

# Lab #6: Introduction to Linear Regression

Name

Date of lab session

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## Lab report

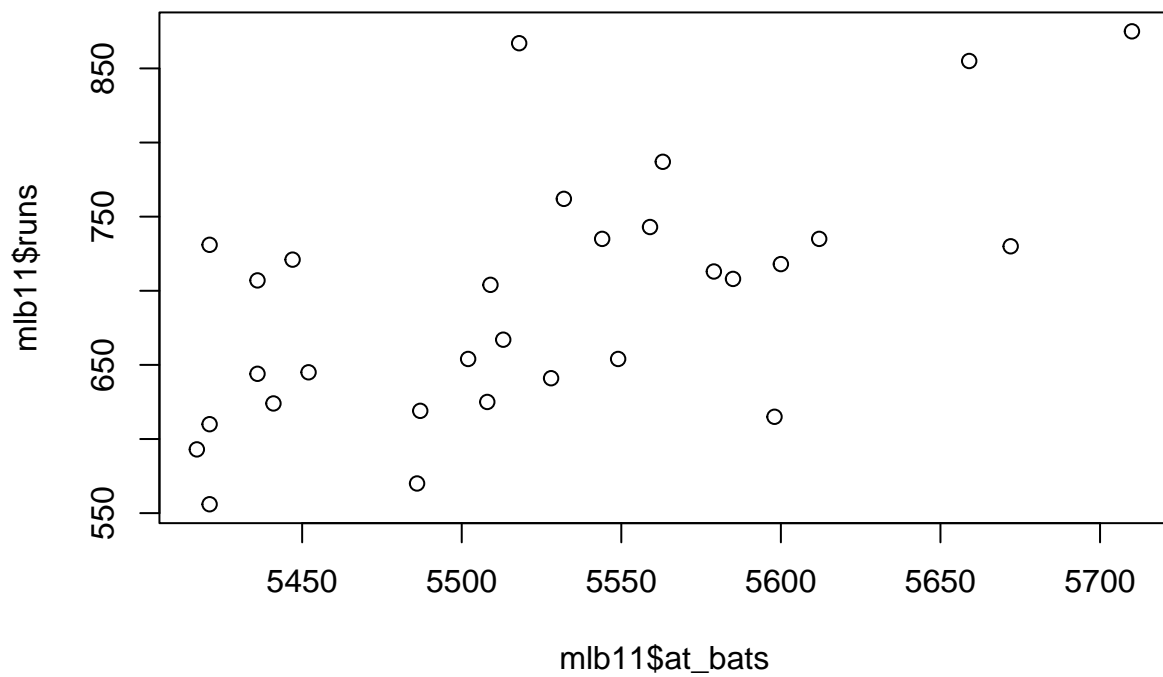
```
download.file("http://www.openintro.org/stat/data/mlb11.RData", destfile = "mlb11.RData")
load("mlb11.RData")
```

**Load data:**

## Exercises:

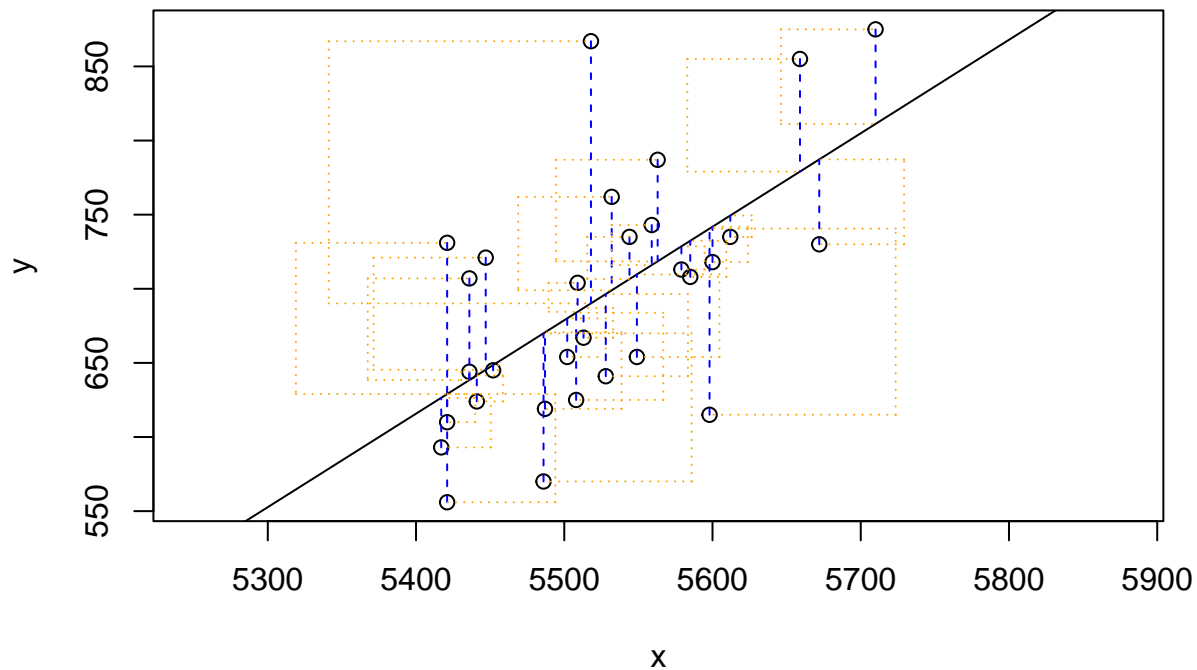
**Exercise 1:** I would use a linear regression plot. The relationship between at\_bats and runs seems linear. Although the model seems to be linear, the association does not seem to be strong, so the prediction might not be too accurate.

```
plot(mlb11$at_bats,mlb11$runs)
```



