计算机系统基础

程序的机器级表示(5)

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提纲

- Arrays
 - One-dimensional
 - Multi-dimensional (nested)
 - Multi-level
- Structures
 - Allocation
 - Access
 - Alignment
- Floating Point



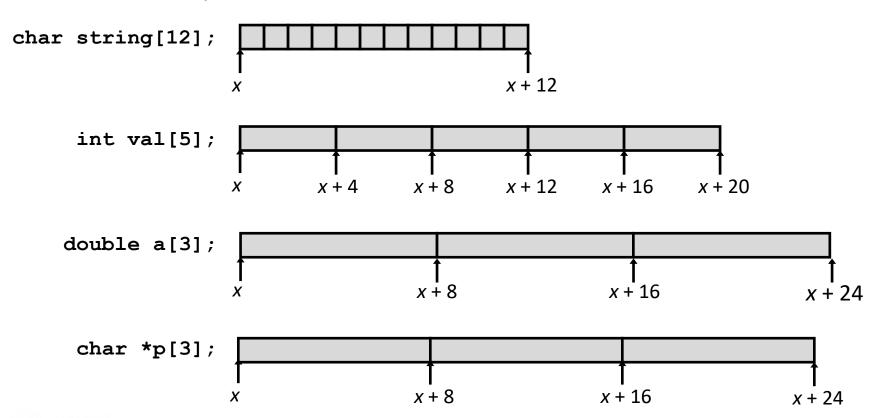


Array Allocation

Basic Principle

$T \mathbf{A}[L];$

- Array of data type T and length L
- Contiguously allocated region of L * sizeof (T) bytes in memory





Array Access

Basic Principle

$T \mathbf{A}[L];$

- Array of data type T and length L
- Identifier A can be used as a pointer to array element 0:
 Type T*

```
int val[5]; 1 5 2 1 3

x x + 4 x + 8 x + 12 x + 16 x + 20
```

Reference Type

val[4] int
val int *
val+1 int *
&val[2] int *
val[5] int
*(val+1) int
val + i int *

Value

3 x x+4 x+8 ?? 5 x+4*i



Array Access

Basic Principle

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T \mathbf{A}[L];
```

- Array of data type T and length L
- Identifier A can be used as a pointer to array element 0:
 Type T*

```
int val[5]; 1 5 2 1 3

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Reference Type Value

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val[4] int 3
val int *
val+1 int *
&val[2] int *
val[5] int
*(val+1) int
val + i int *
```



Array Access

Basic Principle

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T \mathbf{A}[L];
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```
int val[5]; 1 5 2 1 3
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```

Reference Type Value

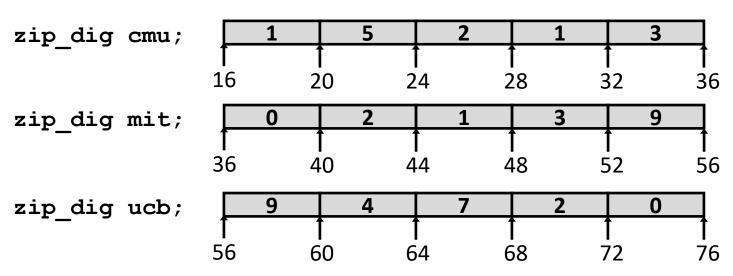
```
val[4] int 3
val int *
val+1 int *
&val[2] int *
val[5] int
*(val+1) int
val + i int *
```



Array Example

```
#define ZLEN 5
typedef int zip_dig[ZLEN];

zip_dig cmu = { 1, 5, 2, 1, 3 };
zip_dig mit = { 0, 2, 1, 3, 9 };
zip_dig ucb = { 9, 4, 7, 2, 0 };
```



- Declaration "zip_dig cmu" equivalent to "int cmu[5]"
- Example arrays were allocated in successive 20 byte blocks
 - Not guaranteed to happen in general



Array Accessing Example

```
int get_digit
  (zip_dig z, int digit)
{
  return z[digit];
}
```

IA32

```
# %rdi = z
# %rsi = digit
movl (%rdi, %rsi, 4), %eax # z[digit]
```

%rdi 数组起始 %rsi 索引 4为数据元素大小

- Register %rdi contains starting address of array
- Register %rsi contains array index
- Desired digit at %rdi + 4*%rsi
- Use memory reference (%rdi,%rsi,4)



Array Loop Example

```
void zincr(zip_dig z) {
   size_t i;
   for (i = 0; i < ZLEN; i++)
      z[i]++;
}</pre>
```

