V4 Lab Main Report

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Introduction

This is the main technical report of the V4 Lab Project. Its aim is twofold: 1) to see what is the level of economic/financial knowledge of Polish and Czech students and what are their attitudes in regard to economic liberalism/socialism; 2) to answer the main research problem posed in this project, that is whether there is a relationship between economic and financial knowledge, liberal/socialist attitudes and type of obtained education (EBMF, SSHA and STEM). Moreover we also check potential connections between knowledge and attitudes and some sociodemographics such as parental education and work experience.

We estimate level of the economic/financial knowledge by three means: 1) we investigate answer patterns to separate items (i.e. which are most diffcult etc.); 2) analyze what we call raw scores, that is sums of correct answers; 3) analyze what we call non-guessed answers, that is the number of correct answers that were not guessed. The last measure is based on an assumption that since the items were of true/false form then in the case when one does not know the correct answer the problem of answering such an item boils down to guessing with 50% chance of hit. Under this assumption it is easy to derive the number of questions that must have been answered correctly in a nonrandom fashion (that is respondent must have been quite certain that the answer he or she gives is the correct one). The number of correct answers may be computed using the following formula: C = 2X - 2E - 1, where C is the score, X is the actual number of correct answers given and E is the expected number of such answers (in this case this is a constant that equals 14.5, since there are 29 items with guessing chance of 50%).

Furthermore, KNOWLEDGE items of true/false form give us one more opportunity - it is easy to partition the item set into three subsets: 1) easy items (those with difficulty significantly below 0.5, what implies that on average respondents do know the correct answer and there is no need for guessing); 2) medium items (those around difficulty level of 0.5, what implies that on average respondents do not know the answer for sure and guess); 3) tricky items (those with difficulty significantly above 0.5, what implies that on average respondents have false beliefs about them).

Liberal/socialist economic attitudes are measured using the Liberalism-Socialism preferential scale that we constructed for the purpose of this project (more information about the scale can be found in the dedicated report). This scale ranges from -8 to 8 and negative score correspond to liberal pole of it and positive to socialist (the in-sample range is a bit narrower and spans from -7 to 7). However, the extreme values of -8 and 8 are not detectable in practice for some technical reasons which we will not discuss here. This problem is not important because no respondents have answer patterns that would lead to this kind of complication.

Parental education is assessed on the basis of three variables. The first two of them are father and mother education. These are categorical variables with four levels: 1) vocational education or lower; 2) high school; 3) higher education (defiend as BA or MA or equivalent); 4) PHD and above. The levels are slightly different from the original answer categories available in the questionnaire we used, where it was more detailed. This is due to the fact that some answers were very rare and we needed to group into wider categories.

The third variable we use to asses parental education is based on the previous ones. We call it the Ordinal Indicator of Joint Parental Education (OIJPE). It is constructed as follows: 1) recode father and mother education to integers ranging from 0 to 3 in such a manner that it preserves the education levels order; 2) add the recoded variables (it creates a variable ranging from 0 to 6). Of course (as the name suggests) OIJPE should not be treated as an interval or rational variable, but only as an ordinal one.

In the end we would like to introduce technical labels for some of the main variables that may appear throught the output tables in this report: • libsoc: Liberalism-Socialism scale

• ngknow: Non-guessed knowledge score

• knowraw: Knowledge raw score

• **peduord:** Ordinal Indicator of the Joint Parental Education (OIJPE)

Descriptive statistics for knowledge and attitudes

Below we provide numerical summaries for the Liberalism-Socialism scale and the raw and non-guessed knowledge scores in terms of mean and positional parameters (quartiles and deciles).

Descriptives for the Joint Sample

Mean and quartiles

##	libsoc	ngknow	knowraw	
##	Min. :-7.0000	Min. $:-14.000$	Min. : 8.00	
##	1st Qu.:-1.0000	1st Qu.: 0.000	1st Qu.:15.00	
##	Median : 1.0000	Median : 6.000	Median :18.00	
##	Mean : 0.3964	Mean : 5.746	Mean :17.87	
##	3rd Qu.: 2.0000	3rd Qu.: 10.000	3rd Qu.:20.00	
##	Max. : 7.0000	Max. : 22.000	Max. :26.00	
##	NA's :22	NA's :57	NA's :57	

Deciles

```
## $libsoc
     0%
          10%
                20%
                      30%
                            40%
                                  50%
                                        60%
                                             70%
                                                    80%
                                                          90% 100%
##
     -7
            -3
                              0
                                                2
                                                      2
                                                            3
                 -2
                       -1
                                    1
                                          1
##
##
   $ngknow
##
     0%
                20%
                      30%
                            40%
                                  50%
                                        60%
                                             70%
          10%
                                                    80%
                                                          90% 100%
##
           -4
                  0
                        2
                              4
                                    6
                                          8
                                               10
                                                     12
                                                           14
                                                                 22
##
##
   $knowraw
##
     0%
                20%
                            40%
                                        60%
                                              70%
                                                    80%
                                                          90%
                                                              100%
          10%
                      30%
                                  50%
##
           13
                 15
                       16
                             17
                                   18
                                         19
                                               20
                                                     21
                                                           22
```

Descriptives by country

Mean and quartiles

```
## $libsoc
  $libsoc$CZ
##
      Min. 1st Qu.
                                                        NA's
                    Median
                               Mean 3rd Qu.
                                                Max.
  -5.0000 -1.0000
                            0.6832 2.0000
                    1.0000
                                             6.0000
##
## $libsoc$PL
##
      Min. 1st Qu.
                    Median
                               Mean 3rd Qu.
                                                Max.
                                                        NA's
  -7.0000 -2.0000
                    1.0000
                            0.1067
                                     2.0000
                                             7.0000
                                                          15
##
```

```
##
## $ngknow
## $ngknow$CZ
   Min. 1st Qu. Median Mean 3rd Qu.
                                      Max. NA's
    -10.0 2.0 6.0
                         5.8 10.0
                                       18.0
                                               30
##
## $ngknow$PL
    Min. 1st Qu. Median
                         Mean 3rd Qu.
                                       Max.
                                             NA's
## -14.000 0.000 6.000
                        5.694 12.000 22.000
##
##
## $knowraw
## $knowraw$CZ
##
    Min. 1st Qu. Median
                         Mean 3rd Qu.
                                             NA's
                                       Max.
##
     10.0
         16.0
                18.0
                         17.9
                                20.0
                                       24.0
                                               30
##
## $knowraw$PL
    Min. 1st Qu. Median
                       Mean 3rd Qu.
                                      Max.
                                            NA's
     8.00 15.00 18.00 17.85 21.00
                                      26.00
                                               27
Deciles
## $libsoc
## $libsoc$CZ
    0% 10% 20% 30% 40% 50% 60% 70% 80% 90% 100%
##
##
           -1
                -1
                     0
                          1
                            1
                                  2
                                     3
                                           3
##
## $libsoc$PL
##
  0% 10% 20% 30% 40% 50% 60% 70% 80% 90% 100%
##
    -7 -3 -2 -1
                    0
                        1
                              1
                                 1
##
##
## $ngknow
## $ngknow$CZ
   0% 10% 20% 30% 40% 50% 60% 70% 80% 90% 100%
## -10 -2
                         6
           0
               2
                    4
                             8
                                10
                                     12
                                         14
                                             18
## $ngknow$PL
   0% 10% 20% 30% 40% 50% 60% 70% 80% 90% 100%
## -14 -4 -2
                            8 10
               2
                    4
                        6
                                         16
                                              22
                                     12
##
##
## $knowraw
## $knowraw$CZ
   0% 10% 20% 30% 40% 50% 60% 70% 80% 90% 100%
##
    10 14 15
               16
                    17
                        18
                            19
                                 20
                                     21
                                          22
##
## $knowraw$PL
##
   0% 10% 20% 30% 40% 50% 60% 70% 80% 90% 100%
##
   8 13 14 16
                    17
                        18
                            19
                                 20
                                     21
```

Descriptives by education type (EBMF, SSHA and STEM)