**Exercise 2:** The two variables seem to have a positive weak linear association. There are also a few outliers around 5600 at bats and 5520 at bats.

```
plot_ss(x = mlb11$at_bats, y = mlb11$runs, showSquares = TRUE)
```



```
## Click two points to make a line.
## Call:
## lm(formula = y ~ x, data = pts)
##
## Coefficients:
## (Intercept)          x
## -2789.2429      0.6305
##
## Sum of Squares:  123721.9
```

**Exercise 3:** The smallest sum of squares I got was 132859.5, some of them with an opposite slope had sums 100s of times larger

**Exercise 4:**  $y = 415.2389 + 1.8345 \cdot \text{homeruns}$  For every homerun, there are 1.8345 runs.

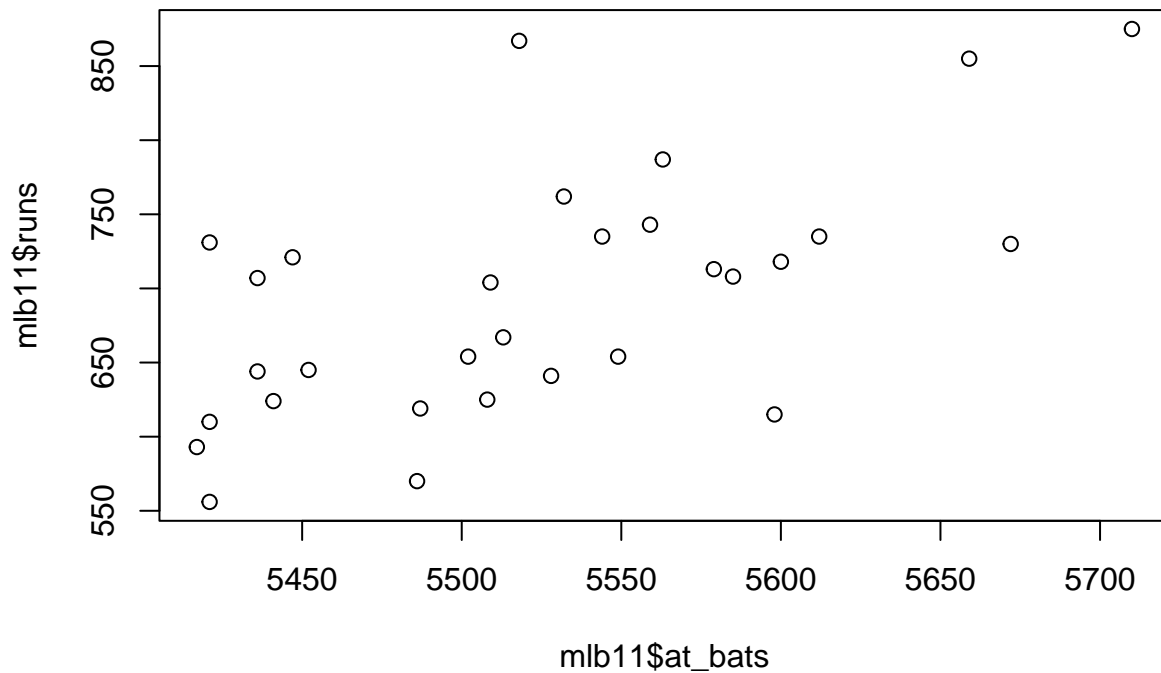
```
m1 <- lm(runs ~ homeruns, data = mlb11)
summary(m1)
```

```
##
## Call:
## lm(formula = runs ~ homeruns, data = mlb11)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
```

```
## -91.615 -33.410 3.231 24.292 104.631
##
## Coefficients:
##             Estimate Std. Error t value Pr(>|t|)
## (Intercept) 415.2389    41.6779   9.963 1.04e-10 ***
## homeruns     1.8345     0.2677   6.854 1.90e-07 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 51.29 on 28 degrees of freedom
## Multiple R-squared:  0.6266, Adjusted R-squared:  0.6132
## F-statistic: 46.98 on 1 and 28 DF, p-value: 1.9e-07
```

