Investigation of the Impact of Chamber Pressure on Specific Impulse of a Rocket Engine

IB Physics HL Internal Assessment May 27, 2025

Contents

1	Introduction	4
2	Research Question	4
3	Background Theory	4
	3.1 Chamber Pressure	. 4
	3.2 Impulse	. 5
	3.3 Mass Flow Rate	. 5
	3.4 Specific Impulse	. 5
	3.5 Nozzle Shape	. 6
	3.6 Rocketry	. 6
4	Hypothesis	6
5	Variables	7
6	Methodology	7
	6.1 Materials	. 7
	6.2 Experimental Setup Diagrams	. 8
	6.3 Procedure	. 8
	6.3.1 Preparation & Setup	. 8
	6.3.2 Force Plate Setup & Air Pressure Control	. 8
	6.3.3 Pressurization & Measurement Process	. 8
	6.4 Risk Assessment	. 9
7	Data Collection	9
	7.1 Raw Data	. 9
	7.2 Tables	. 13
	7.3 Experimental Data Tables	. 14
	7.4 Statistical Analysis	. 14
	7.5 Graphical Analysis	. 15
8	Data Analysis	17
	8.1 Processing the Data	. 17
	8.2 Interpretation of Graphs	. 17
9	Evaluation	17
	9.1 Strengths and Weaknesses	. 17
	9.2 Sources of Error	. 18
	9.3 Improvements	. 18

10	10 Conclusion 19					
\mathbf{A}	App	pendix A: Measuring Data and Methodology	21			
	A.1	A.1 Experimental Setup and Data Collection	21			
	A.2	A.2 Detailed Measuring Data	21			
	A.3	A.3 Water Displacement Measurements	22			

1 Introduction

When designing a rocket, the rocket engine will be a crucial component. If you choose not to buy an already existing engine, but decide to design your own, you will see that having an efficient engine will be one of your big priorities. Your rocket airframe might be the most aerodynamic, and your aviation controls are perfect, but it would matter if your engine cannot compulse it through space, because your engine works efficiently.

I have come to find this exact problem when as a hobbyist trying to design a rocket and my own liquid fueled rocket engine, getting an efficient rocket engine is crucial. And efficiency in such will often be measured in specific impulse. Now there are alot of things impacting specific impulse which have to be considered when designing an engine. I found that some of them like ambient pressure are constrained anyways so I won't be able to impact them to make my engine more efficient. Others like the fuel choice are often very heavily researched already and have a simple answer, where using hydrogen with oxygen will give a higher specific impulse then kerosine with nitrous oxide for factors clarified below.

But one of the factors which I find hard to follow, is the impact of chamber pressure of a rocket, so the pressure inside the engine before the fuel leaves through the nozzle on specific impulse. Not Knowing what pressure should be inside the engine has haltet my design lately, because the chamber pressure also affects the nozzle ratios and so on...

Through my research I have found numerous nasa articles about optimal chamber pressure, but I haven't been able to visualize the impact or if there is really any myself.

This is why in my IA I will investigate in isolation the impact of chamber pressure on specific impulse.

2 Research Question

What is the impact of air chamber pressure inside a small plastic water bottle as a rocket engine on specific impulse?

3 Background Theory

3.1 Chamber Pressure

Chamber pressure is very important in rocketry, and rocket propulsion, the pressure inside the engines chamber will decide how strong the exhaust gases are pushed out. Chamber pressure relates to thermodynamics, fluid dynamics and Newton's 3rd law in physics (2). Chamber pressure is important beyond rocketry, it is important in internal combustion engines, and jet propulsion. Higher pressure gases affect how the rocket engine functions (1). $W = P\Delta V$, higher pressures expect more work. The chamber pressures of the Saturn V's (the rocket which flew to the moon) rocket engines was around 7 MPa, whilst the pressure inside the Raptor engines (propelling space x's star ship) 35 MPa significantly higher.

3.2 Impulse

Impulse is a measure of the total momentum change something has, $J = F\Delta T$, in rockets it would be the momentum a rocket engine delivers to start moving(5). Impulse is very important in reference to change in momentum and energy. Impulse is very important in aerospace engineering and spacecraft design, to work on efficiency (3). To have high impulse means that the rocket is stronger which is often seen positive, impulse is also dependent on the time the force is applied (4), but the saturn v engine produced 6,770 kN of thrust at sea level, whilst the raptor engine only produced 2,260 kN of thrust at sea level. This decrease could be due to the higher pressure, but is likely just because a single Saturn V engine was expected to be stronger than one Raptor engine.