```
# %rdi = z
 movl $0, %eax
                         \# i = 0
                         # goto middle
 jmp .L3
.L4:
                         # loop:
 addl $1, (%rdi,%rax,4) # z[i]++
 addq $1, %rax
                         # 1++
.L3:
                         # middle
 cmpq $4, %rax
                         #
                             i:4
 jbe .L4 size t i 无
                         # if <=, goto loop</pre>
 rep; ret
```

Multidimensional (Nested) Arrays

- Declaration
 - $T \mathbf{A}[R][C];$
 - 2D array of data type T
 - R rows, C columns
 - Type T element requires K bytes
- Array Size
 - R * C * K bytes
- Arrangement
 - Row-Major Ordering

- A[0][0]	• • •	A[0][C-1]
•		•
A[R-1][0] • • •	A[R-1][C-1]

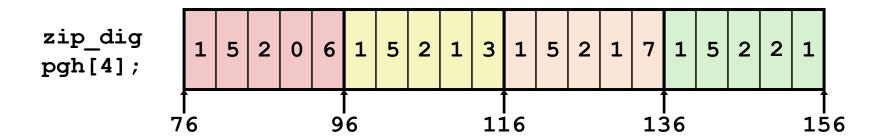
int A[R][C];

A [0] [0]	• • •	A [0] [C-1]	A [1] [0]	• • •	A [1] [C-1]	•	•	•	A [R-1] [0]		A [R-1] [C-1]
-----------------	-------	-------------------	-----------------	-------	-------------------	---	---	---	-------------------	--	---------------------

4*R*C Bytes

ested Array Example

```
#define PCOUNT 4
zip_dig pgh[PCOUNT] =
   {{1, 5, 2, 0, 6},
    {1, 5, 2, 1, 3},
    {1, 5, 2, 1, 7},
    {1, 5, 2, 2, 1 }};
```



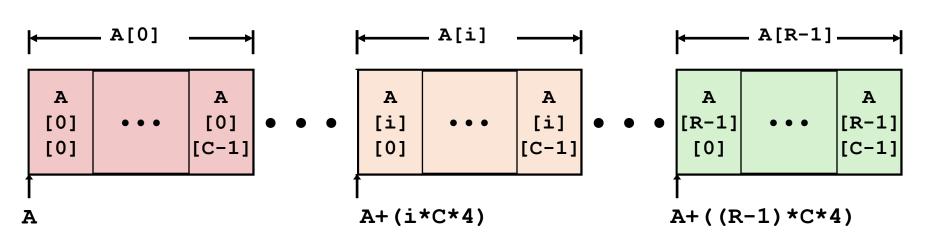
- "zip_dig pgh[4]" equivalent to "int pgh[4][5]"
 - Variable pgh: array of 4 elements, allocated contiguously
 - Each element is an array of 5 int's, allocated contiguously
- "Row-Major" ordering of all elements in memory



Nested Array Row Access

- Row Vectors
 - **A**[i] is array of *C* elements
 - Each element of type T requires K bytes
 - Starting address A + i * (C * K)

int A[R][C];





Nested Array Row Access Code

```
1 5 2 0 6 1 5 2 1 3 1 5 2 1 7 1 5 2 2 1

pgh

pgh

pgh[2]

int *get_pgh_zip(int index)
{
    return pgh[index];
}

# %rdi = index
    leaq (%rdi, %rdi, 4), %rax # 5 * index
    leaq pgh(, %rax, 4), %rax # pgh + (20 * index)
```

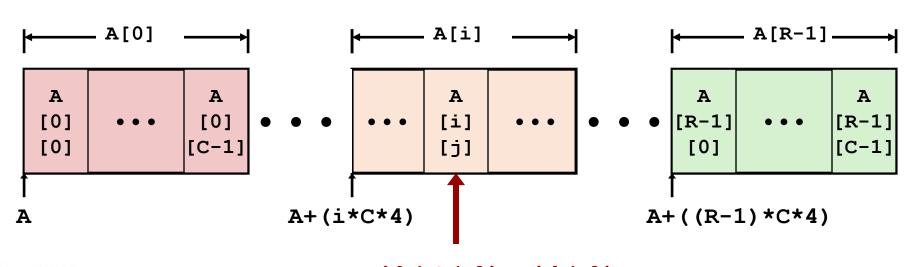
- Row Vector
 - pgh[index] is array of 5 int's
 - Starting address pgh+20*index
- Machine Code
 - Computes and returns address
 - Compute as pgh + 4*(index+4*index)



Nested Array Element Access

- Array Elements
 - A[i][j] is element of type T, which requires K bytes
 - Address **A** + i * (C * K) + j * K = A + (i * C + j) * K

int A[R][C];



$$A+(i*C*4)+(j*4)$$



Nested Array Element Access Code

```
leaq (%rdi,%rdi,4), %rax # 5*index
addl %rax, %rsi # 5*index+dig
movl pgh(,%rsi,4), %eax # M[pgh + 4*(5*index+dig)]
```

- Array Elements
 - pgh[index][dig] is int
 - Address: pgh + 20*index + 4*dig = pgh + 4*(5*index + dig)

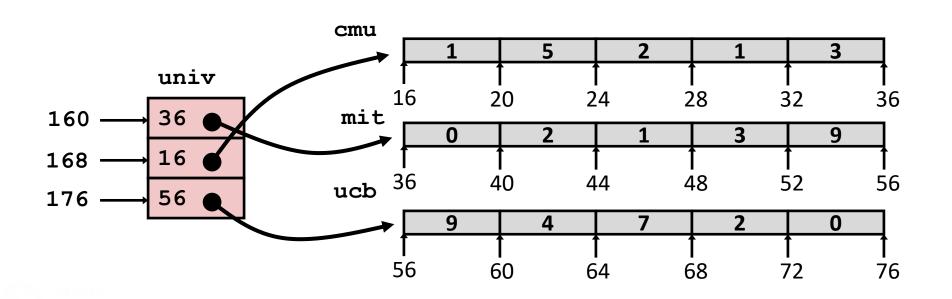


Multi-Level Array Example

