

$$\therefore r = \frac{\lambda}{1 + e \cos \theta} \quad (1.24)$$

$$(x, y) = (r \cos \theta, r \sin \theta) = \left( \frac{\lambda \cos \theta}{1 + e \cos \theta}, \frac{\lambda \sin \theta}{1 + e \cos \theta} \right)$$

$$\frac{(1-e^2)^2}{\lambda^2} \left( \frac{\lambda \cos \theta}{1 + e \cos \theta} + \frac{\lambda e}{1-e^2} \right)^2 + \frac{1-e^2}{\lambda^2} \frac{\lambda^2 \sin^2 \theta}{(1 + e \cos \theta)^2} = 1$$

$$(1-e^2)^2 \left( \frac{\lambda^2 \cos^2 \theta}{(1 + e \cos \theta)^2} + 2 \frac{\lambda^2 e \cos \theta}{(1 + e \cos \theta)(1-e^2)} + \frac{\lambda^2 e^2}{(1-e^2)^2} \right) + (1-e^2) \frac{\lambda^2 \sin^2 \theta}{(1 + e \cos \theta)^2} = \lambda^2$$

$$\frac{(1-e^2)^2 \lambda^2 \cos^2 \theta}{(1 + e \cos \theta)^2} + \frac{2 \lambda^2 e \cos \theta}{1 + e \cos \theta} + \frac{\lambda^2 e^2}{1-e^2} + \frac{\lambda^2 \sin^2 \theta}{(1 + e \cos \theta)^2} = \frac{\lambda^2}{1-e^2}$$

$$\frac{\lambda^2 - e^2 \lambda^2 \cos^2 \theta + 2 \lambda^2 e \cos \theta (1 + e \cos \theta)}{(1 + e \cos \theta)^2} = \lambda^2$$

$$\frac{\lambda^2 (1 + 2e \cos \theta + e^2 \cos^2 \theta)}{(1 + e \cos \theta)^2} = \lambda^2$$

$$\frac{(1-e^2)^2}{\lambda^2} \left( x + \frac{\lambda e}{1-e^2} \right)^2 + \frac{1-e^2}{\lambda^2} y^2 = 1. \text{ 楕円.}$$

$$C = \sqrt{\frac{\lambda^2}{(1-e^2)^2} - \frac{\lambda^2}{1-e^2}} = \sqrt{\frac{\lambda^2 (1 - 1 + e^2)}{(1-e^2)^2}} = \sqrt{\frac{\lambda^2 e^2}{(1-e^2)^2}} = \frac{\lambda e}{1-e^2}$$

$\therefore O$  は楕円の焦点。

$$c = \sqrt{a^2 - b^2}$$

(後述2)  $\Rightarrow H_0 = 0$  の場合

$$(1.20) \Rightarrow (1.21), \quad e = 1$$

$$(1.24)' \quad r = \frac{\lambda}{1 + \cos \theta}$$

$$= \frac{\lambda}{1 + \frac{x}{r}}$$

$$\Rightarrow r + x = \lambda \quad \Rightarrow r = \lambda - x$$

$$\Rightarrow r^2 = \lambda^2 - 2x\lambda + x^2$$

$$\Rightarrow x^2 + y^2 = \lambda^2 - 2x\lambda + x^2$$

$$\Rightarrow y^2 = \lambda^2 - 2x\lambda \quad \text{放物線} \quad \square$$