

# Multiprocessing

Multiprocessing refers to the ability of a system to support more than one processor at the same time. Applications in a multiprocessing system are broken to smaller routines that run independently. The operating system allocates these threads to the processors improving performance of the system. A multiprocessing system can have: multiprocessor, i.e. a computer with more than one central processor. multi-core processor, i.e. a single computing component with two or more independent actual processing units (called “cores”).

**In Python, the multiprocessing module includes a very simple and intuitive API for dividing work between multiple processes.**

In [ ]:

```
# importing the multiprocessing module
import multiprocessing
def print_cube(num):
    """
    function to print cube of given num
    """
    print("Cube: {}".format(num * num * num))

def print_square(num):
    """
    function to print square of given num
    """
    print("Square: {}".format(num * num))

if __name__ == "__main__":
    # creating processes
    p1 = multiprocessing.Process(target=print_square, args=(10, ))
    p2 = multiprocessing.Process(target=print_cube, args=(10, ))

    # starting process 1
    p1.start()
    # starting process 2
    p2.start()

    # wait until process 1 is finished
    p1.join()
    # wait until process 2 is finished
    p2.join()

    # both processes finished
    print("Done!")
```

In [ ]:

Output:  
Square: 100  
Cube: 1000  
Done!

Once the processes start, the current program also keeps on executing. In order to stop execution of current program until a process is complete, we use join method.

As a result, the current program will first wait for the completion of p1 and then p2. Once, they are completed, the next statements of current program are executed.

In [ ]:

```
import multiprocessing
import os

def worker1():
    # printing process id
    print("ID of process running worker1: {}".format(os.getpid()))

def worker2():
    # printing process id
    print("ID of process running worker2: {}".format(os.getpid()))

if __name__ == "__main__":
    # printing main program process id
    print("ID of main process: {}".format(os.getpid()))
    # creating processes
    p1 = multiprocessing.Process(target=worker1)
    p2 = multiprocessing.Process(target=worker2)
    # starting processes
    p1.start()
    p2.start()
    # process IDs
    print("ID of process p1: {}".format(p1.pid))
    print("ID of process p2: {}".format(p2.pid))
    # wait until processes are finished
    p1.join()
    p2.join()
    # both processes finished
    print("Both processes finished execution!")
    # check if processes are alive
    print("Process p1 is alive: {}".format(p1.is_alive()))
    print("Process p2 is alive: {}".format(p2.is_alive()))
```

In [ ]:

```
Output:
ID of main process: 28628
ID of process running worker1: 29305
ID of process running worker2: 29306
ID of process p1: 29305
ID of process p2: 29306
Both processes finished execution!
Process p1 is alive: False
Process p2 is alive: False
```

## Shared memory

In [ ]:

Shared memory : multiprocessing module provides Array and Value objects to share data between processes.

Array: a ctypes array allocated from shared memory.

Value: a ctypes object allocated from shared memory.

In [ ]:

```
import multiprocessing

def square_list(mylist, result, square_sum):
    # append squares of mylist to result array
    for idx, num in enumerate(mylist):
        result[idx] = num * num
    # square_sum value
    square_sum.value = sum(result)
    # print result Array
    print("Result(in process p1): {}".format(result[:]))
    # print square_sum Value
    print("Sum of squares(in process p1): {}".format(square_sum.value))

if __name__ == "__main__":
    # input list
    mylist = [1,2,3,4]
    # creating Array of int data type with space for 4 integers
    result = multiprocessing.Array('i', 4)
    # creating Value of int data type
    square_sum = multiprocessing.Value('i')
    # creating new process
    p1 = multiprocessing.Process(target=square_list, args=(mylist, result, square_sum))
    # starting process
    p1.start()
    # wait until process is finished
    p1.join()
    # print result array
    print("Result(in main program): {}".format(result[:]))
    # print square_sum Value
    print("Sum of squares(in main program): {}".format(square_sum.value))
```

In [ ]:

Output:

Result(in process p1): [1, 4, 9, 16]

Sum of squares(in process p1): 30

Result(in main program): [1, 4, 9, 16]

Sum of squares(in main program): 30

## Server process

In [ ]:

Server process : Whenever a python program starts, a server process **is** also started. From there on, whenever a new process **is** needed, the parent process connects to the server **and** requests it to fork a new process.