```
zip_dig cmu = { 1, 5, 2, 1, 3 };
zip_dig mit = { 0, 2, 1, 3, 9 };
zip_dig ucb = { 9, 4, 7, 2, 0 };
```

```
#define UCOUNT 3
int *univ[UCOUNT] = {mit, cmu, ucb};
```

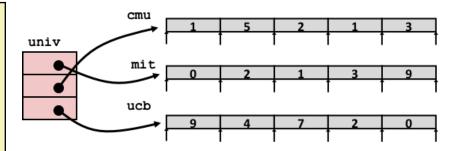
- Variable univ denotes array of 3 elements
- Each element is a pointer
 - 8 bytes
- Each pointer points to array of int's





Element Access in Multi-Level Array

```
int get_univ_digit
  (size_t index, size_t digit)
{
  return univ[index][digit];
}
```



```
salq $2, %rsi左移 # 4*digit
addq univ(,%rdi,8), %rsi # p = univ[index] + 4*digit
movl (%rsi), %eax # return *p
ret
```

存储器访问慢——第一种 方法好

- Computation
 - Element access Mem [Mem [univ+8*index]+4*digit]
 - Must do two memory reads
 - First get pointer to row array
 - Then access element within array



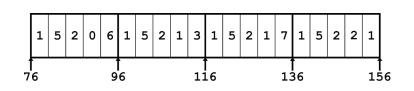
Array Element Accesses

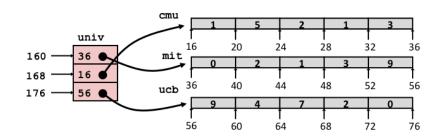
Nested array

```
int get_pgh_digit
  (size_t index, size_t digit)
{
  return pgh[index][digit];
}
```

Multi-level array

```
int get_univ_digit
  (size_t index, size_t digit)
{
  return univ[index][digit];
}
```





Accesses looks similar in C, but address computations very different:

```
Mem[pgh+20*index+4*digit] Mem[Mem[univ+8*index]+4*digit]
```



NXN Matrix Code

- Fixed dimensions
 - Know value of N at compile time
- Variable dimensions, explicit indexing
 - Traditional way to implement dynamic arrays
- Variable dimensions, implicit indexing
 - Now supported by gcc



16 X 16 Matrix Access

Array Elements

- Address **A** + i * (C * K) + j * K
- C = 16, K = 4

```
/* Get element a[i][j] */
int fix_ele(fix_matrix a, size_t i, size_t j) {
  return a[i][j];
}
```

```
# a in %rdi, i in %rsi, j in %rdx
salq $6, %rsi  # 64*i
addq %rsi, %rdi  # a + 64*i
movl (%rdi,%rdx,4), %eax # M[a + 64*i + 4*j]
ret
```



n X n Matrix Access

Array Elements

- Address **A** + i * (C * K) + j * K
- C = n, K = 4
- Must perform integer multiplication

```
/* Get element a[i][j] */
int var_ele(size_t n, int a[n][n], size_t i, size_t j)
{
   return a[i][j];
}
```

```
# n in %rdi, a in %rsi, i in %rdx, j in %rcx
imulq %rdx, %rdi  # n*i
leaq (%rsi,%rdi,4), %rax # a + 4*n*i
movl (%rax,%rcx,4), %eax # a + 4*n*i + 4*j
ret
```



Example: Array Access

```
#include <stdio.h>
#define ZLEN 5
#define PCOUNT 4
typedef int zip dig[ZLEN];
int main(int argc, char** argv) {
zip dig pgh[PCOUNT] =
    \{\{1, 5, 2, 0, 6\},
    {1, 5, 2, 1, 3},
    {1, 5, 2, 1, 7},
    {1, 5, 2, 2, 1 }};
    int *linear zip = (int *) pgh;
    int *zip2 = (int *) pgh[2];
    int result =
       pgh[0][0] +
       linear zip[7] +
        *(linear zip + 8) +
        zip2[1];
   printf("result: %d\n", result);
    return 0;
```

linux> ./array

1分



```
#include <stdio.h>
#define ZLEN 5
#define PCOUNT 4
typedef int zip dig[ZLEN];
int main(int argc, char** argv) {
zip dig pgh[PCOUNT] =
    \{\{1, 5, 2, 0, 6\},\
    {1, 5, 2, 1, 3 }, 强制转化为int* 指针
    {1, 5, 2, 1, 7},
                                             linux> ./array
    {1, 5, 2, 2, 1 }};
                                             result:
    int *linear zip = (int *) pgh;
    int *zip2 = (int *) pgh[2];
                                               [填空1]
    int result =
       pgh[0][0] +
       linear zip[7] +
       *(linear zip + 8) +
       zip2[1];
   printf("result: %d\n", result);
    return 0;
```



Example: Array Access