3.3 Mass Flow Rate

Mass flow rate is required for specific impulse, it is not part of the ib syllabus but it is a great measure of how much propellant is exerted from an engine. It ties into fluid dynamics (6), higher mass flow rate means there are more gases exerted in less time. It is very important for any kind of fuel engine, because it gives an estimate of how much fuel is required for the engine (7). Mass flow rate is affected by the viscosity of the liquid, the mass of the liquid, and the area which the mass flows through, in the ocean there is more movement then in a lake.

3.4 Specific Impulse

Specific impulse is a measurement of fuel efficiency, high specific impulse means the rocket is highly efficient, defined as the amount of thrust produced per unit of propellant consumed over time. Essentially, it tells us how effectively a rocket engine uses fuel. The higher the specific impulse, the more efficient the engine is, meaning it can produce more thrust while using less fuel. Expressed in seconds.

Specific impulse is often affected by the propellant type, what kind of fuel is used in a rocket impacts its efficiency. The engine design is also very important, the size and ratio of the combustion chamber and the ratio to the nozzle affect how efficient the engine will function. The velocity at which the gases exit the nozzle also affect the specific impulse. The temperature of the combustion affects the specific impulse, higher temperatures often

lead to higher efficiency (9). And the mass of the exhaust gases also impact the engine efficiency, often lighter particles will be more efficient.

The ambient pressure is also very important, bigger pressure differentials can affect the exhaust flow, so in a vacuum the difference would be infinite, whilst on sea level the ambient pressure is high already. I am investigating this statement, because by increasing the chamber pressure, I will increase the diffrence from chamber pressure to atmospheric pressure.

The specific impulse of a saturn v engine was 263 seconds whilst a raptor engine had one of 327 seconds, both at sea level (8). Now i hope the increase in efficiency is due to the higher chamber pressure, but the saturn v used less efficient kerosine as a fuel then the methane used by space x, and the velocity of the exhaust gases from the raptor are also higher, and the engine design used by the saturn as a whole was less efficient using a gas generator cycle, instead of a full flow stage cycle.

3.5 Nozzle Shape

Nozzle shape of a rocket engine is very important, the width/size/curvature of a nozzle will determine how much fuel can be expelled by limiting it, it also determines what kind of chamber pressures a rocket engine can function in (10). to be expected is that small nozzle sizes will cause higher pressures in an open system, as the gases need to compress to fit through the nozzle. There is a lot of research into nozzle shapes where typically converging diverging nozzles are overall the best, gases are accelerated in the converging part and after reaching mach 1 they get accelerated even more in the diverging part (11). This is very interesting, but in this experiment the nozzle will just be a small hole at the end of a valve. It is important though that it is small, because this might limit the mass flow rate.

3.6 Rocketry

Rocket engines rely significantly on those kinds of variables to reach efficiency. Rocket engines and engines of all kinds are often very inefficient, so the importance of efficiency is highlighted once more (12) (13). Rocketry is very important to us humans in fields like safety but also and more interesting space exploration and fast travel.

4 Hypothesis

I am predicting that there will be some kind of proportional behaviour between the chamber pressure of a rocket and the impulse of the rocket. Furthermore I will predict that in moderate pressures (all the pressures that I hope to test), the higher pressure will have a linear correlation with higher specific impulse.

I believe this because of the following correlations which i have found, $W \propto P$, $W \propto F$, $F \propto J$, so $P \propto J$, now considering that the specific impulse can be derived from impulse i predict that higher pressure will also cause more efficient engine. Although higher pressure resulting in efficiency might sound unintuitive as high pressures sound very violent.

Nevertheless I predict a linear direct correlation, which does not converge at all (definitely not in the range of pressures in my experiment).

