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ACM/ICPC

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Splay:

```
#include <cstdio>
#include <cstring>
#include <cstdlib>
#include <iostream>
#define N 6000000
#define INF 999999999
using namespace std;
long long root, n, m, flag2[N], list[N], fa[N], l[N], r[N], size[N], f[N][3], g[N], flag[N], sum[N],
a[N];
char s[20];
long long read(){
	long long p=0, q=1;
	char ch=getchar();
	while (ch<'0' || ch>'9'){
		if (ch=='-') q=-1;
		ch=getchar();
	}
	while (ch>='0' && ch<='9') p=p*10+ch-'0', ch=getchar();
	return p*q;
}
void update(long long t){
	if (l[t]) fa[l[t]]=t;
	if (r[t]) fa[r[t]]=t;
	sum[t]=sum[l[t]]+sum[r[t]]+a[t];
	size[t]=size[l[t]]+size[r[t]]+1;
	f[t][0]=max(f[l[t]][0],sum[l[t]]+f[r[t]][0]+a[t]);
	f[t][1]=max(f[r[t]][1],sum[r[t]]+f[l[t]][1]+a[t]);
	f[t][2]=f[l[t]][1]+f[r[t]][0]+a[t];
	f[t][2]=max(f[t][2],max(f[l[t]][2],f[r[t]][2]));
}
void pushdown(long long t){
	if (flag[t]){
		if (l[t]) flag[l[t]]^=1;
		if (r[t]) flag[r[t]]^=1;
		swap(l[t],r[t]);
		swap(f[l[t]][0],f[l[t]][1]);
		swap(f[r[t]][0],f[r[t]][1]);
		flag[t]=0;
	}
	if (flag2[t]){
		if (l[t]){
			sum[l[t]]=g[t]*size[l[t]];
			if (g[t]>0)
```

```
                f[l[t]][0]=f[l[t]][1]=f[l[t]][2]=sum[l[t]];
            else
                f[l[t]][0]=f[l[t]][1]=0, f[l[t]][2]=g[t];
            g[l[t]]=a[l[t]]=g[t];
            flag2[l[t]]=1;
        }
        if (r[t]){
            sum[r[t]]=g[t]*size[r[t]];
            if (g[t]>0)
                f[r[t]][0]=f[r[t]][1]=f[r[t]][2]=sum[r[t]];
            else
                f[r[t]][0]=f[r[t]][1]=0, f[r[t]][2]=g[t];
            g[r[t]]=a[r[t]]=g[t];
            flag2[r[t]]=1;
        }
        flag2[t]=g[t]=0;
    }
}
long long build(long long le, long long ri){
    if (le>ri) return 0;
    long long mid=le+ri>>1;
    l[mid]=build(le,mid-1);
    r[mid]=build(mid+1,ri);
    update(mid);
    return mid;
}
void insert(long long &t, long long k, long long p){
    if (!t){
        if (!size[t=p]){
            size[t]=1;
            f[t][0]=f[t][1]=a[t]>0?a[t]:0;
            f[t][2]=sum[t]=a[t];
        }
        return;
    }
    pushdown(t);
    if (size[l[t]]+1<=k) insert(r[t],k-size[l[t]]-1,p);
    else insert(l[t],k,p);
    update(t);
}
void zig(long long t){
    long long f1=fa[t], f2=fa[f1];
    if (f2)
        if (l[f2]==f1) l[f2]=t;else r[f2]=t;
```

```
    fa[t]=f2;
    l[f1]=r[t];
    r[t]=f1;
    update(f1);
    update(t);
}
void zag(long long t){
    long long f1=fa[t], f2=fa[f1];
    if (f2)
        if (l[f2]==f1) l[f2]=t;else r[f2]=t;
    fa[t]=f2;
    r[f1]=l[t];
    l[t]=f1;
    update(f1);
    update(t);
}
void splay(long long t){
    long long ri=1;
    list[1]=t;
    for (long long i=1;fa[list[i]];i++) list[++ri]=fa[list[i]];
    for (long long i=ri;i;i--) pushdown(list[i]);
    long long f1=fa[t], f2=fa[f1];
    while (f2){
        if (l[f2]==f1)
            if (l[f1]==t) zig(f1), zig(t);
            else zag(t), zig(t);
        else
            if (r[f1]==t) zag(f1), zag(t);
            else zig(t), zag(t);
        f1=fa[t];f2=fa[f1];
    }
    if (f1)
        if (l[f1]==t) zig(t);else zag(t);
    root=t;
}
long long find(long long t, long long k){
    pushdown(t);
    while (size[l[t]]+1!=k){
        if (size[l[t]]+1<k)
            k-=size[l[t]]+1, t=r[t];
        else
            t=l[t];
        pushdown(t);
    }
```

```
    return t;
}
void del(long long x, long long y){
    splay(x);
    fa[r[x]]=0;
    splay(y);
    l[r[root=x]=y]=0;
    update(y);
    update(x);
}
void modify(long long x, long long y, long long z){
    splay(x);
    fa[r[x]]=0;
    splay(y);
    r[root=x]=y;
    flag2[l[y]]=1;
    g[l[y]]=a[l[y]]=z;
    sum[l[y]]=size[l[y]]*z;
    if (z>0)
        f[l[y]][0]=f[l[y]][1]=f[l[y]][2]=sum[l[y]];
    else
        f[l[y]][0]=f[l[y]][1]=0, f[l[y]][2]=z;
    update(y);
    update(x);
}
void reverse(long long x, long long y){
    splay(x);
    fa[r[x]]=0;
    splay(y);
    fa[r[root=x]=y]=x;
    flag[l[y]]^=1;
    swap(f[l[y]][0],f[l[y]][1]);
    update(y);
    update(x);
}
void calc(long long x, long long y){
    splay(x);
    fa[r[x]]=0;
    splay(y);
    fa[r[root=x]=y]=x;
    printf("%d\n", sum[l[y]]);
    update(y);
    update(x);
}
```

```
void print(long long t){
	if (!t) return;
	pushdown(t);
	print(l[t]);
	printf("%d ", a[t]);
	print(r[t]);
}
int main(){
	freopen("sequence4.in","r",stdin);
	freopen("1.ans","w",stdout);
	n=read();m=read();
	for (long long i=1;i<=n;i++) a[i]=read();
	f[0][2]=-INF;
	root=build(1,n);
	a[N-3]=a[N-2]=-INF;
	insert(root,0,N-3);
	insert(root,n+1,N-2);
	for (long long i=1;i<=m;i++){
		scanf("%s", s);
		if (s[0]=='I'){
			long long pos=read(), tot=read(), n2=n+tot, root2;
			if (!tot) continue;
			for (long long i=n+1;i<=n2;i++) a[i]=read();
			root2=build(n+1,n2);
			insert(root,pos+1,root2);
			splay(root2);
			n=n2;
		}
		if (s[0]=='D'){
			long long x=read(), y=read()+x+1;
			if (x+1==y) continue;
			x=find(root,x);
			y=find(root,y);
			del(x,y);
		}
		if (s[2]=='K'){
			long long x=read(), y=read()+x+1, z=read();
			if (x+1==y) continue;
			x=find(root,x);
			y=find(root,y);
			modify(x,y,z);
		}
		if (s[0]=='R'){
			long long x=read(), y=read()+x+1;
```

```
            if (x+1==y) continue;
            x=find(root,x);
            y=find(root,y);
            reverse(x,y);
        }
        if (s[0]=='G'){
            long long x=read(), y=read()+x+1;
            x=find(root,x);
            y=find(root,y);
            calc(x,y);
        }
        if (s[2]=='X'){
            printf("%d\n", f[root][2]);
        }
    }
    return 0;
}
```

LCT:

```
#include <cstdio>
#include <cstring>
#include <cstdlib>
#include <iostream>
#define mo 51061
#define N 200000
typedef unsigned int ll;
using namespace std;
int n, q, size[N], l[N], r[N], fa[N], rev[N], list[N];
ll sum[N], f[N], at[N], mt[N];
int read(){
    int p=0;
    char ch=getchar();
    while (ch<'0' || ch>'9') ch=getchar();
    while (ch>='0' && ch<='9') p=p*10+ch-'0', ch=getchar();
    return p;
}
bool isroot(int t){
    return (l[fa[t]]!=t) && (r[fa[t]]!=t);
}
void calc(int u, int m, int a){
    if (!u) return;
    f[u]=(f[u]*m+a)%mo;
    sum[u]=(sum[u]*m+a*size[u])%mo;
    at[u]=(at[u]*m+a)%mo;
```

```
        mt[u]=(mt[u]*m)%mo;
}
void update(int t){
        if (l[t]) fa[l[t]]=t;
        if (r[t]) fa[r[t]]=t;
        sum[t]=(f[t]+sum[l[t]]+sum[r[t]])%mo;
        size[t]=1+size[l[t]]+size[r[t]];
}
void pushdown(int t){
        if (rev[t]){
                swap(l[t],r[t]);
                if (l[t]) rev[l[t]]^=1;
                if (r[t]) rev[r[t]]^=1;
                rev[t]=0;
        }
        int ta=at[t], tm=mt[t];
        if (ta || tm!=1){
                calc(l[t],tm,ta);
                calc(r[t],tm,ta);
        }
        at[t]=0;mt[t]=1;
}
void zig(int t){
        int f1=fa[t], f2=fa[f1];
        if (!isroot(f1))
                if (l[f2]==f1) l[f2]=t;else r[f2]=t;
        fa[t]=f2;
        l[f1]=r[t];
        r[t]=f1;
        update(f1);
        update(t);
}
void zag(int t){
        int f1=fa[t], f2=fa[f1];
        if (!isroot(f1))
                if (l[f2]==f1) l[f2]=t;else r[f2]=t;
        fa[t]=f2;
        r[f1]=l[t];
        l[t]=f1;
        update(f1);
        update(t);
}
void splay(int t){
        int ri=1;
```

```
        list[1]=t;
        for (int i=1;!isroot(list[i]);i++) list[++ri]=fa[list[i]];
        for (int i=ri;i;i--){
            pushdown(list[i]);
        }
        int f1=fa[t], f2=fa[f1];
        while (!isroot(t) && !isroot(f1)){
            if (l[f2]==f1)
                if (l[f1]==t) zig(f1), zig(t);
                else zag(t), zig(t);
            else
                if (r[f1]==t) zag(f1), zag(t);
                else zig(t), zag(t);
            f1=fa[t];f2=fa[f1];
        }
        if (!isroot(t))
            if (l[f1]==t) zig(t);else zag(t);
}
void access(int u){
        for (int v=0;u;v=u,u=fa[u]){
            splay(u);
            r[u]=v;
            update(u);
        }
}
void makeroot(int u){
        access(u);
        splay(u);
        rev[u]^=1;
}
void split(int u, int v){
        makeroot(u);
        access(v);
        splay(v);
}
void link(int u, int v){
        makeroot(u);
        fa[u]=v;
}
void cut(int u, int v){
        split(u,v);
        fa[u]=l[v]=0;
        update(v);
}
```

```
void modify(int u, int v, int m, int a){
	split(u,v);
	calc(v,m,a);
}
int main(){
	n=read();q=read();
	for (int i=1;i<=n;i++) size[i]=f[i]=sum[i]=mt[i]=1;
	for (int i=1;i<n;i++){
		int u=read(), v=read();
		link(u,v);
	}
	for (int i=1;i<=q;i++){
		char s[2];
		scanf("%s", s);
		int u=read(), v=read();
		if (s[0]=='+'){
			int c=read();
			modify(u,v,1,c);
		}
		if (s[0]=='-'){
			cut(u,v);
			u=read();v=read();
			link(u,v);
		}
		if (s[0]=='*'){
			int c=read();
			modify(u,v,c,0);
		}
		if (s[0]=='/'){
			split(u,v);
			printf("%d\n", sum[v]);
		}
	}
	return 0;
}
```

