Input data

- nurses $n \in \{1, \ldots, N\}$, days $d \in \{1, \ldots, D\}$, shifts $s \in \{1, \ldots, S\}$
- nurses demand per day and shift - $demand_{d,s} \in \mathbb{N}$
- workhours lower and upper limit per nurse - $minhours_n \in \mathbb{N}$, $maxhours_n \in \mathbb{N}$
- vacation requests - $VR \subset N \times D$
- preferred companions - $PC \subset N \times N$
- unpreferred companions - $UC \subset N \times N$
- preferred slots - $PS \subset N \times D \times S$
- unpreferred slots - $US \subset N \times D \times S$

Optimization variables: schedule for each nurse, day and shift

$$schedule_{n,d,s} \in \{0, 1\}$$

and interactions of nurses

$$interaction_{n,n',d,s} \in \{0, 1\}$$

Reward function

$$\begin{aligned} &\lambda_{PC} \cdot \sum_{(n,n') \in PC} \sum_{d,s} interaction_{n,n',d,s} \\ -&\lambda_{UC} \cdot \sum_{(n,n') \in UC} \sum_{d,s} interaction_{n,n',d,s} \\ +&\lambda_{PS} \cdot \sum_{(n,d,s) \in PS} schedule_{n,d,s} \\ -&\lambda_{US} \cdot \sum_{(n,d,s) \in US} schedule_{n,d,s} \end{aligned}$$

Constraints

$$\forall_{d,s} \sum_n schedule_{n,d,s} = demand_{d,s} \quad \text{(demand is met)}$$

$$\forall_n minhours_n \leq \frac{24}{S} \sum_{d,s} schedule_{n,d,s} \leq maxhours_n \quad \text{(workhours limits are not exceeded)}$$

$$\forall_{n,d} \sum_s schedule_{n,d,s} \leq 1 \quad \text{(max 1 shift per day)}$$

$$\forall_{n,d} schedule_{n,d,S} + schedule_{n,d+1,1} \leq 1 \quad \text{(can't continue past midnight)}$$

$$\forall_{(n,d) \in VR} \forall_s schedule_{n,d,s} = 0 \quad \text{(vacations are respected)}$$

$$\forall_{n,n',d,s} interaction_{n,n',d,s} \leq schedule_{n,d,s} \quad \text{(interactions 1)}$$

$$\forall_{n,n',d,s} interaction_{n,n',d,s} \leq schedule_{n',d,s} \quad \text{(interactions 2)}$$

$$\forall_{n,n',d,s} interaction_{n,n',d,s} \geq schedule_{n,d,s} + schedule_{n',d,s} - 1 \quad \text{(interactions 3)}$$