Apache Spark

Lab Objective: Dealing with massive amounts of data often requires parallelization and cluster computing; Apache Spark is an industry standard for doing just that. In this lab we introduce the basics of PySpark, Spark's Python API, including data structures, syntax, and use cases. Finally, we conclude with a brief introduction to the Spark Machine Learning Package.

Apache Spark

Apache Spark is an open-source, general-purpose distributed computing system used for big data analytics. Spark is able to complete jobs substantially faster than previous big data tools (i.e. Apache Hadoop) because of its in-memory caching, and optimized query execution. Spark provides development APIs in Python, Java, Scala, and R. On top of the main computing framework, Spark provides machine learning, SQL, graph analysis, and streaming libraries.

Spark's Python API can be accessed through the PySpark package. You must install Spark, along with the supporting tools like Java, on your local machine for PySpark to work. This will include ensuring that both Java and Spark are included in the environment variable PATH. ¹ Installation of PySpark for local execution or remote connection to an existing cluster can be done with conda or pip commands.²

```
# install Java
$ sudo apt-get install openjdk-8-jdk
# check the version, it may not be exactly the same
$ java -version
openjdk version "1.8.0_242"
OpenJDK Runtime Environment (build 1.8.0_242-b09)
OpenJDK 64-Bit Server VM (build 25.242-b09, mixed mode)

# Install Spark by following instructions in the footnote
# Following these steps, you must configure your PATH environment variable

# CHOOSE ONE
```

¹See the Apache Spark configuration instructions for detailed installation instructions

²You may also use the script provided with the spec file that will completely install Spark and its requirements. Note however that this script is provided AS IS and is not the recommended method.

```
# PySpark installation with conda
$ conda install -c conda-forge pyspark

# PySpark installation with pip
$ pip install pyspark
```

If you use python3 in your terminal, you will need to set the PYSPARK_PYTHON environment variable to python3. When using an IDE, you must call it from the terminal or set the variables inside the editor so that PySpark can be found.

PySpark

One major benefit of using PySpark is the ability to run it in an interactive environment. One such option is the interactive Spark shell that comes prepackaged with PySpark. To use the shell, simply run pyspark in the terminal. In the Spark shell you can run code one line at a time without the need to have a fully written program. This is a great way to get a feel for Spark. To get help with a function use help(function); to exit the shell simply run quit().

In the interactive shell, the SparkSession object - the main entrypoint to all Spark functionality - is available by default as spark. When running Spark in a standard Python script (or in IPython) you need to define this object explicitly. The code box below outlines how to do this. It is standard practice to name your SparkSession object spark.

Achtung!

It is important that when you are finished with a SparkSession you should end it by calling spark.stop().

Note

While the interactive shell is very robust, it may be easier to learn Spark in an environment that you are more familiar with (like IPython). To do so, just use the code given below. Help can be accessed in the usual way for your environment. Just remember to stop() the SparkSession!

```
>>> from pyspark.sql import SparkSession

# instantiate your SparkSession object
>>> spark = SparkSession\
... .builder\
... .appName("app_name")\
... .getOrCreate()

# stop your SparkSession
>>> spark.stop()
```


is somewhat unusual. While this code can be written on a single line, it is often more readable to break it up when dealing with many chained operations; this is standard styling for Spark. Note that you cannot write a comment after a line continuation character '\'.

Resilient Distributed Datasets

The most fundamental data structure used in Apache Spark is the Resilient Distributed Dataset (RDD). RDDs are immutable distributed collections of objects. They are *resilient* because performing an operation on one RDD produces a *new* RDD without altering the original; if something goes wrong, you can always go back to your original RDD and restart. They are *distributed* because the data resides in logical partitions across multiple machines. While RDDs can be difficult to work with, they offer the most granular control of all the Spark data structures.