Suffix array:

```
#include <cstdio>
#include <cstring>
#include <cstdlib>
#include <iostream>
using namespace std;
```

```
int ls, a[3000], wv[3000], sa[3000], rk[3000], y[3000], r[3000], h[3000];
char s[3000];
int main(){
	while (scanf("%s", s)){
		ls=strlen(s);
		int m=max(ls,26);
		for (int i=0;i<2*ls;i++) rk[i]=-1;
		for (int i=0;i<m;i++) wv[i]=0;
		for (int i=0;i<ls;i++) a[i]=s[i]-'a';
		for (int i=0;i<ls;i++) wv[a[i]]++;
		for (int i=1;i<m;i++) wv[i]+=wv[i-1];
		for (int i=0;i<ls;i++) sa[--wv[a[i]]]=i;
		rk[sa[0]]=0;
		for (int i=1;i<ls;i++) rk[sa[i]]=rk[sa[i-1]]+(a[sa[i]]!=a[sa[i-1]]);
		for (int j=1;j<ls;j*=2){
			int p=0;
			for (int i=ls-j;i<ls;i++) y[++p]=i;
			for (int i=0;i<ls;i++)
				if (sa[i]>=j) y[++p]=sa[i]-j;
			for (int i=0;i<m;i++)	wv[i]=0;
			for (int i=0;i<ls;i++) wv[rk[i]]++;
			for (int i=1;i<m;i++) wv[i]+=wv[i-1];
			for (int i=ls;i;i--)	sa[--wv[rk[y[i]]]]=y[i];
			r[sa[0]]=0;
			for (int i=1;i<ls;i++)
				r[sa[i]]=r[sa[i-1]]+(rk[sa[i-1]]!=rk[sa[i]] || rk[j+sa[i-1]]!=rk[j+sa[i]]);
			for (int i=0;i<ls;i++)
				rk[i]=r[i];
		}
		int j=0;
		for (int i=0;i<ls;i++)
		if (rk[i]<ls-1){
			for (;j+sa[rk[i]+1]<ls && j+i<ls && a[j+sa[rk[i]+1]]==a[i+j];++j);
			h[rk[i]]=j?j--:0;
		}
		for (int i=0;i<ls-1;i++) cout<<h[i]<<endl;
	}
	return 0;
}
```

Miller-Rabin:

```
#include <iostream>
```

```
#include <cstdio>
#include <algorithm>
#include <cmath>
#include <cstring>
#include <map>
using namespace std;

const int times = 20;
int number = 0;

map<long long, int>m;
long long Random( long long n )                 //生成[ 0 , n ]的随机数
{
    return ((double)rand( ) / RAND_MAX*n + 0.5);
}

long long q_mul( long long a, long long b, long long mod ) //快速计算  (a*b) % mod
{
    long long ans = 0;
    while(b)
    {
        if(b & 1)
        {
            b--;
            ans =(ans+ a)%mod;
        }
        b /= 2;
        a = (a + a) % mod;

    }
    return ans;
}

long long q_pow( long long a, long long b, long long mod ) //快速计算  (a^b) % mod
{
    long long ans = 1;
    while(b)
    {
        if(b & 1)
        {
            ans = q_mul( ans, a, mod );
        }
        b /= 2;
        a = q_mul( a, a, mod );
```

```
    }
    return ans;
}

bool witness( long long a, long long n )//miller_rabin 算法的精华
{//用检验算子 a 来检验 n 是不是素数
    long long tem = n - 1;
    int j = 0;
    while(tem % 2 == 0)
    {
        tem /= 2;
        j++;
    }
    //将 n-1 拆分为 a^r * s

    long long x = q_pow( a, tem, n ); //得到 a^r mod n
    if(x == 1 || x == n - 1) return true;    //余数为 1 则为素数
    while(j--) //否则试验条件 2 看是否有满足的 j
    {
        x = q_mul( x, x, n );
        if(x == n - 1) return true;
    }
    return false;
}

bool miller_rabin( long long n )   //检验 n 是否是素数
{

    if(n == 2)
        return true;
    if(n < 2 || n % 2 == 0)
        return false;                    //如果是 2 则是素数，如果<2 或者是>2 的偶数则不
是素数

    for(int i = 1; i <= times; i++)   //做 times 次随机检验
    {
        long long a = Random( n - 2 ) + 1; //得到随机检验算子 a
        if(!witness( a, n ))                    //用 a 检验 n 是否是素数
            return false;
    }
    return true;
}
```

```
int main( )
{
	long long tar;
	cout<<rand()<<endl;
	cout<<RAND_MAX<<endl;
	cout<<Random( 100 - 2 )<<endl;
	cout<<Random( 100 - 2 )<<endl;
	while(cin >> tar)
	{
		if(miller_rabin( tar )) //检验 tar 是不是素数
			cout << "Yes, Prime!" << endl;
		else
			cout << "No, not prime.." << endl;
	}
	return 0;
}
```

树链剖分:

```
#include <cstdio>
#include <cstring>
#include <cstdlib>
#include <iostream>
#include <algorithm>
#define N 31000
#define M 100000
#define INF 999999
typedef long long ll;
using namespace std;
int n, cnt, son[N], sum[N*4], dep[N], fa[N], f[N*4], nex[M], nu[M], dfn[N], pre[N], top[N];
char s[10];
int read(){
	int p=0, q=1;
	char ch=getchar();
	while (ch<'0' || ch>'9'){
		if (ch=='-') q=-1;
		ch=getchar();
	}
	while (ch>='0' && ch<='9') p=p*10+ch-'0', ch=getchar();
	return p*q;
}
void add(int u, int v){
	nex[++cnt]=nex[u];nex[u]=cnt;nu[cnt]=v;
}
void dfs1(int u, int father){
```

```
    son[u]=1;
    int p=0;
    for (int j=nex[u];j;j=nex[j]){
        int v=nu[j];
        if (v==father) continue;
        fa[v]=u;
        dep[v]=dep[u]+1;
        dfs1(v,u);
        son[u]+=son[v];
        if (son[v]>son[p]) p=v;
    }
    pre[u]=p;
}
void dfs2(int u, int father){
    if (!u) return;
    if (pre[father]==u) top[u]=top[father];else top[u]=u;
    dfn[u]=++cnt;
    dfs2(pre[u],u);
    for (int j=nex[u];j;j=nex[j]){
        int v=nu[j];
        if (v==father || v==pre[u]) continue;
        dfs2(v,u);
    }
}
void update(int t, int l, int r, int x, int y){
    if (l==r){
        f[t]=sum[t]=y;
        return;
    }
    int mid=l+r>>1;
    if (x<=mid) update(t<<1,l,mid,x,y);else update((t<<1)+1,mid+1,r,x,y);
    sum[t]=sum[t<<1]+sum[(t<<1)+1];
    f[t]=max(f[t<<1],f[(t<<1)+1]);
}
int get_max(int t, int l, int r, int le, int ri){
    if (le<=l && r<=ri) return f[t];
    int mid=l+r>>1, p=-INF;
    if (le<=mid) p=max(p,get_max(t<<1,l,mid,le,ri));
    if (ri>mid) p=max(p,get_max((t<<1)+1,mid+1,r,le,ri));
    return p;
}
void query_max(int u, int v){
    int f1=top[u], f2=top[v], ans=-INF;
    while (f1!=f2)
```

```
            if (dep[f1]<dep[f2])
                ans=max(ans,get_max(1,1,n,dfn[f2],dfn[v])),
                v=fa[f2],
                f2=top[v];
            else
                ans=max(ans,get_max(1,1,n,dfn[f1],dfn[u])),
                u=fa[f1],
                f1=top[u];
        ans=max(ans,get_max(1,1,n,min(dfn[u],dfn[v]),max(dfn[u],dfn[v])));
        printf("%d\n", ans);
}
int get_sum(int t, int l, int r, int le ,int ri){
        if (le<=l && r<=ri) return sum[t];
        int mid=l+r>>1, p=0;
        if (le<=mid) p+=get_sum(t<<1,l,mid,le,ri);
        if (ri>mid) p+=get_sum((t<<1)+1,mid+1,r,le,ri);
        return p;
}
void query_sum(int u, int v){
        int f1=top[u], f2=top[v], ans=0;
        while (f1!=f2)
            if (dep[f1]<dep[f2])
                ans+=get_sum(1,1,n,dfn[f2],dfn[v]),
                v=fa[f2],
                f2=top[v];
            else
                ans+=get_sum(1,1,n,dfn[f1],dfn[u]),
                u=fa[f1],
                f1=top[u];
        ans+=get_sum(1,1,n,min(dfn[u],dfn[v]),max(dfn[u],dfn[v]));
        printf("%d\n", ans);
}
int main(){
        cnt=n=read();
        for (int i=1;i<n;i++){
            int u=read(), v=read();
            add(u,v);
            add(v,u);
        }
        dfs1(1,0);
        dfs2(1,cnt=0);
        for (int i=1;i<=n;i++)
            update(1,1,n,dfn[i],read());
        for (int q=read();q;q--){
```

```
            scanf("%s", s);
            int u=read(), v=read();
            if (s[0]=='C') update(1,1,n,dfn[u],v);
            if (s[1]=='M') query_max(u,v);
            if (s[1]=='S') query_sum(u,v);
        }
        return 0;
}
```