A server process can hold Python objects **and** allows other processes to manipulate them using proxies.

multiprocessing module provides a Manager **class which** controls a server process. Hence, managers provide a way to create data which can be shared between different processes.

Server process managers are more flexible than using shared memory objects because they can be made to support arbitrary **object** types like lists, dictionaries, Queue, Value, Array, etc. Also, a single manager can be shared by processes on different computers over a network. They are, however, slower than using shared memory.

In [ ]:

```
import multiprocessing
def print_records(records):
    """
    function to print record(tuples) in records(List)
    """
    for record in records:
        print("Name: {0}\nScore: {1}\n".format(record[0], record[1]))

def insert_record(record, records):
    """
    function to add a new record to records(List)
    """
    records.append(record)
    print("New record added!\n")

if __name__ == '__main__':
    with multiprocessing.Manager() as manager:
        # creating a list in server process memory
        records = manager.list([('Sam', 10), ('Adam', 9), ('Kevin', 9)])
        # new record to be inserted in records
        new_record = ('Jeff', 8)
        # creating new processes
        p1 = multiprocessing.Process(target=insert_record, args=(new_record, records))
        p2 = multiprocessing.Process(target=print_records, args=(records,))
        # running process p1 to insert new record
        p1.start()
        p1.join()
        # running process p2 to print records
        p2.start()
        p2.join()
```

In [ ]:

```
Output:  
New record added!  
Name: Sam  
Score: 10  
Name: Adam  
Score: 9  
Name: Kevin  
Score: 9  
Name: Jeff  
Score: 8
```

## Communication between processes

In [ ]:

Effective use of multiple processes usually requires some communication between them, so that work can be divided **and** results can be aggregated. multiprocessing supports two types of communication channel between processes:

- Queue
- Pipe

### Queue

In [ ]:

Queue : A simple way to communicate between process **with** multiprocessing **is** to use a Queue to **pass** messages back **and** forth. Any Python **object** can **pass** through a Queue.

In [ ]:

```

import multiprocessing

def square_list(mylist, q):
    """
    function to square a given list
    """
    # append squares of mylist to queue
    for num in mylist:
        q.put(num * num)

def print_queue(q):
    """
    function to print queue elements
    """
    print("Queue elements:")
    while not q.empty():
        print(q.get())
    print("Queue is now empty!")

if __name__ == "__main__":
    # input list
    mylist = [1,2,3,4]
    # creating multiprocessing Queue
    q = multiprocessing.Queue()
    # creating new processes
    p1 = multiprocessing.Process(target=square_list, args=(mylist, q))
    p2 = multiprocessing.Process(target=print_queue, args=(q,))
    # running process p1 to square list
    p1.start()
    p1.join()
    # running process p2 to get queue elements
    p2.start()
    p2.join()

```

In [ ]:

```

Output:
Queue elements:
1
4
9
16
Queue is now empty!

```

## Pipe

In [ ]:

Pipes : A pipe can have only two endpoints. Hence, it **is** preferred over queue when only two-way communication **is** required. multiprocessing module provides Pipe() function which returns a pair of connection objects connected by a pipe. The two connection objects returned by Pipe() represent the two ends of the pipe. Each connection **object** has send() **and** recv() methods (among others).

In [ ]:

```
import multiprocessing
def sender(conn, msgs):
    """
    function to send messages to other end of pipe
    """
    for msg in msgs:
        conn.send(msg)
        print("Sent the message: {}".format(msg))
    conn.close()

def receiver(conn):
    """
    function to print the messages received from other
    end of pipe
    """
    while 1:
        msg = conn.recv()
        if msg == "END":
            break
        print("Received the message: {}".format(msg))

if __name__ == "__main__":
    # messages to be sent
    msgs = ["hello", "hey", "hru?", "END"]
    # creating a pipe
    parent_conn, child_conn = multiprocessing.Pipe()
    # creating new processes
    p1 = multiprocessing.Process(target=sender, args=(parent_conn, msgs))
    p2 = multiprocessing.Process(target=receiver, args=(child_conn,))
    # running processes
    p1.start()
    p2.start()
    # wait until processes finish
    p1.join()
    p2.join()
```

In [ ]:

```
Output:
Sent the message: hello
Sent the message: hey
Sent the message: hru?
Received the message: hello
Sent the message: END
Received the message: hey
Received the message: hru?
```

## Synchronization and Pooling of processes in Python

In [ ]:

Process synchronization **is** defined **as** a mechanism which ensures that two **or** more concurrent processes do **not** simultaneously execute some particular program segment known **as** critical section. Critical section refers to the parts of the program where the shared resource **is** accessed.

