

¹ Supplementary information for ‘Warming waters increase mortality
² for global snow crab populations’

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⁴ **Contents**

⁵ Methods overview	²
⁶ Assessment data	²
⁷ Eastern Bering Sea	²
⁸ Newfoundland	²
⁹ Gulf of St Lawrence	²
¹⁰ Korea	²
¹¹ Barents Sea	²
¹² Japan	²
¹³ Russia/Greenland?	²
¹⁴ Population dynamics model	²
¹⁵ Size structured population	²
¹⁶ Objective function	⁴
¹⁷ Penalties and priors	⁴
¹⁸ Generalized additive models	⁴
¹⁹ Structure	⁴
²⁰ Model fits and diagnostics	⁴
²¹ Population dynamics models convergence	⁴
²² GAM convergence	⁴
²³ Eastern Bering Sea	⁴
²⁴ Newfoundland	⁴
²⁵ Gulf of St Lawrence	⁴
²⁶ Korea	⁴
²⁷ Barents Sea	⁴
²⁸ Japan	⁴
²⁹ Russia/Greenland?	⁴
³⁰ Next steps and caveats	⁴

31 **Methods overview**

32 **Assessment data**

33 **Eastern Bering Sea**

34 **Newfoundland**

35 **Gulf of St Lawrence**

36 **Korea**

37 **Barents Sea**

38 **Japan**

39 **Russia/Greenland?**

40 **Population dynamics model**

41 **Size structured population**

42 The population dynamics model presented here incorporates the best available information on relevant
43 population processes. The model tracks numbers of male crab at size (s) (and maturity state (m) for
44 Chionoecetes) over time ($N_{t,s,m}$) with 5 mm size bins over different ranges of sizes for each population
45 (??). Other mortality (M) is estimated by year (y) (and maturity state (m) for Chionoecetes); fully-selected
46 fishing mortality (F) is estimated by year (y). Other estimated parameters include the initial numbers
47 at size by maturity state, an average recruitment, yearly recruitment deviations, a vector of scalars that
48 determine the proportions of estimated recruitment split into the first three size bins, fishery selectivity, and
49 survey selectivity (see ?? for a list of what parameters are estimated for each stock. Parameters determining
50 growth and maturity are estimated outside of the model based on available data from stock assessments.
51 The timing of the fishery is different for each population and is denoted by the month in which it occurs (q
52 below). Mortality is the only population process that occurs during the first several months of a given year
53 (the crab year begins in July with the bottom trawl survey):

$$N_{t=y+q/12,s,m} = N_{t=y,s,m} e^{-(\frac{q}{12})M_{t,s,m}} \quad (1)$$

54 Fishing occurs as a pulse fishery in which the crab captured and brought on deck of fishing vessels (C_{cap}) are
55 a function of capture selectivity (S_{cap}), the number of crab in the Bering Sea at the time of fishing, and the
56 fishing mortality applied (F_t). A retention ogive (S_{ret}) is applied to the captured crab to determine what
57 fraction of crab at a given size are retained for sale (C_{ret}) and what fraction are discarded back into the
58 ocean (C_{disc}). A discard mortality (d_{mort}) of 25% is applied to the crab returned to the ocean.

$$C_{cap,y} = n_{t=y+q/12,s,m} (1 - e^{-F_t * S_{cap}}) \quad (2)$$

$$C_{ret,y} = C_{cap,y} * S_{ret} \quad (3)$$

$$n_{t=y+q/12,s,m} = n_{t=y+q/12,s,m} e^{-F_t * S_{cap}} + n_{t=y+q/12,s,m} + (1 - d_{mort})C_{cap,y}(1 - S_{ret}) \quad (4)$$

61 Capture selectivity and retention selectivity are logistic functions of size in which the slope and size at which
62 50% selectivity are estimated (two time-invariant parameters for each ogive).

$$S_{cap,s} = \frac{1}{1 + exp(-S_{slope,cap}(size(s) - S_{50,cap}))} \quad (5)$$

63

$$S_{ret,s} = \frac{1}{1 + exp(-S_{slope,ret}(size(s) - S_{50,ret}))} \quad (6)$$

64 Growth occurs after fishing and is represented in the model by multiplying the vector of immature crab
 65 at size by a size-transition matrix $X_{s,s'}$ that defines the size to which crab grow given an initial size. this
 66 process results in two temporary vectors of numbers at size for Chionoecetes species where immature crab
 67 are denoted by the subscript m=1 and mature by m=2.