```
#include <stdio.h>
#define ZLEN 5
#define PCOUNT 4
typedef int zip dig[ZLEN];
int main(int argc, char** argv) {
zip dig pgh[PCOUNT] =
    \{\{1, 5, 2, 0, 6\},
    \{1, 5, 2, 1, 3\},\
    \{1, 5, 2, 1, 7\},\
    {1, 5, 2, 2, 1 }};
    int *linear zip = (int *) pgh;
    int *zip2 = (int *) pgh[2];
    int result =
        pgh[0][0] +
        linear zip[7] +
        *(linear zip + 8) +
        zip2[1];
    printf("result: %d\n", result);
    return 0;
```

```
linux> ./array
result: 9
```

STATE OF THE PARTY OF THE PARTY

提纲

- Arrays
 - One-dimensional
 - Multi-dimensional (nested)
 - Multi-level
- Structures
 - Allocation
 - Access
 - Alignment
- Floating Point





Structure Representation

```
struct rec {
   int a[4];
   size_t i;
   struct rec *next;
};
```

```
r
a i next
0 16 24 32
```

- Structure represented as block of memory
 - Big enough to hold all of the fields
- Fields ordered according to declaration
 - Even if another ordering could yield a more compact representation
- Compiler determines overall size + positions of fields
 - Machine-level program has no understanding of the structures in the source code



Generating Pointer to Structure Member

```
struct rec {
   int a[4];
   size_t i;
   struct rec *next;
};
```

```
r r+4*idx
a i next
0 16 24 32
```

- Generating Pointer to Array Element
 - Offset of each structure member determined at compile time
 - Compute as r + 4*idx

```
int *get_ap
  (struct rec *r, size_t idx)
{
   return &r->a[idx];
}
```

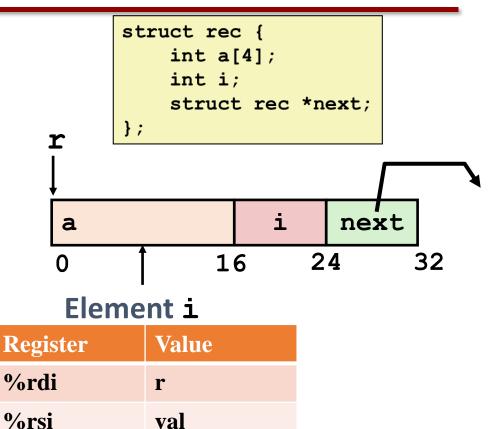
```
# r in %rdi, idx in %rsi
leaq (%rdi,%rsi,4), %rax
ret
```



Following Linked List

• C Code

```
void set_val
  (struct rec *r, int val)
{
  while (r) {
    int i = r->i;
    r->a[i] = val;
    r = r->next;
  }
}
```

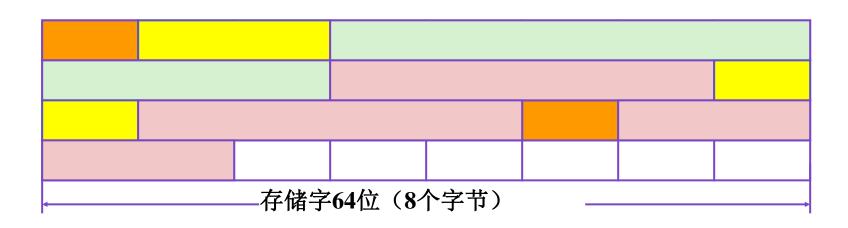




对齐问题

不浪费存储器资源的存放方法

现有一批数据,它们依次为:字节、半字、双字、单字、半字、单字、字节、单字。 4种不同长度的数据一个紧接着一个存放。



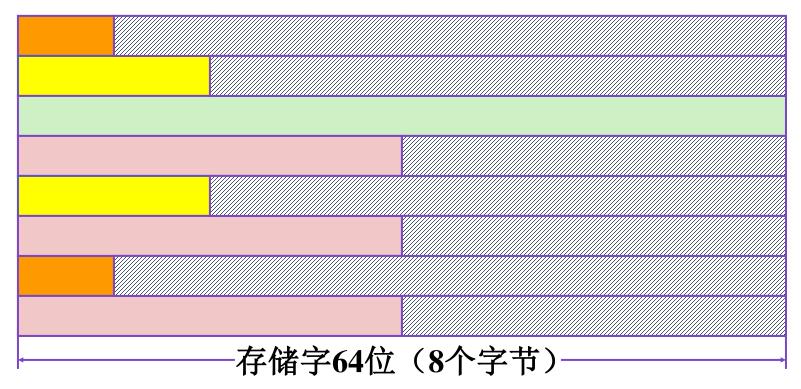
优点:不浪费宝贵的主存资源,

缺点: 当访问的一个双字、单字或半字跨越两个存储单元时,

存储器的工作速度降低了一半,而且读写控制比较复杂。



从存储字的起始位置开始存放



优点: 无论访问一个字节、半字、单字或双字都可以在一个存储周期内完

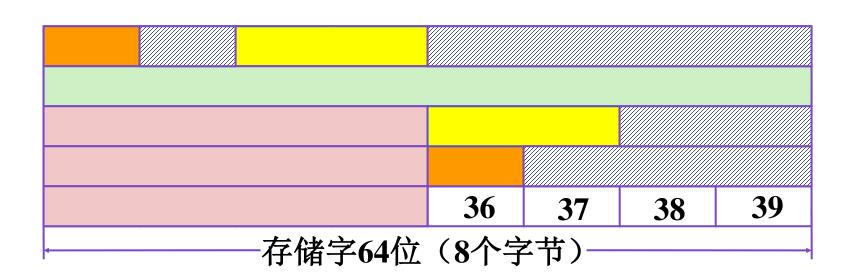
成,读写数据的控制比较简单。

缺点: 浪费了宝贵的存储器资源。



边界对齐的数据存放方法

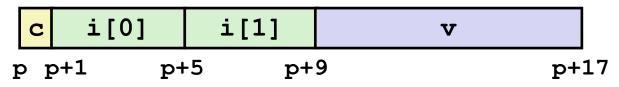
此方法规定,双字地址的最末3个二进制位必须为000,单字地址的最末两位必须为00,半字地址的最末一位必须为0。它能够保证无论访问双字、单字、半字或字节,都在一个存取周期内完成,尽管存储器资源仍然有浪费。





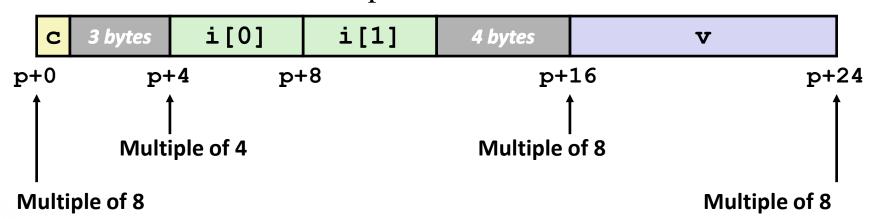
Structures & Alignment

Unaligned Data