There are two main ways of creating RDDs. The first is reading a file directly into Spark and the second is parallelizing an existing collection (list, numpy array, pandas dataframe, etc.). We will use the Titanic dataset³ in most of the examples throughout this lab. The example below shows various ways to load the Titanic dataset as an RDD.

```
# initialize your SparkSession object
>>> spark = SparkSession\
            .builder\
            .appName("app_name")\
            .getOrCreate()
# load the data directly into an RDD
>>> titanic = spark.sparkContext.textFile('titanic.csv')
# the file is of the format
# Pclass, Survived, Name, Sex, Age, Sibsp, Parch, Ticket, Fare
# Survived | Class | Name | Sex | Age | Siblings/Spouses Aboard | Parents/\hookleftarrow
    Children Aboard | Fare
>>> titanic.take(2)
['0,3,Mr. Owen Harris Braund,male,22,1,0,7.25',
 '1,1,Mrs. John Bradley (Florence Briggs Thayer) Cumings,female,38,1,0,71.283']
# note that each element is a single string - not particularly useful
# one option is to first load the data into a numpy array
```

³https://web.stanford.edu/class/archive/cs/cs109/cs109.1166/problem12.html

```
>>> np_titanic = np.loadtxt('titanic.csv', delimiter=',', dtype=list)

# use sparkContext to parallelize the data into 4 partitions
>>> titanic_parallelize = spark.sparkContext.parallelize(np_titanic, 4)

>>> titanic_parallelize.take(2)
[array(['0', '3', ..., 'male', '22', '1', '0', '7.25'], dtype=object),
    array(['1', '1', ..., 'female', '38', '1', '0', '71.2833'], dtype=object)]

# end SparkSession
>>> spark.stop()
```

Achtung!

4

Because Apache Spark partitions and distributes data, calling for the first n objects using the same code (such as take(n)) may yield different results on different computers (or even each time you run it on one computer). This is not something you should worry about; it is the result of variation in partitioning and will not affect data analysis.

RDD Operations

Transformations

There are two types of operations you can perform on RDDs: transformations and actions. Transformations are functions that produce new RDDs from existing ones. Transformations are also lazy; they are not executed until an action is performed. This allows Spark to boost performance by optimizing how a sequence of transformations is executed at runtime.

One of the most commonly used transformations is the map(func), which creates a new RDD by applying func to each element of the current RDD. This function, func, can be any callable python function, though it is often implemented as a lambda function. Similarly, flatMap(func) creates an RDD with the flattened results of map(func).

```
... .take(2)
[['0', '3', 'Mr. Owen Harris Braund', 'male', '22', '1', '0', '7.25'],
   ['1', '1', ..., 'female', '38', '1', '0', '71.283']]

# compare to flatMap(), which flattens the results of each row
>>> titanic.flatMap(lambda row: row.split(','))\
... .take(2)
['0', '3']
```

The filter(func) transformation returns a new RDD containing only the elements that satisfy func. In this case, func should be a callable python function that returns a Boolean. The elements of the RDD that evaluate to True are included in the new RDD while those that evaluate to False are excluded.

```
# create a new RDD containing only the female passengers
>>> titanic = titanic.map(lambda row: row.split(','))
>>> titanic_f = titanic.filter(lambda row: row[3] == 'female')
>>> titanic_f.take(3)
[['1', '1', ..., 'female', '38', '1', '0', '71.2833'],
    ['1', '3', ..., 'female', '26', '0', '0', '7.925'],
    ['1', '1', ..., 'female', '35', '1', '0', '53.1']]
```

Note

A great transformation to help validate or explore your dataset is <code>distinct()</code>. This will return a new RDD containing only the distinct elements of the original. In the case of the Titanic dataset, if you did not know how many classes there were, you could do the following:

Spark Command	Transformation
map(f)	Returns a new RDD by applying f to each element of this RDD
flatmap(f)	Same as map(f), except the results are flattened
filter(f)	Returns a new RDD containing only the elements that satisfy f
distinct()	Returns a new RDD containing the distinct elements of the
	original
reduceByKey(f)	Takes an RDD of (key, val) pairs and merges the values for
	each key using an associative and commutative reduce function f
sortBy(f)	Sorts this RDD by the given function f
sortByKey(f)	Sorts an RDD assumed to consist of (key, val) pairs by the
	given function f
<pre>groupBy(f)</pre>	Returns a new RDD of groups of items based on f
groupByKey()	Takes an RDD of (key, val) pairs and returns a new RDD
	with (key, (val1, val2,)) pairs

```
# the following counts the number of passengers in each class
# note that this isn't necessarily the best way to do this

# create a new RDD of (pclass, 1) elements to count occurances
>>> pclass = titanic.map(lambda row: (row[1], 1))
>>> pclass.take(5)
[('3', 1), ('1', 1), ('3', 1), ('1', 1), ('3', 1)]

# count the members of each class
>>> pclass = pclass.reduceByKey(lambda x, y: x + y)
>>> pclass.collect()
[('3', 487), ('1', 216), ('2', 184)]

# sort by number of passengers in each class, ascending order
>>> pclass.sortBy(lambda row: row[1]).collect()
[('2', 184), ('1', 216), ('3', 487)]

# end SparkSession
>>> spark.stop()
```

Achtung!

Note that you must use .collect() to extract data from an RDD. Using .collect() will return an array.

Problem 1. Write a function that accepts the name of a text file with default filename=huck_finn.txt.^a Load the file as a PySpark RDD, and count the number of occurrences of each word. Sort the words by count, in descending order, and return a list of the (word, count)

pairs for the 20 most used words. The data does not need to be cleaned.

Actions

Actions are operations that return non-RDD objects. Two of the most common actions, take(n) and collect(), have already been seen above. The key difference between the two is that take(n) returns the first n elements from one (or more) partition(s) while collect() returns the contents of the entire RDD. When working with small datasets this may not be an issue, but for larger datasets running collect() can be very expensive.

Another important action is reduce(func). Generally, reduce() combines (reduces) the data in each row of the RDD using func to produce some useful output. Note that func *must* be an associative and commutative binary operation; otherwise the results will vary depending on partitioning.

```
# create an RDD with the first million integers in 4 partitions
>>> ints = spark.sparkContext.parallelize(range(1, 1000001), 4)
# [1, 2, 3, 4, 5, ..., 1000000]
# sum the first one million integers
>>> ints.reduce(lambda x, y: x + y)
500000500000

# create a new RDD containing only survival data
>>> survived = titanic.map(lambda row: int(row[0]))
>>> survived.take(5)
[0, 1, 1, 1, 0]

# find total number of survivors
>>> survived.reduce(lambda x, y: x + y)
500
```

Spark Command	Action
take(n)	returns the first ${\tt n}$ elements of an RDD
collect()	returns the entire contents of an RDD
reduce(f)	merges the values of an RDD using an associative and
	commutative operator f
count()	returns the number of elements in the RDD
min(); max(); mean()	returns the minimum, maximum, or mean of the RDD,
	respectively
sum()	adds the elements in the RDD and returns the result
saveAsTextFile(path)	saves the RDD as a collection of text files (one for each
	partition) in the directory specified
	immediately applies f to each element of the RDD; not to be
foreach(f)	confused with map(), foreach() is useful for saving data
	somewhere not natively supported by PySpark

 $^{^{\}rm a} \rm https://www.gutenberg.org/files/76/76-0.txt$

Problem 2. Since the area of a circle of radius r is $A = \pi r^2$, one way to estimate π is to estimate the area of the unit circle. A Monte Carlo approach to this problem is to uniformly sample points in the square $[-1,1] \times [-1,1]$ and then count the percentage of points that land within the unit circle. The percentage of points within the circle approximates the percentage of the area occupied by the circle. Multiplying this percentage by 4 (the area of the square $[-1,1] \times [-1,1]$) gives an estimate for the area of the circle. ^a

Write a function that uses Monte Carlo methods to estimate the value of π . Your function should accept two keyword arguments: n=10**5 and parts=6. Use n*parts sample points and partition your RDD with parts partitions. Return your estimate.