$$n_{t=y+q/12,s,m=immature} = z_s(1 - \rho_{y,s})X_{s,s'}n_{t=y+q/12,s,m=1} \quad (7)$$

$$n_{t=y+q/12,s,m=mature} = z_s\rho_{y,s}X_{s,s'}n_{t=y+q/12,s,m=1} + (1 - z_s)n_{t=y+q/12,s,m=2} \quad (8)$$

68 A single equation can describe king crab species given the lack of a terminal molt:

$$n_{t=y+q/12,s} = (1 - z_s)X_{s,s'}n_{t=y+q/12,s} + z_sX_{s,s'}n_{t=y+q/12,s} \quad (9)$$

70 The size transition matrices $X_{w,w'}$ used here were constructed using growth increment or tagging data
 71 collected over several years (see assessments for a summary) to estimate a linear relationship between pre-
 72 and post-molt carapace width, (\hat{W}_w^{pre} and \hat{W}_w^{post} , respectively) and the variability around that relationship
 73 was characterized by a discretized and renormalized normal distribution, $Y_{w,w'}$, where w and w' represent
 74 entries in the rows and columns of the matrix.

$$X_{w,w'} = \frac{Y_{w,w'}}{\sum_{w'} Y_{w,w'}} \quad (10)$$

$$Y_{w,w'} = (\bar{W}_{w'} + 2.5 - W_w)^{\frac{\hat{W}_w - (\bar{W}_w - 2.5)}{\beta}} \quad (11)$$

$$\hat{W}_w^{post} = \alpha_+ \beta_1 \hat{W}_w^{pre} \quad (12)$$

75 Where α , β , and β_1 are parameters estimated outside of the population dynamics model.

76 The probability of maturing (ρ) and molting probability (z) are handled differently for king crab vs. Chio-
 77 noecetes species. Chionoecetes species have a terminal molt to maturity, after which they do not grow again
 78 (Tamone et al. 1995). The probability of maturing is based on the observed ogives of the proportion of
 79 mature new shell males by size calculated from chelae height measured in the NMFS survey data (Richar-
 80 and Foy, 2022). These observed probabilities of having undergone terminal molt are input as data in the
 81 model. All immature individuals of Chionoecetes species are assumed to molt (i.e. $z = 1$). King crab do not
 82 have a molt to maturity, but the probability of molting varies with size. Here, a declining logistic function
 83 was estimated for each king crab species within the model:

$$z_s = 1 - \frac{1}{1 + exp(-m_s(size(s) - m_{50}))} \quad (13)$$

84 Where the size at 50% molting probability is m_{50} and the slope of the logistic function is m_s .
 85 Recruitment by year was estimated as a vector of deviations (τ_y) around a mean (μ) in log space and
 86 added to the first three size of classes of crab based on another vector that is determined by the estimated
 87 parameters δ_s with bounds 0-200 and determines the proportion allocated to each size bin ψ_s .

$$tot_d = 20 + \delta_1 + \delta_2 \quad (14)$$

$$\psi_1 = \frac{20}{tot_d} \quad (15)$$

89

$$\psi_{2,3} = \frac{\delta_d}{tot_d} \quad (16)$$

90

$$n_{(t=y+q/12,s=1-3,m=1)} = n_{(t=y+q/12,s=1-3,m=1)} + \psi_s e^{\mu + \tau_y} \quad (17)$$

91 Finally, the remaining other mortality is applied to the population after growth, molting, recruitment, and
 92 fishing occurs. Note that this allows a crab to experience two different mortalities within a given year as it
 93 undergoes terminal molt.

$$N_{t=y+1,s,m=1} = n_{t=y+q/12,s,m=1} e^{-\frac{12-q}{12} M_{t,s,m}} \quad (18)$$

94

$$N_{t=y+1,s,m=2} = n_{t=y+q/12,s,m=2} e^{-\frac{12-q}{12} M_{t,s,m}} \quad (19)$$