```
struct S1 {
  char c;
  int i[2];
  double v;
} *p;
```

- Aligned Data
 - Primitive data type requires **K** bytes
 - Address must be multiple of **K**





Alignment Principles

- Aligned Data
 - Primitive data type requires **K** bytes

编译会加入填充

- Address must be multiple of **K**
- Required on some machines; advised on x86-64
- Motivation for Aligning Data
 - Memory accessed by (aligned) chunks of 4 or 8 bytes (system dependent)
 - Inefficient to load or store datum that spans quad word boundaries
 - Virtual memory trickier when datum spans 2 pages
- Compiler
 - Inserts gaps in structure to ensure correct alignment of fields



Specific Cases of Alignment

- 1 byte: **char**, ...
 - no restrictions on address
- 2 bytes: **short**, ...
 - lowest 1 bit of address must be 0₂
- 4 bytes: int, float, ...
 - lowest 2 bits of address must be 00₂
- 8 bytes: double, long, char *, ...
 - lowest 3 bits of address must be 000₂
- 16 bytes: long double (GCC on Linux)
 - lowest 4 bits of address must be 0000₂



Satisfying Alignment with Structures

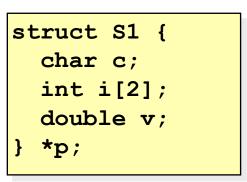
- Within structure:
 - Must satisfy each element's alignment requirement
- Overall structure placement
 - Each structure has alignment requirement **K**
 - **K** = Largest alignment of any element
 - Initial address & structure length must be multiples of **K**
- Example:
 - **K** = 8, due to **double** element NOTE: K < sizeof(struct S1)

```
p+0 p+4 p+8 p+16 p+24

Multiple of 4 Multiple of 8

Multiple of 8

Internal padding
```

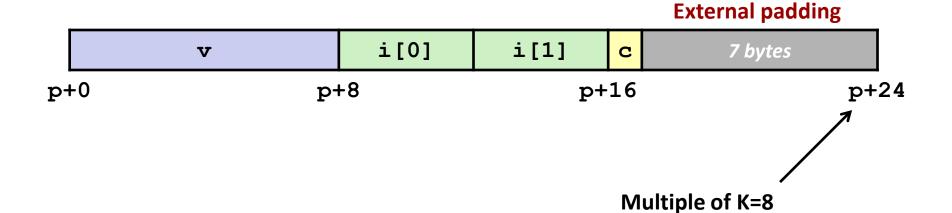




Meeting Overall Alignment Requirement

- For largest alignment requirement K
- Overall structure must be multiple of K