5 Variables

TypeDescriptionNumber of pumps / chamber pressureIndependentForce exerted
Time taken to exertDependentImpulse
Mass flow rate
Specific impulseControlVolume of rocket, for consistency and no interference in PV = nRT
Positioning on the force plate, for equal measurements
Temperature, for consistency and no inter-

ference in PV = nRT

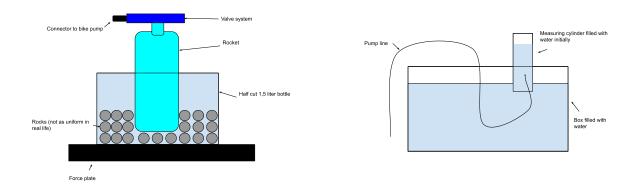
Table 1: Experimental Variables

6 Methodology

6.1 Materials

- Water rocket setup (small plastic water bottle, a pump, a valve, a stand, O-rings)
- Air
- Force measuring plate
- Water
- Measuring cylinder
- 320 g of rocks

6.2 Experimental Setup Diagrams



(a) Force measurement setup

(b) Water displacement measurement

Figure 1: Detailed experimental setup diagrams

6.3 Procedure

6.3.1 Preparation & Setup

- 1. Cut a 2.5 L cola bottle in half.
- 2. Fill the bottom half with 20 g of rocks.
- 3. Place the bottle/rocket upside down, positioning it securely.
- 4. Surround the rocket base with 300 g of rocks to prevent movement.

6.3.2 Force Plate Setup & Air Pressure Control

- 1. Position the cola bottle on the force plate, ensuring stability.
- 2. Mark the exact location of the bottle on the force plate.
- 3. Tare the force plate to reset baseline measurement.
- 4. Ensure the system is airtight before pressurization.

6.3.3 Pressurization & Measurement Process

- 1. Begin pressurizing the rocket.
- 2. Start the force plate measurement.
- 3. Open the bottle valve to release pressure.
- 4. Record the force plate readings throughout the process.
- 5. Repeat the procedure with different pressure levels for comparison.

6.4 Risk Assessment

Table 2: Risk Assessment

Risk Factor	Description	Safety Measure
High pressure water bottle	high pressure, at such pres-	Test pressures much higher than the experiment will be conducted at, if the rocket survives, it will also at the pressures that are in- vestigated

7 Data Collection

7.1 Raw Data

From my collected data I will show by the use of the example of 50 pumps all my calculations:

First, using the number of pumps as an independent variable did not satisfy me, instead I measured the volume of the rocket by filling it up with water.

$$V_{\text{rocket}} = 250(1) \,\text{mL}$$

Also the volume added to every pump, by measuring the displacement of air by pumping air into a cylinder filled with water.

$$V_{\text{per pump}} = V_{\text{final measurement}} - V_{\text{initial measurement}} = 47.0(5) \,\text{mL} - 9.0(5) \,\text{mL} = 38(1) \,\text{mL}$$

$$V_{50} = V_{\text{rocket}} + 50 \times V_{\text{per pump}} = 250(1) \,\text{mL} + 38(1) \,\text{mL} \times 50 = 2150(51) \,\text{mL}$$

Now I tried finding the amount of moles after 50 pumps.

$$n_{50} = n_{\text{rocket}}(250 \,\text{mL of air}) + 50 \times n_{\text{per pump}}(38 \,\text{mL of air})$$

I measured the temperature at the start of the experiment and at the end.

$$T_1 = 23.1(1)$$
 °C (1)

$$T_2 = 23.5(1)$$
 °C (2)

$$T_{\text{avg}} = \frac{23.1 + 23.5}{2} = 23.3 \,^{\circ}\text{C}$$
 (3)

I was unable to measure the density of my local air, but through research I found the expected M_r for my pressure and temperature, assuming it is constant. I treated researched values as constant and assumed no uncertainties.

$$M_{r,air} = 0.0290 \,\mathrm{kg} \,\mathrm{mol}^{-1}$$

Now assuming PV = nRT I could calculate the pressure, from the initial pressure, I could not measure my local atmospheric pressure, but in my weather app I found the local pressure at the time of my experiment.

