 Maps
 - HashMap
- 5 Excercises
 - Test Driven Development (TDD)
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- **6** Summary
 - What have we learned today?

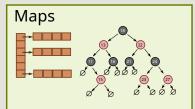
Introduction

- Java collections are sophisticated implementations of algorithms for storing data (see also Cormen's "Introduction to algorithms")
- All collections implement iteration
- Lists are implemented as sequential collections backed by arrays and linked lists
- Sets, besides iteration, are also allowing checking if the item is present.
- Maps are associative containers which allow quick access by object-key (any object, also other than integer).
- Trees are underlying some implementations of Maps and Sets
- Lists maintain item order while it is not guaranteed in Sets and Maps.



Hello





$$\sum_{i=1}^{n}$$

$$0<\left|\lim_{x\to\infty}\frac{f(x)}{g(x)}\right|<\infty$$

Algorithm analysis

Complexity calculation and nomenclature

The Big O, Ω , Θ notation

When there exists $n_0 > 0$ and c > 0 for which we can say that:

$$\forall n > n_0 \ f(n) \leq c \cdot g(n)$$

we say that f is big-O g and write f(x) = O(g(x))When there exists $n_0 > 0$ and c > 0 for which we can say that:

$$\forall n > n_0 \ f(n) \geq c \cdot g(n)$$

we say that f is big- Ω g and write $f(x) = \Omega(g(x))$

The Big Θ notation

When we can say that $f(x) = O(g(x)) \wedge f(x) = \Omega(g(x))$ we say that f is Big Θ g and write:

$$f(x) = \Theta(g(x))$$

Algorithmics Complexity calculation and nomenclature

Examples

- Given $g(x) = x^2$ and $f(x) = 3x^2 + 4$ we can say that f(x) = O(g(x))...
- Given $g(x) = x^3$ and $f(x) = 100x^2 + 4x^3$ we can say that f(x) = O(g(x))...
- Given $g(x) = 2^x$ and $f(x) = 2^x + x^{64}$ we can say that f(x) = O(g(x))...

We can also easily say that $x^2 = O(2^x)$, and $x^2 = \Omega(1)$ but it is not very interesting. This observation is very weak. We are rather interested in finding the closest matches.

Complexity calculation and nomenclature

Θ sufficient condition

The most interesting is finding the simple in form, but exact, match of the function. This match is symbolised by Θ .

$$f(x) = O(g(x)) \land f(x) = o(g(x)) \Longrightarrow f(x) = \Theta(g(x))$$

If $f(x) = \Theta(g(x))$, it means that f is grows asymptotically as fast as g.

Sufficient condition for $f(x) = \Theta(g(x))$ is:

$$0 < \lim_{x \to \infty} \left| \frac{f(x)}{g(x)} \right| < \infty$$

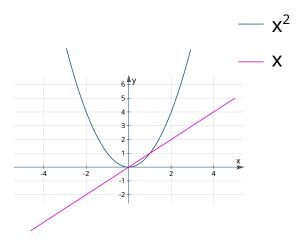
Some things that programmers usually know

We use given notation extensively to describe algorithm time of execution (and memory consumption). Hence for us (generally):

- x^2 is worse than x
- x is worse than $\log x$
- 2^x is worse than x^{16} and it's bad
- x! it's so much, we don't distinguish between x! and 2^x . Those are equally BAD.
- We often don't distinguish between logarithm and exponential bases

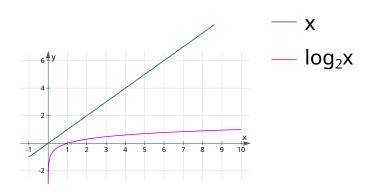
Complexity calculation and nomenclature

Examples



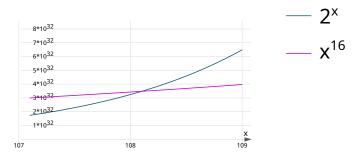
Complexity calculation and nomenclature

Examples



Complexity calculation and nomenclature

Examples



Complexity calculation and nomenclature

Worst case scenario

Programmers also consider worst case (pessimistic) scenarios of algorithms and their complexity. Some algorithms work very slow on some special cases of input data. E.g. **quicksort**, despite of being $O(n \cdot \log n)$ runs at n^2 time, when in every partitioning selected pivot divides data to lengths: 1 and rest. Having that in mind, we can select, for example, **heapsort**, which has worst case running time still $n \cdot \log n$

Need to know by heart

• All arrays and lists in Java are indexed from 0!!!

