Schema Refinement & Normalization Theory 5

Week 13 - 1

Third Normal Form: Motivation

- There are some situations where
 - BCNF is not dependency preserving, and
 - efficient checking for FD violation on updates is important
- Solution: define a weaker normal form, called Third Normal Form (3NF)
 - Allows some redundancy (with resultant problems; we will see examples later)
 - But functional dependencies can be checked on individual relations without computing a join.
 - There is always a lossless-join, dependency-preserving decomposition into 3NF.

Third Normal Form (3NF)

- If R is in BCNF, obviously in 3NF.
- If R is in 3NF, some redundancy is possible. It is a compromise, used when BCNF not achievable (e.g., no "good" decomposition, or performance considerations).
 - Lossless-join, dependency-preserving decomposition of R into a collection of 3NF relations always possible.

3NF

- Relation R with FDs F is in 3NF if, for each FD $X \rightarrow A$ ($X \in R$ and $A \in R$) in F, one of the following statements is true:
 - $-A \in X$ (trivial FD), or
 - X is a superkey, <u>or</u>
 - A is part of some <u>key</u> for R

If one of these two is satisfied for ALL FDs, then R is in BCNF



Not just superkey! (why not?)

What Does 3NF Achieve?

- If 3NF is violated by $X\rightarrow A$, one of the following holds:
 - X is a subset of some key K (partial redundancy)
 - We store (X, A) pairs redundantly.
 - X is not a proper subset of any key.
 - There is a chain of FDs $K \to X \to A$, which means that we cannot associate an X value with a K value unless we also associate an A value with an X value.
- But: even if reln is in 3NF, these problems could arise.
 - e.g., Reserves SBDC (sid, bid, date, credit_card). Keys are SBD, CBD. FD = $\{S \rightarrow C, C \rightarrow S\}$. R is in 3NF, but for each reservation of sailor S, same (S, C) pair is stored.
- Thus, 3NF is indeed a compromise relative to BCNF.

Decomposition into 3NF

- Obviously, the algorithm for lossless join decomp into BCNF can be used to obtain a lossless join decomp into 3NF (typically, can stop earlier).
- To ensure dependency preservation, one idea:
 - If $X \rightarrow Y$ is not preserved, add relation XY.
 - Problem is that XY may violate 3NF!
- Refinement: Instead of the given set of FDs F, use a *minimal cover for F*.

Minimal Cover for a Set of FDs

- Minimal cover G for a set of FDs F:
 - Closure of F = closure of G.
 - Right hand side of each FD in G is a single attribute.
 - If we modify G by deleting an FD or by deleting attributes from an FD in G, the closure changes.
- Intuitively, every FD in G is needed, and "as small as possible" in order to get the same closure as F.

Obtaining Minimal Cover

- Step 1: Put the FDs in a standard form (i.e. right-hand side should contain only single attribute)
- Step 2: Minimize the left side of each FD
- Step 3: Delete redundant FDs

Find minimal cover for F = {ABH → CK,
 A → D, C → E, BGH → L, L → AD, E →
 L, BH → E}

• Step 1: Make RHS of each FD into a single attribute:

$$F = \{ABH \rightarrow C, ABH \rightarrow K, A \rightarrow D, C \rightarrow E, BGH \rightarrow L, L \rightarrow A, L \rightarrow D, E \rightarrow L, BH \rightarrow E\}$$

- $F = \{ABH \rightarrow C, ABH \rightarrow K, A \rightarrow D, C \rightarrow E, BGH \rightarrow L, L \rightarrow A, L \rightarrow D, E \rightarrow L, BH \rightarrow E\}$
- Step 2: Eliminate redundant attributes from LHS, e.g. Can an attribute be deleted from ABH → C?
 - Compute (AB)+, (BH)+, (AH)+ and see if any of them contains C. (Why?)
 - (AB)+ = ABD, (BH)+ = ABCDEHKL, (AH)+ = ADH. Since $C \in (BH)+$, BH → C is entailed by F. So A is redundant in ABH → C. Similarly, A is also redundant in ABH → K. Check further to see if B or H is redundant as well.
 - Similarly, for BGH \rightarrow L, G is redundant since L \in (BH)+.
 - $F = \{BH \rightarrow C, BH \rightarrow K, A \rightarrow D, C \rightarrow E, BH \rightarrow L, L \rightarrow A, L \rightarrow D, E \rightarrow L, BH \rightarrow E\}$