Qsort:

```
#include <ctime>
#include <cstdio>
#include <cstring>
#include <cstdlib>
#include <iostream>
using namespace std;
int n, a[11000];
void qsort(int l, int r){
        int i=l, j=r, x=a[l+r>>1];
        while (i<=j){
            while (a[i]<x && i<r) i++;
            while (a[j]>x && j>l) j--;
            if (i<=j) swap(a[i++],a[j--]);
        }
        if (i<r) qsort(i,r);
        if (j>l) qsort(l,j);
}
int main(){
        srand(unsigned(time(NULL)));
        n=300;
        for (int i=1;i<=n;i++) a[i]=rand()%100;
        qsort(1,n);
        for (int i=1;i<=n;i++) cout<<a[i]<<' ';
        return 0;
}
```

整体二分:

```
#include <map>
#include <cstdio>
#include <cstring>
#include <cstdlib>
#include <iostream>
#include <algorithm>
```

```
#define N 80010
#define S 2000000
using namespace std;
int n, m, T, x, gt, cnt, DFN, LSH;
int a[N], k[N], u[N], v[N], c[N], ans[N], q[N];
int fa[N][21], dep[N], trans[N*2], lsh[N*2], nex[N*3], nu[N*3], dfn[N][2];
map<int,int> mp;
char s[S+100];
struct qlz_ques{
	int k, u, v, n;
}l[N*6], b1[N*6], b2[N*6];
int read(){
	int p=0;
	while (s[x]<'0' || s[x]>'9') x++;
	while (s[x]>='0' && s[x]<='9') p=p*10+s[x++]-'0';
	return p;
}
void add_edge(int u, int v){
	nex[++cnt]=nex[u];nex[u]=cnt;nu[cnt]=v;
}
void dfs(int u, int father){
	dfn[u][0]=++DFN;
	fa[u][0]=father;
	for (int i=1;fa[fa[u][i-1]][i-1];i++)
		fa[u][i]=fa[fa[u][i-1]][i-1];
	//cout<<DFN<<' '<<u<<endl;
	for (int j=nex[u];j;j=nex[j]){
		int v=nu[j];
		if (v==father) continue;
		dep[v]=dep[u]+1;
		dfs(v,u);
	}
	dfn[u][1]=DFN+1;
}
int LCA(int u, int v){
	if (dep[u]<dep[v]) swap(u,v);
	//cout<<u<<' '<<v<<endl;
	for (int i=20;i>=0;i--)
		if (dep[fa[u][i]]>=dep[v]) u=fa[u][i];
	if (u==v) return u;
	for (int i=20;i>=0;i--)
		if (fa[u][i]!=fa[v][i]) u=fa[u][i], v=fa[v][i];
	return fa[u][0];
}
```

```
void add(int k, int u, int v){
	l[++gt].k=k, l[gt].u=u, l[gt].v=v;
}
void update(int u, int v){
	for (int i=u;i<=n;i+=i&(-i)) c[i]+=v;
}
int sum(int u){
	int p=0;
	for (int i=dfn[u][0];i;i-=i&(-i)) p+=c[i];
	return p;
}
void solve(int le, int ri, int L, int R){
	//cout<<le<<' '<<ri<<' '<<L<<' '<<R<<endl;
	if (le>ri) return;
	if (L==R){
		for (int i=le;i<=ri;i++)
			if (l[i].n) ans[l[i].n]=L;
		return;
	}
	int mid=L+R>>1, ct1=0, ct2=0;
	for (int i=le;i<=ri;i++){
		if (l[i].n){
			int u=l[i].u, v=l[i].v, lca=LCA(u,v),k=sum(u)+sum(v)-sum(lca)-sum(fa[lca][0]);
			if (k>=l[i].k)
				b2[++ct2]=l[i];
			else
				l[i].k-=k,
				b1[++ct1]=l[i];

		}
		else
			if (l[i].v>mid || l[i].v<-mid)
				b2[++ct2]=l[i],
				update(l[i].u,l[i].v>0?1:-1);
			else
				b1[++ct1]=l[i];
	}
	for (int i=1;i<=ct1;i++) l[le+i-1]=b1[i];
	for (int i=1;i<=ct2;i++) l[le+ct1+i-1]=b2[i];
	for (int i=le;i<=ri;i++)
		if (!l[i].n && (l[i].v>mid || l[i].v<-mid))
			update(l[i].u,l[i].v>0?-1:1);
	solve(le,le+ct1-1,L,mid);
	solve(le+ct1,ri,mid+1,R);
```

```
}
int main(){
	freopen("network10.in","r",stdin);
	freopen("整体二分.out","w",stdout);
//read
	fread(s,1,S,stdin);
	cnt=n=read();m=read();
	for (int i=1;i<=n;i++)
		lsh[++LSH]=a[i]=read();
	for (int i=1;i<n;i++){
		int u=read(), v=read();
		add_edge(u,v);
		add_edge(v,u);
	}
	for (int i=1;i<=m;i++)
		k[i]=read(),
		u[i]=read(),
		v[i]=read(),
		(!k[i]?lsh[++LSH]=v[i]:0);
//lsh
	dfs(dep[1]=1,0);
	sort(lsh+1,lsh+1+LSH);
	trans[mp[0]=++T]=0;
	for (int i=1;i<=LSH;i++)
		if (lsh[i]!=lsh[i-1]) trans[mp[lsh[i]]=++T]=lsh[i];
	for (int i=1;i<=n;i++)
		add(0,dfn[i][0],mp[a[i]]),
		add(0,dfn[i][1],-mp[a[i]]);
	for (int i=1;i<=m;i++)
		if (k[i])
			add(k[i],u[i],v[i]),
			l[gt].n=i,
			q[i]=1;
		else
			add(0,dfn[u[i]][0],-mp[a[u[i]]]),
			add(0,dfn[u[i]][1],mp[a[u[i]]]),
			add(0,dfn[u[i]][0],mp[a[u[i]=v[i]]),
			add(0,dfn[u[i]][1],-mp[v[i]]);
//work
	solve(1,gt,0,T);
	//int tot=0;
	for (int i=1;i<=m;i++)
		if(q[i]){
			//tot++;
```

```
                if (ans[i]) printf("%d\n", trans[ans[i]]);
                else printf("invalid request!\n");
            }
        //cout<<n<<' '<<m<<' '<<tot<<' '<<m-tot<<endl;
        return 0;
}
```

主席树:

```
#include <map>
#include <cstdio>
#include <cstring>
#include <cstdlib>
#include <iostream>
#include <algorithm>
#define N 80010
#define M 8001000
#define S 2000000
using namespace std;
int n, m, T, x, cnt, DFN, LSH, ct_in, ct_out, cnt_tree;
int f[M], ls[M], rs[M];
int fa[N][21], dep[N], trans[N*2], lsh[N*2], a[N], nex[N*3], nu[N*3], root[N], bit[N], b1[N*2],
b2[N*2], dfn[N][2];
char s[S+100];
map<int,int> mp;
struct qlz_in{
        int n, dfn;
}in[N];
struct qlz_out{
        int n, dfn;
}out[N];
struct qlz_ques{
        int k, u, v;
}l[N];
int read(){
        int p=0;
        while (s[x]<'0' || s[x]>'9') x++;
        while (s[x]>='0' && s[x]<='9') p=p*10+s[x++]-'0';
        return p;
}
void add_edge(int u, int v){
        nex[++cnt]=nex[u];nex[u]=cnt;nu[cnt]=v;
}
bool cmp_in(qlz_in a, qlz_in b){return a.dfn<b.dfn;}
```

```
bool cmp_out(qlz_out a, qlz_out b){return a.dfn<b.dfn;}
void dfs(int u, int father){
	fa[u][0]=father;
	for (int i=1;fa[fa[u][i-1]][i-1];i++)
		fa[u][i]=fa[fa[u][i-1]][i-1];
	in[++ct_in].dfn=dfn[u][0]=++DFN;
	//cout<<DFN<<' '<<u<<endl;
	in[ct_in].n=u;
	for (int j=nex[u];j;j=nex[j]){
		int v=nu[j];
		if (v==father) continue;
		dep[v]=dep[u]+1;
		dfs(v,u);
	}
	out[++ct_out].dfn=dfn[u][1]=DFN+1;
	out[ct_out].n=u;
}
void add_b1(int u, int &ct1){
	if (root[dfn[u][0]]) b1[++ct1]=root[dfn[u][0]];
	for (int i=dfn[u][0];i;i-=i&(-i))
		if (bit[i]) b1[++ct1]=bit[i];
}
void add_b2(int u, int &ct2){
	if (root[dfn[u][0]]) b2[++ct2]=root[dfn[u][0]];
	for (int i=dfn[u][0];i;i-=i&(-i))
		if (bit[i]) b2[++ct2]=bit[i];
}
int LCA(int u, int v){
	if (dep[u]<dep[v]) swap(u,v);
	//cout<<u<<' '<<v<<endl;
	for (int i=20;i>=0;i--)
		if (dep[fa[u][i]]>=dep[v]) u=fa[u][i];
	if (u==v) return u;
	for (int i=20;i>=0;i--)
		if (fa[u][i]!=fa[v][i]) u=fa[u][i], v=fa[v][i];
	return fa[u][0];
}
void solve(int u, int v, int k){
	int ct1=0, ct2=0, l=0, r=T, lca=LCA(u,v);
	add_b1(u,ct1);
	add_b1(v,ct1);
	add_b2(lca,ct2);
	add_b2(fa[lca][0],ct2);
	//cout<<u<<' '<<v<<' '<<k<<' '<<lca<<endl;
```

```
        //for (int i=1;i<=ct1;i++) cout<<b1[i]<<' ';cout<<endl;
        //for (int i=1;i<=ct2;i++) cout<<b2[i]<<' ';cout<<endl;
        while (l<r){
            int mid=l+r>>1, p=0;
            for (int i=1;i<=ct1;i++) p+=f[rs[b1[i]]];
            for (int i=1;i<=ct2;i++) p-=f[rs[b2[i]]];
            //cout<<l<<' '<<r<<' '<<mid<<' '<<p<<' '<<k<<endl;
            if (p<k){
                for (int i=1;i<=ct1;i++)
                    b1[i]=ls[b1[i]],
                    (!b1[i]?b1[i--]=b1[ct1--]:0);
                for (int i=1;i<=ct2;i++)
                    b2[i]=ls[b2[i]],
                    (!b2[i]?b2[i--]=b2[ct2--]:0);
                k-=p;
                r=mid;
            }
            else{
                for (int i=1;i<=ct1;i++)
                    b1[i]=rs[b1[i]],
                    (!b1[i]?b1[i--]=b1[ct1--]:0);
                for (int i=1;i<=ct2;i++)
                    b2[i]=rs[b2[i]],
                    (!b2[i]?b2[i--]=b2[ct2--]:0);
                l=mid+1;
            }
        }
        if (l) printf("%d\n", trans[l]);
        else printf("invalid request!\n");
}
void update(int x, int y, int z){
        int ct=0, l=0, r=T;
        for (int i=x;i<=DFN;i+=i&(-i)){
            if (!bit[i]) bit[i]=++cnt_tree;
            f[b1[++ct]=bit[i]]+=z;
        }
        while (l<r){
            int mid=l+r>>1;
            if (y<=mid){
                r=mid;
                for (int i=1;i<=ct;i++){
                    if (!ls[b1[i]]) ls[b1[i]]=++cnt_tree;
                    f[b1[i]=ls[b1[i]]]+=z;
                }
```

```
            }
            else{
                l=mid+1;
                for (int i=1;i<=ct;i++){
                    if (!rs[b1[i]]) rs[b1[i]]=++cnt_tree;
                    f[b1[i]=rs[b1[i]]]+=z;
                }
            }
        }
}
int main(){
    freopen("network10.in","r",stdin);
    freopen("p1146_主席树静态建树查询优化.out","w",stdout);
//read
    fread(s,1,S,stdin);
    cnt=n=read();m=read();
    for (int i=1;i<=n;i++)
        lsh[++LSH]=a[i]=read();
    for (int i=1;i<n;i++){
        int u=read(), v=read();
        add_edge(u,v);
        add_edge(v,u);
    }
    for (int i=1;i<=m;i++)
        l[i].k=read(),
        l[i].u=read(),
        l[i].v=read(),
        (!l[i].k?lsh[++LSH]=l[i].v:0);
//lsh
    sort(lsh+1,lsh+1+LSH);
    trans[mp[0]=++T]=0;
    for (int i=1;i<=LSH;i++)
        if (lsh[i]!=lsh[i-1]) trans[mp[lsh[i]]=++T]=lsh[i];
    for (int i=1;i<=n;i++) a[i]=mp[a[i]];
//build
    dfs(dep[1]=1,0);
    sort(in+1,in+1+n,cmp_in);
    sort(out+1,out+1+n,cmp_out);
    int j=1;
    for (int i=1;i<=n;i++){
        int k=root[in[i].dfn]=++cnt_tree, kk=root[in[i].dfn-1], l=0, r=T, v=a[in[i].n];
        while (l<r){
            int mid=l+r>>1;
            if (v<=mid)
```

```
                rs[k]=rs[kk],
                f[k=ls[k]=++cnt_tree]=f[kk=ls[kk]]+1,
                r=mid;
            else
                ls[k]=ls[kk],
                f[k=rs[k]=++cnt_tree]=f[kk=rs[kk]]+1,
                l=mid+1;
        }
        while (out[j].dfn==in[i].dfn){
            kk=root[in[i].dfn], k=root[in[i].dfn]=++cnt_tree, l=0, r=T, v=a[out[j++].n];
            while (l<r){
                int mid=l+r>>1;
                if (v<=mid)
                    rs[k]=rs[kk],
                    f[k=ls[k]=++cnt_tree]=f[kk=ls[kk]]-1,
                    r=mid;
                else
                    ls[k]=ls[kk],
                    f[k=rs[k]=++cnt_tree]=f[kk=rs[kk]]-1,
                    l=mid+1;
            }
        }
    }
//work
    for (int i=1;i<=m;i++)
        if (l[i].k)
            solve(l[i].u,l[i].v,l[i].k);
        else{
            int u=l[i].u, v=mp[l[i].v];
            update(dfn[u][0],a[u],-1);
            update(dfn[u][1],a[u],1);
            update(dfn[u][0],a[u]=v,1);
            update(dfn[u][1],a[u],-1);
        }
    return 0;
}
```