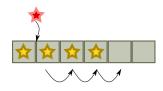
ArrayList

- Allocated as a one block in memory (more "array-ish" than "list-ish")
- Quick "please get me an element at position n" (further referred to as **get**): $\Theta(1)$
- Slow "please insert element at position n, moving all following elements to the right" (further referred to as **insert**): O(n)
- Slow "please delete element at position n, moving all following elements to the left" (further referred to as **delete**): O(n)

- Quick **append** a special-case of the insert at the last place, i.e. when for n equal number of elements: $\Theta(1)$, but only when the underlying array size is N>n+1
- When ArrayList is full, to perform insert we need to expand underlying array. We do it by increasing size by twice the current size.
- Is really the **append** operation $\Theta(1)$???

ArrayList pros and cons

• Insert at an arbitrary place costs n operations for n = s - i where s is number of items and i is the position we insert at.



Amortised cost. Amortised analysis

- We analyse amortised cost of operations amortised by their number.
- Amortised cost for given f(n) is F(n) that:

$$F(n) = \frac{T(n)}{n}$$

where

$$T(n) = \sum_{x=0}^{n} f(x)$$

Amortised cost. Amortised analysis

 For array initialised to 2, in the append operation we have cost:

$$1, 1, n_1 = 2, 1, 1, n_2 = 4, 1, 1, 1, 1, n_3 = 8$$

where n_x is n-th resize cost equals array's size at the moment of resize.

 If we use an accounting method to tell that every operation, we put additional 2 operations' time on a special account, for a later use, we can reuse that time at critical sections of resizing. Our account state is then:

Amortised cost. Amortised analysis

Operation	Account state	
+2	2	
+2	4	
-2	2	
+2	4	
+2	6	
-4	2	
+2	4	
+2	6	
+2	8	
+2	10	
-8	2	

Table 1: Amortised analysis using accounting method

Amortised cost. Amortised analysis

SVG Animation for the amortised cost accounting method

Amortised cost. Amortised analysis

• In this case we say that operation **append** on ArrayList is O(1) and keep in mind that sometimes it can stop our system for a very long time. So if we want to get overall computation time fit, we can allow us to expand a very large ArrayList, but when we are low-latency needers, we might need to search for a better solution.

```
public void addToList(List<? extends Number> lst) {
   Number item1 = lst.get(0);
   lst.add(3);
}
List<Float> floatList = ...;
addToList(floatList);
```

```
public void addToList(List<? extends Number> lst) {
  Number item1 = lst.get(0); // ok
  lst.add(3); // error
}
List<Float> floatList = ...;
addToList(floatList);
```

```
public void addToList(List<? super Integer>) {
   Integer i = lst.get(0);
   lst.add(4);
}
List<Number> numberList = ...;
addToList(numberList);
```

```
public void addToList(List<? super Integer>) {
   Integer i = lst.get(0); // error
   lst.add(4); // ok
}
List<Number> numberList = ...;
addToList(numberList);
```

```
// https://stackoverflow.com/questions/4343202
public class Collections {
   public static <T> void copy(List<? super T> dest,
   List<? extends T> src) {
      for (int i = 0; i < src.size(); i++)
            dest.set(i, src.get(i));
   }
}</pre>
```

Type erasure

```
private T data;
                                                                       private Object data;
private Node<T> next;
                                                                       private Node next;
public Node(T data, Node<T> next) {
                                                                              Node(Object data, Node next) {
    this.data - data;
                                                                            this.data - data;
    this.next = next:
                                                                           this.next = next:
public void setData([ data) {
                                                                              void setData(Object data) {
    this.data - data;
                                                                            this.data - data;
public T getData() {
                                                                       public Object getData() {
                                                                            return this.data;
public static void main(String[] args) {
                                                                              Main() {
    Node <Integer> node - new Node <>(10, null);
  Integer i = node.getData();
                                                                       public static void main(String[] args) {
    node.setData(20);
                                                                           Node node = new Node(10, (Node)null);
                                                                            Integer i = (Integer) node.getData();
                                                                            node.setData(20);
```

Figure 5: Type erasure

Type erasure

- Replace unbound type E with Object
- Add typecasting to all method calls
- Object has no information of type it was created with¹
- ClassCastException will be called if contraints are violated

¹except for class that inherits type-specified generic

Allocated as linked list of many objects

- Every inserted object needs a wrapper object, so the number of objects in memory are at least twice the number of elements in list.
- Fast **append**: $\Theta(1)$
- Fast insert but only when given a preceding node in the list.
- Fast delete but under the same conditions as insert
- Slow **get**: *O*(*n*)
- Does not need to grow append is not lagging from time to time.