$$n = \frac{PV}{RT} \tag{4}$$

$$n_{\text{rocket}} = \frac{1.016 \times 10^5 \,\text{Pa} \times 0.000 \,250(1) \,\text{m}^3}{8.31 \,\text{J} \,\text{mol}^{-1} \,\text{K}^{-1} \times 296.3(1) \,\text{K}} = 0.010 \,31 \,\text{mol}$$
 (5)

$$n_{\text{pump}} = \frac{1.016 \times 10^5 \,\text{Pa} \times 0.000 \,038 \,\text{m}^3}{8.31 \,\text{J} \,\text{mol}^{-1} \,\text{K}^{-1} \times 296.3(1) \,\text{K}} = 0.001 \,567 \,\text{mol}$$
 (6)

$$n_{50} = 0.010310 \,\text{mol} + 50 \times 0.001567 \,\text{mol} = 0.08866 \,\text{mol}$$
 (7)

Assuming temperature is constant:

$$P_{\rm atm} \propto \frac{n}{V}$$
, $1.016 \times 10^5 \, {\rm Pa} \propto \frac{0.010 \, 31 \, {\rm mol}}{0.000 \, 250(1) \, {\rm m}^3}$

$$P_{50} = P_1 \times \frac{n/V}{\text{reference}} = 1.016 \times 10^5 \,\text{Pa} \times \frac{0.088\,66\,\text{mol}/0.000\,250(1)\,\text{m}^3}{0.010\,31\,\text{mol}/0.000\,250(1)\,\text{m}^3} = 8.737 \times 10^5 \,\text{Pa}$$

But actually:

$$\frac{V_{50}}{V_{\rm rocket}} \propto \frac{n_{50}}{n_{\rm rocket}}$$

So:

$$P_{50} = P_{\rm atm} \times \frac{V_{50}}{V_{\rm rocket}} = 1.016 \times 10^5 \, \text{Pa} \times \frac{0.002\,150(51)\,\text{m}^3}{0.000\,250(1)\,\text{m}^3} = 8.737 \times 10^5 \, \text{Pa}$$

% uncertainty(
$$P_{50}$$
) = $\left(\frac{\pm 1 \text{ mL}}{250 \text{ mL}} + \frac{\pm 51 \text{ mL}}{(2150 \text{ mL} - 250 \text{ mL})}\right) \times 100 = 3.08\%$

Now that I have pressure as my independent variable, I can calculate the impulse. From my measurements I got the time where the peak measurement in the force plate starts and ends so first I took averages of change in time and peak force.

For 50 pump measurements:

$$F_{\text{avg peak }50} = \frac{F_1 + F_2 + F_3 + F_4 + F_5}{5} \tag{8}$$

$$= \frac{(32(1) N + 34(1) N + 19(1) N + 22(1) N + 30(1) N)}{5}$$
(9)

$$= 27.4(10) \,\mathrm{N} \tag{10}$$

$$\Delta t_{\text{avg }50} = \frac{(T_2 - T_1) + (T_4 - T_3) + (T_6 - T_5) + (T_8 - T_7) + (T_{10} - T_9)}{5}$$

$$= 0.039 \, 82(20) \, \text{s}$$
(11)

Now because the graph was in a shape of a triangle I could use the formula for the area of a triangle to calculate impulse:

$$J_{50} = A_t = \frac{1}{2}(b\Delta tF) = \frac{1}{2} \times (0.03982(20) \text{ s} \times 27.4(10) \text{ N}) = 0.5455 \text{ N s}$$

% uncertainty(
$$J_{50}$$
) = $\left(\frac{\pm 0.0002 \,\mathrm{s}}{0.03982 \,\mathrm{s}} + \frac{\pm 1 \,\mathrm{N}}{27.4 \,\mathrm{N}}\right) \times 100 = 4.15\%$

Now that I know what the change in momentum is, what mass carries this momentum out, the mass flow rate.

$$\dot{m} = \frac{\Delta m}{\Delta t}$$

I don't have the mass of the air, but from my previous research I can figure out the density of air:

$$n = \frac{m}{M_r} \tag{13}$$

$$\rho = \frac{m}{V} \tag{14}$$

$$PV = nRT = \frac{mRT}{M_r} \tag{15}$$

$$P = \frac{\rho RT}{M_r} \tag{16}$$

$$\rho = \frac{PM_r}{RT} \tag{17}$$

$$\rho_{\rm atm} = \frac{1.016 \times 10^5 \, \rm Pa \pm 0.4\% \times 0.0290 \, kg \, mol^{-1}}{8.31 \, \rm J \, mol^{-1} \, K^{-1} \times 296.3 \, K \pm 0.1 \, K} = 1.195 \, kg \, m^{-3}$$