Cdq(三维偏序):

```
#include <cstdio>
#include <cstring>
#include <cstdlib>
#include <iostream>
#include <algorithm>
```

```
#define N 600
#define M 500000
using namespace std;
int n, m, x, cnt, ans[M], q[M], c[N][N];
char s[6000010];
struct qlz{
    int n, v, x, y, c, x1, x2, y1, y2;
}l[M], b1[M], b2[M];
inline int read(){
    int p=0;
    while (s[x]<'0' || s[x]>'9') x++;
    while (s[x]>='0' && s[x]<='9') p=p*10+s[x++]-'0';
    return p;
}
inline bool cmp(qlz a, qlz b){return a.c<b.c;}
inline void update(int x, int y, int z){
    for (int i=x;i<=n;i+=i&(-i))
        for (int j=y;j<=n;j+=j&(-j))
            c[i][j]+=z;
}
inline int sum(int x, int y){
    int p=0;
    for (int i=x;i;i-=i&(-i))
        for (int j=y;j;j-=j&(-j))
            p+=c[i][j];
    return p;
}
inline void solve(int le, int ri, int L, int R){
    if (le>ri) return;
    if (L==R){
        for (int i=le;i<=ri;i++)
            if (!l[i].v) ans[l[i].n]=L;
        return;
    }
    int mid=L+R>>1;
    int ct1=0, ct2=0;
    for (int i=le;i<=ri;i++)
        if (l[i].v){
            if (l[i].v<=mid)
                b1[++ct1]=l[i],
                update(l[i].x,l[i].y,1);
            else
                b2[++ct2]=l[i];
        }
```

```
        else{
            int k=sum(l[i].x2,l[i].y2)+sum(l[i].x1-1,l[i].y1-1)-sum(l[i].x1-1,l[i].y2)-sum(l[i].x2,l[i].y1-
1);
            if (k>=l[i].c)
                b1[++ct1]=l[i];
            else
                l[i].c-=k,
                b2[++ct2]=l[i];
        }
    for (int i=1;i<=ct1;i++) l[le+i-1]=b1[i];
    for (int i=1;i<=ct2;i++) l[le+ct1+i-1]=b2[i];
    //memcpy(l+le,b1+1,sizeof(l[0])*ct1);
    //memcpy(l+le+ct1,b2+1,sizeof(l[0])*ct2);
    for (int i=le;i<=ri;i++)
        if (l[i].v && l[i].v<=mid) update(l[i].x,l[i].y,-1);
    solve(le,le+ct1-1,L,mid);
    solve(le+ct1,ri,mid+1,R);
}
int main(){
    fread(s,1,6000000,stdin);
    n=read();m=read();
    for (int i=1;i<=n;i++)
        for (int j=1;j<=n;j++)
            l[++cnt].c=read(),
            l[cnt].x=i,
            l[cnt].y=j;
    sort(l+1,l+1+cnt,cmp);
    for (int i=1;i<=cnt;i++) q[l[i].v=i]=l[i].c;
    for (int i=1;i<=m;i++)
        l[++cnt].x1=read(),
        l[cnt].y1=read(),
        l[cnt].x2=read(),
        l[cnt].y2=read(),
        l[cnt].c=read(),
        l[cnt].n=i;
    solve(1,cnt,1,n*n);
    for (int i=1;i<=m;i++) printf("%d\n", q[ans[i]]);
    return 0;
}
```

Kmp:

```
#include <cstdio>
#include <cstring>
```

```
#include <cstdlib>
#include <iostream>
#define N 1010000
#define mo 1000000007
typedef long long ll;
using namespace std;
int ls, n, f[N], p[N];
char s[N];
int read(){
    int p=0;
    char ch=getchar();
    while (ch<'0' || ch>'9') ch=getchar();
    while (ch>='0' && ch<='9') p=p*10+ch-'0', ch=getchar();
    return p;
}
void pre(){
    ls=strlen(s+1);
    int j=0;
    f[1]=1;
    for (int i=2;i<=ls;i++){
        while (j && s[j+1]!=s[i]) j=p[j];
        f[i]=f[p[i]=j+=s[j+1]==s[i]]+1;
    }
}
void solve(){
    ll ans=1;
    int j=0;
    for (int i=2;i<=ls;i++){
        while (j && s[j+1]!=s[i]) j=p[j];
        if (s[j+1]==s[i]) j++;
        while ((j<<1)>i && j) j=p[j];
        ans=ans*(f[j]+1)%mo;
    }
    cout<<ans<<endl;
}
void __init(){
    for (int i=read();i;i--){
        scanf("%s", s+1);
        pre();
        solve();
    }
}
int main(){
    __init();
```

```
    return 0;
}
```