A race condition occurs when two **or** more processes can access shared data **and** they **try** to change it at the same time. As a result, the values of variables may be unpredictable **and** vary depending on the timings of context switches of the processes.

## Race Condition

In [ ]:

```
# Python program to illustrate
# the concept of race condition
# in multiprocessing
import multiprocessing
# function to withdraw from account
def withdraw(balance):
    for _ in range(10000):
        balance.value = balance.value - 1
# function to deposit to account
def deposit(balance):
    for _ in range(10000):
        balance.value = balance.value + 1

def perform_transactions():
    # initial balance (in shared memory)
    balance = multiprocessing.Value('i', 100)
    # creating new processes
    p1 = multiprocessing.Process(target=withdraw, args=(balance,))
    p2 = multiprocessing.Process(target=deposit, args=(balance,))
    # starting processes
    p1.start()
    p2.start()
    # wait until processes are finished
    p1.join()
    p2.join()
    # print final balance
    print("Final balance = {}".format(balance.value))

if __name__ == "__main__":
    for _ in range(10):
        # perform same transaction process 10 times
        perform_transactions()
```



In [ ]:

```
Output:
Final balance = 1311
Final balance = 199
Final balance = 558
Final balance = -2265
Final balance = 1371
Final balance = 1158
Final balance = -577
Final balance = -1300
Final balance = -341
Final balance = 157
```

In [ ]:

In above program, 10000 withdraw **and** 10000 deposit transactions are carried out **with** initial balance **as** 100. The expected final balance **is** 100 but what we get **in** 10 iterations of perform\_transactions function **is** some different values.

This happens due to concurrent access of processes to the shared data balance. This unpredictability **in** balance value **is** nothing but race condition.

## Using Locks

In [ ]:

multiprocessing module provides a Lock **class** to deal **with** the race conditions. Lock **is** implemented using a Semaphore **object** provided by the Operating System.

A semaphore **is** a synchronization **object** that controls access by multiple processes to a common resource **in** a parallel programming environment.

It **is** simply a value **in** a designated place **in** operating system (**or** kernel) storage that each process can check **and** then change.

Depending on the value that **is** found, the process can use the resource **or** will find that it **is** already **in** use **and** must wait **for** some period before trying again.

Semaphores can be binary (0 **or** 1) **or** can have additional values. Typically, a process using semaphores checks the value **and** then, **if** it using the resource,

changes the value to reflect this so that subsequent semaphore users will know to wait.

In [ ]:

```
import multiprocessing
# function to withdraw from account
def withdraw(balance, lock):
    for _ in range(10000):
        lock.acquire()
        balance.value = balance.value - 1
        lock.release()
# function to deposit to account
def deposit(balance, lock):
    for _ in range(10000):
        lock.acquire()
        balance.value = balance.value + 1
        lock.release()
def perform_transactions():
    # initial balance (in shared memory)
    balance = multiprocessing.Value('i', 100)
    # creating a lock object
    lock = multiprocessing.Lock()
    # creating new processes
    p1 = multiprocessing.Process(target=withdraw, args=(balance,lock))
    p2 = multiprocessing.Process(target=deposit, args=(balance,lock))
    # starting processes
    p1.start()
    p2.start()
    # wait until processes are finished
    p1.join()
    p2.join()
    # print final balance
    print("Final balance = {}".format(balance.value))

if __name__ == "__main__":
    for _ in range(10):
        # perform same transaction process 10 times
        perform_transactions()
```

In [ ]:

Output:

```
Final balance = 100
Final balance = 100
Final balance = 100
Final balance = 100
Final balance = 100
Final balance = 100
Final balance = 100
Final balance = 100
Final balance = 100
Final balance = 100
```

## Pooling between processes

In [ ]:

```

Python program to find
# squares of numbers in a given list
def square(n):
    return (n*n)
if __name__ == "__main__":
    # input list
    mylist = [1,2,3,4,5]
    # empty list to store result
    result = []
    for num in mylist:
        result.append(square(num))
    print(result)

```

Only one of the cores is used for program execution and it's quite possible that other cores remain idle.