$$\rho_{50} = \frac{8.737 \times 10^5 \,\mathrm{Pa} \pm 2.77\% \times 0.0290 \,\mathrm{kg \, mol}^{-1}}{8.31 \,\mathrm{J \, mol}^{-1} \,\mathrm{K}^{-1} \times 296.3 \,\mathrm{K} \pm 0.1 \,\mathrm{K}} = 10.29 \,\mathrm{kg \, m}^{-3}$$

$$m_i = 1.195 \,\mathrm{kg} \,\mathrm{m}^{-3} \times (0.000 \,250 \,\mathrm{m}^3 \pm 0.000 \,001 \,\mathrm{m}^3) = 0.000 \,298 \,8 \,\mathrm{kg}$$
 (18)

$$m_{50} = 10.29 \,\mathrm{kg} \,\mathrm{m}^{-3} \times (0.000 \,250 \,\mathrm{m}^3 \pm 0.000 \,001 \,\mathrm{m}^3) = 0.002 \,571 \,\mathrm{kg}$$
 (19)

$$\dot{m}_{50} = \frac{\Delta m}{\Delta t} = \frac{0.002571 \,\mathrm{kg} - 0.0002988 \,\mathrm{kg}}{0.03982 \,\mathrm{s}} = 0.05702 \,\mathrm{kg} \,\mathrm{s}^{-1} \tag{20}$$

% uncertainty(
$$\dot{m}_{50}$$
) = 3.08% + 0.4% + $\frac{\pm 2 \,\mathrm{mL}}{250 \,\mathrm{mL}} \times 100 = 4.28\%$

With the mass flow rate we can finally calculate the efficiency of the rocket dependent on the pressure, the specific impulse.

$$I_{sp} = \frac{F}{\dot{m} \times q}$$

This required the average force, for a triangle:

$$F_{\text{avg}} = \frac{2A}{\text{Base}(\Delta T)}$$

And I researched the gravitational acceleration of my location:

$$I_{sp,50} = \frac{2 \times J_{50}}{\Delta t \times \dot{m}_{50} \times g} = \frac{2 \times 0.71 \,\mathrm{N\,s}}{0.039 \,82 \,\mathrm{s} \times 0.057 \,02 \,\mathrm{kg\,s^{-1}} \times 9.818 \,33 \,\mathrm{m\,s^{-2}}} = 48.94 \,\mathrm{s}$$

% uncertainty(
$$I_{sp,50}$$
) = 4.56% × 2 + $\frac{\pm 0.0002 \text{ s}}{0.03982 \text{ s}}$ + 4.28% = 13.09%

7.2 Tables

Table 3: Pressure Data

Amount of pumps	Volume / m ³	Pressure / Pa	Relative uncertainty / $\%$
0	0.000250	1.016×10^5	0.40
10	0.000630	2.560×10^{5}	3.29
20	0.001010	4.105×10^{5}	3.16
30	0.001390	5.649×10^{5}	3.12
40	0.001770	7.193×10^{5}	3.10
50	0.002150	8.738×10^{5}	3.08

Table 4: Force Measurements

Pumps amount	Peak start / s	Peak end / s	Peak height / N
	1 ear start / s	1 eak end / s	Teak neight / N
50	2.5071	2.5843	19
40	4.8642	4.9227	12
30	2.9819	3.0025	24
20	2.1416	2.1864	12
10	3.8678	3.8821	14
50	2.3462	2.3567	34
40	3.5060	3.5140	40
30	1.8302	1.8381	27
20	2.1203	2.1328	17
10	2.3507	2.3630	17
50	2.1928	2.2020	32
40	2.0100	2.0240	26
30	2.6686	2.6769	24
20	1.9926	2.0040	20
10	1.5973	1.6063	16
50	3.0298	3.0876	22
40	1.7300	1.7791	12
30	4.0077	4.0268	20
20	3.6033	3.6281	17
10	2.1055	2.1473	4
50	2.6245	2.6689	30
40	2.6613	2.6804	19
30	4.6452	4.6890	11
20	2.0122	2.0399	14
10	2.2739	2.2986	5

