$$X_{\mathbf{a}}[n] = \frac{-1}{2\pi} \left[\frac{e^{j\frac{\pi}{2}n} + \frac{\pi}{2}e^{j\frac{\pi}{2}n}}{n^2 - 1} \right] - \left[\frac{-i\frac{\pi}{2}n}{n^2 - 1} \right] = \frac{-i\frac{\pi}{2}n}{n^2 - 1}$$

$$X_{a}[n] = \frac{-1}{2\pi(n^{2}-1)} \left[e^{\frac{-1\pi}{2}n} - \frac{\pi}{12}n + \frac{\pi}{12}n \left(e^{\frac{-1\pi}{2}n} - e^{\frac{-1\pi}{2}n} \right) \right]$$

$$= \frac{-1}{2\pi(n^2-1)} \left[\frac{\cos(\frac{\pi}{2}n)}{2} - \pi \cos(\frac{\pi}{2}n) \right]$$

$$X_{a}[n] = \frac{-\cos\left(\frac{\pi}{2}n\right)\left(\frac{1}{2}-\pi\right)}{2\pi\left(n^{2}-1\right)}$$