

# Culvert

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## Abstract

Equations for culvert calculations.

## 1 Inlet Control Equations

### 1.1 Unsubmerged Inlet Control Equations

$$\frac{Q}{AD^{0.5}} \leq 3.5 \text{ (1.93 SI)}$$

$$\frac{HW_i}{D} = \frac{H_c}{D} + K \left[ \frac{K_u Q}{AD^{0.5}} \right]^M + K_s S \quad (1)$$

### 1.2 Submerged Inlet Control Equations

$$\frac{Q}{AD^{0.5}} \geq 4.0 \text{ (2.21 SI)}$$

$$\frac{HW_i}{D} = c \left[ \frac{K_u Q}{AD^{0.5}} \right]^2 + Y + K_s S \quad (2)$$

where

$HW_i$  = Headwater depth above inlet control section invert, ft (m),

$D$  = Interior height of culvert barrel, ft (m),

$H_c$  = Specific head at critical depth ( $d_c + v_c^2/2g$ ), ft (m),

$Q$  = Discharge, ft<sup>3</sup>/s (m<sup>3</sup>/s),

$A$  = Full cross sectional area of culvert barrel, ft<sup>2</sup>(m<sup>2</sup>),

$S$  = Culvert barrel slope, ft/ft (m/m),

$K_u$  = unit conversion factor, 1 for English units (1.811 for SI), and

$K_s$  = slope correction, -0.5 (mitered inlets 0.7).

$$H_c = d_c + \frac{v_c^2}{2g} = d_c + \frac{v_c^2}{2g} = d_c + \frac{D_{h,c}}{2} = d_c + \frac{A_c}{2T_c} \quad (3)$$

## 2 Outlet Control

For full flow conditions, energy balance equation is

$$HW_o + LS + \frac{V_u^2}{2g} = TW + \frac{V_d^2}{2g} + H_L \quad (4)$$

where

$HW_o$  = Headwater depth above the entrance invert in outlet control, ft (m),

$V_u$  = Approach velocity, ft/s (m/s),

$TW_o$  = Tailwater depth above the outlet invert, ft (m),

$V_d$  = Downstream velocity, ft/s (m/s),

$H_L$  = Sum of all losses including entrance ( $H_e = K_e \frac{V_u^2}{2g}$ ), friction ( $H_f = \frac{K_u n^2 L}{R^{1.33}} \frac{V^2}{2g}$ ), exit ( $\frac{V^2}{2g} - \frac{V_d^2}{2g}$ ), and other losses)  $H_b$ ,  $H_j$ , ft (m),

$K_u$  = unit conversion factor, 29 for English units (19.63 for SI),

$L$  = Length of the culvert, ft (m), and

$S$  = Culvert barrel slope, ft/ft (m/m),

In general,  $V_u$  and  $V_d$  are neglected

$$HW_o = \max(TW, \frac{d_c + D}{2}) + H_L - LS = \max(TW, \frac{d_c + D}{2}) - LS + \left(1 + K_e + \frac{K_u n^2 L}{R^{1.33}}\right) \frac{V^2}{2g} \quad (5)$$

with  $V = Q/A$  where  $A$  is the full cross section area.

For unsubmerged outlet,