**Exercise 5:** Predicted runs for 5579 at bats is 728.3166 runs. This is a overestimate as the data point is at 713, so an overestimate by 15.3166. Which means the residual is also 15.3166.

```
plot(mlb11$runs ~ mlb11$at_bats)
abline(m1)
```



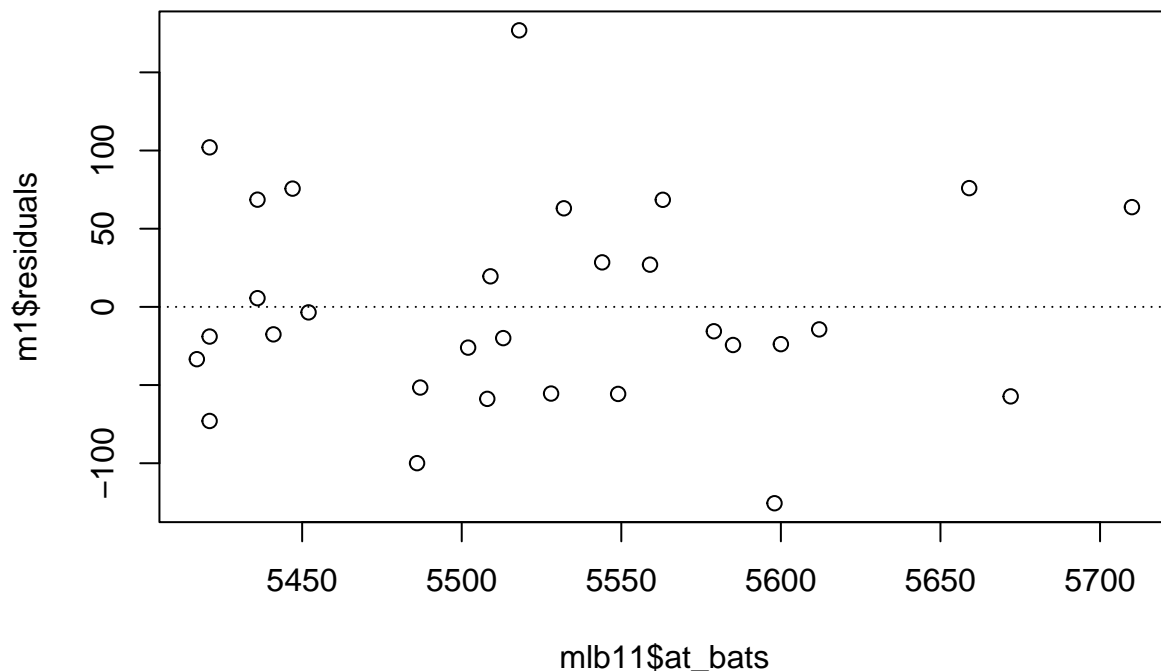
```
m1 <- lm(runs ~ at_bats, data = mlb11)
summary(m1)
```

```
##
## Call:
```

```
## lm(formula = runs ~ at_bats, data = mlb11)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -125.58  -47.05  -16.59   54.40  176.87
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept) -2789.2429   853.6957  -3.267 0.002871 **
## at_bats       0.6305     0.1545   4.080 0.000339 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 66.47 on 28 degrees of freedom
## Multiple R-squared:  0.3729, Adjusted R-squared:  0.3505
## F-statistic: 16.65 on 1 and 28 DF,  p-value: 0.0003388
```