点分治:

```
#include <cstdio>
#include <cstdlib>
#include <cstring>
#include <iostream>
#define N 100000
using namespace std;
int n, ans, cnt, sum, t[2][3], va[N], nu[N], next[N], son[N], f[N], root;
bool vis[N];
int rd(){
	int p=0;
	char ch=getchar();
	while (ch<'0' || ch>'9') ch=getchar();
	while (ch>='0' && ch<='9') p=p*10+ch-'0', ch=getchar();
	return p;
}
void add(int u, int v, int w){
	next[++cnt]=next[u];next[u]=cnt;nu[cnt]=v;va[cnt]=w;
}
void read(){
	cnt=n=rd();
	for (int i=1;i<n;i++){
		int u=rd(), v=rd(), w=rd()%3;
		add(u,v,w);
		add(v,u,w);
	}
}
void getroot(int t, int fa){
	son[t]=1;f[t]=0;
	for (int j=next[t];j;j=next[j]){
		int v=nu[j];
		if (vis[v] || v==fa) continue;
		getroot(v,t);
		son[t]+=son[v];
		f[t]=max(son[v],f[t]);
	}
	f[t]=max(f[t],sum-son[t]);
	if (f[t]<f[root]) root=t;
}
void getdeep(int u, int fa, int f){
	t[1][f]++;
```

```
        son[u]=1;
        for (int j=next[u];j;j=next[j]){
            int v=nu[j];
            if (vis[v] || v==fa) continue;
            getdeep(v,u,(f+va[j])%3);
            son[u]+=son[v];
        }
}
void calc(int x, int va){
        t[1][0]=t[1][1]=t[1][2]=0;
        getdeep(x,0,va);
        ans+=t[0][1]*t[1][2]+t[0][2]*t[1][1]+t[0][0]*t[1][0]+t[1][0];
        t[0][0]+=t[1][0];
        t[0][1]+=t[1][1];
        t[0][2]+=t[1][2];
}
void solve(int x){
        vis[x]=1;
        t[0][0]=t[0][1]=t[0][2]=0;
        for (int j=next[x];j;j=next[j]){
            int v=nu[j];
            if (vis[v]) continue;
            calc(v, va[j]);
        }
        for (int j=next[x];j;j=next[j]){
            int v=nu[j];
            if (vis[v]) continue;
            root=0;sum=son[v];
            getroot(v,0);
            solve(root);
        }
}
int gcd(int a, int b){return !b?a:gcd(b,a%b);}
int main(){
        read();
        sum=n;
        f[0]=n;
        getroot(1,0);
        solve(root);
        ans=ans*2+n;
        int gys=gcd(ans,n*n);
        cout<<ans/gys<<'/'<<n*n/gys;
        return 0;
}
```

```
//WC2010 重建计划---按子树深度递增处理
#include <cstdio>
#include <cstring>
#include <cstdlib>
#include <iostream>
#include <algorithm>
#define N 300000
#define M 1500000
#define INF (double)99999999*99999
#define eps 1e-4
using namespace std;
int mx, n, m, L, R, cnt, sum, root, posL, head, tail, check_flag;
int next[M], nu[M], va[M];
int dep[N], a[N], to[N], q[N], vis[N], flag[N], ff[N], son[N], l[N];
double  g[N], f[N];
int read(){
    int p=0;
    char ch=getchar();
    while (ch<'0' || ch>'9') ch=getchar();
    while (ch>='0' && ch<='9') p=p*10+ch-'0', ch=getchar();
    return p;
}
void add(int u, int v, int w){
    next[++cnt]=next[u];next[u]=cnt;nu[cnt]=v;va[cnt]=w;
}
void getroot(int t, int fa){
    son[t]=1;
    ff[t]=0;
    for (int j=next[t];j;j=next[j]){
        int v=nu[j];
        if (v==fa || vis[v]) continue;
        getroot(v,t);
        son[t]+=son[v];
        ff[t]=max(ff[t],son[v]);
    }
    ff[t]=max(ff[t],sum-son[t]);
    if (ff[t]<ff[root]) root=t;
}
void clear(int t, int fa, int depth){
    flag[t]=0;
    f[dep[t]=depth]=-INF;
```

```
        son[t]=1;
        for (int j=next[t];j;j=next[j]){
            int v=nu[j];
            if (v==fa || vis[v])    continue;
            clear(v,t,depth+1);
            son[t]+=son[v];
            dep[t]=max(dep[t],dep[v]);
        }
    }
    void calc(int ll, int rr, double x, int dep){
        if (ll>rr) return;
        int ri=rr;
        while (posL && posL+dep>=L){
            while (tail>=head && f[q[tail]]<f[posL]) tail--;
            q[++tail]=posL--;
        }
        while (head<=tail && q[head]+dep>R) head++;
        for (int i=ll;i<=rr;i++){
            int t=l[i];
            flag[t]=1;
            if (head<=tail && g[t]+f[q[head]]>=0 || dep>=L && dep<=R && g[t]>=0){
                check_flag=1;
                return;
            }
            for (int j=next[t];j;j=next[j]){
                int v=nu[j];
                if (vis[v] || flag[v]) continue;
                g[v]=g[t]+va[j]-x;
                l[++ri]=v;
            }
        }
        calc(rr+1,ri,x,dep+1);
        if (check_flag) return;
        for (int i=ll;i<=rr;i++) f[dep]=max(f[dep],g[l[i]]);
    }
    bool cmp(int x, int y){return dep[x]<dep[y];}
    void solve(int t, int la, double x){
        clear(t,0,0);
        if (dep[t]*2<L) return;
        flag[t]=vis[t]=1;
        mx=posL=0;
        int ra=la;
        for (int j=next[t];j;j=next[j]){
            int v=nu[j];
```

```
            if (vis[v]) continue;
            a[ra++]=v;
            to[v]=va[j];
        }
        if (la<ra) sort(a+la,a+ra,cmp);
        for (int i=la;i<ra;i++){
            int v=a[i];
            l[1]=v;
            g[v]=to[v]-x;
            head=1;tail=0;
            calc(1,1,x,1);
            posL=mx=max(mx,dep[v]);
            if (check_flag) return;
        }
        for (int i=la;i<ra;i++){
            int v=a[i];
            root=0;sum=son[v];
            getroot(v,0);
            solve(root,ra,x);
        }
}
bool check(double x){
    check_flag=0;
    for (int i=1;i<=n;i++) vis[i]=0;
    sum=ff[root=0]=n;
    getroot(1,0);
    solve(root,1,x);
    return check_flag;
}
int main(){
    freopen("1.in","r",stdin);
    freopen("1.out","w",stdout);
    cnt=n=read();
    L=read();R=read();
    double le=0, ri=0, mid;
    for (int i=1;i<n;i++){
        int u=read(), v=read(), w=read();
        ri=max(ri,double(w));
        add(u,v,w);
        add(v,u,w);
    }
    while (ri-le>eps){
        mid=(le+ri)/2;
        if (check(mid)) le=mid;
```

```
        else ri=mid;
    }
    printf("%.3lf\n", le);
    return 0;
}
```

无向图：

1. 桥：low[v]>dfn[u]，则<u,v>为桥

   Code:

```
#include <cstdio>
#include <cstring>
#include <cstdlib>
#include <iostream>
#include <algorithm>
#define N 2010
using namespace std;
int n, m, cnt, ans, dfn[N], low[N], flag[N], bridge[N], nu[N*3], num[N*3], nex[N*3];
int vis[N], x[N], y[N];
int read(){
 int p=0;
 char ch=getchar();
 while (ch<'0' || ch>'9') ch=getchar();
 while (ch>='0' && ch<='9') p=p*10+ch-'0', ch=getchar();
 return p;
}
void add(int u, int v, int n){
 nex[++cnt]=nex[u];nex[u]=cnt;nu[cnt]=v;num[cnt]=n;
}
void initialize(){
 cnt=n+n%2+1;
 for (int i=1;i<=n;i++) nex[i]=dfn[i]=low[i]=0;
 for (int i=1;i<=m;i++) bridge[i]=0;
}
void tarjan(int u, int from){
 dfn[u]=low[u]=++cnt;
 for (int j=nex[u];j;j=nex[j])
     if (j^from^1){
         int v=nu[j];
         if (dfn[v]) low[u]=min(low[u],dfn[v]);
         else{
             tarjan(v,j);
             low[u]=min(low[u],low[v]);
             bridge[num[j]]=low[v]>dfn[u];
```

```
            }
        }
    }
    int gcd(int a, int b){return b?gcd(b,a%b):a;}
    int main(){
     n=read();m=read();
     cnt=n+n%2+1;
     for (int i=1;i<=m;i++){
        int u=x[i]=read(), v=y[i]=read();
        add(u,v,i);
        add(v,u,i);
     }
     for (int i=1;i<=n;i++)
        if (!dfn[i]) tarjan(i,0);
     for (int i=1;i<=m;i++) flag[i]=bridge[i];
     for (int i=1;i<=m;i++)
        if (!vis[i] && !flag[i]){
            initialize();
            vis[i]=1;
            int tot=1;
            for (int j=1;j<=m;j++)
                if (j!=i) add(x[j],y[j],j),add(y[j],x[j],j);
            for (int j=1;j<=n;j++)
                if (!dfn[j]) tarjan(j,0);
            for (int j=1;j<=m;j++)
                if (bridge[j] && !flag[j]) tot++, vis[j]=1;
            ans=gcd(ans,tot);
        }
     for (int i=1;i<=ans;i++)
        if (ans%i==0) printf("%d%c", i, i==ans?'\n':' ');
     return 0;
}
```

2. 割点：对于点 u，存在边<u,v>，满足 low[v]>=dfn[u]，则 u 为割点
3. 边双连通分量：分量中无桥边，两种求法

   1). Dfs 中不走桥边即可。每一个连通分量即是边双连通分量。

   2). Dfs 找割点，然后对于任意点 i 和 j，如果 low[i]==low[j]，那么它们属于同一个边-双连通分量，不会。
4. 点双联通分量：分量中无割点

有向图：

1. 桥：同无向图
2. 割点：同无向图
3. 强连通分量：代码如下

```
#include <cstdio>
#include <cstring>
```

```
#include <cstdlib>
#include <iostream>
#define N 200000
#define M 800000
using namespace std;
int cnt, n, m, top, tot, in[N], out[N], f[N], flag[N], dfn[N], low[N], co[N], stack[N],
nex[M], nu[M];
int nex2[N], nu2[N];
double ans;
int read(){
 int p=0;
 char ch=getchar();
 while (ch<'0' || ch>'9') ch=getchar();
 while (ch>='0' && ch<='9') p=p*10+ch-'0', ch=getchar();
 return p;
}
void add(int u, int v){
 nex[++cnt]=nex[u];nex[u]=cnt;nu[cnt]=v;
}
void add2(int u, int v){
 nex2[++cnt]=nex2[u];nex2[u]=cnt;nu2[cnt]=v;
}
void tarjan(int u){
 dfn[u]=low[u]=++cnt;
 flag[u]=1;
 stack[++top]=u;
 for (int j=nex[u];j;j=nex[j]){
        int v=nu[j];
        if (!dfn[v]){
                tarjan(v);
                low[u]=min(low[u],low[v]);
        }
        else if (flag[v]) low[u]=min(low[u],dfn[v]);
 }
 if (dfn[u]==low[u]){
        co[stack[top]]=++tot;
        flag[stack[top]]=0;
        while (stack[top--]!=u) flag[stack[top]]=0, co[stack[top]]=tot;
 }
}
int main(){
 cnt=n=read();m=read();
 for (int i=1;i<=m;i++){
        int u=read(), v=read();
```

```
        add(u,v);
    }
    for (int i=1;i<=n;i++) if (!dfn[i]) tarjan(i);
    cnt=n;
    for (int i=1;i<=n;i++){
        int u=co[i];
        f[u]++;
        for (int j=nex[i];j;j=nex[j]){
            int v=co[nu[j]];
            if (v==u) continue;
            in[v]++;
            out[u]++;
            add2(u,v);
        }
    }
    for (int i=1;i<=tot;i++)
        if (!in[i]) ans++;
    for (int i=1;i<=tot;i++)
        if (!in[i] && f[i]==1){
            int flag=1;
            for (int j=nex2[i];j;j=nex2[j])
                if (in[nu2[j]]==1){
                    flag=0;
                    break;
                }
            if (flag){
                ans--;
                break;
            }
        }
    ans=(double)(n-ans)/n;
    printf("%.6lf\n", ans);
    return 0;
}
```