```
struct S2 {
  double v;
  int i[2];
  char c;
} *p;
```

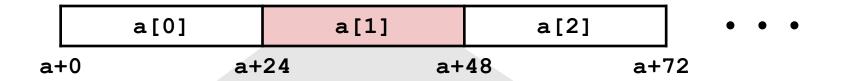


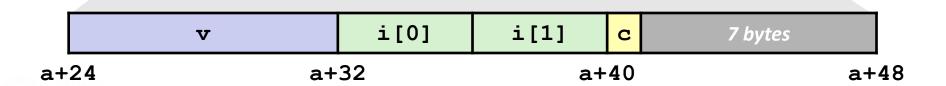


Arrays of Structures

- Overall structure length multiple of K
- Satisfy alignment requirement for every element

```
struct S2 {
  double v;
  int i[2];
  char c;
} a[10];
```







Accessing Array Elements

- Compute array offset 12*idx
 - sizeof(S3), including alignment spacers
- Element j is at offset 8 within structure
- Assembler gives offset a+8
 - Resolved during linking

```
a[0] • • • a[idx] • • • • a+12*idx

i 2 bytes v j 2 bytes
a+12*idx a+12*idx+8
```

```
short get_j(int idx)
{
   return a[idx].j;
}
```

```
# %rdi = idx
leaq (%rdi,%rdi,2),%rax # 3*idx
movzwl a+8(,%rax,4),%eax
```

struct S3 {

short i;

float v;

short j;

} a[10];



Alignment

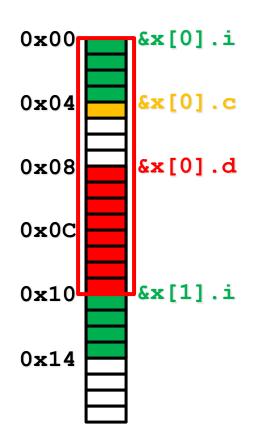
- Structure data type
 - may need to insert gaps in the field allocation
 - may need to add padding to the end of the structure



Simple Example

```
struct xxx {
  int i;
  char c;
  double d;
};
```

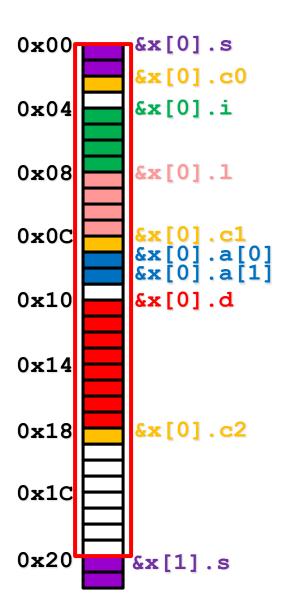
Struct整体对齐规则 由其中最大的元素决定 (此例为8字节)





Complex Example

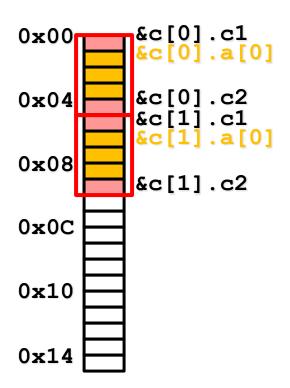
```
struct xxx {
    short s;
    char c0;
    int i;
    long 1;
    char c1;
    char a[2];
    double d;
    char c2;
};
struct xxx x[2];
```





Array

```
struct ccc {
    char c1;
    char a[3];
    char c2;
};
```

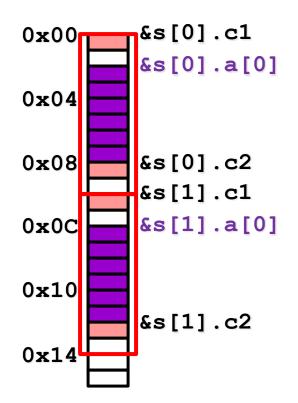


42



Array

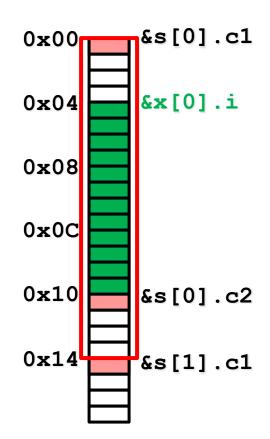
```
struct ccc {
    char c1;
    short a[3];
    char c2;
};
```





Array

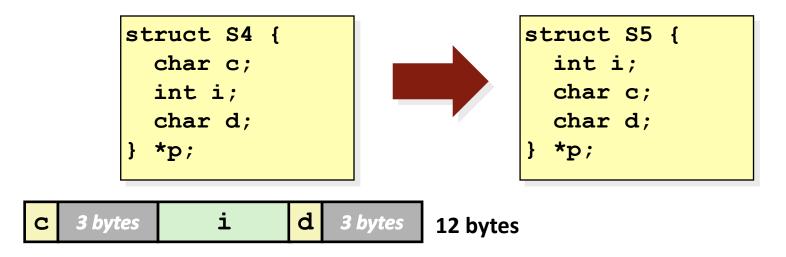
```
struct iii {
    char c1;
    int a[3];
    char c2;
};
```



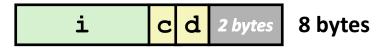


Saving Space

• Put large data types first



• Effect (largest alignment requirement K=4)





Union

- •两个/多个部分,同一段内存有不同的解读方式
- A single object can be referenced by using different data types
- The syntax of a union declaration is identical to that for structures, but its semantics are very different
- Rather than having the different fields reference different blocks of memory, they all reference the same block



Union