LinkedList

LinkedList - pros

 LinkedList implements Deque which gives us nice stack and fifo methods: pollFirst, pollLast, peekFirst, peekLast LinkedList

LinkedList - cons

• Every item in LinkedList is of a class LinkedList.Item which has much overhead.

mark hash gcAge tLock tld	klassPtr ref to class	length length ptr	padding
4-8 bytes	4-8 bytes	4 bytes	up to mod arch

// remove all words containing letter a

Remove all strings containing letter a

LinkedList

Remove all strings containing letter a

Hello Algorithmics List Maps Excercises Summary LinkedList

ListIterator

How much do the object weight in Java

LinkedList

```
class A {}

class B extends A {}

class C {
  boolean a;
}
```

How much do the object weight in Java - compressed pointers

```
java -XX:+UseCompressedOops
sizeof A = 16
sizeof B = 16
sizeof C = 16
sizeof Boolean = 16
sizeof Char = 16
sizeof Integer = 16
sizeof Long = 24
sizeof class java.util.LinkedList\$Node = 24
```

```
java -XX:-UseCompressedOops

sizeof A = 16
sizeof B = 16
sizeof C = 24
sizeof Boolean = 24
sizeof Char = 24
sizeof Integer = 24
sizeof Long = 24
sizeof class java.util.LinkedList\$Node = 40
```

How much do the object weight in Java

```
public class C1 {
  boolean a;
  int b;
} // size 24
public class C2 {
  boolean a;
  int b;
  int c;
} // size 24
public class C3 {
  boolean a;
  int b;
  int c;
} // size 32
```

- Fast finding element by the key (further referred to as: lookup): O(1).²
- Fast putting a key-value pair (further referred to as: **insert**): (O(1), pessimitically n = size, when map needs to grow.
- Fast remove: O(1) (HashMap does not shrink).
- Values with the same hash stored in LinkedList, collisions may occur.

 $^{^2}$ When time is longer, in properly setup map (i.e. number of buckets > size), it means that collisions occur. This can be the sign of incorrect hash function.

HashMap

 $x.equals(y) \Longrightarrow x.hashCode() == y.hashCode()$

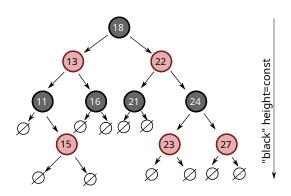
 $x.hashCode() == y.hashCode() \implies x.equals(y)$

TreeMap

- Implemented by Red-Black tree.
- Keys are sorted.
- Quite good lookup: $O(\log n)$
- Quite good insert: $O(\log n)$
- Quite good delete: $O(\log n)$
- Memory consumption: O(n).

Red-black tree

For each path count of black nodes ("black length") is constant



Algorithms visualised

https://www.cs.usfca.edu/~galles/visualization/java/visualization.html

How to write tests

- Create test that checks constraint on empty or broken code
- Run the test to confirm that it fails (if it passes, the checks are incorrect)
- During the test compilation it might be needed to create more empty methods - this is the Development part in TDD
- Fix the code and fill the empty methods
- Tests should pass

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- in src/main/java/t1 we have code that we need to fix
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- Run the efficiency test PerformanceTestsForT1 all should

- see src/main/java/t2 and src/test/java/t2
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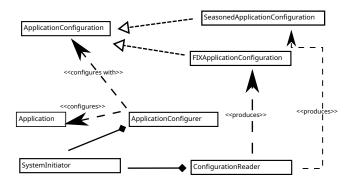
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- Next focus on second_excercise_testPLNtoGBP

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- why there is no such currency conversion, providing that we have added it in the map in initStatic method?
- Next focus on second_excercise_testPLNtoGBP
- Why the test is failing? What is the printed result?

- see src/main/java/t3 and src/test/java/t3
- List must not grow, must throw proper exceptions.
- List must contain the java's Array as as storage for the items
- How to initialize the storing array for any T? Why new T[] is not working?

- see src/main/java/t4 and src/test/java/t4
- Why the assertNull does not work?

- see src/main/java/t5 and src/test/java/t5
- Uncomment code in the test
- Why the code does not compile? How can we fix it?



- see src/main/java/t6 and src/test/java/t6
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- testMemEfficiencyMaster try to achieve 12 MB by writing your own suited int-based collection.

What have we learned today?

Summary

Test Driven Development

Always start with test

Test Driven Development

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- Test must fail

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- Make the test passing by fixing the code

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Complexity as a gift from Java

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Complexity as a gift from Java

- Big O notation, small o notation, theta θ notation
- Java's sophisticated collections give us access to best algorithm implementation
- Even though, using incorrect implementation, we can break things up
- Even though, sometimes we may need to have our own implementation (read: use libraries)

Generics

- One code for many usages
- ? extends and ? super
- Type erasure will clear typed info

What have we learned today?					
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Hello	Algorithmics	List	Maps	Excercises	Summary

Thank you