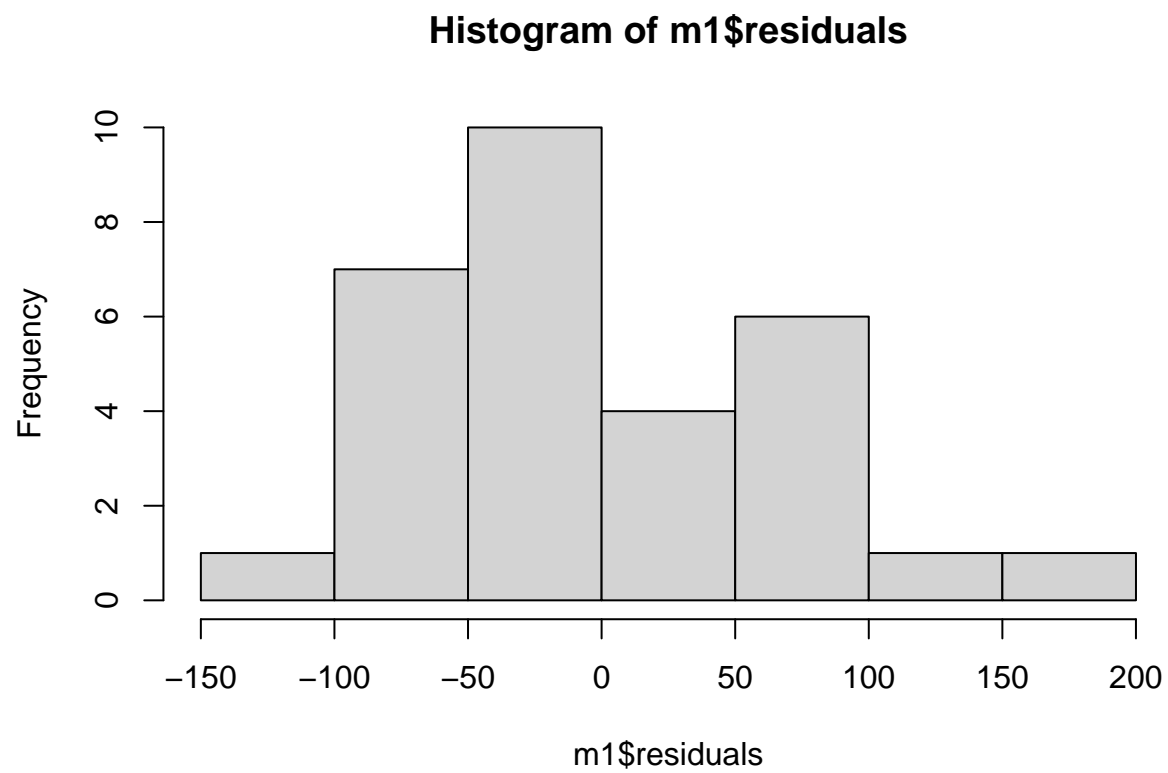
**Exercise 6:** Since there seems to be no apparent pattern, we can say that there is linearity.

```
plot(m1$residuals ~ mlb11$at_bats)
abline(h = 0, lty = 3) # adds a horizontal dashed line at y = 0
```

