

$$\begin{aligned}
 & V^1 \{ \underbrace{(A_{11} A_{21} A_{32} + A_{21} A_{31} A_{12} + A_{31} A_{11} A_{22} - A_{11} A_{31} A_{22} - A_{21} A_{11} A_{32} - A_{31} A_{21} A_{12})}_{dx^1 \wedge dx^2} \\
 & + \underbrace{(A_{11} A_{21} A_{33} + A_{21} A_{31} A_{13} + A_{31} A_{11} A_{23} - A_{11} A_{31} A_{23} - A_{21} A_{11} A_{33} - A_{31} A_{21} A_{13})}_{dx^1 \wedge dx^3} \\
 & + (A_{11} A_{22} A_{33} + A_{21} A_{32} A_{13} + A_{31} A_{12} A_{23} - A_{11} A_{32} A_{23} - A_{21} A_{12} A_{33} - A_{31} A_{22} A_{13}) dx^2 \wedge dx^3 \} \\
 & V^2 \{ \underbrace{(A_{12} A_{21} A_{32} + A_{22} A_{31} A_{12} + A_{32} A_{11} A_{22} - A_{12} A_{31} A_{22} - A_{22} A_{11} A_{32} - A_{32} A_{21} A_{12})}_{dx^1 \wedge dx^2} \\
 & + (A_{12} A_{21} A_{33} + A_{22} A_{31} A_{13} + A_{32} A_{11} A_{23} - A_{12} A_{31} A_{23} - A_{22} A_{11} A_{33} - A_{32} A_{21} A_{13}) dx^1 \wedge dx^3 \\
 & + \underbrace{(A_{12} A_{22} A_{33} + A_{22} A_{32} A_{13} + A_{32} A_{12} A_{23} - A_{12} A_{32} A_{23} - A_{22} A_{12} A_{33} - A_{32} A_{22} A_{13})}_{dx^2 \wedge dx^3} \} \\
 & V^3 \{ (A_{13} A_{21} A_{32} + A_{23} A_{31} A_{12} + A_{33} A_{11} A_{22} - A_{13} A_{31} A_{22} - A_{23} A_{11} A_{32} - A_{33} A_{21} A_{12}) dx^1 \wedge dx^2 \\
 & \underbrace{(A_{13} A_{21} A_{33} + A_{23} A_{31} A_{13} + A_{33} A_{11} A_{23} - A_{13} A_{31} A_{23} - A_{23} A_{11} A_{33} - A_{33} A_{21} A_{13})}_{dx^1 \wedge dx^3} \\
 & \underbrace{(A_{13} A_{22} A_{33} + A_{23} A_{32} A_{13} + A_{33} A_{12} A_{23} - A_{13} A_{32} A_{23} - A_{23} A_{12} A_{33} - A_{33} A_{22} A_{13})}_{dx^2 \wedge dx^3} \}
 \end{aligned}$$

$$= V^1 \det A \, dx^2 \wedge dx^3 + V^2 \det A \, dx^3 \wedge dx^1 + V^3 \det A \, dx^1 \wedge dx^2$$

$$= \det A \, i_2(V)$$

□

$$\circ \quad A \in \quad \Rightarrow \quad \det A = -1, \text{ or } 1$$

$$A = \begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & -1 \end{pmatrix} \text{ の場合 } \quad (x, y \text{ 平面についての鏡像})$$

△ 再定義 極性ベクトル ... 鏡に映い 符号が変わる。

軸性ベクトル ... 鏡に映い 符号が変わらない。