Mean and quartiles

-3

\$libsoc\$SSHA

##

-3

-2

-1

-1

1

```
## $libsoc
## $libsoc$EBMF
     Min. 1st Qu. Median
                             Mean 3rd Qu.
                                             Max.
                                                     NA's
## -7.0000 -2.0000 -1.0000 -0.2487 1.0000 7.0000
                                                        5
##
## $libsoc$SSHA
##
     Min. 1st Qu. Median
                             Mean 3rd Qu.
                                             Max.
                                                     NA's
##
     -5.00
           0.00
                     1.00
                             1.04
                                     3.00
                                             6.00
##
## $libsoc$STEM
##
     Min. 1st Qu. Median
                             Mean 3rd Qu.
                                                     NA's
                                             Max.
## -5.0000 -1.0000 1.0000 0.2416 2.0000 6.0000
##
##
## $ngknow
## $ngknow$EBMF
##
     Min. 1st Qu. Median
                             Mean 3rd Qu.
                                             Max.
                                                     NA's
##
     -8.00
             6.00
                    10.00
                             9.76
                                    14.00
                                            22.00
                                                        6
##
## $ngknow$SSHA
     Min. 1st Qu. Median
                             Mean 3rd Qu.
                                             Max.
                                                     NA's
## -14.000 -2.000
                    2.000
                            2.793
                                    8.000 18.000
                                                       18
## $ngknow$STEM
     Min. 1st Qu. Median
                             Mean 3rd Qu.
                                                     NA's
                            5.111 10.000 22.000
##
  -8.000 0.000
                    6.000
                                                       31
##
##
## $knowraw
## $knowraw$EBMF
##
     Min. 1st Qu. Median
                             Mean 3rd Qu.
                                             Max.
                                                     NA's
##
     11.00 18.00
                    20.00
                            19.88
                                    22.00
                                            26.00
                                                        6
##
## $knowraw$SSHA
                                                     NA's
##
     Min. 1st Qu. Median
                             Mean 3rd Qu.
                                             Max.
      8.0
##
           14.0
                     16.0
                             16.4
                                     19.0
                                             24.0
                                                       18
##
## $knowraw$STEM
##
     Min. 1st Qu. Median
                             Mean 3rd Qu.
                                                     NA's
                                             Max.
     11.00 15.00
                   18.00
                            17.56
                                    20.00
                                            26.00
Deciles
## $libsoc
## $libsoc$EBMF
    0% 10% 20% 30% 40%
                            50%
                                 60%
                                     70% 80%
                                                90% 100%
```

```
##
             20% 30% 40% 50% 60% 70% 80% 90% 100%
##
         -2
              -1
                     0
                         1
                               1
                                    2
                                         2
                                              3
                                                   3
##
## $libsoc$STEM
##
    0% 10%
            20%
                  30%
                       40%
                            50%
                                 60%
                                     70% 80%
                                                90% 100%
##
         -3
              -2
                         0
                              1
                                   1
                                         1
                                              2
                                                   3
                   -1
##
##
## $ngknow
##
  $ngknow$EBMF
     0% 10% 20%
                  30%
                       40% 50% 60% 70% 80% 90% 100%
  -8.0 2.0 4.4
                  6.0 8.8 10.0 12.0 14.0 14.0 16.0 22.0
##
##
## $ngknow$SSHA
##
    0% 10% 20%
                  30%
                       40%
                            50%
                                 60%
                                     70% 80%
                                                90% 100%
##
   -14
        -6
              -2
                     0
                          2
                               2
                                    4
                                         6
                                              8
                                                  10
                                                       18
##
## $ngknow$STEM
             20%
##
    0% 10%
                  30%
                       40%
                            50%
                                 60%
                                      70%
                                           80%
                                                 90% 100%
##
         -2
               0
                     2
                         4
                              6
                                   6
                                         8
                                             10
                                                  12
##
##
## $knowraw
## $knowraw$EBMF
    0% 10% 20% 30% 40% 50% 60% 70% 80% 90% 100%
## 11.0 16.0 17.2 18.0 19.4 20.0 21.0 22.0 22.0 23.0 26.0
##
## $knowraw$SSHA
##
    0% 10% 20%
                  30%
                       40%
                            50%
                                 60%
                                      70%
                                           80%
                                                 90% 100%
##
        12
              14
                    15
                         16
                              16
                                   17
                                        18
                                             19
                                                  20
                                                       24
##
## $knowraw$STEM
             20%
##
     0% 10%
                  30%
                        40%
                             50%
                                  60%
                                      70%
                                            80%
                                                 90% 100%
##
                                             20
                                                       26
     11
         14
               15
                    16
                         17
                              18
                                   18
                                        19
                                                  21
```

Descriptives by education type and country

Mean and quartiles

```
## $libsoc
## $libsoc$EBMF.CZ
      Min. 1st Qu.
                      Median
                                  Mean 3rd Qu.
                                                    Max.
                                                             NA's
## -4.00000 -2.00000 0.00000 -0.03125 2.00000 6.00000
                                                                1
##
## $libsoc$SSHA.CZ
##
     Min. 1st Qu.
                   Median
                              Mean 3rd Qu.
                                              Max.
                                                      NA's
##
   -3.000 0.000
                     1.000
                             1.014
                                     2.500
                                             6.000
                                                         5
##
## $libsoc$STEM.CZ
     Min. 1st Qu.
                   Median
                             Mean 3rd Qu.
                                                      NA's
                                              Max.
##
   -5.000 -0.250
                    1.000
                             1.017
                                     3.000
                                             5.000
## $libsoc$EBMF.PL
```

##	Min.	1st Qu.	Median	Mean	3rd Qu.	Max.	NA's			
##	-7.0000	-2.0000	-1.0000	-0.4639	1.0000	7.0000	4			
##										
		\$libsoc\$SSHA.PL								
		1st Qu.								
	-5.000	0.000	1.000	1.089	3.000	4.000	4			
##	47.1	hampy Di								
		STEM.PL	M - 44	W	01 0	M	NA 1 -			
		1st Qu. -2.0000								
##	-5.0000	-2.0000	0.0000	-0.1525	1.0000	6.0000	5			
##										
	\$ngknow									
	_	BEBMF.CZ								
	•	1st Qu.	Median	Mean	3rd Qu.	Max.	NA's			
	-8.00			8.43		18.00				
##										
##	\$ngknow\$	SSHA.CZ								
##	Min.	1st Qu.	Median	Mean	3rd Qu.	Max.	NA's			
	-10.000					16.000				
##										
		\$ngknow\$STEM.CZ								
		1st Qu.								
	-6.000	4.000	6.000	7.098	12.000	18.000	10			
##	A 1 (henve ni								
		BEBMF.PL	M = 4	M	2 0	M	N A I -			
##	-8.00	1st Qu.	12.00	11.01		Max. 22.00				
##	0.00	0.00	12.00	11.01	10.00	22.00	2			
	\$nøknow	SSHA.PL								
		1st Qu.	Median	Mean	3rd Qu.	Max.	NA's			
	-14.00				6.00					
##										
##	\$ngknow	STEM.PL								
##	Min.	1st Qu.	Median	Mean	3rd Qu.	Max.	NA's			
##	-8.000	0.000	4.000	4.118	8.000	22.000	21			
##										
##										
	\$knowrav									
	-	√\$EBMF.CZ			0 1 0		37.4.1			
##		1st Qu.			•					
## ##	11.00	18.00	20.00	19.22	21.00	24.00	4			
	\$knowraw\$SSHA.CZ									
##	-	1st Qu.		Mean	3rd Qu	Max	NA's			
##		15.00			•		16			
##										
##	\$knowraw\$STEM.CZ									
##	Min.	1st Qu.	Median	Mean	3rd Qu.	Max.	NA's			
##	12.00	17.00	18.00	18.55	21.00	24.00	10			
##										
##	\$knowraw\$EBMF.PL									
##		1st Qu.			3rd Qu.					
##	11.00	19.00	21.00	20.51	23.00	26.00	2			

```
##
## $knowraw$SSHA.PL
    Min. 1st Qu. Median
                         Mean 3rd Qu.
                                       {\tt Max.}
                                             NA's
     8.00 13.00 16.00 15.79 18.00
                                      24.00
##
                                                 2
## $knowraw$STEM.PL
                       Mean 3rd Qu.
    Min. 1st Qu. Median
                                              NA's
                                       Max.
    11.00 15.00 17.00 17.06 19.00
##
                                      26.00
                                                21
Deciles
## $libsoc
## $libsoc$EBMF.CZ
   0% 10% 20% 30% 40% 50% 60% 70% 80% 90% 100%
##
   -4 -3 -2 -2 -1
                         0
                             1
                                 1
                                          3
##
## $libsoc$SSHA.CZ
    0% 10% 20% 30% 40% 50% 60% 70% 80% 90% 100%
##
   -3 -1
           -1
                  0
                                   2
                                       3
                    1
                        1
                             1
## $libsoc$STEM.CZ
   0% 10% 20% 30% 40% 50% 60% 70% 80% 90% 100%
    -5 -2 -1
##
               0
                    1
                          1
                              2
                                   2
                                       3
                                           3
##
## $libsoc$EBMF.PL
   0% 10% 20% 30% 40% 50% 60% 70% 80% 90% 100%
## -7.0 -3.4 -3.0 -2.0 -1.0 -1.0 0.0 1.0 2.0 3.0 7.0
## $libsoc$SSHA.PL
## 0% 10% 20% 30% 40% 50% 60% 70% 80% 90% 100%
## -5.0 -2.0 -0.4 1.0 1.0 1.0 2.0 2.0 3.0 3.0 4.0
##
## $libsoc$STEM.PL
##
   0% 10% 20% 30% 40% 50% 60% 70% 80% 90% 100%
    -5 -3 -3 -1
                    -1
                          0
                             1
                                 1
##
##
## $ngknow
## $ngknow$EBMF.CZ
   0% 10% 20% 30% 40% 50% 60% 70% 80% 90% 100%
##
   -8 2
            4
                 6
                    6
                        10
                             10
                                  12
                                      14
                                           14
##
## $ngknow$SSHA.CZ
  0% 10% 20% 30% 40% 50% 60% 70% 80% 90% 100%
##
## -10 -4 -2
                 0
                      2
                          4
                              6
                                  6
                                       8
                                           10
##
## $ngknow$STEM.CZ
   0% 10% 20% 30% 40% 50% 60% 70% 80%
##
                                          90% 100%
##
           4
                 4
                      6
                          6
                              8
                                 10
                                      12
                                           14
## $ngknow$EBMF.PL
  0% 10% 20% 30% 40% 50% 60% 70% 80% 90% 100%
```

