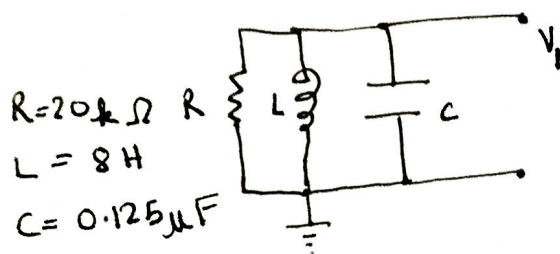


CIRCUITS

I Parallel RLC Resonator



$$V_2 = \frac{dV_1}{dt}$$

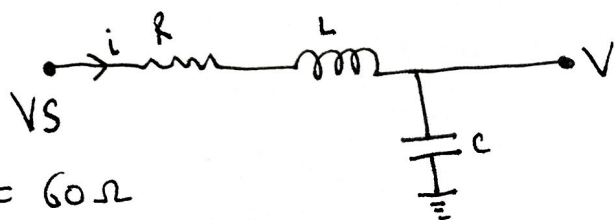
$$V_1(0) = 0 \text{ V}$$

$$\left. \frac{dV_2}{dt} \right|_{t=0} = 1 \text{ V/s}$$

$$\frac{dV_2}{dt} = -\frac{V_2}{RC} - \frac{V_1}{LC}$$

$$\text{Resonant frequency} = 159.15 \text{ Hz}$$

II Low-Pass Filter



$$\frac{di}{dt} = (V_S - V - iR) / L$$

$$\frac{dV}{dt} = \frac{i}{C}$$

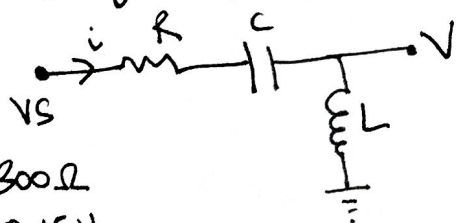
$$V(0) = 0$$

$$i(0) = 0$$

$$V_S = \sin(2\pi \cdot 20t) + \sin(2\pi \cdot 500t) + \sin(2\pi \cdot 140t)$$

$$\text{Cut-off frequency} = 44.67 \text{ Hz}$$

III High-Pass Filter



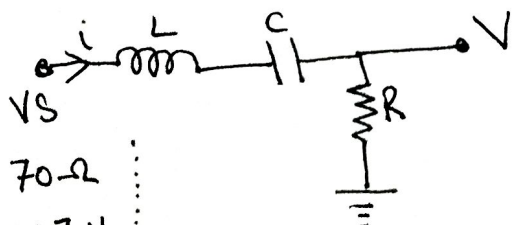
$$i_1 = \frac{di}{dt} ; V_1 = \frac{dV}{dt}$$

$$\frac{di_1}{dt} = \frac{V_1}{L} ; \frac{dV_1}{dt} = \frac{d^2 V_S}{dt^2} - \frac{i_1}{C} - \frac{R V_1}{L}$$

$$V_S = \sin(2\pi \cdot 10t) + \sin(2\pi \cdot 500t)$$

$$\text{Cut-off frequency} = 410.94 \text{ Hz}$$

IV Band-Pass Filter



$$i_1 = \frac{di}{dt} ; V_1 = \frac{dV}{dt} ; \frac{di_1}{dt} = \left(\frac{dV_S}{dt} - V_1 - \frac{i}{C} \right) / L$$

$$\frac{dV_1}{dt} = \frac{R}{L} \times \left(\frac{dV_S}{dt} - V_1 - \frac{i}{C} \right)$$

$$\text{Center-frequency} = 141.28 \text{ Hz}$$

$$V_S = \sin(2\pi \cdot 10t) + \sin(2\pi \cdot 500t) + \sin(2\pi \cdot 140t)$$