In order to utilize all the cores, multiprocessing module provides a Pool class. The Pool class represents a pool of worker processes.

It has methods which allows tasks to be offloaded to the worker processes in a few different ways.

Here, the task is offloaded/distributed among the cores/processes automatically by Pool object. User doesn't need to worry about creating processes explicitly.

In [ ]:

```

import multiprocessing
import os

def square(n):
    print("Worker process id for {0}: {1}".format(n, os.getpid()))
    return (n*n)
if __name__ == "__main__":
    # input list
    mylist = [1,2,3,4,5]
    # creating a pool object
    p = multiprocessing.Pool()
    # map list to target function
    result = p.map(square, mylist)
    print(result)

```

In [ ]:

Output:

```

Worker process id for 2: 4152
Worker process id for 1: 4151
Worker process id for 4: 4151
Worker process id for 3: 4153
Worker process id for 5: 4152
[1, 4, 9, 16, 25]

```

## MultiThreading

In [ ]:

Just like multiprocessing, multithreading **is** a way of achieving multitasking. In multithreading, the concept of threads **is** used.  
A thread **is** an entity within a process that can be scheduled **for** execution. Also, it **is** the smallest unit of processing that can be performed **in** an OS (Operating System).

In [ ]:

A thread contains **all** this information **in** a Thread Control Block (TCB):  
Thread Identifier: Unique **id** (TID) **is** assigned to every new thread  
Stack pointer: Points to thread's stack **in** the process. Stack contains the local variables under thread's scope.  
Program counter: a register which stores the address of the instruction currently being executed by thread.  
Thread state: can be running, ready, waiting, start **or** done.  
Thread's register **set**: registers assigned to thread **for** computations.  
Parent process Pointer: A pointer to the Process control block (PCB) of the process that the thread lives on.

In [ ]:

Multiple threads can exist within one process where:

Each thread contains its own register **set** **and** local variables (stored **in** stack).  
All threads of a process share **global** variables (stored **in** heap) **and** the program code.

**Multithreading is defined as the ability of a processor to execute multiple threads concurrently.**

In [ ]:

```

in a simple, single-core CPU, it is achieved using frequent switching between threads.
This is termed as context switching. In context switching,
the state of a thread is saved and state of another thread is loaded whenever any inter
rupt (due to I/O or manually set) takes place.
Context switching takes place so frequently that all the threads appear to be running p
arallely (this is termed as multitasking).
# Python program to illustrate the concept
# of threading
# importing the threading module
import threading
def print_cube(num):
    """
    function to print cube of given num
    """
    print("Cube: {}".format(num * num * num))

def print_square(num):
    """
    function to print square of given num
    """
    print("Square: {}".format(num * num))

if __name__ == "__main__":
    # creating thread
    t1 = threading.Thread(target=print_square, args=(10,))
    t2 = threading.Thread(target=print_cube, args=(10,))
    # starting thread 1
    t1.start()
    # starting thread 2
    t2.start()
    # wait until thread 1 is completely executed
    t1.join()
    # wait until thread 2 is completely executed
    t2.join()
    # both threads completely executed
    print("Done!")

```

In [ ]:

```
# Python program to illustrate the concept
# of threading
import threading
import os

def task1():
    print("Task 1 assigned to thread: {}".format(threading.current_thread().name))
    print("ID of process running task 1: {}".format(os.getpid()))

def task2():
    print("Task 2 assigned to thread: {}".format(threading.current_thread().name))
    print("ID of process running task 2: {}".format(os.getpid()))

if __name__ == "__main__":
    # print ID of current process
    print("ID of process running main program: {}".format(os.getpid()))
    # print name of main thread
    print("Main thread name: {}".format(threading.main_thread().name))
    # creating threads
    t1 = threading.Thread(target=task1, name='t1')
    t2 = threading.Thread(target=task2, name='t2')
    # starting threads
    t1.start()
    t2.start()
    # wait until all threads finish
    t1.join()
    t2.join()
```