- $F = \{BH \rightarrow C, BH \rightarrow K, A \rightarrow D, C \rightarrow E, BH \rightarrow L, L \rightarrow A, L \rightarrow D, E \rightarrow L, BH \rightarrow E\}$
- Step 3: Delete redundant FDs from F.
 - If $F \{f\}$ infers f, then f is redundant, i.e. if f is $X \to A$, then check if X + using F f still contains A. If it does, then it means $X \to A$ can be inferred by other FDs.
 - E.g. For BH → L, (BH)+ (not using BH → L) = ACDEKL, which contains L. This means BH → L can be inferred by other FDs, so it's a redundant FD.
 - In fact, BH → L can be inferred by BH \rightarrow E, E \rightarrow L.
 - Check other FDs using the same algorithm.
- Note: the order of Step 2 and Step 3 should not be exchanged.

What to do with Minimal Cover?

- After obtaining the minimal cover, for each FD $X \rightarrow A$ in the minimal cover that is not preserved, create a table consisting of XA (so we can check dependency in this new table, i.e. dependency is preserved).
- Why does this new table is guaranteed to be in 3NF (whereas if we created the new table from F, it might not?)
 - Since $X \rightarrow A$ is in the minimal cover, $Y \rightarrow A$ does not hold for any Y that is a strict subset of X.
 - So X is a key for XA (satisfies condition #2)
 - If any other dependencies hold over XA, the right side can involve only attributes in X because A is a single attribute (satisfies condition #3).

Comparison of BCNF and 3NF

- It is always possible to decompose a relation into a set of relations that are in 3NF such that:
 - the decomposition is lossless
 - the dependencies are preserved
- It is always possible to decompose a relation into a set of relations that are in BCNF such that:
 - the decomposition is lossless
 - it may not be possible to preserve dependencies.

Normalization Review

- Identify all FD's in F⁺
- Identify candidate keys
- Identify (strongest, or specific) normal forms
 - BCNF, 3NF
- Schema decomposition
 - When to decompose
 - How to check if a decomposition is lossless-join and/or dependency preserving
 - Use projection of F⁺ to check for dependency preservation
 - Decompose into:
 - Lossless-join
 - Dependency preserving
 - Use minimal cover

Normalization Theory - Practice Questions

A	В	С
1	1	2
1	1	3
2	2	3
2	2	2

FDs with A as the left side:	Satisfied by the relation?
A→A	Yes (trivial FD)
A→B	Yes
A→C	No: tuples 1&2
AB →A	Yes (trivial FD)
AC →B	Yes

Let $F = \{ A \rightarrow BC, B \rightarrow C \}$. Is $C \rightarrow AB$ in F^+ ?

Answer: No. Either of the following 2 reasons is ok:

Reason 1) C⁺=C, and does not include AB.

Reason 2) We can find a relation instance such that it satisfies F but does not satisfy

 $C \rightarrow AB$.

A	В	С
1	1	2
2	1	2

List all the non-trivial FDs in F⁺

• Given $F=\{A \rightarrow B, B \rightarrow C\}$. Compute F^+ (with attributes A, B, C).

	A	В	C	AB	AC	BC	ABC
A							
В							
C							
AB							
AC							
BC							
ABC							

Attribute closure
A ⁺ =ABC
$B^+=BC$
$C_{+}=C$
AB+=ABC
AC+=ABC
BC+=BC
ABC+=ABC

• Given $F=\{A \rightarrow B, B \rightarrow C\}$. Find a relation that satisfies F:

A	В	C
1	1	2
2	1	2

- Given $F=\{A \rightarrow B, B \rightarrow C\}$. Find a relation that satisfies F but does not satisfy $B \rightarrow A$. Well, the above example suffices.
- Can you find an instance that satisfies F but not $A \rightarrow C$? No. Because $A \rightarrow C$ is in F^+

$$R(A, B, C, D, E),$$

 $F = \{A \rightarrow B, C \rightarrow D\}$

Candidate key: ACE. How do we know?

Intuitively,

- B cannot be in a candidate key.
- A is not determined by any other attributes (like E), and A has to be in a candidate key (because a candidate key has to determine all the attributes).
- Now if A is in a candidate key, B cannot be in the same candidate key, since we can drop B from the candidate without losing the property of being a "key".
- Same reasoning apply to others attributes.