```
struct S3 {
  char c;
  int i[2];
  double v;
};
union U3 {
  char c;
  int i[2];
  double v;
```

The offsets of the fields, as well as the total size of data types S3 and U3, are:

Type	С	i	٧	size
53	0	4	12	20
U3	0	0	0	8

SUVERS/TI-OCCULINA 1937 F. F.

提纲

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Background

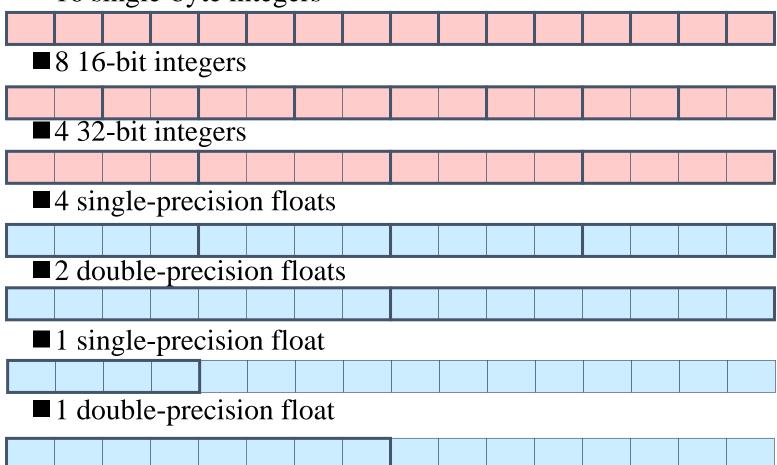
- History
 - x87 FP
 - Legacy, very ugly
 - SSE FP
 - Supported by server machines
 - Special case use of vector instructions
 - AVX FP
 - Newest version
 - Similar to SSE
 - Documented in book



Programming with SSE3

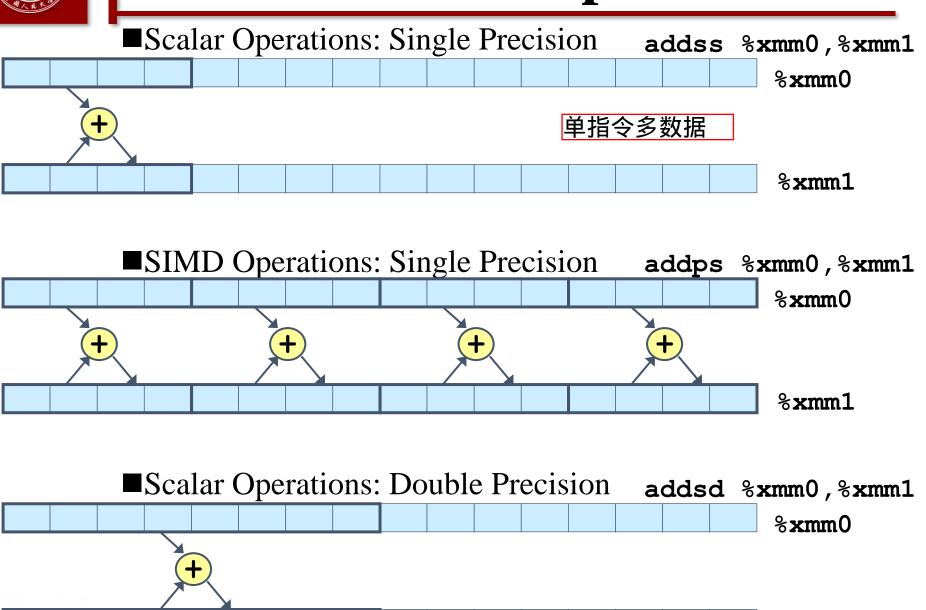
XMM Registers

- 16 total, each 16 bytes
- 16 single-byte integers





Scalar & SIMD Operations



%xmm1



FP Basics

- Arguments passed in %xmm0, %xmm1, ...
- Result returned in %xmm0
- All XMM registers caller-saved

```
float fadd(float x, float y)
{
    return x + y;
}
```

```
double dadd(double x, double y)
{
    return x + y;
}
```

```
# x in %xmm0, y in %xmm1
addss %xmm1, %xmm0
ret
```

```
# x in %xmm0, y in %xmm1
addsd %xmm1, %xmm0
ret
```



FP Memory Referencing

- Integer (and pointer) arguments passed in regular registers
- FP values passed in XMM registers
- Different mov instructions to move between XMM registers, and between memory and XMM registers

```
double dincr(double *p, double v)
{
    double x = *p;
    *p = x + v;
    return x;
}
```