In [ ]:

Output:  
ID of process running main program: 11758  
Main thread name: MainThread  
Task 1 assigned to thread: t1  
ID of process running task 1: 11758  
Task 2 assigned to thread: t2  
ID of process running task 2: 11758

## Using Locks

In [ ]:

```
import threading

# global variable x
x = 0

def increment():
    """
    function to increment global variable x
    """
    global x
    x += 1

def thread_task(lock):
    """
    task for thread
    calls increment function 100000 times.
    """
    for _ in range(100000):
        lock.acquire()
        increment()
        lock.release()

def main_task():
    global x
    # setting global variable x as 0
    x = 0
    # creating a lock
    lock = threading.Lock()
    # creating threads
    t1 = threading.Thread(target=thread_task, args=(lock,))
    t2 = threading.Thread(target=thread_task, args=(lock,))
    # start threads
    t1.start()
    t2.start()
    # wait until threads finish their job
    t1.join()
    t2.join()

if __name__ == "__main__":
    for i in range(10):
        main_task()
        print("Iteration {0}: x = {1}".format(i,x))
```

In [ ]:

```
Output:
Iteration 0: x = 200000
Iteration 1: x = 200000
Iteration 2: x = 200000
Iteration 3: x = 200000
Iteration 4: x = 200000
Iteration 5: x = 200000
Iteration 6: x = 200000
Iteration 7: x = 200000
Iteration 8: x = 200000
Iteration 9: x = 200000
```

# Data Structure

## Stack

In [ ]:

Implementation 1:

Stack works on the principle of "Last-in, first-out". Also, the inbuilt functions in Python make the code short and simple.

To add an item to the top of the list, i.e., to push an item, we use append() function and to pop out an element we use pop() function.

These functions work quite efficiently and fast in end operations.

*# Python code to demonstrate Implementing*

*# stack using list*

```
stack = ["Amar", "Akbar", "Anthony"]
```

```
stack.append("Ram")
```

```
stack.append("Iqbal")
```

```
print(stack)
```

```
print(stack.pop())
```

```
print(stack)
```

```
print(stack.pop())
```

```
print(stack)
```



In [ ]:

Implementation 2:

```

class Stack:
    def __init__(self):
        self.items = []

    def isEmpty(self):
        return self.items == []

    def push(self, item):
        self.items.append(item)

    def pop(self):
        return self.items.pop()

    def peek(self):
        return self.items[len(self.items)-1]

    def size(self):
        return len(self.items)

s=Stack()

print(s.isEmpty())
s.push(4)
s.push('dog')
print(s.peek())
s.push(True)
print(s.size())
print(s.isEmpty())
s.push(8.4)
print(s.pop())
print(s.pop())
print(s.size())

```

## Queue

In [ ]:

Implementing queue **is** a bit different. Queue works on the principle of “First-in, first-out”. Due to the properties of **list**, which **is** fast at the end operations but slow at the beginning operations, **as all** other elements have to be shifted one by one. So, we prefer the use of **collections.deque** over **list**, which was specially designed to have fast appends **and** pops **from both** the front **and** back end.

In [ ]:

Implementation 1:

```
# Python code to demonstrate Implementing
# Queue using deque and List
from collections import deque
queue = deque(["Ram", "Tarun", "Asif", "John"])
print(queue)
queue.append("Akbar")
print(queue)
queue.append("Birbal")
print(queue)
print(queue.popleft())
print(queue.popleft())
print(queue)
```

In [ ]:

Implementation 2:

```
class Queue:
    def __init__(self):
        self.items = []

    def isEmpty(self):
        return self.items == []

    def enqueue(self, item):
        self.items.insert(0,item)

    def dequeue(self):
        return self.items.pop()

    def size(self):
        return len(self.items)
```

## Linkedlist

In [ ]:

Simple Creation of Node and linkedlist:

```
# Node class
class Node:
    # Function to initialize the node object
    def __init__(self, data):
        self.data = data # Assign data
        self.next = None # Initialize
                        # next as null

# Linked List class
class LinkedList:
    # Function to initialize the Linked
    # List object
    def __init__(self):
        self.head = None
```

