

Algo Notes

January 31, 2020

$m = \# \text{ of parties}$

$n = \text{max set size per party}$

$t = \text{threshold}$ (both thresholds, intersection and the secret sharing threshold)

Each bin is padded to max.

Assumptions:

- Keyholder is semi-honest
- Keyholder is not a party
- Keyholder sees at most $t-1$ shares (ever)

Scheme F

prime p , generator g
 $H(\cdot), H_B(\cdot)$
Keyholder: K_1, K_2
 $r_1, \dots, r_{t-1} \leftarrow \mathbb{F}_p$

} Set up
} global randomness

Share gen on next page.

"Homomorphic" Enc Scheme

• $PK, SK, Enc(\cdot)$

Share gen:

(For each element holder i)

identify r

Keyholder

$$K \leftarrow K_1, K_2$$

Element holder

x

$$\alpha \xleftarrow{P} \mathbb{F}_p$$

$$H(x)^\alpha, g^\alpha, id$$

$$r \xleftarrow{P} \mathbb{F}_p$$

$$g^{r\alpha} \cdot H(x)^{K_1\alpha}$$

$$\rightarrow R^\alpha H(x)^{\alpha K_1}$$

$$\text{where } R^\alpha = (g^r)^\alpha$$

not known by
element holder

$$R H(x)^{K_1}$$

"homomorphic"

Computes remaining $R = g^r$

* Choose encryption scheme

$$\leftarrow \text{Enc}_{pk}[R H(x)^{K_1}]$$

$$\text{Enc}_{pk}[H(x)^{K_1}]$$

For each global r_i :

$$g^{r_i\alpha} \cdot H(x)^{r_i\alpha}$$

$$\rightarrow \text{Enc}_{pk}[R H(x)^{r_i}]$$

$$\text{Enc}[H(x)^{K_1} R] \cdot \text{Enc}(\frac{1}{R})$$

$$\sum (id^i \text{Enc}(H(x)^{r_i}) + \text{Enc}(H(x)^{K_1}))$$

$$= \text{Enc}[SS(H(x)^{K_1}, id)]$$

* MAC?

$$(H(x) \bmod \# \text{ of bins}, SS(H(x)^{K_1}, id))$$

Recon:

Each participant sends their shares to the reconstructor \mathcal{R} who is a participant

For each bin

For each $\binom{m}{t}$ subset of the participants
- use Lagrange interpolation

↳ magically validate it for
our t requirements.