95 **Objective function**

96 **Penalties and priors**

97 **Generalized additive models**

98 **Structure**

99 **Model fits and diagnostics**

100 **Population dynamics models convergence**

101 **GAM convergence**

102 **Eastern Bering Sea**

103 **Newfoundland**

104 **Gulf of St Lawrence**

105 **Korea**

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108 **Russia/Greenland?**

109 **Next steps and caveats**

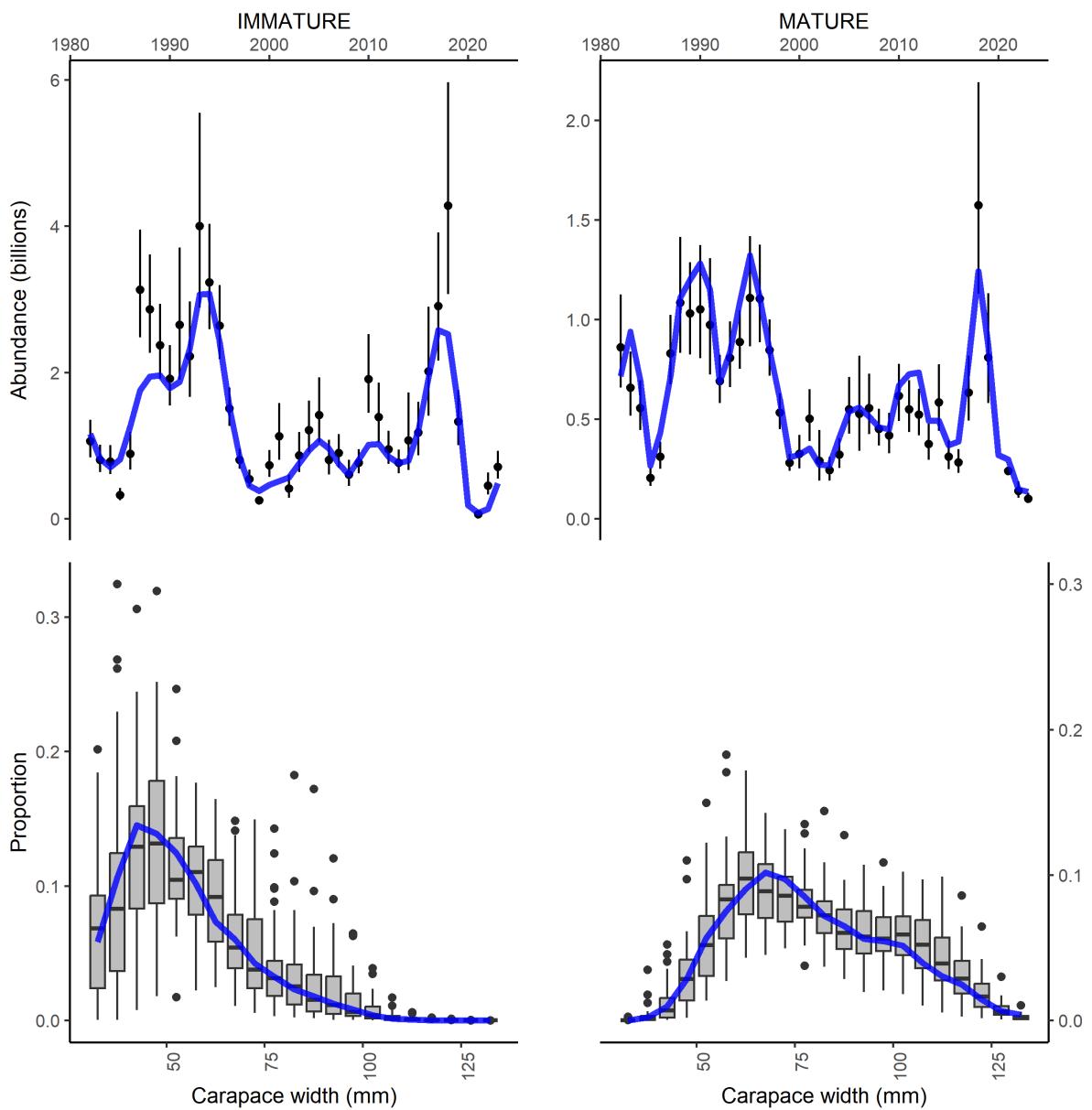


Figure 1: Fits to surveys from eastern Bering Sea.