In [ ]:

```
# A simple Python program to introduce a Linked List

# Node class
class Node:
    # Function to initialise the node object
    def __init__(self, data):
        self.data = data # Assign data
        self.next = None # Initialize next as null

# Linked List class contains a Node object
class LinkedList:
    # Function to initialize head
    def __init__(self):
        self.head = None

# Code execution starts here
if __name__ == '__main__':
    # Start with the empty list
    llist = LinkedList()
    llist.head = Node(1)
    second = Node(2)
    third = Node(3)

    '''
    Three nodes have been created.
    We have references to these three blocks as first,
    second and third

    llist.head      second      third
      |              |           |
      |              |           |
    +---+---+---+   +---+---+---+   +---+---+---+
    | 1 | None |   | 2 | None |   | 3 | None |
    +---+---+---+   +---+---+---+   +---+---+---+
    '''

    llist.head.next = second; # Link first node with second

    '''
    Now next of first Node refers to second. So they
    both are linked.

    llist.head      second      third
      |              |           |
      |              |           |
    +---+---+---+   +---+---+---+   +---+---+---+
    | 1 | o----->| 2 | null |   | 3 | null |
    +---+---+---+   +---+---+---+   +---+---+---+
    '''

    second.next = third; # Link second node with the third node

    '''
    Now next of second Node refers to third. So all three
    nodes are linked.

    llist.head      second      third
      |              |           |
      |              |           |
    +---+---+---+   +---+---+---+   +---+---+---+
    | 1 | |         | 2 | |         | 3 | |
    +---+---+---+   +---+---+---+   +---+---+---+
    '''
```

```

+-----+-----+      +-----+-----+      +-----+-----+
| 1 | o----->| 2 | o----->| 3 | null |
+-----+-----+      +-----+-----+      +-----+-----+
'''

```

## Transverse

In [ ]:

```

# A simple Python program for traversal of a Linked List

# Node class
class Node:

    # Function to initialise the node object
    def __init__(self, data):
        self.data = data # Assign data
        self.next = None # Initialize next as null

# Linked List class contains a Node object
class LinkedList:

    # Function to initialize head
    def __init__(self):
        self.head = None

    # This function prints contents of linked list
    # starting from head
    def printList(self):
        temp = self.head
        while (temp):
            print temp.data,
            temp = temp.next

# Code execution starts here
if __name__ == '__main__':
    # Start with the empty list
    llist = LinkedList()
    llist.head = Node(1)
    second = Node(2)
    third = Node(3)
    llist.head.next = second; # Link first node with second
    second.next = third; # Link second node with the third node
    llist.printList()

```

# Algorithms

## Linear Search

In [ ]:

A simple approach **is** to do linear search, i.e  
 Start **from the** leftmost element of arr[] **and** one by one compare x **with** each element of arr[]  
 If x matches **with** an element, **return** the index.  
 If x doesn't match **with any** of elements, **return** -1.  
*# Python3 code to linearly search x in arr[].*  
*# If x is present then return its location,*  
*# otherwise return -1*  
 Implementation 1:  

```
def search(arr, n, x):
    for i in range (0, n):
        if (arr[i] == x):
            return i;
    return -1;
```

*# Driver Code*  

```
arr = [ 2, 3, 4, 10, 40 ];
x = 10;
n = len(arr);
result = search(arr, n, x)
if(result == -1):
    print("Element is not present in array")
else:
    print("Element is present at index", result)
```

In [ ]:

```
Implementation 2:
list_ = list(map(int,input().split()))
variable = int(input())
index = [x for x,y in enumerate(list_) if y == variable]
print(index[0])
```

**The time complexity of above algorithm is  $O(n)$ .**

**Linear search is rarely used practically because other search algorithms such as the binary search algorithm and hash tables allow significantly faster**

**searching comparison to Linear search.**

## Binary Search

In [ ]:

Binary Search: Search a **sorted** array by repeatedly dividing the search interval **in** half . Begin **with** an interval covering the whole array.  
 If the value of the search key **is** less than the item **in** the middle of the interval, narrow the interval to the lower half.  
 Otherwise narrow it to the upper half. Repeatedly check until the value **is** found **or** the interval **is** empty.