7.3 Experimental Data Tables

Table 5: Pressure and Volume Measurements with Uncertainties

Pumps	Volume / m ³	Pressure / Pa	Relative Uncertainty / %
0	0.000250	1.016×10^{5}	0.40
10	0.000630	2.560×10^{5}	3.29
20	0.001010	4.105×10^{5}	3.16
30	0.001390	5.649×10^{5}	3.12
40	0.001770	7.193×10^{5}	3.10
50	0.002150	8.738×10^{5}	3.08

Table 6: Comprehensive Results Summary

Pumps	Pressure / bar	Impulse / Ns	Mass Flow Rate / $kg s^{-1}$	Specific Impulse / s
10	2.6	0.11	0.0222	51
20	4.1	0.19	0.0375	43
30	5.6	0.21	0.0683	32
40	7.2	0.32	0.0583	38
50	8.7	0.55	0.0570	49

Note: All measurements include experimental uncertainties as detailed in the methodology section.

7.4 Statistical Analysis

The correlation coefficients between pressure and key parameters were calculated:

- Pressure vs Impulse: 0.989 (strong positive correlation)
- Pressure vs Specific Impulse: -0.236 (weak negative correlation)

7.5 Graphical Analysis

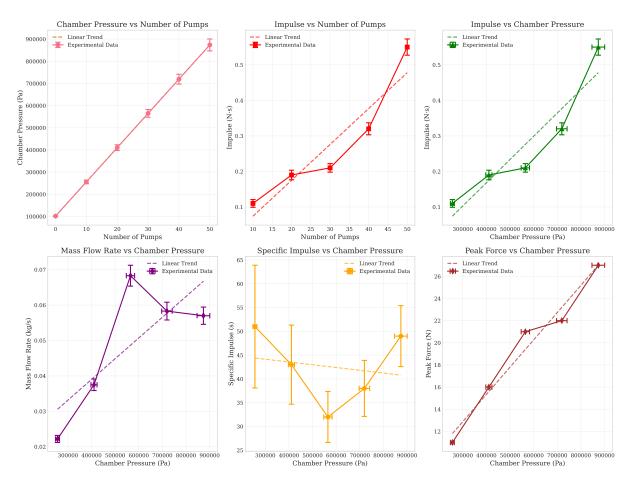
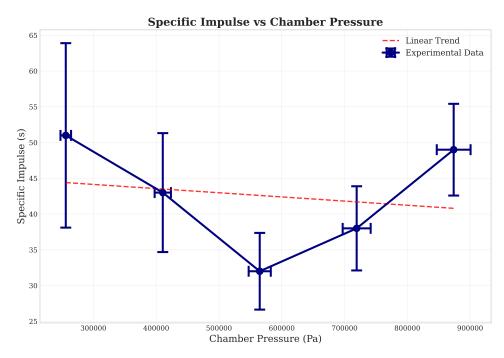
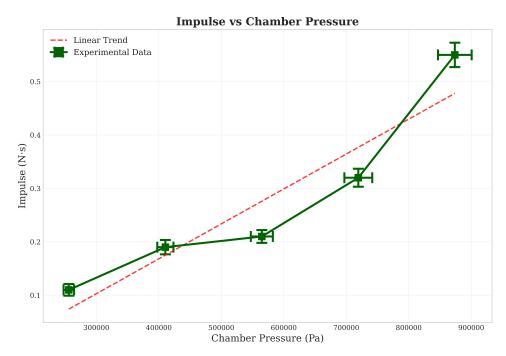


Figure 2: Comprehensive analysis showing relationships between pressure, impulse, mass flow rate, and specific impulse. Error bars indicate measurement uncertainties.



(a) Detailed analysis of specific impulse as a function of chamber pressure, showing error bars and linear trend



(b) Detailed analysis of impulse as a function of chamber pressure, showing error bars and linear trend

Figure 3: Detailed analysis of key relationships showing measurement uncertainties and trends

8 Data Analysis

8.1 Processing the Data

I had an incredible increase and range in pressure which I didn't actually expect, reaching all the way to more than 8 times atmospheric pressure. It would seem that one expects this to have a significant impact on performance. Then unfortunately there seems to be an outlier 30 pump measuring point, which is constantly deviating from the other expected values.

I think this might be because after finding leaks in my palimetry I added more O-rings to seal the chamber, it could be that even those rings did not seal the chamber correctly after pressures exceeded the pressure at 30 pumps reducing the actual pressure in the chamber than what I calculated due to leaks, for the following measurements. But I did not witness any signs of leaks when conducting my experiment.