DataFrames

While RDDs offer granular control, they can be slower than their Scala and Java counterparts when implemented in Python. The solution to this was the creation of a new data structure: Spark DataFrames. Just like RDDs, DataFrames are immutable distributed collections of objects; however, unlike RDDs, DataFrames are organized into named (and typed) columns. In this way they are conceptually similar to a relational database (or a pandas DataFrame).

The most important difference between a relational database and Spark DataFrames is in the execution of transformations and actions. When working with DataFrames, Spark's Catalyst Optimizer creates and optimizes a logical execution plan before sending any instructions to the drivers. After the logical plan has been formed, an optimal physical plan is created and executed. This provides significant performance boosts, especially when working with massive amounts of data. Since the Catalyst Optimizer functions the same across all language APIs, DataFrames bring performance parity to all of Spark's APIs.

Spark SQL and DataFrames

Creating a DataFrame from an existing text, csv, or JSON file is generally easier than creating an RDD. The DataFrame API also has arguments to deal with file headers or to automatically infer the schema.

^aSee Example 7.1.1 in the Volume 2 textbook

```
# load the titanic dataset specifying the schema
>>> schema = ('survived INT, pclass INT, name STRING, sex STRING, '
          'age FLOAT, sibsp INT, parch INT, fare FLOAT'
>>> titanic = spark.read.csv('titanic.csv', schema=schema)
>>> titanic.show(2)
+----+
|survived|pclass|
                      name| sex|age|sibsp|parch| fare|
3|Mr. Owen Harris B... | male | 22|
                                     1 0 7.25
          1|Mrs. John Bradley...|female| 38|
                                     1|
                                          0|71.2833|
+----+
only showing top 2 rows
# for files with headers, the following is convenient
spark.read.csv('my_file.csv', header=True, inferSchema=True)
```

Note

To convert a DataFrame to an RDD use my_df.rdd; to convert an RDD to a DataFrame use spark.createDataFrame(my_rdd). You can also use spark.createDataFrame() on numpy arrays and pandas DataFrames.

DataFrames can be easily updated, queried, and analyzed using SQL operations. Spark allows you to run queries directly on DataFrames similar to how you perform transformations on RDDs. Additionally, the pyspark.sql.functions module contains many additional functions to further analysis. Below are many examples of basic DataFrame operations; further examples involving the pyspark.sql.functions module can be found in the additional materials section. Full documentation can be found at https://spark.apache.org/docs/latest/api/python/pyspark.sql.html.

```
| age|
+---+
|18.0|
[64.0]
10.421
+---+
only showing top 3 rows
# filter the DataFrame for passengers between 20-30 years old (inclusive)
>>> titanic.filter(titanic.age.between(20, 30)).show(3)
+----+
|survived|pclass| name| sex| age|sibsp|parch| fare|
+----+
     0| 3|Mr. Owen Harris B...| male|22.0| 1| 0| 7.25|
     1|
         3|Miss. Laina Heikk...|female|26.0| 0| 0| 7.925|
     0| 3| Mr. James Moran| male|27.0| 0| 0|8.4583|
only showing top 3 rows
# find total fare by pclass (or use .avg('fare') for an average)
>>> titanic.groupBy('pclass')\
... .sum('fare')\
      .show()
+----+
|pclass|sum(fare)|
+----+
   1 | 18177.41 |
   3| 6675.65|
| 2| 3801.84|
+----+
# group and count by age and survival; order age/survival descending
>>> titanic.groupBy("age", "survived").count()\
     .sort("age", "survived", ascending=False)\
        .show(2)
+---+
|age|survived|count|
+---+
| 80|
| 74|
       1 1
       0| 1|
+---+
only showing top 2 rows
# join two DataFrames on a specified column (or list of columns)
>>> titanic_cabins.show(3)
+----+
          name| cabin|
+----+
|Miss. Elisabeth W...| B5|
```

```
Note
If you prefer to use traditional SQL syntax you can use spark.sql("SQL QUERY"). Note that
this requires you to first create a temporary view of the DataFrame.
# create the temporary view so we can access the table through SQL
>>> titanic.createOrReplaceTempView("titanic")
# query using SQL syntax
>>> spark.sql("SELECT age, COUNT(*) AS count\
                FROM titanic\
                GROUP BY age\
                ORDER BY age DESC").show(3)
 +---+
 |age|count|
 +---+
 | 80| 1|
 | 74| 1|
 | 71| 2|
 +---+
only showing top 3 rows
```