In [24]:

```
def binarySearch(alist, item):
    first = 0
    last = len(alist)-1

    while first<=last:
        midpoint = (first + last)//2
        if alist[midpoint] == item:
            return midpoint+1
        else:
            if item < alist[midpoint]:
                last = midpoint-1
            else:
                first = midpoint+1
    return False

testlist = [0, 1, 2, 8, 13, 17, 19, 32, 42,]
print(binarySearch(testlist, 42))
print(binarySearch(testlist, 13))
```

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the binary search is  $O(\log n)$ .

## Sorting

### Bubble Sort

In [ ]:

Bubble Sort

Bubble Sort **is** the simplest sorting algorithm that works by repeatedly swapping the adjacent elements **if** they are **in** wrong order.

Example:

First Pass:

( 5 1 4 2 8 )  $\rightarrow$  ( 1 5 4 2 8 ), Here, algorithm compares the first two elements, **and** swaps since  $5 > 1$ .  
 ( 1 5 4 2 8 )  $\rightarrow$  ( 1 4 5 2 8 ), Swap since  $5 > 4$   
 ( 1 4 5 2 8 )  $\rightarrow$  ( 1 4 2 5 8 ), Swap since  $5 > 2$   
 ( 1 4 2 5 8 )  $\rightarrow$  ( 1 4 2 5 8 ), Now, since these elements are already **in** order ( $8 > 5$ ), algorithm does **not** swap them.

Second Pass:

( 1 4 2 5 8 )  $\rightarrow$  ( 1 4 2 5 8 )  
 ( 1 4 2 5 8 )  $\rightarrow$  ( 1 2 4 5 8 ), Swap since  $4 > 2$   
 ( 1 2 4 5 8 )  $\rightarrow$  ( 1 2 4 5 8 )  
 ( 1 2 4 5 8 )  $\rightarrow$  ( 1 2 4 5 8 )

Now, the array **is** already **sorted**, but our algorithm does **not** know **if** it **is** completed. The algorithm needs one whole **pass** without **any** swap to know it **is sorted**.

Third Pass:

( 1 2 4 5 8 )  $\rightarrow$  ( 1 2 4 5 8 )  
 ( 1 2 4 5 8 )  $\rightarrow$  ( 1 2 4 5 8 )  
 ( 1 2 4 5 8 )  $\rightarrow$  ( 1 2 4 5 8 )  
 ( 1 2 4 5 8 )  $\rightarrow$  ( 1 2 4 5 8 )

In [29]:

```
def bubbleSort(alist):
    for passnum in range(len(alist)-1,0,-1):
        for i in range(passnum):
            if alist[i]>alist[i+1]:
                temp = alist[i]
                alist[i] = alist[i+1]
                alist[i+1] = temp

alist = [54,26,93,17,77,31,44,55,20]
bubbleSort(alist)
print(alist)
```

```
[17, 20, 26, 31, 44, 54, 55, 77, 93]
```

**Worst and Average Case Time Complexity:  $O(n*n)$ . Worst case occurs when array is reverse sorted.**

**Best Case Time Complexity:  $O(n)$ . Best case occurs when array is already sorted.**

**Auxiliary Space:  $O(1)$**

**Boundary Cases: Bubble sort takes minimum time (Order of  $n$ ) when elements are already sorted.**

**Sorting In Place: Yes**

**Stable: Yes**

## Selection Sort

In [ ]:

The selection sort improves on the bubble sort by making only one exchange **for** every **pass** through the **list**. In order to do this, a selection sort looks **for** the largest value **as** it makes a **pass** **and**, after completing the **pass**, places it **in** the proper location.

In [ ]:

```
import sys
A = [64, 25, 12, 22, 11]
# Traverse through all array elements
for i in range(len(A)):
    # Find the minimum element in remaining
    # unsorted array
    min_idx = i
    for j in range(i+1, len(A)):
        if A[min_idx] > A[j]:
            min_idx = j
    # Swap the found minimum element with
    # the first element
    A[i], A[min_idx] = A[min_idx], A[i]
# Driver code to test above
print ("Sorted array")
for i in range(len(A)):
    print ("%d" %A[i]),
```

**Time Complexity:  $O(n^2)$  as there are two nested loops.**

In [ ]: