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Summary of Theory of Superconductivity

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Background

The phenomenon of superconductivity was first discovered by Onnes¹ in 1911. At that time and for many years after, it was thought of simply as the vanishing of all electrical resistance below the transition temperature.

The next major discovery regarding superconductivity was the discovery of the Meissner Effect² in 1933. It was shown that a superconductor is a perfect diamagnet; the Magnetic flux is excluded from all but a thin penetration region near the surface of the material.

London and London³ expanded on it by proposing a phenomenological theory of the electromagnetic properties of superconductors in which the diamagnetic aspects assumed to be basic in 1935.

F. London⁴ in 1935, suggest a *quantum-theoretic approach to a theory in which it was *assumed that there is somehow a coherence or rigidity in the superconducting state such that the wave functions are not modified very much when a magnetic field is applied.

Pippard⁵ in 1953 proposed a nonlocal modification of the aforementioned London equations in which a coherence distance, ξ_0 , is introduced. **The modification was based on experiments on penetration phenomena.**

One of the current authors, J. Bardeen⁶ pointed out in 1955, that an energy-gap model would most likely lead to the Pippard theory.

The preceding theory for metals, the **Sommerfeld-Bloch theory** states,

- i In the first approximation one may neglect correlations between the positions of the electrons and assume that each electron moves independently in self consistent field determined by the conduction electrons and ions.
- ii Wave functions of the metal as a whole are designated by occupation of Bloch individual-particle states of energy $\epsilon(k)$ defined by wave vector k and spin σ
- iii In the ground state all levels with energies below the Fermi energy, \mathcal{E}_F are occupied and above are unoccupied.

One of the key motivators of the paper and BCS theory is pointed out in the article as the deficiencies of the **Sommerfield-Bloch Individual Particle Model**.

They can be characterized as:

- i Although a fairly good description of normal metals, the model fails to account of superconductivity
- ii The correlations between electrons brought about by coulomb forces and interactions between electrons and lattice vibrations (phonos) are neglected.

Requirements for a Theory of Superconductivity

According to the paper, the "main facts which a theory of Superconductivity" must explain" are:

1. A second order phase transition at the Critical Temperature, T_c
2. An electronic specific heat varying as $\exp(\frac{-T_0}{T})$ and other evidence of energy gap for individual particle-like excitations.
3. The Meissner-Oschenfeld Effect
4. Effects associated with infinite conductivity
5. The dependence of T_c on isotropic mass. $T_c\sqrt{M} = Const.$

BCS Theory

- One of the main criterion for a superconducting phase is that for low energy transitions ($\Delta e < hw$), the electron-phonon interaction (which is attractive) dominates the repulsive coulomb interaction. This type of attractive of interaction can give rise to a cooperative many-particle state.
- The most important contribution is given by short wavelength phonons.
- The Meissner effect is intimately related to the the existence of an energy gap.
- Superconducting properties are not dependent on the band structure but rather the gross features.
- In the ground state, the interaction that produces the energy difference between normal and superconducting phases arise from the exchange of phonons and the screened Coulomb repulsion between electrons.
- Other interactions are essentially the same between normal and superconducting phases.
- Phonons are decoupled from the electrons by a renormalization procedure and the frequencies are though to be unaltered between phase transistitions. (Phonons are the same from temperature changes?)

Notes

Transition Temperature: Critical temperature at which the electrical resistivity of the metal drops to zero. The change is sudden and complete. Almost akin to phase transition of matter.

Diamagnetism: Repulsion to applied magnetic field. Quantum mechanical effect that induces magnetic fields in the material opposing magnetic attraction.

Phenomenological Theory: Theory based on the experimental data

Coherence or Rigidity: (Unsure in context to Wavefunction)

Superconducting State: Does the wavefunction change when there is a phase transition?

Coherence Distance: Spatial changes in quantities, especially relating to phase transitions have a lower bound, ξ_0 .

First Approximation: Linear approximation terms. Shows the largest contribution to the model described.

Conduction Electron: Non localized/ free electrons

Bloch Individual Particle State:

Electron Correlation: Interaction between electrons. Coherence energy is the energy related to the coulomb interaction of all other electrons.

Lattice Vibrations (Phonons): Vibrational energy associated with a lattice. Quasi-particle used to model mathematically.

Energy Gap:

Decoupling:

Renormalization:

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