最大二分图匹配（匈牙利算法）：

```
#include <cstdio>
#include <cstring>
#include <cstdlib>
#include <iostream>
#include <algorithm>
#define N 110
typedef long long ll;
using namespace std;
```

```
int cnt, n, m, g[N][2], fr[N*2], flag[N*2], nex[N*200], nu[N*200], a[N][N];
ll ans;
int read(){
	int p=0;
	char ch=getchar();
	while (ch<'0' || ch>'9') ch=getchar();
	while (ch>='0' && ch<='9') p=p*10+ch-'0', ch=getchar();
	return p;
}
void add(int u, int v){
	nex[++cnt]=nex[u];nex[u]=cnt;nu[cnt]=v;
}
bool find(int u){
	for (int j=nex[u];j;j=nex[j]){
		int v=nu[j];
		if (flag[v]) continue;
		flag[v]=1;
		if (!fr[v] || find(fr[v])) {
			fr[v]=u;
			return 1;
		}
	}
	return 0;
}
int main(){
	cnt=(n=read())+(m=read());
	for (int i=1;i<=n;i++)
		for (int j=1;j<=m;j++) (a[i][j]=read())?(ans+=a[i][j]-1):0;
	for (int i=1;i<=n;i++){
		int ma=0;
		for (int j=1;j<=m;j++) ma=max(ma,a[i][j]);
		if (ma)	ans-=ma-1;
		g[i][0]=ma;
	}
	for (int j=1;j<=m;j++){
		int ma=0;
		for (int i=1;i<=n;i++) ma=max(ma,a[i][j]);
		if (ma) ans-=ma-1;
		g[j][1]=ma;
	}
	for (int i=1;i<=n;i++)
		for (int j=1;j<=m;j++)
			if (g[i][0]==g[j][1] && a[i][j])
				add(i,j+n),
```

```
                add(j+n,i);
        for (int i=1;i<=n;i++){
                memset(flag,0,sizeof(flag));
                if (find(i)) ans+=g[i][0]-1;
        }
        cout<<ans<<endl;
        return 0;
}
```

最小费用流(spfa):

```
#include <cstdio>
#include <cstring>
#include <cstdlib>
#include <iostream>
#define N 10000
#define M 50000
#define INF 1000000000
using namespace std;
int n, m ,cnt, s, t, nex[M], nu[M], va[M], w[M];
int dis[N], fl[N], fr[N], flag[N], l[N*10];
int read(){
        int p=0;
        char ch=getchar();
        while (ch<'0' || ch>'9') ch=getchar();
        while (ch>='0' && ch<='9') p=p*10+ch-'0', ch=getchar();
        return p;
}
void add(int u, int v, int flow, int cost){
        nex[++cnt]=nex[u];nex[u]=cnt;nu[cnt]=v;va[cnt]=flow;w[cnt]=cost;
        nex[++cnt]=nex[v];nex[v]=cnt;nu[cnt]=u;va[cnt]=0;w[cnt]=-cost;
}
void __init(){
        n=read();m=read();
        cnt=(n+1)*2+1;
        s=2*n+1;t=2*n+2;
        for (int i=1;i<=n;i++){
                int x=read();
                add(s,i+n,1,x);
                add(s,i,1,0);
                add(i+n,t,1,0);
        }
        for (int i=1;i<=m;i++){
                int u=read(), v=read(), w=read();
                if (u>v) swap(u,v);
```

```
            add(u,v+n,1,w);
        }
    }
    bool spfa(){
        int le=0, ri=1;
        for (int i=1;i<=t;i++) dis[i]=INF, flag[i]=0;
        dis[l[1]=s]=0;
        flag[s]=1;
        while (le<ri){
            int u=l[++le];
            flag[u]=0;
            for (int j=nex[u];j;j=nex[j]){
                if (!va[j]) continue;
                int v=nu[j];
                if (dis[u]+w[j]<dis[v]){
                    fr[v]=u;
                    fl[v]=va[j];
                    dis[v]=dis[u]+w[j];
                    if (!flag[v]){
                        flag[v]=1;
                        l[++ri]=v;
                    }
                }
            }
        }
        return dis[t]<INF;
    }
    int sub(){
        int j=t, mi=INF;
        while (j!=s) mi=min(mi,fl[j]), j=fr[j];
        j=t;
        while (j!=s){
            for (int k=nex[fr[j]];k;k=nex[k])
                if (nu[k]==j){
                    va[k]-=mi;
                    va[k^1]+=mi;
                    break;
                }
            j=fr[j];
        }
        return mi*dis[t];
    }
    void solve(){
        int ans=0;
```

```
	while (spfa()) ans+=sub();
	cout<<ans<<endl;
}
int main(){
	__init();
	solve();
	return 0;
}
```

快速傅里叶变换(FFT):

```
#include <cmath>
#include <cstdio>
#include <cstring>
#include <cstdlib>
#include <complex>
#include <iostream>
#include <algorithm>
#define pi acos(-1)
#define N 131077
using namespace std;
typedef long long ll;
typedef long double ld;
typedef complex<double> com;
int n, m, L;
com a[N], b[N];
int c[N], rev[N];
char s[100000];
void init(){
	cin>>n;
	scanf("%s", s);
	for (int i=0;i<n;i++) a[i]=s[n-1-i]-'0';
	scanf("%s", s);
	for (int i=0;i<n;i++) b[i]=s[n-1-i]-'0';
}
void get_bit(){
	for (n=1, L=0;n<m;n<<=1) L++;
}
void get_rtable(){
	for (int i=0;i<n;i++)
		rev[i]=(rev[i>>1]>>1)|((i&1)<<(L-1));
}
void mul(com *a, com*b){
	for (int i=0;i<n;i++) a[i]*=b[i];
}
```

```
void FFT(com *a, int flag){
	for (int i=0;i<n;i++)
		if (i<rev[i]) swap(a[i],a[rev[i]]);
	for (int i=1;i<n;i<<=1){
		com wn(cos(2*pi/(i*2)),flag*sin(2*pi/(i*2)));
		for (int j=0;j<n;j+=(i<<1)){
			com w(1,0);
			for (int k=0;k<i;k++, w*=wn){
				com x=a[j+k], y=w*a[j+k+i];
				a[j+k]=x+y;
				a[j+k+i]=x-y;
			}
		}
	}
	if (flag==-1) for (int i=0;i<n;i++) a[i]/=n;
}
void solve(){
	m=n<<1;
	get_bit();
	get_rtable();
	FFT(a,1), FFT(b,1);
	mul(a,b);
	FFT(a,-1);
}
void print(){
	for (int i=0;i<m;i++) c[i]=(int)(a[i].real()+0.5);
	for (;c[m-1]==0;m--);
	for (int i=0;i<m;i++){
		if (c[i]>=10){
			c[i+1]+=c[i]/10;
			c[i]%=10;
			if (i==m-1) m++;
		}
	}
	for (int i=m-1;i>=0;i--) printf("%d", c[i]);
}
int main(){
	init();
	solve();
	print();
	return 0;
}
```

lsap:

```
#include<iostream>
#include<cstdio>
#include<algorithm>
#include<cmath>
#include<cstring>
#define maxn 80000
#define maxm 3000000
#define inf 2147483647
using namespace std;
struct et
{
    int s,t,val,next;
}e[maxm];
const int dx[4]={0,1,0,-1};
const int dy[4]={1,0,-1,0};
int fir[maxn],dis[maxn],gap[maxn],last[maxn];
int v,s[60][60][60];
int st,ed,n,m,h,num,tot,D,cnt;
int dfs(int now,int flow)
{
    if (now==ed) return flow;
    int sap=0;
    for (int j=last[now];j;j=e[j].next)
    {
        int k=e[j].t;
        if (e[j].val&&dis[now]==dis[k]+1)
        {
            last[now]=j;
            int tmp=dfs(k,min(e[j].val,flow-sap));
            e[j].val-=tmp;
            e[j^1].val+=tmp;
            sap+=tmp;
            if (sap==flow) return sap;
        }
    }
    if (dis[st]>=num) return sap;
    if (!(--gap[dis[now]])) dis[st]=num;
    ++gap[++dis[now]];
    last[now]=fir[now];
    return sap;
}
void add(int x,int y,int z)
{
```

```
    e[++tot].s=x; e[tot].t=y; e[tot].val=z; e[tot].next=fir[x]; fir[x]=tot;
    e[++tot].s=y; e[tot].t=x; e[tot].val=0; e[tot].next=fir[y]; fir[y]=tot;
}
int main()
{
    scanf("%d%d%d",&n,&m,&h);
    scanf("%d",&D);
    for (int k=1;k<=h+1;k++)
        for (int i=1;i<=n;i++)
            for (int j=1;j<=m;j++)
                s[k][i][j]=++cnt;
    st=0; ed=cnt+1; num=cnt+2; tot=1;
    for (int i=1;i<=n;i++)
        for (int j=1;j<=m;j++)
            add(st,s[1][i][j],inf),add(s[h+1][i][j],ed,inf);
    for (int k=1;k<=h;k++)
        for (int i=1;i<=n;i++)
            for (int j=1;j<=m;j++)
                scanf("%d",&v),add(s[k][i][j],s[k+1][i][j],v);
    for (int k=1;k<=h;k++)
        for (int i=1;i<=n;i++)
            for (int j=1;j<=m;j++)
                for (int p=0;p<4;p++)
                    if (s[k+D][i+dx[p]][j+dy[p]])
                        add(s[k+D][i+dx[p]][j+dy[p]],s[k][i][j],inf);
    memset(dis,0,sizeof(dis));
    memset(gap,0,sizeof(gap));
    gap[0]=num;
    for (int i=st;i<=ed;i++) last[i]=fir[i];
    int ans=0;
    while (dis[st]<num) ans+=dfs(st,inf);
    printf("%d\n",ans);
    return 0;
}
```

Manacher:

```
#include <cstdlib>
#include <cstring>
#include <cstdio>
#include <iostream>
#include <algorithm>
using namespace std;
const int N = 110005;
char str[N], cpy[N<<1];
```

```
int seq[N<<1];
void manacher(char s[], int length, int rad[]) {
    for (int i=1,j=0,k; i < length; i+=k) {
        while (s[i-j-1] == s[i+j+1]) ++j;
        rad[i] = j;
        for (k = 1; k <= rad[i] && rad[i-k] != rad[i]-k; ++k) { // 利用类似镜像的方法缩短了
时间
            rad[i+k] = min(rad[i-k], rad[i]-k);
        }
        j = max(j-k, 0);
    }
}
int main() {
    while (scanf("%s", str) != EOF) {
        int len = strlen(str);
        cpy[0] = '(', cpy[1] = '#';
        for (int i=0, j=2; i < len; ++i, j+=2) {
            cpy[j] = str[i];
            cpy[j+1] = '#';
        }
        len = len*2+3;
        cpy[len-1] = ')';
        manacher(cpy, len, seq);
        int Max = 1;
        for (int i = 0; i < len; ++i) {
            Max = max(Max, seq[i]);
        }
        printf("%d\n", Max);
    }
    return 0;
}
```