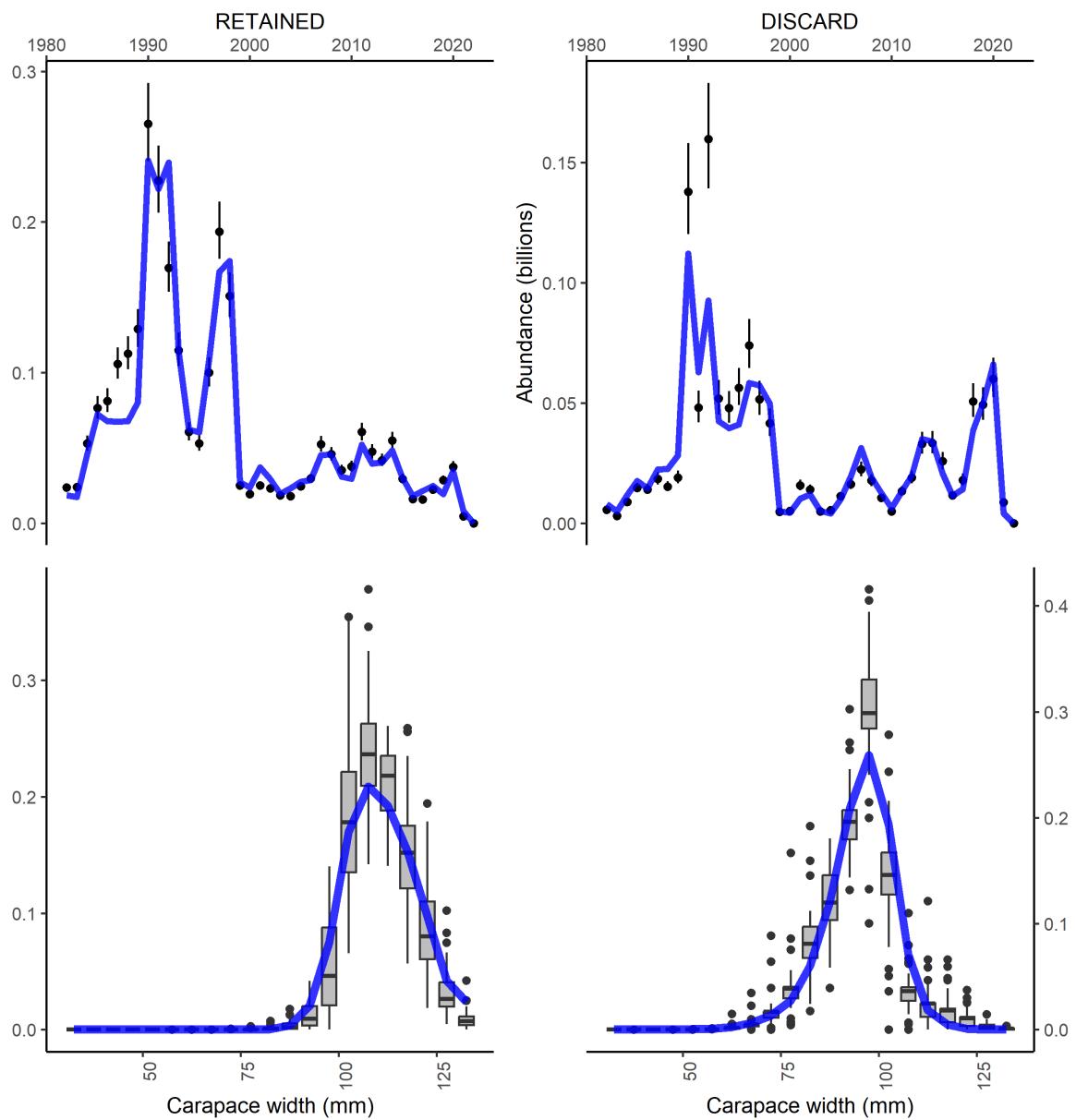


Figure 2: Fits to fishery data from eastern Bering Sea.