R(A, B, C, D, E), $F = \{A \rightarrow B, C \rightarrow D\}$ [Same as previous]

Which normal form?

Not in BCNF. This is the case where all attributes in the FDs appear in R. We consider A, and C to see if either is a superkey of not. Obviously, neither A nor C is a superkey, and hence R is not in BCNF. More precisely, we have $A \rightarrow B$ is in F^+ and non-trivial, but A is not a superkey of R.

R(A, B, C, D, E) $F = \{A \rightarrow B, C \rightarrow D\}$ [Same as previous]

Which normal form?

We already know that it's not in BCNF. Not in 3NF either. We have $A \rightarrow B$ is in F^+ and non-trivial, but A is not a superkey of R. Furthermore, B is not in any candidate key (since the only candidate key is ACE).

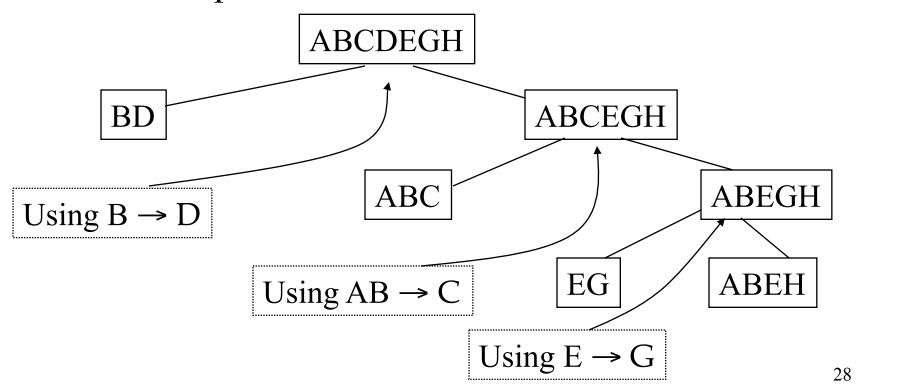
- R(A,B,F), $F = \{AC \rightarrow E, B \rightarrow F\}$.
- Candidate key? AB
- BCNF? No, because of $B \rightarrow F$ (B is not a superkey).
- 3NF? No, because of $B \rightarrow F$ (F is not part of a candidate key).

- $R(D, C, H, G), F = \{A \rightarrow I, I \rightarrow A\}$
- Candidate key? DCHG
- BCNF? Yes
- 3NF? Yes

- R(A, B, C, D, E, G, H) $F=\{AB \rightarrow C, AC \rightarrow B, B \rightarrow D, BC \rightarrow A, E \rightarrow G\}$
- Candidate keys?
 - H has to be in all candidate keys
 - E has to be in all candidate keys
 - G cannot be in any candidate key (since E is in all candidate keys already).
 - Since $AB \rightarrow C$, $AC \rightarrow B$ and $BC \rightarrow A$, we know no candidate key can have ABC together.
 - AEH, BEH, CEH are not superkeys.
 - Try ABEH, ACEH, BCEH. They are all superkeys. And we know they are all candidate keys (since above properties)
 - These are the only candidate keys: (1) each candidate key either contains A, or B, or C since no attributes other than A,B,C determine A, B, C, and (2) if a candidate key contains A, then it must contain either B, or C, and so on.

- Same as previous
- Not in BCNF, not in 3NF
- Decomposition:

R(A, B, C, D, E, G, H) $F=\{AB \rightarrow C, AC \rightarrow B, B \rightarrow D, BC \rightarrow A, E \rightarrow G\}$



- R(A, B, C, D, E, G, H) $F=\{AB \rightarrow C, AC \rightarrow B, B \rightarrow D, BC \rightarrow A, E \rightarrow G\}$
- Decomposition: BD, ABC, EG, ABEH
- Why good decomposition?
 - They are all in BCNF
 - Lossless-join decomposition
 - All dependencies are preserved.

- R(A, B, D, E) decomposed into R1(A, B, D), R2 (A, B, E)
- $F = \{AB \rightarrow DE\}$
- It is a dependency preserving decomposition!
 - $-AB \rightarrow D$ can be checked in R1
 - $-AB \rightarrow E$ can be checked in R2
 - $\{AB \rightarrow DE\}$ is equivalent to $\{AB \rightarrow D, AB \rightarrow E\}$