SegmentTree_2D_单点修改单点查询:

```
#include <map>
#include <queue>
#include <cmath>
#include <ctime>
#include <vector>
#include <cstdio>
#include <cstdlib>
#include <cstring>
#include <iostream>
#include <algorithm>
#define N 1000000
```

```
typedef unsigned long long ull;
typedef long long ll;
using namespace std;
int n, m, k, T, x1, yy, x2 ,y2, cnt, x;
//map <int, int> g;
int son[N*2][5], g[N*2];
char s[N*50+5];
int read(){
	int p=0;
	while (s[x]<'0' || s[x]>'9') x++;
	while (s[x]>='0' && s[x]<='9') p=p*10+s[x++]-'0';
	return p;
}
void pushdown(int t){
	if (!g[t]) return;
	for (int i=0;i<4;i++)
		if (son[t][i])
			if (!g[son[t][i]] || g[son[t][i]]==g[t]) g[son[t][i]]=g[t];
			else g[son[t][i]]=-1;
	g[t]=0;
}
void upd(int t, int l1, int r1, int l2, int r2){
	if (x1<=l1 && r1<=x2 && yy<=l2 && r2<=y2){
		if (!g[t] || g[t]==k) g[t]=k;
		else g[t]=-1;
		return;
	}
	if (g[t]<0) return;
	pushdown(t);
	int midx=(l1+r1)>>1, midy=(l2+r2)>>1;
	if (x1<=midx && yy<=midy) upd(son[t][0],l1,midx,l2,midy);
	if (x1<=midx && y2>midy) upd(son[t][1],l1,midx,midy+1,r2);
	if (x2>midx && yy<=midy) upd(son[t][2],midx+1,r1,l2,midy);
	if (x2>midx && y2>midy) upd(son[t][3],midx+1,r1,midy+1,r2);
}
int query(int t, int l1, int r1, int l2, int r2){
	if (l1==r1 && l2==r2 || g[t]<0) return g[t];
	pushdown(t);
	int midx=(l1+r1)>>1, midy=(l2+r2)>>1;
	if (x1<=midx && yy<=midy) return query(son[t][0],l1,midx,l2,midy);
	if (x1<=midx && yy>midy) return query(son[t][1],l1,midx,midy+1,r2);
	if (x1>midx && yy<=midy) return query(son[t][2],midx+1,r1,l2,midy);
	return query(son[t][3],midx+1,r1,midy+1,r2);
}
```

```
void build(int &t, int l1, int r1, int l2, int r2){
	if (l1>r1 || l2>r2) return;
	t=++cnt;
	if (l1==r1 && l2==r2) return;
	int midx=l1+r1>>1, midy=l2+r2>>1;
	build(son[t][0], l1, midx, l2, midy);
	build(son[t][1], l1, midx, midy+1, r2);
	build(son[t][2], midx+1, r1, l2, midy);
	build(son[t][3], midx+1, r1, midy+1, r2);
}
int main(){
	fread(s,1,N*50,stdin);
	n=read();m=read();T=read();
	int p, q=n*m;
	build(p,1,n,1,m);
	x1=yy=x2=y2=1;
	for (int i=1;i<=q;++i){
		k=read(),
		upd(1,1,n,1,m);
		//cout<<x1<<' '<<yy<<' '<<query(1,1,n,1,m)<<endl;;
		if (++yy>m) x1++, yy=1;
		if (++y2>m) x2++, y2=1;
	}
	for (int i=1;i<=T;++i)
		x1=read(),
		yy=read(),
		x2=read(),
		y2=read(),
		k=read(),
		upd(1,1,n,1,m);
	int ans=0;
	x1=yy=1;
	for (int i=1;i<=q;++i){
		ans+=query(1,1,n,1,m)>=0;
		//cout<<x1<<' '<<yy<<' '<<query(1,1,n,1,m)<<endl;
		if (++yy>m) x1++, yy=1;
	}
	cout<<n*m-ans<<endl;
	return 0;
}
```

Priority_queue

```
class Student
{
```

```
    int id;
    char name[20];
    bool gender;
    bool operator < (Student &a) const
    {
        return id > a.id;
    }
};
priority_queue<int, vector<int>, less<int> > maxHeap; //存储小的值，值越大，优先级越高
priority_queue<int, vector<int>, greater<int> > minHeap; //存储大的值，值越小，优先级越高
```

Dijkstra+Priority_Queue:

```
#include <queue>
#include <vector>
#include <cstdio>
#include <cstring>
#include <cstdlib>
#include <iostream>
#include <algorithm>
#define N 100000
#define M 500000
#define INF 999999999
#define num(x) ((x)>='0' && (x)<='9')
typedef unsigned long long ull;
typedef long long ll;
using namespace std;
int n, cnt, m, st, ed, flag[N], nex[M], nu[M], va[M], dist[N];
struct node{
    int n, dist;
    node (int n, int dist): n(n), dist(dist){}
    bool operator <(const node &o) const {return this->dist<o.dist;}
    bool operator >(const node &o) const {return this->dist>o.dist;}
};
//priority_queue<int> qq;//这是个大猪蹄子，大根堆
//typedef pair<int, int> P;
//priority_queue<P, vector<P>, greater<P> > Q; pair 按字典序比较
priority_queue<node, vector<node>, greater<node> > q;
int read(){
    int p=0, q=1;
    char ch=getchar();
    while (!num(ch)) (ch=='-'?q=-1:0), ch=getchar();
    while (num(ch)) p=p*10+ch-'0', ch=getchar();
    return p*q;
```

```
}
void add(int u, int v, int w){
	nex[++cnt]=nex[u];nex[u]=cnt;nu[cnt]=v;va[cnt]=w;
}
void dijkstra(){
	for (int i=1;i<=n;i++) dist[i]=INF, flag[i]=0;
	dist[st]=0;
	q.push(node(st,0));
	while (!q.empty()){
		node curNode=q.top();
		q.pop();
		int u=curNode.n;
		flag[u]=1;
		for (int j=nex[u];j;j=nex[j]){
			int v=nu[j];
			if (!flag[v] && dist[u]+va[j]<dist[v])
				dist[v]=dist[u]+va[j],
				q.push(node(v,dist[v]));
		}
		while (!q.empty() && flag[q.top().n]) q.pop();
	}
}
int main(){
	cnt=n=read();m=read();
	st=read();ed=read();
	for (int i=1;i<=m;i++){
		int u=read(), v=read(), w=read();
		add(u, v, w);
		add(v, u, w);
	}
	dijkstra();
	cout<<dist[ed]<<endl;
	return 0;
}
```

dc3_by_ez_zkj:

```
#include <bits/stdc++.h>
#define N 50100
#define F(x) ((x)/3+((x)%3==1?0:tb))
#define G(x) ((x)<tb?(x)*3+1:((x)-tb)*3+2)
using namespace std;

char s[N];
int sa[10*N],rk[N],h[N];
```

```
int r[10*N],wa[10*N],wb[10*N],wv[10*N];
int wws[10*N];
int n;

void sort(int *r,int *a,int *b,int n,int m)
{
	int i;
	for(i=0;i<n;i++) wv[i]=r[a[i]];
	for(i=0;i<m;i++) wws[i]=0;
	for(i=0;i<n;i++) wws[wv[i]]++;
	for(i=1;i<m;i++) wws[i]+=wws[i-1];
	for(i=n-1;i>=0;i--) b[--wws[wv[i]]]=a[i];
	return;
}
int c0(int *r,int a,int b) {return r[a]==r[b]&&r[a+1]==r[b+1]&&r[a+2]==r[b+2];}

int c12(int k,int *r,int a,int b)
{
	if(k==2) return r[a]<r[b]||(r[a]==r[b]&&c12(1,r,a+1,b+1));
	else	 return r[a]<r[b]||(r[a]==r[b]&&wv[a+1]<wv[b+1]);
}



void dc3(int *r,int *sa,int n,int m)
{
	int i,j,*rn=r+n,*san=sa+n,ta=0,tb=(n+1)/3,tbc=0,p;
	r[n]=r[n+1]=0;
	for(i=0;i<n;i++) if(i%3!=0) wa[tbc++]=i;
	sort(r+2,wa,wb,tbc,m);
	sort(r+1,wb,wa,tbc,m);
	sort(r,wa,wb,tbc,m);
	for(p=1,rn[F(wb[0])]=0,i=1;i<tbc;i++) rn[F(wb[i])]=c0(r,wb[i-1],wb[i])?p-1:p++;
	if(p<tbc) dc3(rn,san,tbc,p);
	else for(i=0;i<tbc;i++) san[rn[i]]=i;
	for(i=0;i<tbc;i++) if(san[i]<tb) wb[ta++]=san[i]*3;
	if(n%3==1) wb[ta++]=n-1;
	sort(r,wb,wa,ta,m);
	for(i=0;i<tbc;i++) wv[wb[i]=G(san[i])]=i;
	for(i=0,j=0,p=0;i<ta && j<tbc;p++)
		sa[p]=c12(wb[j]%3,r,wa[i],wb[j])?wa[i++]:wb[j++];
	for(;i<ta;p++) sa[p]=wa[i++];
	for(;j<tbc;p++) sa[p]=wb[j++];
}
```

```
void geth()
{
	int j=0,k; h[1]=0;
	for (int i=1;i<=n;i++) if (rk[i]>1)
	{
		k=sa[rk[i]-1];
		while (i+j<=n&&k+j<=n&&s[i+j-1]==s[k+j-1]) j++;
		h[rk[i]]=j; if (j>0) j--;
	}
}


int main()
{
	scanf("%s\n",s);
	n=strlen(s); int m=255;                          //s 从 0 开始     n 长度    m 字符集大小
	for (int i=0;i<n;i++) r[i]=(int)s[i]; r[n]=0;
	dc3(r,sa,n+1,m+1);                                  //dc3 过程后 r 会被破坏
	for (int i=1;i<=n;i++) rk[sa[i]]=i;
	for (int i=1;i<=n;i++) sa[i]++;
	for (int i=n;i>0;i--) rk[i]=rk[i-1];          //sa、rk 均从下标 1 开始
	geth();
	for (int i=1;i<=n;i++) printf("%d ",rk[i]); puts("");
	for (int i=1;i<=n;i++) printf("%d ",h[i]);    puts("");
}
```