8.2 Interpretation of Graphs

From looking at the graphs it is obvious that an increase in pressure very much increases impulse very directly, with a strong correlation, both against number of pumps and pressure. But the correlation between pressure and mass flow rate is almost as strong, but the angle of the line is less steep, this is probably because the nozzle throat does not limit the amount of mass that can exist at a time, which means the time which it takes for the mass to flow out is longer because there is more air particles in the rocket and therefore mass flow is strongly affected. And because the mass flow rate seems to be affected in this way the higher force measured gets cancelled out in the formula for specific impulse where we divide by the mass flow rate. In turn the higher force gets divided by a higher mass flow rate dampening the change, due to pressure.

Which is actually interesting to find out as well, I did not consider that both changes can cancel each other out leading to almost no visible correlation between pressure and specific impulse.

Although it has to be said that the uncertainty of 25% could also mean that the correlation might not be visible even though there may actually be one.

9 Evaluation

9.1 Strengths and Weaknesses

I think my experiment overall was not too bad, I did not go into this experiment expecting a crazy correlation so I am very happy with my findings. Apart from my force uncertainties which I was unable to impact as I had one force plate as an option only, I think that

especially my uncertainties which I made sure to keep low after preliminary testing were very strong.

A big weakness though was probably the noise and inconsistency of my readings. The force plate was constantly measuring force changes, only \pm 1 N, even if nothing was happening, this created some noise in my data which was hard to account for, and possibly my data would have been different. Also the inconsistency of my force and time measurements were not good, the spread across my measurements were too big for my liking.

Even though I very much enjoyed calculating surrounding variables like the pressures and the density of air, I think there might be better solutions possible. But actually it doesn't matter what the actual values are for this experiment as I am only investigating the correlation, and that would stay the same no matter if the values were wrong.

9.2 Sources of Error

A big source of my force readings will likely be that the force plate used was designed for far bigger forces which affect its accuracy and the accuracy of my measurements in the experiment. Not having equipment that can measure ambient pressure or that can take tests on the surrounding air, might have caused any wrong calculations due to researched values.

9.3 Improvements

Next time I would possibly look into using a scale as a force plate instead, which often goes to $0.001\,\mathrm{g}$ significant figures, far more accurate than the force plate, and then accounting for gravity to calculate the forces. This could decrease the % uncertainty and reduce the inconsistency of measurements.

Getting access to measurement equipment which can measure more atmosphere specific things similar to ones used in weather stations could have a huge impact on the relevance of my measurements to the surroundings of my experiment.

After digging even deeper I found that the mass flow rate is changing differently in proportion to pressure after the gases reach Mach 1 in the engine, because of the shock created in the nozzle limiting the mass flow rate completely, choking it, any further increase in pressure does not contribute to increase in mass flow rate. It is very possible that my experiment never choked at the nozzle, which means that there is a possibility for a stronger correlation from pressure to specific impulse at even higher pressures. So for future experiments, investigating how specific impulse is affected by pressure at high speed nozzles like the bell nozzle can be interesting as well, or at even higher pressures like my references like 100 bar.

Also using a proper converging diverging nozzle could lead to higher exhaust speeds, instead of just using a small hole. I have not listed this in sources of error, because the measurements would not be affected, the nozzle is constant throughout the measurements. But higher exhaust speed can contribute to the choked nozzle, giving the same possibility for a higher correlation between pressure and specific impulse.

Considering that one of my errors might be caused due to leaks as mentioned as an outlier. In the future, I would like to experiment with a correctly sealed real rocket engine, assuming that this can survive even higher pressures and does not leak.

10 Conclusion

In conclusion the chamber pressure of a rocket will have some impact on the specific impulse, and being able to reach higher pressures inside a rocket can be beneficial, as long as it is safe. But there might be other variables to look into which affect specific impulse more strongly [12] [13].

From this research I will be able to use my understanding to go out and design my rocket engine to be able to withstand higher pressures, although all pressures used in this experiment were only close to 8 bars I am looking forward to predicting even higher specific impulse in my rocket at 100-200 bars.

