

# UNIVERSITY OF CENTRAL PUNJAB, LAHORE

## Multivariate Calculus

Assignment#3

Attach this sheet with your assignment.

Name: \_\_\_\_\_ Reg. \_\_\_\_\_

### Question No.1

Two products are manufactured in quantities  $q_1$  and  $q_2$  and sold at prices of  $p_1$  and  $p_2$  respectively. The cost of producing them is given by  $C = 2q_1^2 + 2q_2^2 + 10$ .

- Find the maximum profit that can be made, assuming the prices are fixed.
- Find the rate of change of that maximum profit as  $p_1$  increases.

### Question No.2

For  $f(x, y) = A - (x^2 + Bx + y^2 + Cy)$ , what values of  $A, B$  and  $C$  give  $f$  a local maximum value of 15 at the point  $(-2, 1)$ ?

### Question No.3

Show that the function

$$Z = bX^aY^{1-a}$$

Satisfy the equation

$$X \frac{\partial Z}{\partial X} + Y \frac{\partial Z}{\partial Y} = Z$$