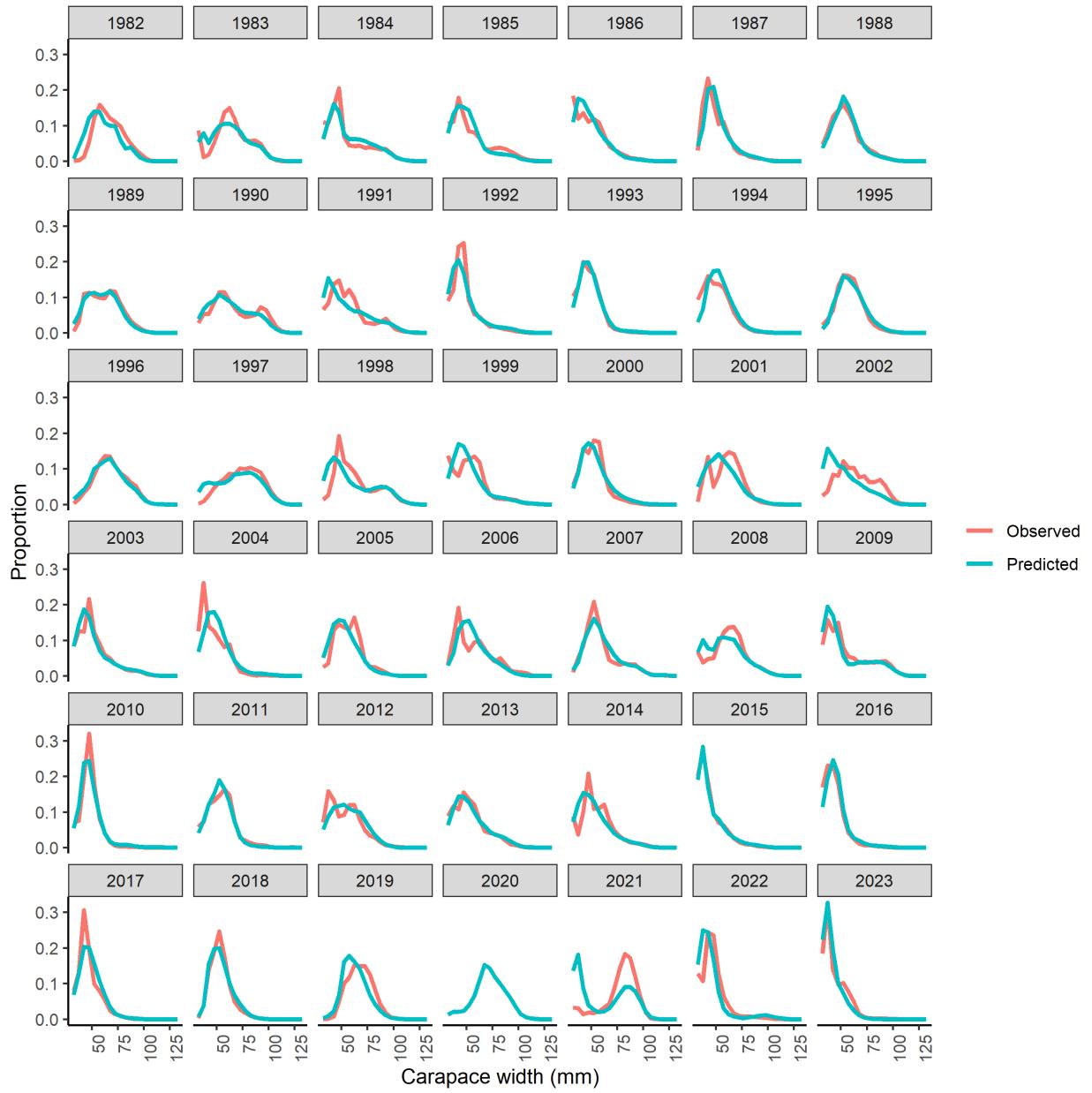


Figure 3: Fits to immature survey size data from eastern Bering Sea.