The experimental results show that while there is a relationship between chamber pressure and rocket performance, the relationship is complex and influenced by multiple factors including nozzle design, mass flow characteristics, and measurement limitations [12]. The data suggests that increased chamber pressure does generally lead to improved performance, but the relationship is not simply linear as initially hypothesized.

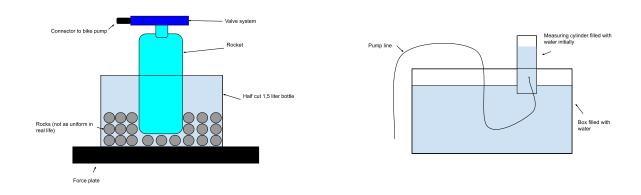
References

- [1] Space Stack Exchange. How is chamber pressure determined for rocket engines? Retrieved from: https://space.stackexchange.com/questions/21758/how-is-chamber-pressure-determined-for-rocket-engines
- [2] Lund University Publications. Retrieved from: https://lup.lub.lu.se/luur/download?func=downloadFile&recordOId=9183792&fileOId=9183793
- [3] Physics LibreTexts. Rocket Propulsion. Retrieved from: https://phys.libretexts.org/Bookshelves/University_Physics/University_Physics_
 (OpenStax)/Book:_University_Physics_I_-_Mechanics_Sound_Oscillations_
 and_Waves_(OpenStax)/09:_Linear_Momentum_and_Collisions/9.11:
 _Rocket_Propulsion

- [4] University of Central Florida. Rocket Propulsion. Retrieved from: https://pressbooks.online.ucf.edu/osuniversityphysics/chapter/9-7-rocket-propulsion/
- [5] MIT. Rocket Propulsion. Retrieved from: https://web.mit.edu/16.unified/www/SPRING/propulsion/notes/node103.html
- [6] Engineer Excel. Mass Flow Rate. Retrieved from: https://engineerexcel.com/mass-flow-rate/
- [7] MDPI. Retrieved from: https://www.mdpi.com/1996-1073/17/24/6455
- [8] Northwestern University. What is Specific Impulse? Retrieved from: https://web.archive.org/web/20160704233223/http://www.qrg.northwestern.edu/projects/vss/docs/Propulsion/3-what-is-specific-impulse.html
- [9] NASA. Specific Impulse. Retrieved from: https://www.grc.nasa.gov/WWW/k-12/airplane/specimp.html
- [10] NASA Technical Reports. Retrieved from: https://web.archive.org/web/20060825031851/http://trs.nis.nasa.gov/archive/00000186/01/sp8120.pdf
- [11] MIT. Nozzle Design. Retrieved from: https://wikis.mit.edu/confluence/pages/viewpage.action?pageId=153816550
- [12] Embry-Riddle Aeronautical University. Rocket Engines. Retrieved from: https://eaglepubs.erau.edu/introductiontoaerospaceflightvehicles/chapter/rocket-engines/
- [13] Space Voyage Ventures. Fuel Efficiency in Space-craft. Retrieved from: https://spacevoyageventures.com/fuel-efficiency-in-spacecraft-innovations-in-propulsion-and-energy-use/

A Appendix A: Measuring Data and Methodology

A.1 A.1 Experimental Setup and Data Collection

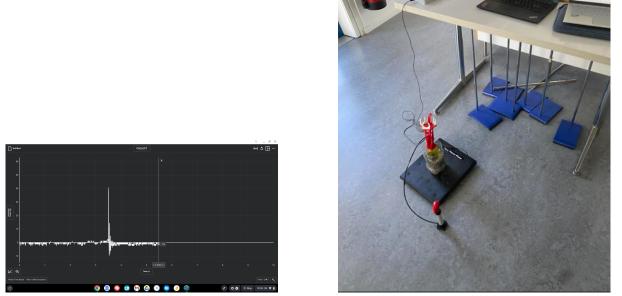


(a) Force measurement setup

(b) Water displacement measurement

Figure 4: Detailed experimental setup diagrams

A.2 A.2 Detailed Measuring Data



- (a) Experimental setup details
- (b) Detailed measuring data collection

Figure 5: Comprehensive experimental measurement data and setup details

A.3 Water Displacement Measurements



Figure 6: Water displacement measurement procedure and data collection

The water displacement measurements were conducted as described in the methodology section using the apparatus shown in Figure 4b. The detailed measurement procedure and data collection are documented in Figure 6.