```
# p in %rdi, v in %xmm0
movapd %xmm0, %xmm1  # Copy v
movsd (%rdi), %xmm0  # x = *p
addsd %xmm0, %xmm1  # t = x + v
movsd %xmm1, (%rdi) # *p = t
ret
```



Other Aspects of FP Code

- *Lots* of instructions
 - Different operations, different formats, ...
- Floating-point comparisons
 - Instructions ucomiss and ucomis
 - Set condition codes ZF, PF and CF Parity Flag
 - Zeros OF and SF

UNORDERED: ZF,PF,CF←111

GREATER THAN: ZF,PF,CF←000

LESS THAN: ZF,PF,CF←001

EQUAL: ZF,PF,CF←100

- Using constant values
 - Set XMM0 register to 0 with instruction xorpd %xmm0, %xmm0
 - Others loaded from memory



课堂练习

```
下面的定义声明了一类结构,用来构建二叉树:
                                              // 表示tree_ptr实际上是ELE*类型
        typedef struct ELE *tree_ptr;
        struct ELE {
                 tree_ptr
                           left;
4
                 tree ptr
                           right;
5
                 long
                           val;
6
        对于如下函数原型
                           long trace(tree_ptr tp); GCC产生了下面的x86-64代码:
                                    ; tp in %rdi
1 trace:
                           $0, %eax
                 movl
                           %rdi, %rdi
                 testq
                           .L3
                 je
        .L5
                           16(%rdi), %rax
6
                 movq
                           (%rdi), %rdi
                 movq
8
                           %rdi, %rdi
                 testq
9
                           .L5
                 ine
10
        .L3
                           ;函数返回,返回值一般放在%rax中
11
                 ret
```

(1) 请写出该函数的最简洁的C语言版本,使用while循环; (2) 用自然语言解释该函数的功能。



课堂练习

你负责维护一个大型的C程序,遇到下面的代码:编译时常数 CNT和结构a_struct的声明是在一个你没有访问权限的文件中。

```
1 typedef struct {
```

- 2 int first;
- 3 a_struct a[CNT];
- 4 int last;
- 5 }b_struct;
- 6 void test(long i, b_struct *bp)
- 7 int n = bp->first + bp->last;
- 8 $a_{\text{struct }}*ap = \&bp->a[i];$
- 9 ap->x[ap->idx] = n;
- 10}

幸好你有代码的.o版本,反汇编的代码为:

void test(long i, b_struct *bp) {

i in %rdi, bp in %rsi

1 000000000000 <test>:

2 0: 8b 8e 20 01 00 00 mov 0x120(%rsi), %ecx

3 6: 03 0e add (%rsi), %ecx

4 8: 48 8d 04 bf lea (%rdi, %rdi, 4), %rax

5 c: 48 8d 04 c6 lea (%rsi, %rax, 8), %rax

6 10: 48 8b 50 08 mov 0x8(%rax), %rdx

7 14: 48 63 c9 movslq %ecx, %rcx

8 17: 48 89 4c d0 10 mov %rcx, 0x10(%rax, %rdx, 8)

9 1c: c3. retq

请推断:

A. CNT的值; 40?

B. 结构体a_struct的完整声明,假设其中只有字段idx和x,且都是有符号数



课堂练习

```
typedef union {
                       // 32位机环境下
 struct{
                       //up@eax, dest@edx
                       void get(u_type *up, TYPE *dest) {
  short v;
  short d;
                         *dest = EXPR;
  int s;
                       EXPR分为为以下值时,求TYPE和get
 } t1;
                       函数的汇编代码:
 struct{
                       1. up->t1.s
  int a[2];
                       2. up->t1.v
  char *p;
                       3. &up->t1.d
 } t2;
                       4. up->t2.a
}u_type;
                       5. up->t2.a[up->t1.s]
                       6. *up->t2.p
```



练习答案

```
struct{
                                                 short v;
                                                 short d;
// 32位机环境下
                                                 int s;
                                                } t1;
//up@eax, dest@edx
                                                struct{
void get(u_type *up, TYPE *dest) {
                                                 int a[2];
  *dest = EXPR;
                                                 char *p;
                                                } t2;
                                               }u_type;
EXPR分为为以下值时,求TYPE和get
函数的汇编代码:
                     1) int, movl 4(%eax), %eax
                                                   movl %eax, (%edx)
1. up->t1.s
                     2) short, movw (%eax),%ax
                                                   movw %ax, (%edx)
2. up->t1.v
                     3) short *, leal 2(%eax), %eax
                                                   movl %eax, (%edx)
3. &up->t1.d
                     4) int *, movl %eax, (%edx)
4. up->t2.a
                     5) int, movl 4(%eax), %ecx
5. up->t2.a[up->t1.s]
                     movl (%eax, %ecx, 4), %eax
                                                   movl %eax, (%edx)
6. *up->t2.p
```

6) char, movb 8(%eax), %al

typedef union {

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movb al, (%edx)

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Summary

- Arrays
 - Elements packed into contiguous region of memory
 - Use index arithmetic to locate individual elements
- Structures
 - Elements packed into single region of memory
 - Access using offsets determined by compiler
 - Possible require internal and external padding to ensure alignment
- Combinations
 - Can nest structure and array code arbitrarily
- Floating Point
 - Data held and operated on in XMM registers