

University of Central Punjab  
Theory of Automata  
Spring 2023 - Midterm  
All Sections

Allowed Time: 90 minutes

Note: Manage your time during solution of Questions. Total Questions are 5

Problem 1: (2,8)

- Give at least 6 strings in ascending order of string length of the following language
- Design a DFA of the following language.

$$L = \{w \in \{a,b\}^* \mid w \text{ contains the substring } aba \text{ and } bb \text{ not necessarily together}\}$$

Problem 2: (5+5)

Design an NFA of the following language with at most 4 states

- Design NFA without NULL transition of the following language with at most 4 states

$$0(101 + 10)^*$$

- Design an NFA of the following language with at most 4 states

$$L = \{w \in \{0,1\}^* \mid w \text{ starts with } 01 \text{ or } 10 \text{ but does not end at } 11\}$$

Problem 3: (10)

Covert the following NFA into DFA. (Start State 1 and Final State 3)

	$\delta(q,a)$	$\delta(q,b)$
$\rightarrow 1$	$\{1,2,3,4,5\}$	$\{4,5\}$
2	$\{3\}$	$\{5\}$
3 *	$\emptyset$	$\{2\}$
4	$\{5\}$	$\{4\}$
5	$\emptyset$	$\emptyset$

Problem 4: (4,6)

	$\delta(q,a)$	$\delta(q,b)$	$\delta(q,\epsilon)$
$\rightarrow 1$	$\{1\}$	$\emptyset$	$\{2,4\}$
2	$\{3\}$	$\{5\}$	$\emptyset$
3	$\emptyset$	$\{2\}$	$\emptyset$
4	$\{4,5\}$	$\emptyset$	$\emptyset$
5 *	$\emptyset$	$\emptyset$	$\{1\}$

Consider the above Finite Automata answer the following. Start State is 1 and Final State is 5.

- Compute  $\epsilon$ -Closure (NULL CLOSURE) of all states
- Draw tree of string babab.

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Problem 5: (5 + 5)

- a. Give the Regular Expression of the language with set of strings that contains odd number of 0's or odd number 1's.
- b. Give a Regular Expression of the language which contains substrings either aa or aba or both but ends at b.