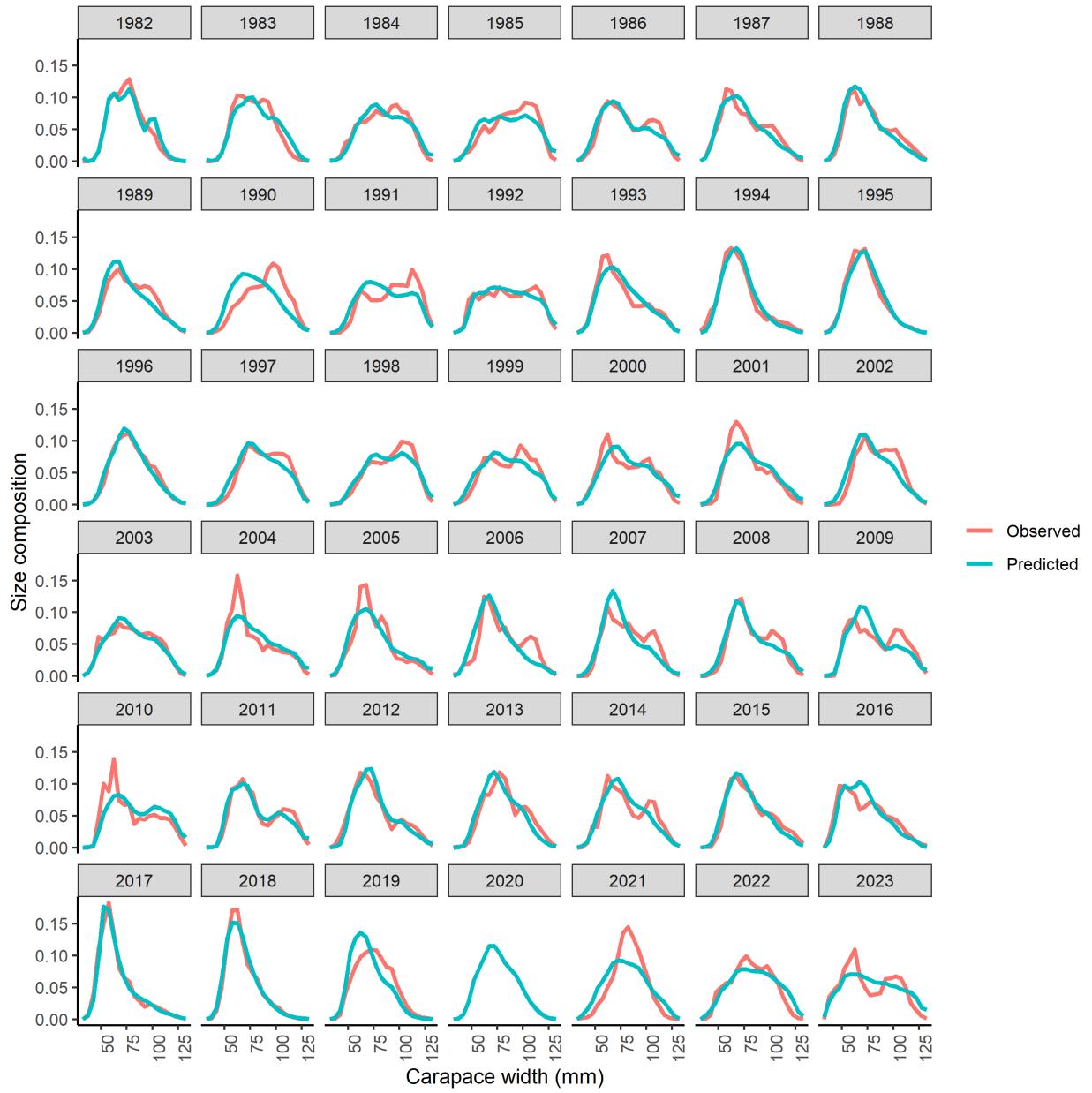


Figure 4: Fits to mature survey size data from eastern Bering Sea.