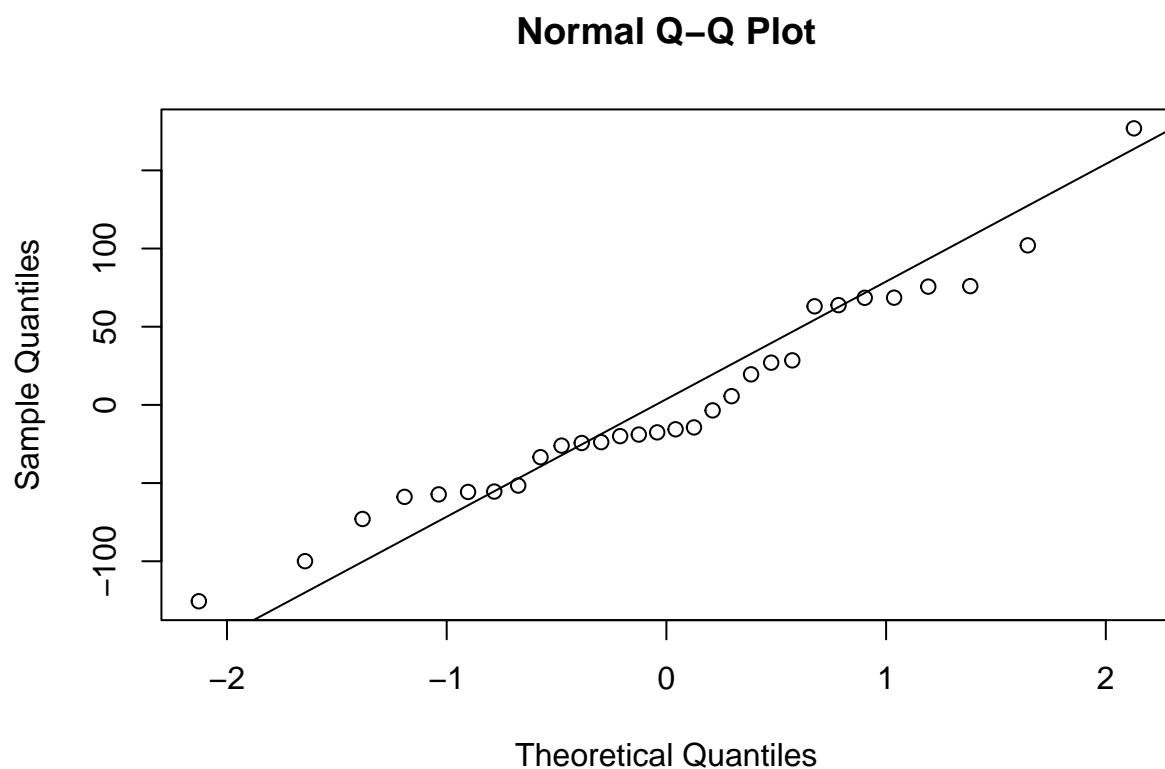


**Exercise 7:** Based on these two plots, it does not seem to be following a normal distribution.

```
hist(m1$residuals)
```



```
qqnorm(m1$residuals)  
qqline(m1$residuals)
```



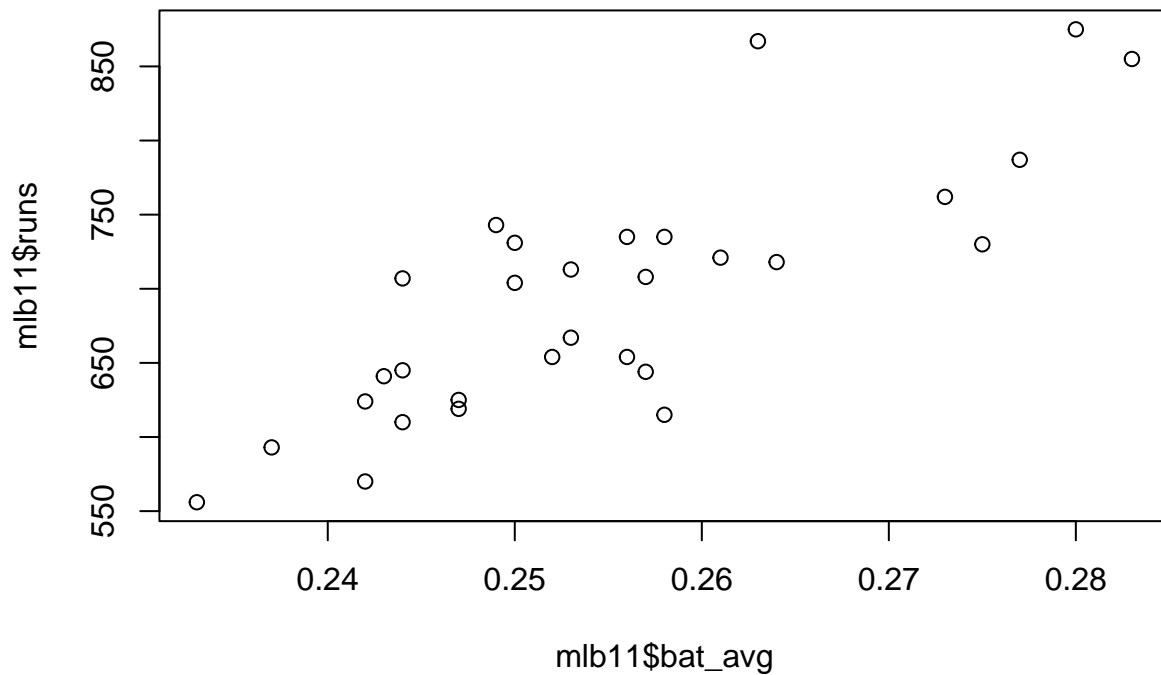
**Exercise 8:** Since there is no apparent pattern in the residual plot, we can see the variability condition is met.

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**On your own:**

1: There seems to be a linear association.

```
plot(mlb11$runs ~ mlb11$bat_avg)
```



2: Based on the two R Squareds it seems that batting average is a better fit for the data than at bats as there is a higher R Squared value.

```
m1 <- lm(runs ~ at_bats, data = mlb11)
summary(m1)
```

```
##
## Call:
## lm(formula = runs ~ at_bats, data = mlb11)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -125.58  -47.05  -16.59   54.40  176.87
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept) -2789.2429   853.6957  -3.267 0.002871 **
## at_bats       0.6305     0.1545   4.080 0.000339 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 66.47 on 28 degrees of freedom
## Multiple R-squared:  0.3729, Adjusted R-squared:  0.3505
## F-statistic: 16.65 on 1 and 28 DF, p-value: 0.0003388
```



```
m2 <- lm(runs ~ bat_avg, data = mlb11)
summary(m2)
```

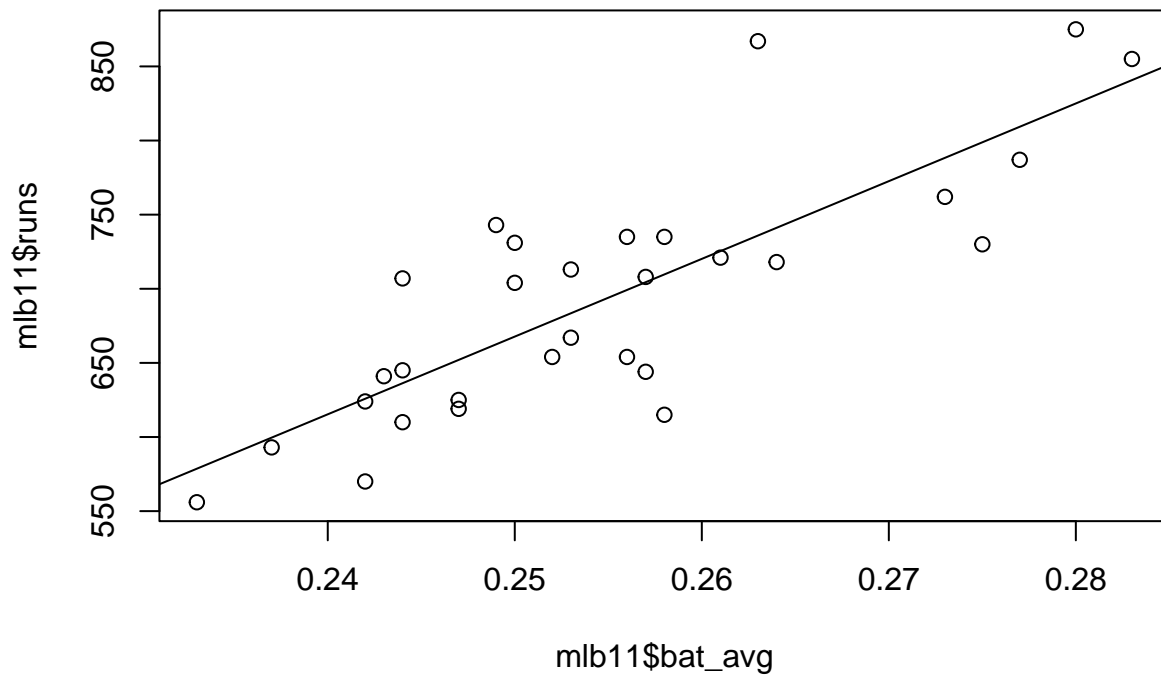
```
##
## Call:
## lm(formula = runs ~ bat_avg, data = mlb11)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -94.676 -26.303  -5.496  28.482 131.113
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)   -642.8      183.1   -3.511  0.00153 **
## bat_avg       5242.2      717.3    7.308  5.88e-08 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 49.23 on 28 degrees of freedom
## Multiple R-squared:  0.6561, Adjusted R-squared:  0.6438
## F-statistic: 53.41 on 1 and 28 DF,  p-value: 5.877e-08
```

3: Batting average seems to be the best predictor for runs as it has the highest R squared at 0.64.

```
m2 <- lm(runs ~ bat_avg, data = mlb11)
summary(m2)
```

```
##
## Call:
## lm(formula = runs ~ bat_avg, data = mlb11)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -94.676 -26.303  -5.496  28.482 131.113
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)   -642.8      183.1   -3.511  0.00153 **
## bat_avg       5242.2      717.3    7.308  5.88e-08 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 49.23 on 28 degrees of freedom
## Multiple R-squared:  0.6561, Adjusted R-squared:  0.6438
## F-statistic: 53.41 on 1 and 28 DF,  p-value: 5.877e-08
```

```
plot(mlb11$runs ~ mlb11$bat_avg)
abline(m2)
```



4: It seems that on base plus slugging is the best as R squared is 0.93.

```
m2 <- lm(runs ~ new_onbase, data = mlb11)
summary(m2)
```

```
##
## Call:
## lm(formula = runs ~ new_onbase, data = mlb11)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -58.270 -18.335   3.249  19.520  69.002
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)  -1118.4      144.5   -7.741 1.97e-08 ***
## new_onbase     5654.3      450.5  12.552 5.12e-13 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 32.61 on 28 degrees of freedom
## Multiple R-squared:  0.8491, Adjusted R-squared:  0.8437
## F-statistic: 157.6 on 1 and 28 DF, p-value: 5.116e-13
```

