

$$V^1 \{ \underbrace{A_{11} A_{21} A_{32}} + \underbrace{A_{21} A_{31} A_{12}} + \underbrace{A_{31} A_{11} A_{22}} - \underbrace{A_{11} A_{31} A_{22}} - \underbrace{A_{21} A_{11} A_{32}} - \underbrace{A_{31} A_{21} A_{12}} \} dx^1 \wedge dx^2$$

$$+ \{ \underbrace{A_{11} A_{21} A_{33}} + \underbrace{A_{21} A_{31} A_{13}} + \underbrace{A_{31} A_{11} A_{23}} - \underbrace{A_{11} A_{31} A_{23}} - \underbrace{A_{21} A_{11} A_{33}} - \underbrace{A_{31} A_{21} A_{13}} \} dx^1 \wedge dx^3$$

$$+ \{ \underbrace{A_{11} A_{22} A_{33}} + \underbrace{A_{21} A_{32} A_{13}} + \underbrace{A_{31} A_{12} A_{23}} - \underbrace{A_{11} A_{32} A_{23}} - \underbrace{A_{21} A_{12} A_{33}} - \underbrace{A_{31} A_{22} A_{13}} \} dx^2 \wedge dx^3 \}$$

$$V^2 \{ \underbrace{A_{12} A_{21} A_{32}} + \underbrace{A_{22} A_{31} A_{12}} + \underbrace{A_{32} A_{11} A_{22}} - \underbrace{A_{12} A_{31} A_{22}} - \underbrace{A_{22} A_{11} A_{32}} - \underbrace{A_{32} A_{21} A_{12}} \} dx^1 \wedge dx^2$$

$$+ \{ \underbrace{A_{12} A_{21} A_{33}} + \underbrace{A_{22} A_{31} A_{13}} + \underbrace{A_{32} A_{11} A_{23}} - \underbrace{A_{12} A_{31} A_{23}} - \underbrace{A_{22} A_{11} A_{33}} - \underbrace{A_{32} A_{21} A_{13}} \} dx^1 \wedge dx^3$$

$$+ \{ \underbrace{A_{12} A_{22} A_{33}} + \underbrace{A_{22} A_{32} A_{13}} + \underbrace{A_{32} A_{12} A_{23}} - \underbrace{A_{12} A_{32} A_{23}} - \underbrace{A_{22} A_{12} A_{33}} - \underbrace{A_{32} A_{22} A_{13}} \} dx^2 \wedge dx^3 \}$$

$$V^3 \{ \underbrace{A_{13} A_{21} A_{32}} + \underbrace{A_{23} A_{31} A_{12}} + \underbrace{A_{33} A_{11} A_{22}} - \underbrace{A_{13} A_{31} A_{22}} - \underbrace{A_{23} A_{11} A_{32}} - \underbrace{A_{33} A_{21} A_{12}} \} dx^1 \wedge dx^2$$

$$+ \{ \underbrace{A_{13} A_{21} A_{33}} + \underbrace{A_{23} A_{31} A_{13}} + \underbrace{A_{33} A_{11} A_{23}} - \underbrace{A_{13} A_{31} A_{23}} - \underbrace{A_{23} A_{11} A_{33}} - \underbrace{A_{33} A_{21} A_{13}} \} dx^1 \wedge dx^3$$

$$+ \{ \underbrace{A_{13} A_{22} A_{33}} + \underbrace{A_{23} A_{32} A_{13}} + \underbrace{A_{33} A_{12} A_{23}} - \underbrace{A_{13} A_{32} A_{23}} - \underbrace{A_{23} A_{12} A_{33}} - \underbrace{A_{33} A_{22} A_{13}} \} dx^2 \wedge dx^3 \}$$

$$= V^1 \det A \, dx^2 \wedge dx^3 + V^2 \det A \, dx^3 \wedge dx^1 + V^3 \det A \, dx^1 \wedge dx^2$$

$$= \det A \, i_2(V)$$

□

$$\circ \quad A \in \quad \Rightarrow \quad \det A = -1, \text{ or } 1$$

$$A = \begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & -1 \end{pmatrix} \text{ の場合 } \quad (\text{x, y 平面についての鏡像})$$

△ 再定義 極性ベクトル ... 鏡に映い 符号が変わる。

軸性ベクトル ... 鏡に映い 符号が変わらない。