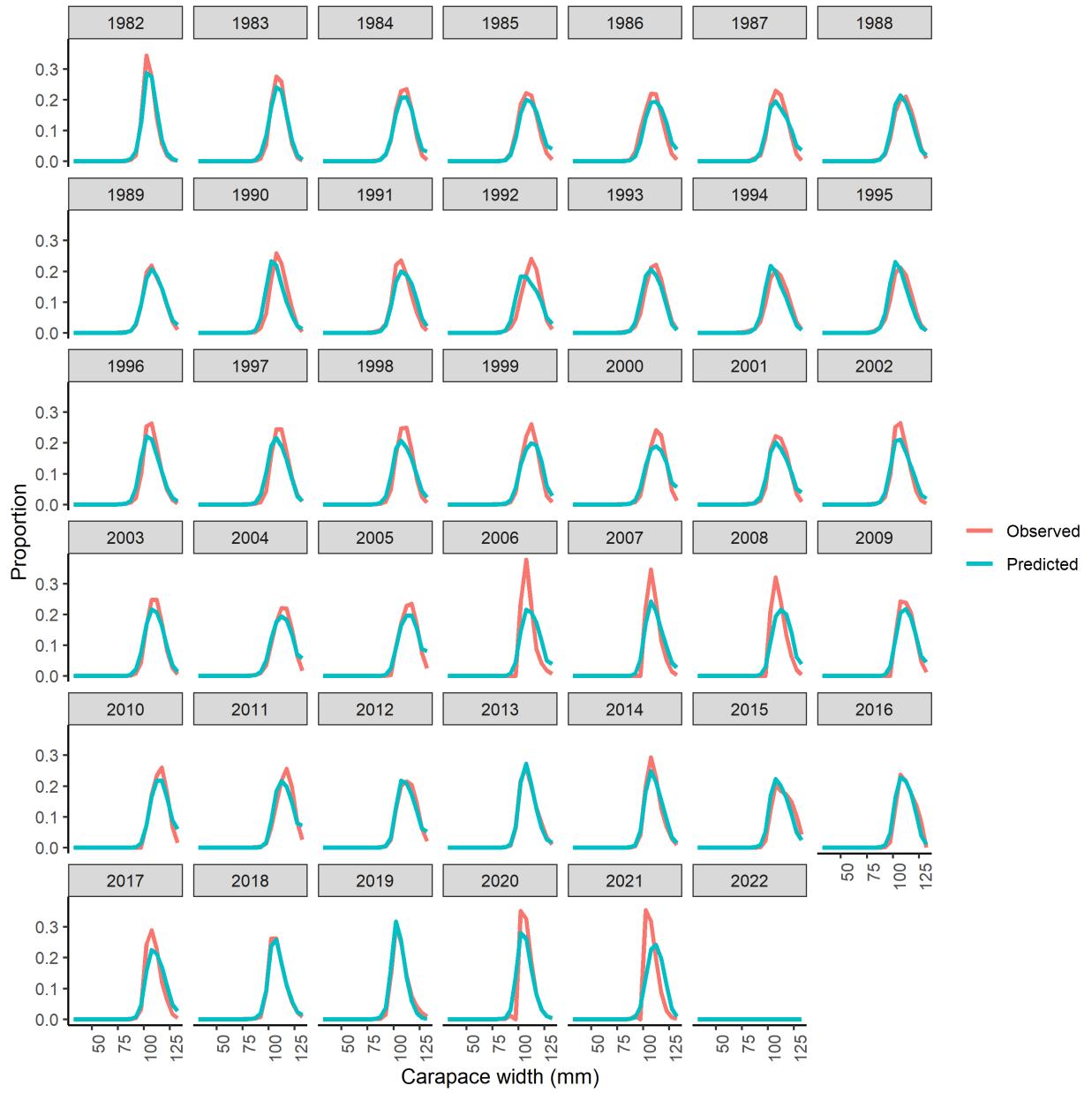


Figure 5: Fits to retained size data from eastern Bering Sea.

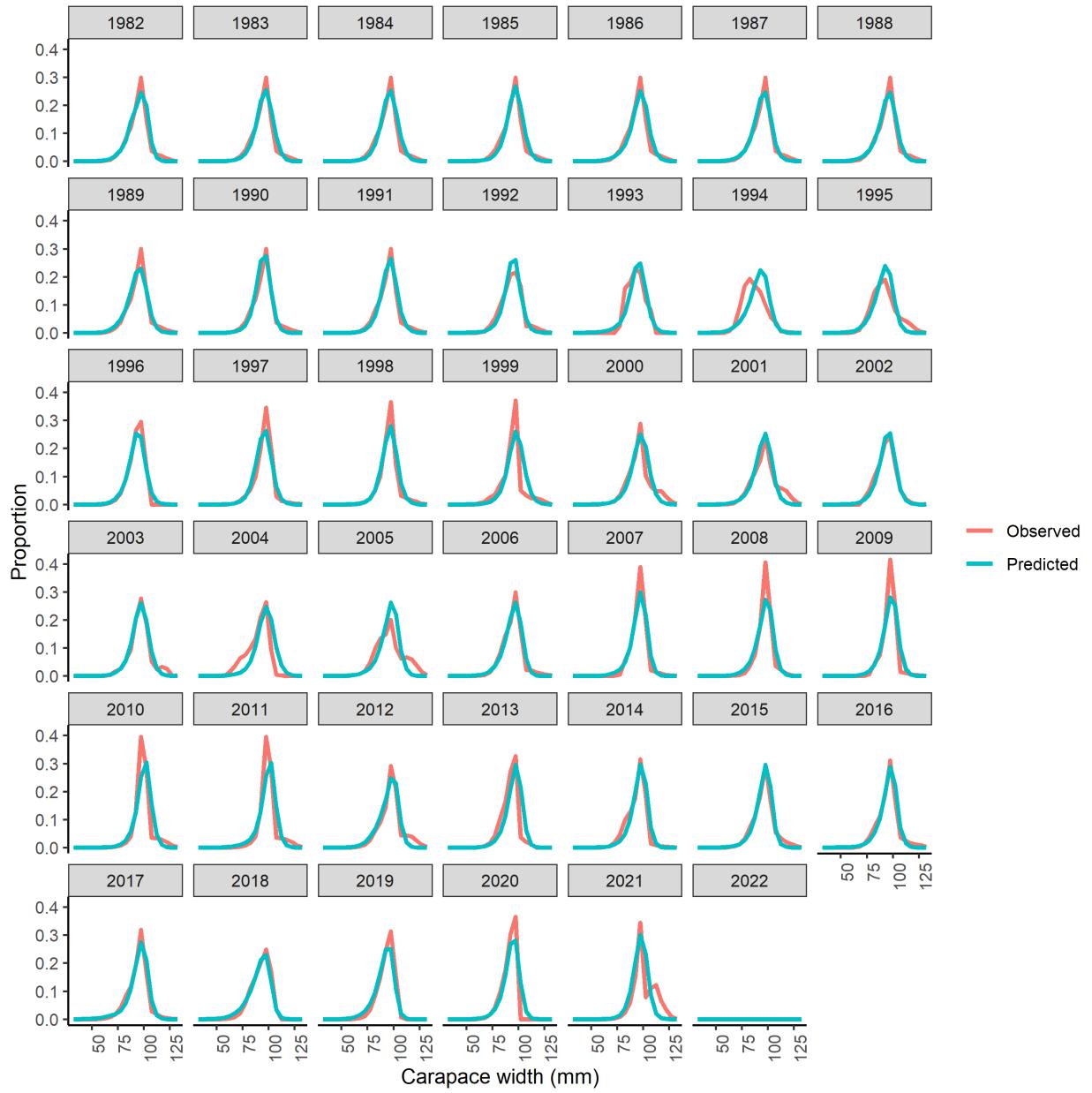


Figure 6: Fits to discarded size data from eastern Bering Sea.