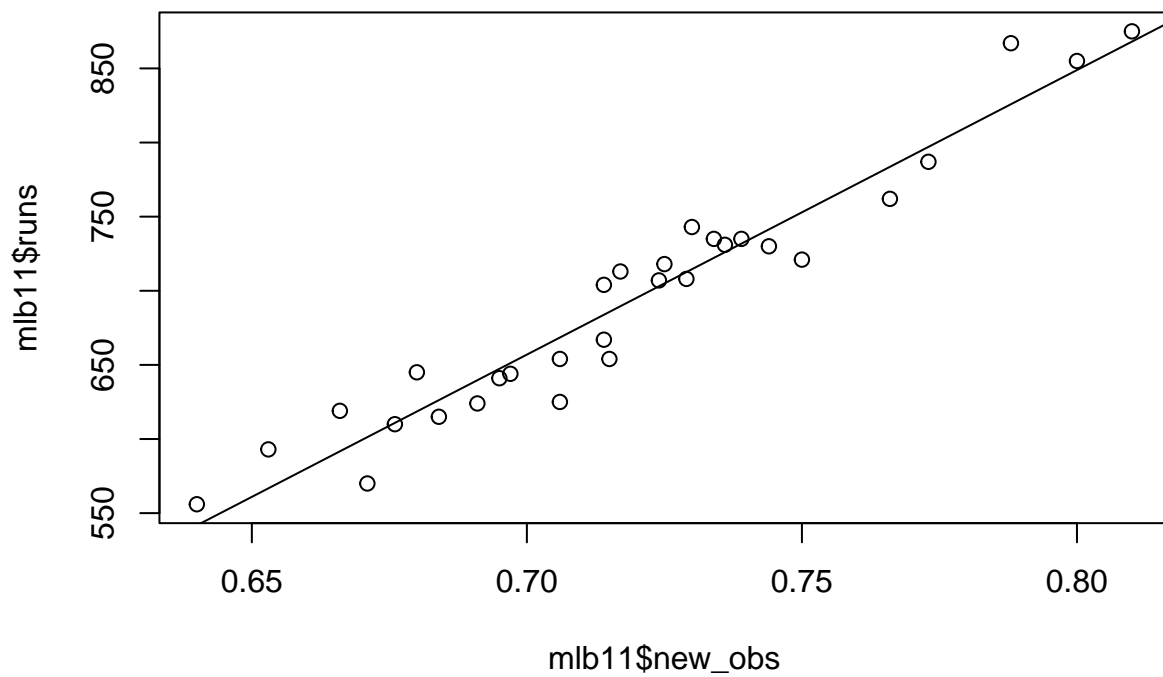
```
m3 <- lm(runs ~ new_slug, data = mlb11)
summary(m3)
```

```
##
## Call:
## lm(formula = runs ~ new_slug, data = mlb11)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -45.41 -18.66  -0.91  16.29  52.29
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)  -375.80      68.71   -5.47 7.70e-06 ***
## new_slug      2681.33     171.83   15.61 2.42e-15 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 26.96 on 28 degrees of freedom
## Multiple R-squared:  0.8969, Adjusted R-squared:  0.8932
## F-statistic: 243.5 on 1 and 28 DF,  p-value: 2.42e-15
```

```
m4 <- lm(runs ~ new_obs, data = mlb11)
summary(m4)
```

```
##
## Call:
## lm(formula = runs ~ new_obs, data = mlb11)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -43.456 -13.690   1.165  13.935  41.156
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)  -686.61      68.93   -9.962 1.05e-10 ***
## new_obs       1919.36     95.70   20.057 < 2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 21.41 on 28 degrees of freedom
## Multiple R-squared:  0.9349, Adjusted R-squared:  0.9326
## F-statistic: 402.3 on 1 and 28 DF,  p-value: < 2.2e-16
```

