Labs **Machine Learning Course** Fall 2021

EPFL

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Problem Set 12, Dec 7, 2021 (Theory Questions SVD)

Goals. The goal of this exercise is to

- familiarize yourself with the theory related to SVD.
- have time to discuss Project 2 with the assistants and teammates.

1 Theory Questions

Problem 1 (How to compute U and S efficiently):

In class, we saw that solving the eigenvector/value problem for the matrix XX^{\top} gives us a way to compute U and S. But in some instances $D \gg N$. In those cases, is there a way to accomplish this computation more efficiently?

Problem 2 (Positive semi-definite):

Show that if \boldsymbol{X} is a $N \times N$ symmetric matrix then the SVD has the form $\boldsymbol{U}\boldsymbol{S}\boldsymbol{U}^{\top}$, where \boldsymbol{U} is a $N \times N$ unitary matrix and \boldsymbol{S} is a $N \times N$ diagonal matrix with non-necessarily positive entries. Show that if \boldsymbol{X} is positive semi-definite, then all entries of \boldsymbol{S} are non-negative.

2 Generative Adversarial Networks

Recommended reading: explore how to implement a simple GAN in PyTorch using the Jupyter notebook gans.ipynb:

- Open in Google Colab: colab.research.google.com/github/epfml/ML_course/blob/master/labs/ex12/gans.ipynb.
 This gives you access to a free GPU.
- ullet Change the 'runtime type' to GPU under 'Runtime o Change runtime type'.