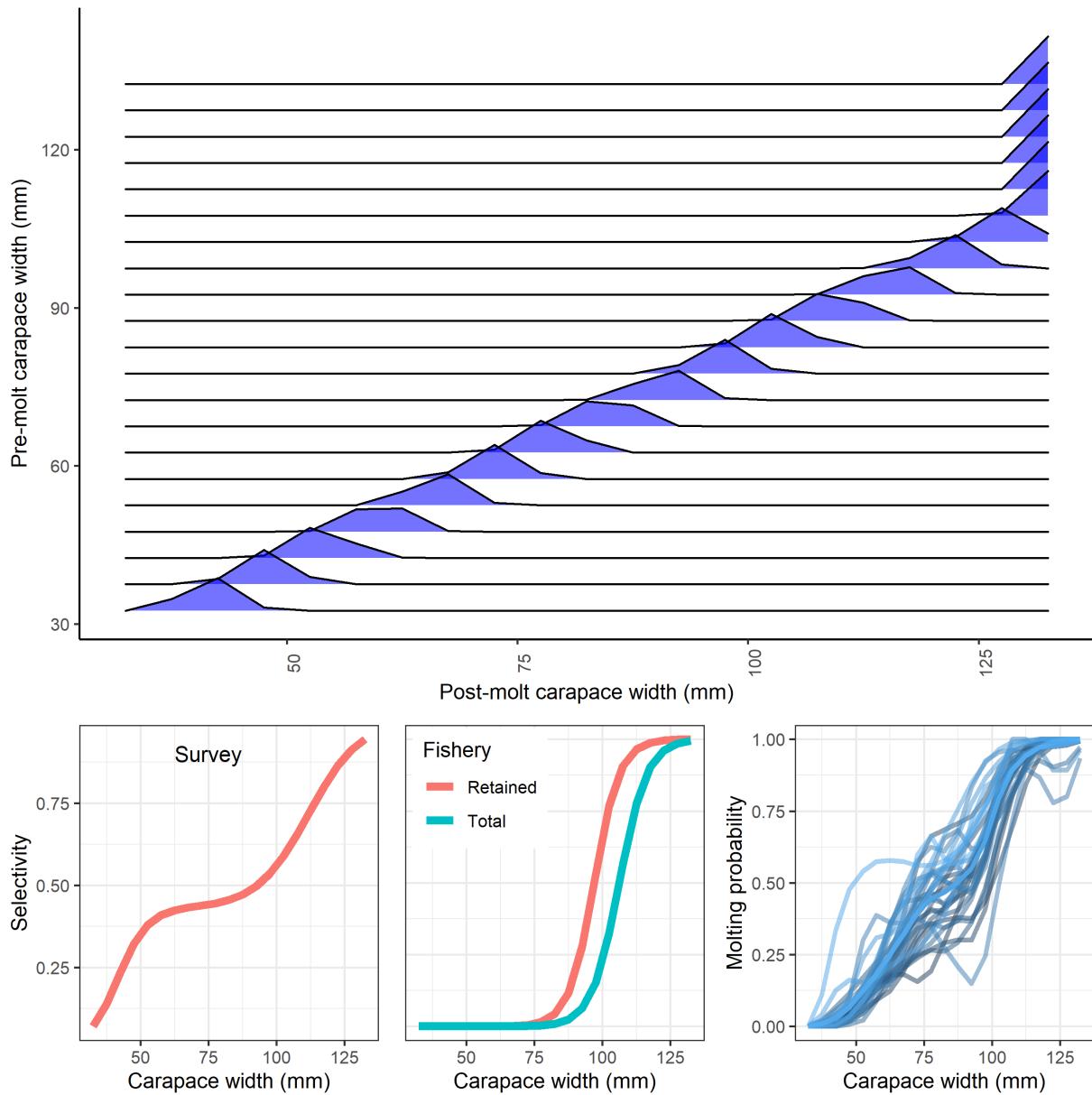


Figure 7: Fits to discarded size data from eastern Bering Sea.