虚树+倍增 lca+倍增树路径 min 值:

```
#include <set>
#include <cstdio>
#include <cstdlib>
#include <cstring>
#include <iostream>
#include <algorithm>
#define LOGN 30
#define N 500050
#define num(x) ((x)>='0' && (x)<='9')
typedef unsigned long long ull;
typedef long long ll;
using namespace std;
const int INF=1999999999;
int _, n, m, cnt, top, stack[N], flag[N], tag[N], lg[N], h[N];
int nex[N*5], nu[N*5], va[N*5];
int dfn[N], dep[N];
int fa[N][LOGN], g[N][LOGN];
```

```
ll f[N];
int read(){
	int p=0, q=1;
	char ch=getchar();
	while (!num(ch)) (ch=='-'?q=-1:0), ch=getchar();
	while (num(ch)) p=p*10+ch-'0', ch=getchar();
	return p*q;
}
void add(int u, int v, int w){
	nex[++cnt]=nex[u];nex[u]=cnt;nu[cnt]=v;va[cnt]=w;
}
void dfs(int u, int dad, int w){
	dfn[u]=++cnt;
	dep[u]=dep[dad]+1;
	fa[u][0]=dad;
	g[u][0]=w;
	for (int j=1;fa[u][j-1];j++)
		fa[u][j]=fa[fa[u][j-1]][j-1],
		g[u][j]=min(g[u][j-1],g[fa[u][j-1]][j-1]);
	for (int j=nex[u];j;j=nex[j]){
		int v=nu[j];
		if (v==dad) continue;
		dfs(v,u,va[j]);
	}
}
void initialize(){
	lg[1]=0;
	for (int i=2;i<=n;i++) lg[i]=lg[i>>1]+1;
	for (int i=1;i<=n;i++)
		for (int j=0;j<=lg[n];j++)
			g[i][j]=INF;
	cnt=0;
	dfs(1,0,INF);
}
int get_lca(int u, int v){
	if (dep[u]<dep[v]) swap(u,v);
	while (dep[u]>dep[v]) u=fa[u][lg[dep[u]-dep[v]]];
	if (u==v) return u;
	for (int j=lg[n];j>=0;j--)
		if (fa[u][j]==fa[v][j]) continue;
		else u=fa[u][j], v=fa[v][j];
	return fa[u][0];
}
int get_min(int u, int v){
```

```
        //cout<<u<<' '<<v<<' ';
        int mi=INF;
        while (u!=v){
            mi=min(mi,g[v][lg[dep[v]-dep[u]]]);
            v=fa[v][lg[dep[v]-dep[u]]];
        }
        //cout<<mi<<endl;
        return mi;
}
void link(int u, int v){
        if (tag[u]!=_) tag[u]=_, nex[u]=0;
        if (tag[v]!=_) tag[v]=_, nex[v]=0;
        add(u,v,get_min(u,v));
}
void pop(){
        int v=stack[top--];
        //cout<<v<<endl;
        if (!top) return;
        int u=stack[top];
        link(u,v);
}
void push(int u){
        stack[++top]=u;
}
void build_vt(){
        cnt=n;
        stack[top=1]=1;
        for (int i=1;i<=m;i++){
            int u=h[i], v=stack[top];
            int LCA=get_lca(u,v);
            //cout<<u<<' '<<v<<' '<<LCA<<' '<<endl;
            while (top>1 && dep[stack[top-1]]>=dep[LCA]) pop();
            if (stack[top]!=LCA){
                link(LCA,stack[top]);
                top--;
                push(LCA);
            }
            push(u);
        }
        while (top) pop();
}
bool cmp(int a, int b) { return dfn[a]<dfn[b];}
void dp(int u){
        f[u]=0;
```

```
	for (int j=nex[u];j;j=nex[j]){
		int v=nu[j];
		if (flag[v]==_) f[v]=INF;else dp(v);
		f[u]+=min((ll)va[j],f[v]);
	}
	//cout<<u<<' '<<f[u]<<endl;
}
void solve(){
	m=read();
	for (int i=1;i<=m;i++) h[i]=read(), flag[h[i]]=_;
	sort(h+1,h+1+m,cmp);
	build_vt();
	dp(1);
	printf("%lld\n", f[1]);
}
int main(){
	cnt=n=read();
	for (int i=1;i<n;i++){
		int u=read(), v=read(), w=read();
		add(u,v,w);
		add(v,u,w);
	}
	initialize();
	for (_=read();_;_--) solve();
	return 0;
}
```

可持久化并查集+启发式合并: O(nlog^2n)

```
#include<bits/stdc++.h>
#define max(x,y) ((x)>(y)?(x):(y))
#define min(x,y) ((x)<(y)?(x):(y))
#define LL long long
#define swap(x,y) (x^y?(x^=y,y^=x,x^=y):0)
#define tc() (A==B&&(B=(A=ff)+fread(ff,1,100000,stdin),A==B)?EOF:*A++)
#define pc(ch) (pp_<100000?pp[pp_++]=(ch):(fwrite(pp,1,100000,stdout),pp[(pp_=0)++]=(ch)))
#define N 200000
int pp_=0;char ff[100000],*A=ff,*B=ff,pp[100000];
using namespace std;
int n,Q,tot=0,rt[N+5],a[N+5];
struct Chairman_Tree
{
	int Son[2],fa,level;
}node[N*20];
```

```
inline void read(int &x)
{
	x=0;int f=1;char ch;
	while(!isdigit(ch=tc())) f=ch^'-'?1:-1;
	while(x=(x<<3)+(x<<1)+ch-'0',isdigit(ch=tc()));
	x*=f;
}
inline void write(int x)
{
	if(x<0) pc('-'),x=-x;
	if(x>9) write(x/10);
	pc(x%10+'0');
}
inline void Build(int &rt,int l,int r)//初始的建树，一开始每个节点的 fa 都是本身，这是并查集的基础思想
{
	rt=++tot;
	int mid=l+r>>1;
	if(!(l^r)) {node[rt].fa=l;return;}
	Build(node[rt].Son[0],l,mid),Build(node[rt].Son[1],mid+1,r);
}
inline void NewPoint(int &rt,int lst,int l,int r,int x,int fa)//新插入一个节点
{
	rt=++tot;
	int mid=l+r>>1;
	if(!(l^r)) {node[rt].fa=fa,node[rt].level=node[lst].level;return;}//更新 fa，并复制以前版本的这个节点的 level
	node[rt].Son[0]=node[lst].Son[0],node[rt].Son[1]=node[lst].Son[1];
	if(x<=mid) NewPoint(node[rt].Son[0],node[lst].Son[0],l,mid,x,fa);
	else NewPoint(node[rt].Son[1],node[lst].Son[1],mid+1,r,x,fa);
}
inline void Add_level(int rt,int l,int r,int x)//增加一个节点的在按秩合并时的优先级
{
	int mid=l+r>>1;
	if(!(l^r)) {++node[rt].level;return;}
	if(x<=mid) Add_level(node[rt].Son[0],l,mid,x);
	else Add_level(node[rt].Son[1],mid+1,r,x);
}
inline int Query(int rt,int l,int r,int x)//询问 x 节点在某一版本下的位置
{
	int mid=l+r>>1;
	if(!(l^r)) return rt;
	if(x<=mid) return Query(node[rt].Son[0],l,mid,x);
	else return Query(node[rt].Son[1],mid+1,r,x);
```

```
}
inline int getfa(int rt,int x)//询问 x 节点在某一版本下的祖先
{
	int fa=Query(rt,1,n,x);
	return node[fa].fa^x?getfa(rt,node[fa].fa):fa;//如果 x 节点在该版本下的父亲等于它本身，就返回 x，否则返回 x 的父亲在这个版本下的祖先，和经典的 getfa()函数差不多
}
inline void connect(int v,int x,int y)//在版本 v 中连接 x 和 y，将他们放入一个集合中
{
	int fx=getfa(rt[v],x),fy=getfa(rt[v],y);//先求出版本 v 中它们的祖先
	if(!(fx^fy)) return;//如果祖先相同，就退出函数
	if(node[fx].level<node[fy].level) swap(fx,fy);//如果 x 的优先级小于 y 的优先级，就交换 x 和 y
	NewPoint(rt[v],rt[v-1],1,n,node[fy].fa,node[fx].fa);//将优先级小的节点的父亲连向优先级大的节点的父亲
	if(!(node[fx].level^node[fy].level)) Add_level(rt[v],1,n,node[fx].fa);//如果它们的优先级相同，就将它们合并后的祖宗的优先级加 1
}
int main()
{
	register int i;
	for(read(n),read(Q),Build(rt[0],i=1,n);i<=Q;++i)//先建一棵树，然后进行操作
	{
		int op,x,y;read(op),read(x);
		if(op^2) read(y),rt[i]=rt[i-1];
		switch(op)
		{
			case 1:connect(i,x,y);break;//在当前版本下连接 x 和 y
			case 2:rt[i]=rt[x];break;//将当前版本还原回曾经的版本 x
			case 3:pc(getfa(rt[i],x)^getfa(rt[i],y)?'0':'1'),pc('\n');break;//若当前版本下 x 和 y 的父亲相同，输出 1，否则输出 0
		}
	}
	return fwrite(pp,1,pp_,stdout),0;
}

__int128: (need linux)
#include <bits/stdc++.h>
using namespace std;
//__int128: -2^126~2^126
inline __int128 read()
{
	__int128 x=0,f=1;
	char ch=getchar();
```

```
    while(ch<'0'||ch>'9')
    {
        if(ch=='-')
            f=-1;
        ch=getchar();
    }
    while(ch>='0'&&ch<='9')
    {
        x=x*10+ch-'0';
        ch=getchar();
    }
    return x*f;
}
inline void write(__int128 x)
{
    if(x<0)
    {
        putchar('-');
        x=-x;
    }
    if(x>9)
        write(x/10);
    putchar(x%10+'0');
}
int main()
{
    __int128 a = read();
    __int128 b = read();
    write(a + b);
    return 0;
}
```

Compare_In_Linux:

```
#!/bin/sh
echo '1' > p1537.out
echo '1' > std.out
g++ data.cpp -o data
g++ std.cpp -o std
g++ p1537.cpp -o p1537
while (diff p1537.out std.out) do
echo '==data=='
./data
echo '==std=='
./std
echo '==p1537=='
./p1537
done;
```