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## Summary of Theory of Superconductivity

#### **Article Description**

(J. Bardeen, PR V.108 N.5)

#### Background

The phenomenon of superconductivity was first discovered by Onnes<sup>1</sup> in 1911. At that time and for many years after, it was though of simply as the vanishing of all electrical resistance below the <u>transition</u> temperature.

The next major discovery regarding superconductivity was the discovery of the Meissner Effect<sup>2</sup> in 1933. It was shown that a superconductor is a perfect diamagnet; the Magnetic flux is excluded from all but a thin penetration region near the surface of the material.

London and London <sup>3</sup> expanded on it by proposing a <u>phenomenological</u> theory of the electromagnetic properties of super conductors in which the diamagnetic aspects assumed to be basic in 1935.

F. London<sup>4</sup> in 1935, suggest a \*quantum-theoretic approach to a theory in which it was \*assumed that there is somehow a <u>coherence or rigidity</u> in the <u>superconducting state</u> such that the wave functions are not modified very much when a magnetic field is applied.

Pippard<sup>5</sup> in 1953 proposed a nonlocal modification of the aforementioned London equations in which a coherence distance,  $\xi_0$ , is introduced. The modification was based on experiments on penetration phenomena.

One of the current authors, J. Bardeen <sup>6</sup> pointed out in 1955, that an <u>energy-gap model</u> would most likely lead to the Pippard theory.

The preceding theory for metals, the **Sommerfiled-Bloch theory** states,

- i In the <u>first approximation</u> one may neglect correlations between the positions of the electrons and assume that each electron moves independently in self consistent field determined by the <u>conduction electrons</u> and ions.
- ii Wave functions of the metal as a whole are designated by occupation of Bloch individual-particle states of energy  $\epsilon(k)$  defined by wave vector k and spin  $\sigma$
- iii In the ground state all levels with energies below the Fermi energy,  $\mathscr{E}_F$  are occupied and above are unoccupied.

One of the key motivators of the paper and BCS theory is pointed out in the article as the deficiencies of the Sommerfield-Bloch Individual Particle Model.

They can be characterized as:

- i Although a fairly good description of normal metals, the model fails to account of superconductivity
- ii The <u>correlations</u> between electrons brought about by coulomb forces and interactions between electrons and lattice vibrations (phonos) are neglected.

#### Notes

Transition Temperature:

Diamagnet:

Phenomenological:

Coherence or Rigidity:

Superconducting State:

Coherence Distance:

First Approximation:

Conduction Electron:

Bloch Individual Particle State:

Electron Correlation:

Lattice Vibrations (Phonons):

### References

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