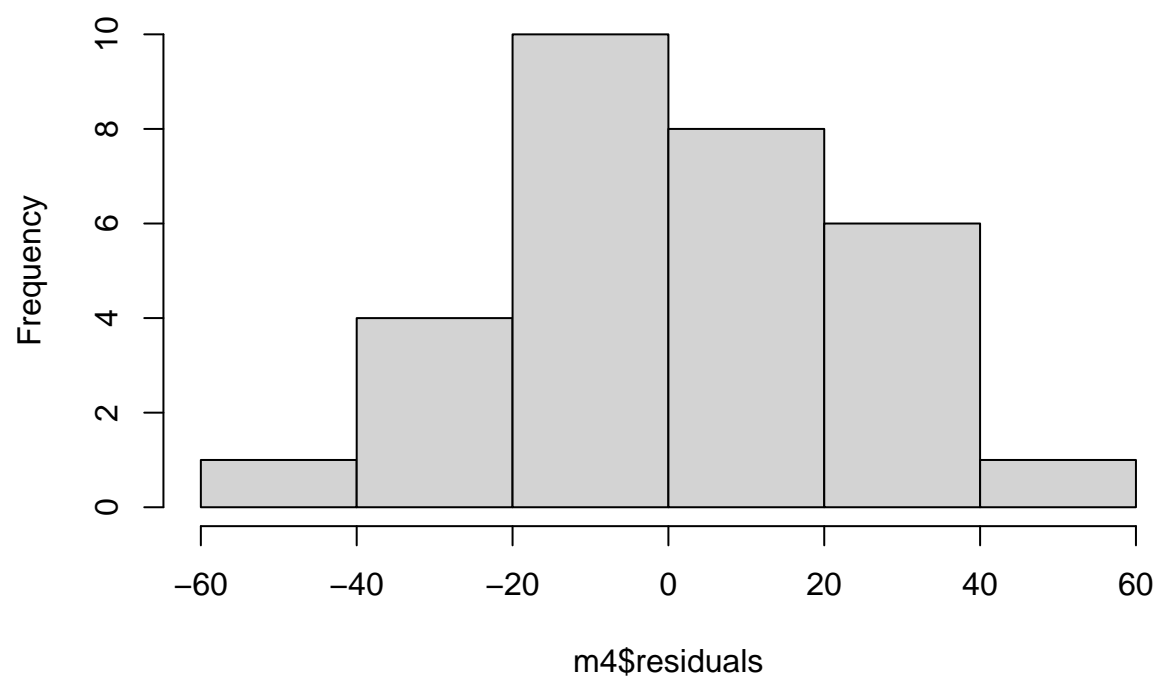
```
plot(mlb11$runs ~ mlb11$new_obs)
abline(m4)
```



**5:** Seems to be relatively normal, but there seems to be no linearity or constant variability as there is an apparent pattern in the residual graph.

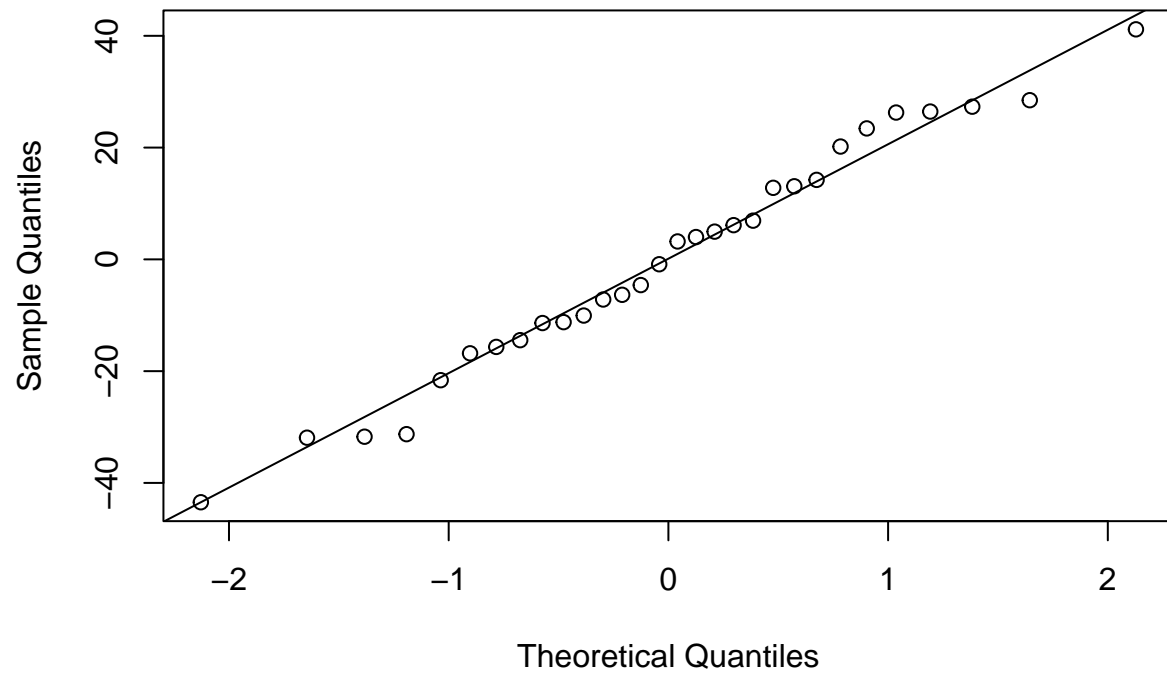
```
m4 <- lm(runs ~ new_obs, data = mlb11)
hist(m4$residuals)
```

**Histogram of m4\$residuals**



```
qqnorm(m4$residuals)  
qqline(m4$residuals)
```

Normal Q-Q Plot



```
plot(m1$residuals ~ mlb11$new_obs)
abline(h = 0, lty = 3) # adds a horizontal dashed line at y = 0
```