-8.0 2.0 6.0 8.0 10.0 12.0 12.0 14.0 16.0 18.4 22.0

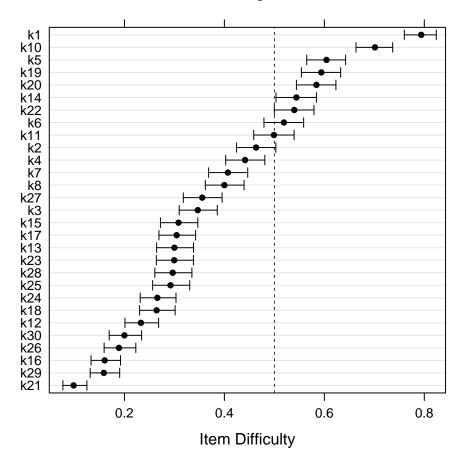
```
##
##
   $ngknow$SSHA.PL
##
     0%
          10%
                20%
                     30%
                           40%
                                 50%
                                       60%
                                            70%
                                                  80%
                                                        90% 100%
                              0
                                   2
                                         4
                                               4
                                                    8
##
           -8
                 -4
                      -2
                                                         10
                                                               18
##
   $ngknow$STEM.PL
##
##
          10%
                20%
                     30%
                           40%
                                       60%
                                            70%
                                                  80%
                                                        90% 100%
                                 50%
           -4
                        0
                              2
                                         6
                                               8
                                                   10
                                                         12
##
                 -2
                                   4
                                                               22
##
##
##
   $knowraw
   $knowraw$EBMF.CZ
##
                     30%
##
     0%
         10%
                20%
                           40%
                                 50%
                                       60%
                                            70%
                                                  80%
                                                        90% 100%
                                  20
                                        20
                                              21
                                                    22
                                                         22
##
     11
           16
                 17
                       18
                            18
                                                               24
##
##
   $knowraw$SSHA.CZ
##
     0%
          10%
                20%
                     30%
                           40%
                                 50%
                                       60%
                                            70%
                                                  80%
                                                        90% 100%
##
           13
                 14
                       15
                            16
                                  17
                                        18
                                              18
                                                   19
                                                         20
                                                               23
##
##
   $knowraw$STEM.CZ
##
     0%
          10%
                20%
                     30%
                           40%
                                 50%
                                       60%
                                            70%
                                                  80%
                                                        90% 100%
##
           15
                 17
                       17
                            18
                                  18
                                        19
                                              20
                                                   21
                                                         22
                                                               24
##
   $knowraw$EBMF.PL
##
     0% 10%
               20%
                     30%
                           40%
                                 50%
                                      60%
                                            70%
                                                  80%
                                                        90% 100%
##
##
   11.0 16.0 18.0 19.0 20.0 21.0 21.0 22.0 23.0 24.2 26.0
##
   $knowraw$SSHA.PL
##
                                                  80%
##
     0%
         10%
                20%
                     30%
                           40%
                                 50%
                                       60%
                                            70%
                                                        90% 100%
##
           11
                 13
                       14
                            15
                                  16
                                        17
                                              17
                                                   19
                                                         20
                                                               24
##
##
   $knowraw$STEM.PL
                                            70%
                                                  80%
                                                        90% 100%
##
     0%
          10%
                20%
                     30%
                           40%
                                 50%
                                       60%
##
                            16
                                              19
                                                   20
                                                         21
                                                               26
     11
           13
                 14
                       15
                                  17
                                        18
```

Analysis of the KNOWLEDGE items set

Now we turn to the analysis of the KNOWLEDGE items set. We will partition it into subsets of easy, medium and tricky items and check whether items orderings in regard to difficulty levels are the same in different subgroups.

For this purpose we will inspect numerical values of difficulty levels (difficulty of an item is of course the fraction of respondents giving the correct answer) and visualize this data using dotplots with 95% Agresti-Coul confidence intervals.

KNOWLEDGE items set in the Joint Sample



We see from the plot that items may be partitioned (according to our rule) in the following way:

```
## $tricky
## [1] "k1" "k10" "k5" "k19" "k20" "k14" "k22"
##
## $medium
## [1] "k6" "k11" "k2"
##
## $easy
## [1] "k4" "k7" "k8" "k27" "k3" "k15" "k17" "k13" "k23" "k28" "k25"
## [12] "k24" "k18" "k12" "k30" "k26" "k16" "k29" "k21"
```

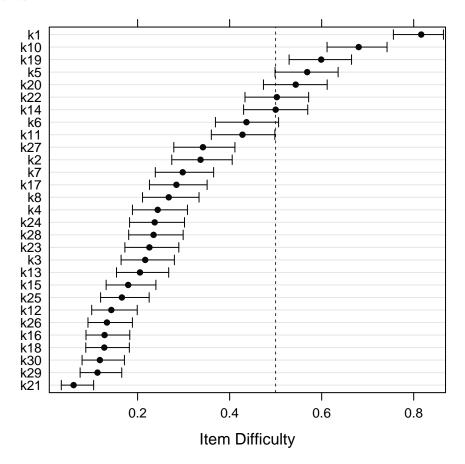
Below we provide numerical values for the difficulties and their confidence intervals:

```
##
       difficulty lower upper
## k1
            0.206 0.176 0.240
## k2
            0.537 0.497 0.576
## k3
            0.653 0.614 0.690
            0.559 0.519 0.597
## k4
## k5
            0.396 0.357 0.435
            0.481 0.441 0.521
## k6
## k7
            0.593 0.553 0.632
            0.600 0.561 0.638
## k8
```

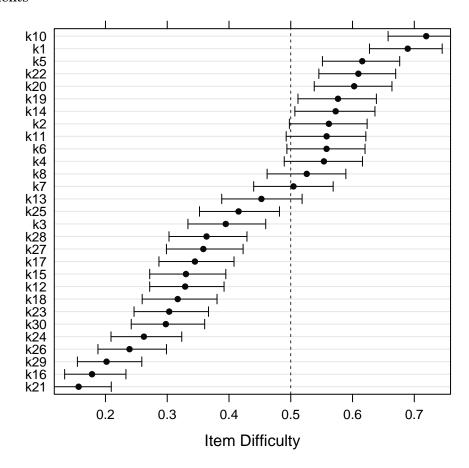
```
0.299 0.263 0.337
## k10
## k11
            0.501 0.460 0.541
            0.767 0.732 0.799
## k12
## k13
            0.700 0.662 0.736
## k14
            0.456 0.416 0.497
## k15
            0.692 0.653 0.728
## k16
            0.839 0.808 0.867
            0.696 0.658 0.731
## k17
## k18
            0.736 0.699 0.770
## k19
            0.406 0.367 0.446
## k20
            0.416 0.377 0.456
            0.902 0.875 0.923
## k21
## k22
            0.460 0.421 0.500
## k23
            0.700 0.662 0.736
## k24
            0.734 0.697 0.768
## k25
            0.708 0.669 0.744
## k26
            0.811 0.777 0.841
            0.644 0.605 0.682
## k27
## k28
            0.703 0.665 0.739
            0.841 0.810 0.869
## k29
            0.800 0.766 0.830
## k30
```

Knowledge scores and type of education

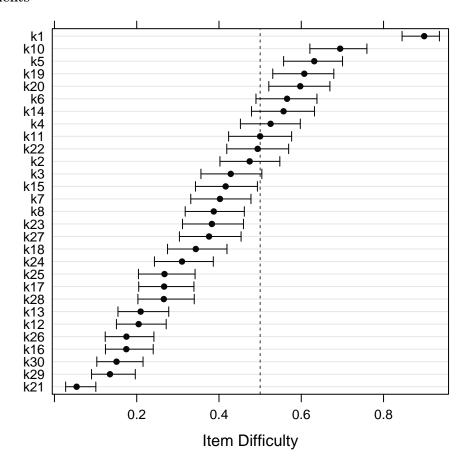
EBMF students



SSHA students

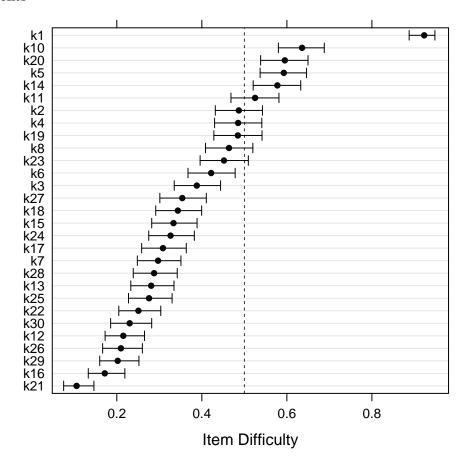


STEM students



Knowledge scores and country

Polish students



We see from the plot that items may be partitioned (according to our rule) in the following way:

```
## $tricky
## [1] "k1" "k10" "k20" "k5" "k14"
##
## $medium
## [1] "k11" "k2" "k4" "k19" "k8" "k23"
##
## $easy
## [1] "k6" "k3" "k27" "k18" "k15" "k24" "k17" "k7" "k28" "k13" "k25"
## [12] "k22" "k30" "k12" "k26" "k29" "k16" "k21"
```

Below we provide numerical values for the difficulties and their confidence intervals:

```
## k1 0.077 0.052 0.112

## k2 0.513 0.457 0.568

## k3 0.612 0.556 0.665

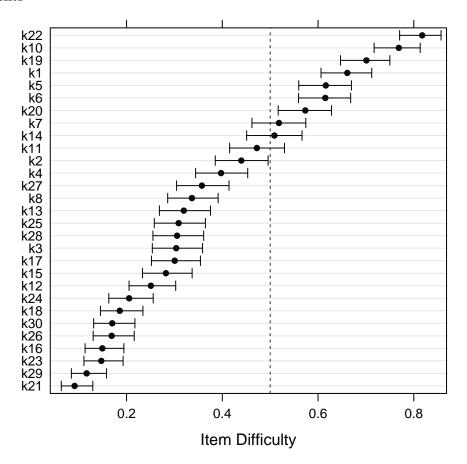
## k4 0.515 0.459 0.570

## k5 0.407 0.354 0.463

## k6 0.578 0.522 0.633
```

```
0.703 0.649 0.752
## k7
## k8
            0.536 0.480 0.591
## k10
            0.364 0.312 0.420
            0.475 0.419 0.531
## k11
## k12
            0.785 0.735 0.828
## k13
            0.719 0.666 0.767
## k14
            0.422 0.367 0.479
            0.667 0.611 0.718
## k15
## k16
            0.828 0.781 0.867
## k17
            0.692 0.637 0.742
## k18
            0.656 0.600 0.708
            0.515 0.458 0.572
## k19
## k20
            0.405 0.350 0.462
## k21
            0.895 0.854 0.925
            0.749 0.697 0.795
## k22
## k23
            0.548 0.491 0.604
## k24
            0.674 0.618 0.725
            0.724 0.670 0.772
## k25
            0.790 0.740 0.833
## k26
            0.646 0.589 0.699
## k27
## k28
            0.712 0.658 0.761
## k29
            0.798 0.748 0.840
            0.770 0.718 0.815
## k30
```

Czech students



We see from the plot that items may be partitioned (according to our rule) in the following way:

```
## $tricky
## [1] "k22" "k10" "k19" "k1"
                               "k5"
                                      "k6"
                                            "k20"
##
## $medium
## [1] "k7"
             "k14" "k11"
##
## $easy
  [1] "k2"
              "k4"
                    "k27" "k8"
                                "k13" "k25" "k28" "k3"
                                                         "k17" "k15" "k12"
## [12] "k24" "k18" "k30" "k26" "k16" "k23" "k29" "k21"
```

Below we provide numerical values for the difficulties and their confidence intervals:

```
##
       difficulty lower upper
## k1
            0.339 0.288 0.394
## k2
            0.560 0.504 0.615
## k3
            0.696 0.641 0.746
## k4
            0.603 0.547 0.656
## k5
            0.384 0.330 0.440
## k6
            0.385 0.332 0.441
            0.482 0.426 0.538
## k7
            0.663 0.609 0.714
## k8
## k10
            0.231 0.187 0.283
## k11
            0.528 0.470 0.585
## k12
            0.749 0.697 0.795
            0.680 0.625 0.731
## k13
## k14
            0.491 0.433 0.549
## k15
            0.718 0.663 0.767
## k16
            0.850 0.806 0.887
## k17
            0.699 0.646 0.748
## k18
            0.814 0.766 0.855
## k19
            0.299 0.250 0.353
## k20
            0.427 0.372 0.483
## k21
            0.908 0.871 0.936
## k22
            0.182 0.143 0.230
## k23
            0.853 0.807 0.889
## k24
            0.795 0.744 0.837
## k25
            0.691 0.635 0.742
## k26
            0.831 0.784 0.870
## k27
            0.643 0.586 0.696
## k28
            0.694 0.639 0.745
## k29
            0.883 0.842 0.915
## k30
            0.830 0.783 0.869
```

Before moving to the next part of the analysis it would be good to compare items partitioning in the Joint Sample and Polish and Czech samples.

```
## Joint Sample
## $tricky
## [1] "k1" "k10" "k5" "k19" "k20" "k14" "k22"
```

```
##
## $medium
##
  [1] "k6"
            "k11" "k2"
##
## $easy
   [1] "k4"
             "k7" "k8" "k27" "k3" "k15" "k17" "k13" "k23" "k28" "k25"
##
## [12] "k24" "k18" "k12" "k30" "k26" "k16" "k29" "k21"
## PL Sample
## $tricky
## [1] "k1"
            "k10" "k20" "k5" "k14"
## $medium
## [1] "k11" "k2"
                   "k4"
                         "k19" "k8"
##
## $easy
   [1] "k6"
              "k3" "k27" "k18" "k15" "k24" "k17" "k7" "k28" "k13" "k25"
## [12] "k22" "k30" "k12" "k26" "k29" "k16" "k21"
## CZ Sample
## $tricky
## [1] "k22" "k10" "k19" "k1"
##
## $medium
## [1] "k7" "k14" "k11"
##
## $easy
   [1] "k2"
              "k4"
                   "k27" "k8"
                                "k13" "k25" "k28" "k3"
                                                        "k17" "k15" "k12"
## [12] "k24" "k18" "k30" "k26" "k16" "k23" "k29" "k21"
```

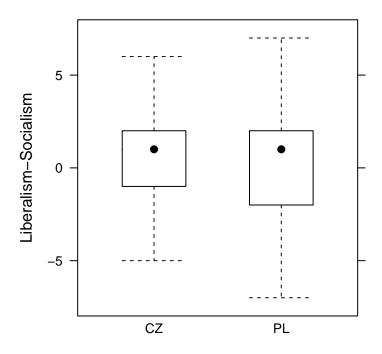
Clearly some items do overlap in different groups, but not all of them.

Associations analysis

In this section we will examine various associations between knowledge scores and the Liberalism-Socialism axis as well as parental education, work experience and type of education.

Liberalism-Socialism amongst Polish and Czech students

We begin with an analysis of the differences in regard to the Liberalism-Socialism scale scores between Polish and Czech students. We see that the distributions are slightly different - the Polish one is more spread out and shifted a bit more in the direction of liberalism; however both have means above zero, that is on the 'socialist' side of the scale.



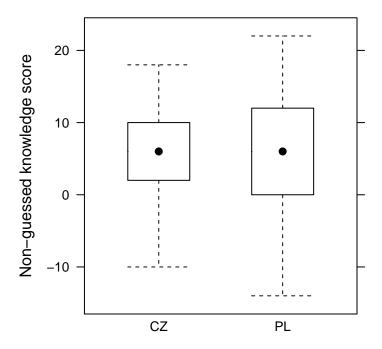
```
## country libsoc.mean libsoc.sd
## 1 CZ 0.6831683 2.152762
## 2 PL 0.1066667 2.369389
```

Formal test show that indeed Polish students are closer to the midpoint of the scale, while Czechs gravitate more to the side of socialism. Although the effect is significant its magnitude is rather small (as Cohen's d coefficients shows).

```
##
   Welch Two Sample t-test
##
##
## data: libsoc by country
## t = 3.1261, df = 594.38, p-value = 0.001858
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
   0.2143203 0.9386830
## sample estimates:
  mean in group CZ mean in group PL
          0.6831683
                           0.1066667
##
##
## Cohen's d
##
## d estimate: 0.2547366 (small)
## 95 percent confidence interval:
##
          inf
                     sup
## 0.09386418 0.41560912
```

Knowledge scores in the Polish and Czech samples

In this case distributions are very similar (since non-guessed score is a function of raw score we show charts only for the non-guessed).



```
## country ngknow.mean knowraw.mean ngknow.sd knowraw.sd
## 1 CZ 5.800000 17.90000 5.973898 2.986949
## 2 PL 5.694444 17.84722 7.644795 3.822398
```

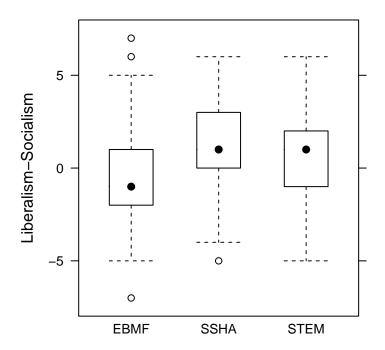
Formal tests also prove that there is no significant difference in this regard between the samples.

```
## $ngknow
##
##
   Welch Two Sample t-test
##
## data: x by data$country
## t = 0.18364, df = 541.14, p-value = 0.8544
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
   -1.023535 1.234646
## sample estimates:
  mean in group CZ mean in group PL
##
           5.800000
                            5.694444
##
##
## $knowraw
##
##
   Welch Two Sample t-test
##
## data: x by data$country
## t = 0.18364, df = 541.14, p-value = 0.8544
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
   -0.5117673 0.6173229
## sample estimates:
## mean in group CZ mean in group PL
           17.90000
                            17.84722
##
```

```
## $ngknow
##
##
  Cohen's d
##
##
  d estimate: 0.01535998 (negligible)
##
  95 percent confidence interval:
          inf
                      sup
## -0.1497788
               0.1804988
##
##
   $knowraw
##
## Cohen's d
##
## d estimate: 0.01535998 (negligible)
## 95 percent confidence interval:
##
          inf
                      sup
## -0.1497788
               0.1804988
```

Liberalism-Socialism and education type

Now we compare education type groups (EBMF, SSHA and STEM) in a context of the Liberalism-Socailism scale scores. It is easy to see that EBMF group is shifted towards liberalism, while SSHA tends to have stronger socialist attitudes. The STEM group is between and closie to the midpoint.



```
## eduprog3 libsoc.mean libsoc.sd

## 1 EBMF -0.2487047 2.455926

## 2 SSHA 1.0398230 1.921390

## 3 STEM 0.2415730 2.310150
```

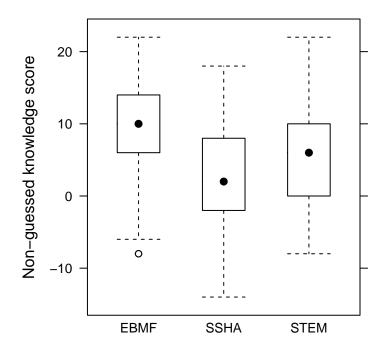
A formal test (ANOVA) shows that education type matters and that about 5.7% of the variance of the Liberalism-Socialism scale scores is associated with it. Moreover EBMF mean is not significantly greater

than 0 (the scale's midpoint) and both STEM and SSHA groups have higher (more socialist) means than it - although this effect is stronger in the SSHA group.

```
##
## Call:
## lm(formula = libsoc ~ eduprog3, data = data)
##
## Residuals:
##
       Min
                1Q
                    Median
                                 3Q
                                        Max
                            1.7584
##
   -6.7513 -1.7513 -0.0398
                                     7.2487
##
## Coefficients:
##
                Estimate Std. Error t value Pr(>|t|)
                 -0.2487
                              0.1600
                                      -1.555
                                               0.1205
##
  (Intercept)
  eduprog3SSHA
                  1.2885
                              0.2178
                                       5.916 5.57e-09 ***
  eduprog3STEM
                  0.4903
                              0.2309
                                       2.123
                                               0.0342 *
##
                     '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## Signif. codes:
                   0
##
## Residual standard error: 2.222 on 594 degrees of freedom
     (28 observations deleted due to missingness)
## Multiple R-squared: 0.05723,
                                     Adjusted R-squared:
## F-statistic: 18.03 on 2 and 594 DF, p-value: 2.501e-08
```

Knowledge scores and education type

Without a doubt the EBMF group have much higher scores. On average EBMF students gave almost 10 correct answers without guessing while STEM students gave about 5 and SSHA students below 3.



```
## eduprog3 ngknow.mean knowraw.mean ngknow.sd knowraw.sd
## 1 EBMF 9.760417 19.88021 6.187718 3.093859
```

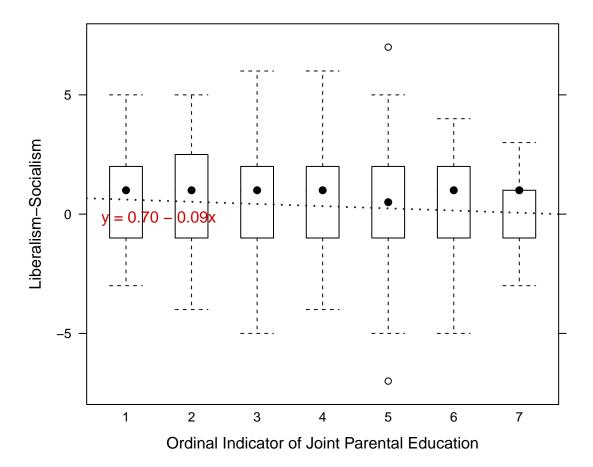
```
## 2 SSHA 2.792627 16.39631 6.149250 3.074625
## 3 STEM 5.111111 17.55556 6.047570 3.023785
```

19.3% of variance of the knowledge scores is associated with the effect of education type and both STEM and SSHA groups have significantly lower means than the EBMF group.

```
##
## Call:
## lm(formula = ngknow ~ eduprog3, data = data)
##
## Residuals:
##
        Min
                  1Q
                       Median
                                    3Q
                                            Max
                       0.8889
##
  -17.7604
            -3.7604
                                4.2396
                                       16.8889
##
## Coefficients:
##
                Estimate Std. Error t value Pr(>|t|)
                  9.7604
                             0.4428 22.045 < 2e-16 ***
## (Intercept)
## eduprog3SSHA
                 -6.9678
                             0.6078 -11.463
                                            < 2e-16 ***
                 -4.6493
                             0.6649 -6.993 7.71e-12 ***
  eduprog3STEM
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 6.135 on 559 degrees of freedom
     (63 observations deleted due to missingness)
## Multiple R-squared: 0.1935, Adjusted R-squared: 0.1906
## F-statistic: 67.04 on 2 and 559 DF, p-value: < 2.2e-16
```

Liberalism-Socialism and OIJPE

Numerical values show that there is some variation in the group means, however it is hard to say whether it is something more than noise. The line on the plot depicts the linear regression model that tries to predict group means assuming that the relationship between the Liberalism-Socialism scale scores nad the OIJPE values is close to linear.



```
peduord libsoc.mean libsoc.sd
##
## 1
                0.6250000
                            2.226732
## 2
            1
                            2.284957
                0.6323529
## 3
                0.3962264
                            2.105228
## 4
           3
                0.6899225
                            2.221340
## 5
           4
                0.2241379
                            2.373089
           5
## 6
                0.2142857
                            2.484875
## 7
           6
                0.1764706
                            1.740521
```

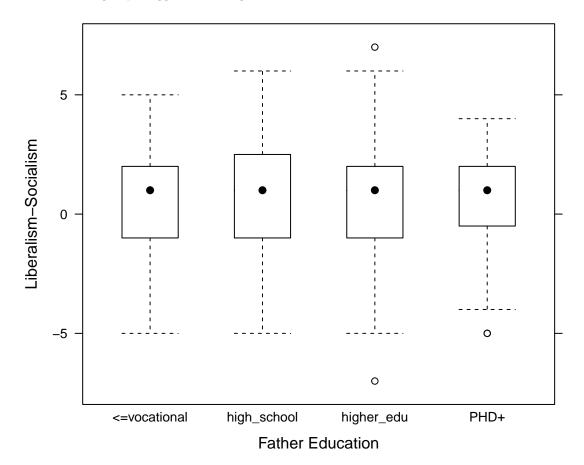
A formal test shows that there is no significant relationship between the Liberalism-Socialism scale scores and the OIJPE scores.

```
##
## Call:
## lm(formula = libsoc ~ peduord, data = data)
##
##
  Residuals:
##
       Min
                1Q
                                 3Q
                    Median
                                        Max
##
   -7.3341 -1.5184
                    0.4816
                             1.6429
                                     6.6659
##
##
  Coefficients:
               Estimate Std. Error t value Pr(>|t|)
##
## (Intercept)
                0.70271
                            0.21109
                                      3.329 0.000929 ***
               -0.09216
## peduord
                            0.06600
                                     -1.396 0.163135
## ---
```

```
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 2.253 on 560 degrees of freedom
## (63 observations deleted due to missingness)
## Multiple R-squared: 0.00347, Adjusted R-squared: 0.001691
## F-statistic: 1.95 on 1 and 560 DF, p-value: 0.1631
```

Liberalism-Socialism and father education

Distributions in the groups suggest no strong association.



father_edu libsoc.mean libsoc.sd ## 1 <=vocational 0.4628099 2.232492 high_school 0.5945946 2.212635 ## 2 2.307708 ## 3 higher_edu 0.3067729 ## 4 PHD+ 0.5813953 2.162809

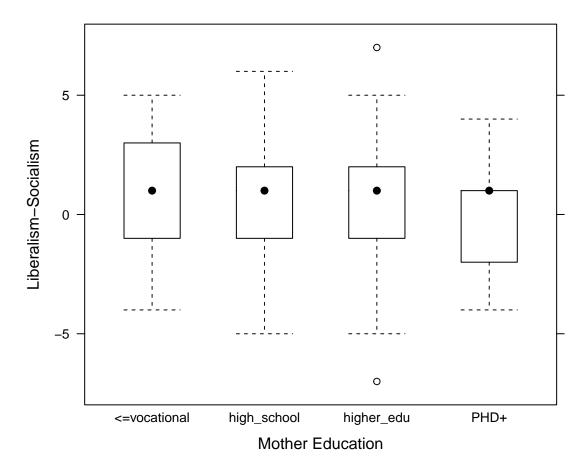
A formal test confirms this supposition. There is no significant relationship between the variables.

```
##
## Call:
## lm(formula = libsoc ~ father_edu, data = data)
##
## Residuals:
```

```
##
                1Q
                    Median
                                 3Q
                                        Max
##
  -7.3068 -1.5814
                   0.4054
                           1.6932
                                    6.6932
##
## Coefficients:
##
                         Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                           0.4628
                                       0.2051
                                                2.256
                                                        0.0244 *
## father_eduhigh_school
                           0.1318
                                       0.2765
                                                0.477
                                                        0.6339
## father_eduhigher_edu
                                               -0.625
                          -0.1560
                                       0.2497
                                                        0.5323
## father_eduPHD+
                           0.1186
                                       0.4006
                                                0.296
                                                        0.7673
##
## Signif. codes:
                   0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 2.256 on 559 degrees of freedom
     (62 observations deleted due to missingness)
##
## Multiple R-squared: 0.003121,
                                    Adjusted R-squared:
## F-statistic: 0.5834 on 3 and 559 DF, p-value: 0.6261
```

Liberalism-Socialism and mother education

In this case it seems that the higher mother education is the more centrist attitudes a child has.



```
## mother_edu libsoc.mean libsoc.sd
## 1 <=vocational 0.7187500 2.333121
## 2 high_school 0.6030151 2.095737</pre>
```

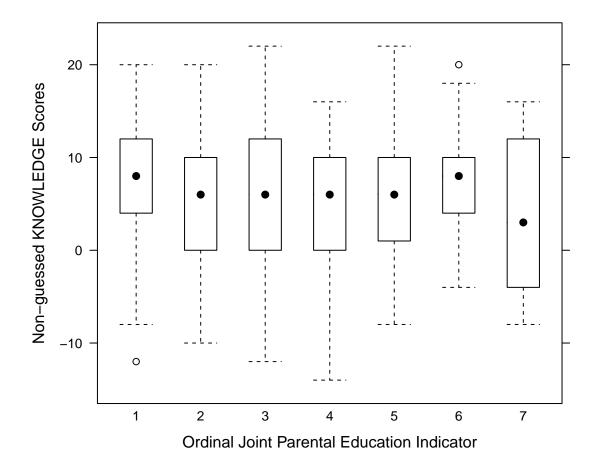
```
## 3 higher_edu 0.2820513 2.352472
## 4 PHD+ 0.0000000 2.154729
```

However, formal testing does not confirm this.

```
##
## Call:
## lm(formula = libsoc ~ mother_edu, data = data)
## Residuals:
##
      Min
              1Q Median
                            3Q
                                  Max
## -7.282 -1.603 0.397
                        1.718
                                6.718
## Coefficients:
##
                         Estimate Std. Error t value Pr(>|t|)
                                               2.552
                                                        0.011 *
## (Intercept)
                           0.7187
                                      0.2816
## mother_eduhigh_school -0.1157
                                      0.3238 -0.357
                                                        0.721
## mother_eduhigher_edu
                          -0.4367
                                      0.3129
                                              -1.396
                                                        0.163
## mother_eduPHD+
                                      0.5043 -1.425
                          -0.7188
                                                        0.155
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 2.253 on 561 degrees of freedom
     (60 observations deleted due to missingness)
## Multiple R-squared: 0.007884,
                                    Adjusted R-squared:
## F-statistic: 1.486 on 3 and 561 DF, p-value: 0.2173
```

Knowledge scores and OIJPE

Distributions suggest that there is no clear relationship with the OIJPE scores.



```
##
     peduord ngknow.mean knowraw.mean ngknow.sd knowraw.sd
                6.857143
                                        7.034130
## 1
           0
                              18.42857
                                                    3.517065
## 2
           1
                5.441176
                              17.72059
                                       7.029538
                                                    3.514769
## 3
                5.557692
                              17.77885
                                        7.368032
                                                    3.684016
## 4
           3
                5.190083
                              17.59504
                                        6.199884
                                                    3.099942
## 5
           4
                5.964912
                              17.98246
                                        7.020889
                                                    3.510444
           5
## 6
                7.172414
                              18.58621
                                        6.083167
                                                    3.041584
## 7
           6
                4.142857
                              17.07143 7.979369
                                                    3.989685
```

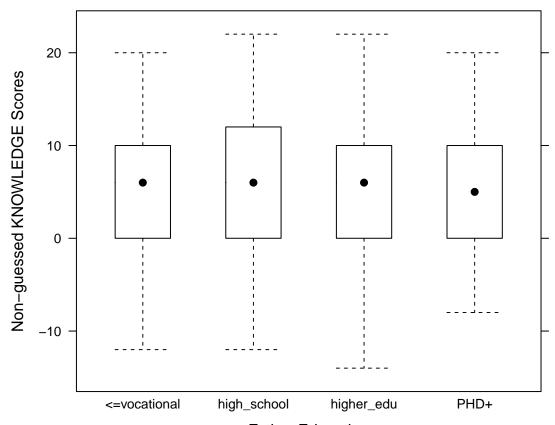
Formal testing confirms this.

```
##
## Call:
## lm(formula = ngknow ~ peduord, data = data)
##
## Residuals:
##
        Min
                  1Q
                       Median
                                    3Q
                                            Max
   -19.7227 -5.7186
                       0.2773
                                4.2855
##
                                        16.2814
##
## Coefficients:
                Estimate Std. Error t value Pr(>|t|)
## (Intercept) 5.734974
                           0.665892
                                      8.612
                                              <2e-16 ***
## peduord
               -0.004095
                           0.208318
                                     -0.020
                                               0.984
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

```
##
## Residual standard error: 6.89 on 540 degrees of freedom
## (83 observations deleted due to missingness)
## Multiple R-squared: 7.156e-07, Adjusted R-squared: -0.001851
## F-statistic: 0.0003864 on 1 and 540 DF, p-value: 0.9843
```

Knowledge scores and father education

Again distributions show no pattern.



Father Education

```
##
       father_edu ngknow.mean knowraw.mean ngknow.sd knowraw.sd
## 1 <=vocational
                     5.155172
                                   17.57759
                                            7.033588
                                                         3.516794
                                   18.02778
     high_school
                     6.055556
                                             6.915856
## 2
                                                         3.457928
## 3
       higher_edu
                     5.777778
                                   17.88889
                                             6.832107
                                                         3.416053
## 4
             PHD+
                                   17.87500 6.735859
                     5.750000
                                                         3.367929
```

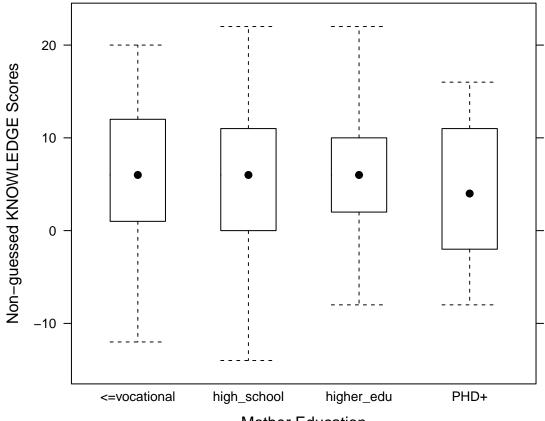
And formal testing confirms it too.

```
##
## Call:
## lm(formula = ngknow ~ father_edu, data = data)
##
## Residuals:
## Min 1Q Median 3Q Max
```

```
## -19.7778 -5.4526
                       0.2222
                                4.8448 16.2222
##
## Coefficients:
                         Estimate Std. Error t value Pr(>|t|)
##
## (Intercept)
                           5.1552
                                      0.6398
                                               8.057 5.04e-15 ***
## father_eduhigh_school
                           0.9004
                                      0.8597
                                                1.047
                                                         0.295
## father_eduhigher_edu
                           0.6226
                                      0.7777
                                                0.801
                                                         0.424
                                                0.471
                                                         0.638
## father_eduPHD+
                           0.5948
                                      1.2635
## ---
                   0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## Signif. codes:
## Residual standard error: 6.891 on 539 degrees of freedom
     (82 observations deleted due to missingness)
## Multiple R-squared: 0.002108,
                                    Adjusted R-squared:
## F-statistic: 0.3795 on 3 and 539 DF, p-value: 0.7678
```

Knowledge scores and mother education

No clear pattern in distributions.



Mother Education

```
mother_edu ngknow.mean knowraw.mean ngknow.sd knowraw.sd
## 1 <=vocational
                     6.237288
                                  18.11864
                                            6.919087
                                                        3.459543
## 2
    high_school
                     5.560209
                                  17.78010 7.001901
                                                        3.500951
## 3
       higher_edu
                     5.835821
                                  17.91791
                                            6.746556
                                                        3.373278
## 4
             PHD+
                                  17.25926 7.515985
                     4.518519
                                                        3.757992
```

Formal testing shows that indeed there is no association between the variables.

```
##
## Call:
## lm(formula = libsoc ~ mother_edu, data = data)
## Residuals:
##
      Min
              1Q Median
                             3Q
                                   Max
                          1.718
##
  -7.282 -1.603 0.397
                                 6.718
##
## Coefficients:
##
                          Estimate Std. Error t value Pr(>|t|)
                                                 2.552
## (Intercept)
                            0.7187
                                       0.2816
                                                          0.011 *
                          -0.1157
                                               -0.357
                                                          0.721
## mother_eduhigh_school
                                       0.3238
## mother eduhigher edu
                           -0.4367
                                       0.3129
                                               -1.396
                                                          0.163
## mother_eduPHD+
                           -0.7188
                                       0.5043
                                               -1.425
                                                          0.155
##
                   0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## Signif. codes:
##
## Residual standard error: 2.253 on 561 degrees of freedom
     (60 observations deleted due to missingness)
## Multiple R-squared: 0.007884,
                                     Adjusted R-squared:
                                                           0.002579
## F-statistic: 1.486 on 3 and 561 DF, p-value: 0.2173
```

Knowledge scores and the Liberalism-Socialism scale

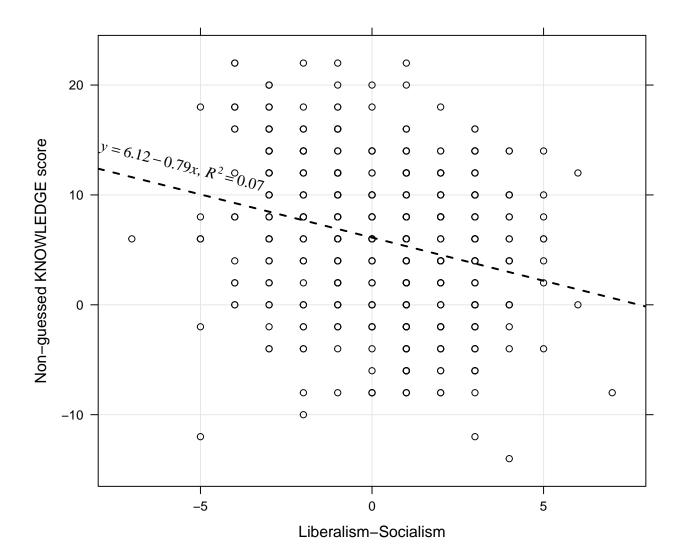
Now we turn to the problem of the relationship between the knowledge scores and the Liberalism-Socialism scale scores. Simple correlation coefficient indicates that there may be some sort of an association. The negative value of the coefficient shows that the negative pole of the Liberalism-Socialism scale (that is liberalism) is related to better knowledge scores.

```
## libsc ngknw
## libsoc 1.00
## ngknow -0.26 1.00
```

Regression model shows that indeed there is significant relationship of such kind; Liberalism-Socialism scale scores are associated with 6.9% of the variance of the knowledge scores and on average the stronger liberal attitude of a person is, the better knowledge score he or she gets. According to the model equation (see the plot below) a person with a score of -5 on the Liberalism-Socialism (quite strong liberal attitude) axis would give about 10 nonrandom correct answers, while a person with a score of 5 (quite strong socialist attitude) on the axis would give only about 2 nonrandom correct answers.

```
##
## Call:
  lm(formula = ngknow ~ libsoc, data = data, subset = knowIV ==
##
##
## Residuals:
##
                                  3Q
                                         Max
       Min
                 1Q
                     Median
## -22.047
            -4.904
                      0.239
                              5.096
                                      16.668
##
## Coefficients:
```

```
##
               Estimate Std. Error t value Pr(>|t|)
                 6.1183
                            0.2845
                                    21.502 < 2e-16 ***
## (Intercept)
                -0.7858
                            0.1229
##
  libsoc
                                    -6.396 3.43e-10 ***
##
## Signif. codes:
                           0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 6.595 on 547 degrees of freedom
##
     (19 observations deleted due to missingness)
## Multiple R-squared: 0.06958,
                                    Adjusted R-squared: 0.06788
## F-statistic: 40.91 on 1 and 547 DF, p-value: 3.427e-10
```



Knowledge scores and the Liberalism-Socialism scale while controlling for country

Now we extends the model in order to control for the effect of a country, since the dynamics of this relationship may differ between Poland and Czech Republic. Correlation coefficients in countries suggest that the effect may be weaker in amongst Czech students.

Polish sample

```
## libsc ngknw
## libsoc 1.00
## ngknow -0.32 1.00

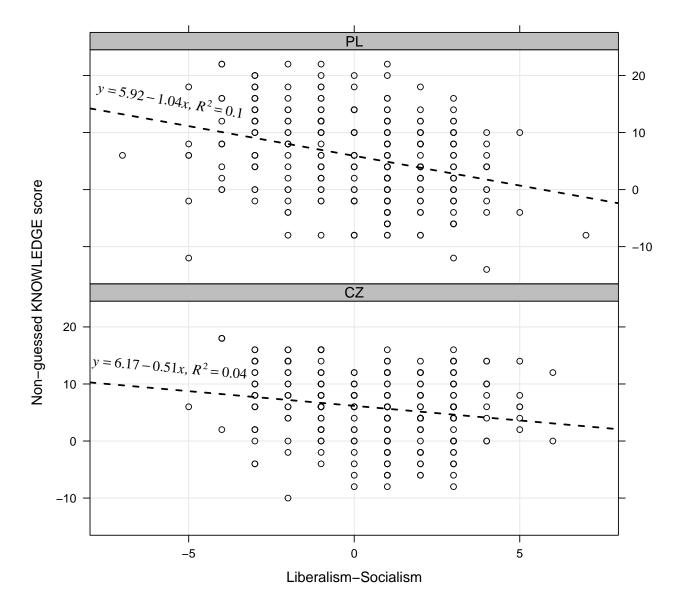
## Czech sample

## libsc ngknw
## libsoc 1.00
## ngknow -0.19 1.00
```

Formal test indeed showed that there is a significant effect of an interaction between country and liberalism-socialism, which cause the effect in the Polish sample to be more than two times stronger than the corresponding effect in the Czech sample. In the Polish sample 10.5% of the variance of the knowledge scores is associated with the liberalism-socialism scale scores, while in the Czech sample it is only 3.5%. In the Joint Sample it is 7.8%.

```
##
## Call:
## lm(formula = ngknow ~ libsoc * country, data = data, subset = knowIV ==
##
       0)
##
## Residuals:
##
        Min
                  1Q
                       Median
                                    3Q
                                            Max
  -23.1270 -4.7945
                       0.1639
                                5.0392
                                        17.1223
##
## Coefficients:
##
                    Estimate Std. Error t value Pr(>|t|)
                                        14.954
## (Intercept)
                      6.1690
                                 0.4125
                                                 < 2e-16 ***
## libsoc
                     -0.5137
                                 0.1813
                                         -2.833
                                                 0.00479 **
## countryPL
                     -0.2497
                                 0.5723
                                         -0.436
                                                 0.66275
                                                 0.03333 *
## libsoc:countryPL
                    -0.5279
                                 0.2474
                                        -2.133
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 6.576 on 545 degrees of freedom
     (19 observations deleted due to missingness)
## Multiple R-squared: 0.07831,
                                    Adjusted R-squared:
## F-statistic: 15.43 on 3 and 545 DF, p-value: 1.193e-09
##
## Call:
## lm(formula = ngknow ~ libsoc, data = data, subset = knowIV ==
##
       0 & country == "PL")
##
## Residuals:
                  1Q
                       Median
                                    3Q
        Min
##
  -23.1270 -5.0439
                       0.0808
                                5.1223
                                        17.1223
##
## Coefficients:
               Estimate Std. Error t value Pr(>|t|)
##
## (Intercept)
                 5.9192
                            0.4345 13.624 < 2e-16 ***
                -1.0416
                            0.1844
                                   -5.649 4.05e-08 ***
## libsoc
## ---
```

```
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 7.202 on 273 degrees of freedom
## (13 observations deleted due to missingness)
## Multiple R-squared: 0.1047, Adjusted R-squared: 0.1014
## F-statistic: 31.91 on 1 and 273 DF, p-value: 4.045e-08
##
## Call:
## lm(formula = ngknow ~ libsoc, data = data, subset = knowIV ==
      0 & country == "CZ")
##
## Residuals:
       Min
               1Q Median
                                 3Q
                                         Max
## -17.1963 -4.1690 0.3447 4.3857 11.3720
## Coefficients:
             Estimate Std. Error t value Pr(>|t|)
## (Intercept) 6.1690 0.3689 16.721 < 2e-16 ***
                          0.1622 -3.167 0.00171 **
## libsoc
             -0.5137
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 5.881 on 272 degrees of freedom
## (6 observations deleted due to missingness)
## Multiple R-squared: 0.03557, Adjusted R-squared: 0.03203
## F-statistic: 10.03 on 1 and 272 DF, p-value: 0.001713
```



Knowledge scores and the Liberalism-Socialism scale while controlling for education type

Correlation coefficients in group suggest that the relationship is much stronger in the EBMF group.

```
## EBMF

## libsc ngknw
## libsoc 1.00

## ngknow -0.36 1.00

## SSHA

## libsc ngknw
## libsoc 1.00

## ngknow -0.05 1.00

## STEM
```

```
## libsoc 1.0
## ngknow -0.1 1.0
```

Formal test confirms that there is an interaction between education type and liberalism-socialism scores. The model parameters show that in this case the interaction means that in the EBMF group association between liberalism-socialism scoresn and knowledge scores is much stronger (in SSHA group it is even non-existent see the equations on the plot). The model with interaction explains about 22.7% of the variance (fractions of variance explained in the subgroup are on the plot).

```
##
## Call:
## lm(formula = ngknow ~ libsoc * eduprog3, data = data, subset = knowIV ==
##
##
## Residuals:
##
       Min
                  1Q
                       Median
                                    3Q
                                             Max
## -16.4036 -4.3507
                       0.7367
                                4.3871
                                        15.6243
##
  Coefficients:
##
                       Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                         9.4381
                                    0.4414 21.384 < 2e-16 ***
## libsoc
                        -0.9126
                                    0.1772
                                            -5.149 3.67e-07 ***
## eduprog3SSHA
                        -6.4313
                                    0.6454
                                            -9.965 < 2e-16 ***
## eduprog3STEM
                        -4.1239
                                    0.6634
                                             -6.217 1.02e-09 ***
## libsoc:eduprog3SSHA
                         0.7618
                                    0.2779
                                              2.741
                                                    0.00633 **
## libsoc:eduprog3STEM
                                    0.2819
                                             2.296 0.02207 *
                         0.6472
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 6.017 on 539 degrees of freedom
     (23 observations deleted due to missingness)
## Multiple R-squared: 0.2266, Adjusted R-squared: 0.2194
## F-statistic: 31.58 on 5 and 539 DF, p-value: < 2.2e-16
```

