## Input data

• nurses 
$$n \in \{1, \dots, N\}$$
, days  $d \in \{1, \dots, D\}$ , shifts  $s \in \{1, \dots, S\}$ 

• week numbers 
$$w \in \{0, \dots, W\}, W = \lfloor D/7 \rfloor - 1$$

• nurses demand per day and shift - 
$$demand_{d,s} \in \mathbb{N}$$

• workhours lower and upper limit per nurse - 
$$maxhours_n \in \mathbb{N}$$

• vacation requests - 
$$VR \subset N \times D$$

• preferred companions - 
$$PC \subset N \times N$$

$$\bullet$$
 unpreferred companions -  $UC \subset N \times N$ 

• preferred slots - 
$$PS \subset N \times D \times S$$

$$\bullet$$
 unpreferred slots -  $US \subset N \times D \times S$ 

Optimization variables: schedule for each nurse, day and shift

$$schedule_{n,d,s} \in \{0,1\}$$

and interactions of nurses (weekends 2)

$$interaction_{n,n',d,s} \in \{0,1\}$$

and "worked in given weekend" indicators

$$weekend_{n,w} \in \{0,1\}$$

and "fraction of contract fulfilled" proportions, as well as lower and upper bound for those

 $\alpha_{min}, \ \alpha_{max}$ 

## Reward function

$$\begin{split} & \lambda_{PC} \cdot \sum_{(n,n') \in PC} \sum_{d,s} interaction_{n,n',d,s} \\ & - \lambda_{UC} \cdot \sum_{(n,n') \in UC} \sum_{d,s} interaction_{n,n',d,s} \\ & + \lambda_{PS} \cdot \sum_{(n,d,s) \in PS} schedule_{n,d,s} \\ & - \lambda_{US} \cdot \sum_{(n,d,s) \in US} schedule_{n,d,s} \end{split}$$

 $-\lambda_{\text{WHS}}(\alpha_{max} - \alpha_{min})$  (tight alpha gap iff work distributed proportionately to wokrhours specified)

## Constraints

$$\forall_{d,s} \sum_{n} schedule_{n,d,s} = demand_{d,s} \quad \text{(demand is met)}$$

$$\forall_{n} \frac{24}{S} \sum_{d,s} schedule_{n,d,s} \leq maxhours_{n} \quad \text{(workhours limits are not exceeded)}$$

$$\forall_{n,d} \sum_{s} schedule_{n,d,s} \leq 1 \quad \text{(max 1 shift per day)}$$

$$\forall_{n,w} \sum_{d=7w+1}^{\min(7(w+1),D)} schedule_{n,d,S} \leq 6 \quad \text{(max 6 night shifts per week)}$$

$$\forall_{n,d} schedule_{n,d,S} + schedule_{n,d+1,1} \leq 1 \quad \text{(can't continue past midnight)}$$

$$\forall_{(n,d) \in VR} \forall_{s} schedule_{n,d,s} = 0 \quad \text{(vacations are respected)}$$

$$\forall_{n,n',d,s} interaction_{n,n',d,s} \leq schedule_{n,d,s} \quad \text{(interactions 1)}$$

$$\forall_{n,n',d,s} interaction_{n,n',d,s} \leq schedule_{n,d,s} \quad \text{(interactions 2)}$$

$$\forall_{n,n',d,s} interaction_{n,n',d,s} \geq schedule_{n,d,s} + schedule_{n',d,s} - 1 \quad \text{(interactions 3)}$$

$$\forall_{n,w} weekend_{n,w} \geq \frac{1}{S} \sum_{s} (schedule_{n,7w+6,s} + schedule_{n,7w+7,s}) \quad \text{(weekends 1)}$$

$$\forall_{n,w} weekend_{n,w} \leq \sum_{s} (schedule_{n,7w+6,s} + schedule_{n,7w+7,s}) \quad \text{(weekends 2)}$$

$$\forall_{n,w} weekend_{n,w} \leq \frac{24}{S} \sum_{d,s} schedule_{n,d,s} \\ workhours_{n} \leq \alpha_{max} \quad \text{(alphas with bounds)}$$