

Exercise 3.1 MLE for the Bernoulli/ binomial model

$$\frac{d}{d\theta}p(D|\theta) = \frac{d}{d\theta}(\theta^{N_1}(1-\theta)^{N_0}) \quad (1)$$

$$= N_1\theta^{N_1-1}(1-\theta)^{N_0} - N_0\theta^{N_1}(1-\theta)^{N_0-1} \quad (2)$$

$$= \theta^{N_1-1}(1-\theta)^{N_0-1}(N_1(1-\theta) - N_0\theta) \quad (3)$$

$$= \theta^{N_1-1}(1-\theta)^{N_0-1}(N_1 - N\theta) \quad (4)$$

$$\therefore \theta_{\text{MLE}} = \frac{N_1}{N} \quad (5)$$