Spark SQL Command	SQLite Command
select(*cols)	SELECT
groupBy(*cols)	GROUP BY
sort(*cols, **kwargs)	ORDER BY
filter(condition)	WHERE
when(condition, value)	WHEN
between(lowerBound, upperBound)	BETWEEN
drop(*cols)	DROP
<pre>join(other, on=None, how=None)</pre>	JOIN (join type specified by how)
count()	COUNT()
sum(*cols)	SUM()
avg(*cols) or mean(*cols)	AVG()
collect()	fetchall()

Problem 3. Write a function with keyword argument filename='titanic.csv'. Load the file into a PySpark DataFrame and find (1) the number of women on-board, (2) the number of men on-board, (3) the survival rate of women, and (4) the survival rate of men. Return these four values in the order given as a tuple of floats.

Problem 4. In this problem, you will be using the london_income_by_borough.csv and the london_crime_by_lsoa.csv files to visualize the relationship between income and the frequency of crime.^a The former contains estimated mean and median income data for each London borough, averaged over 2008-2016; the first line of the file is a header with columns borough, mean-08-16, and median-08-16. The latter contains over 13 million lines of crime data, organized by borough and LSOA (Lower Super Output Area) code, for London between 2008 and 2016; the first line of the file is a header, containing the following seven columns:

lsoa_code: LSOA code (think area code) where the crime was committed

borough: London borough were the crime was committed major_category: major or general category of the crime minor_category: minor or specific category of the crime

value: number of occurrences of this crime in the given lsoa_code, month, and year

year: year the crime was committed month: month the crime was committed

Write a function that accepts three keyword arguments:

crimefile='london_crime_by_lsoa.csv', incomefile='london_income_by_borough.csv', and major_cat='Robbery'. Load the two files as PySpark DataFrames. Use them to create a new DataFrame. The new DataFrame will contain a row for each borough and have columns for borough, total number of crimes for the given major category (major_cat), and median income. Order the DataFrame by the total number of crimes for major_cat, descending. The final DataFrame should have three columns: borough, major_cat_total_crime, and median -08-16 (column names may be different).

Convert the DataFrame to a numpy array using np.array(df.collect()), and create

a scatter plot of the number of major_cat= crimes by the median income for each borough. Return the numpy array.

^adata.london.gov.uk

Machine Learning with Apache Spark

Apache Spark includes a vast and expanding ecosystem to perform machine learning. PySpark's primary machine learning API, pyspark.ml, is DataFrame-based.

Here we give a start to finish example using Spark ML to tackle the classic Titanic classification problem.

```
# prepare data
# convert the 'sex' column to binary categorical variable
>>> from pyspark.ml.feature import StringIndexer, OneHotEncoder
>>> sex_binary = StringIndexer(inputCol='sex', outputCol='sex_binary')
# one-hot-encode pclass (Spark automatically drops a column)
>>> onehot = OneHotEncoder(inputCols=['pclass'],
                                outputCols=['pclass_onehot'])
# create single features column
from pyspark.ml.feature import VectorAssembler
features = ['sex_binary', 'pclass_onehot', 'age', 'sibsp', 'parch', 'fare']
features_col = VectorAssembler(inputCols=features, outputCol='features')
# now we create a transformation pipeline to apply the operations above
# this is very similar to the pipeline ecosystem in sklearn
>>> from pyspark.ml import Pipeline
>>> pipeline = Pipeline(stages=[sex_binary, onehot, features_col])
>>> titanic = pipeline.fit(titanic).transform(titanic)
# drop unnecessary columns for cleaner display (note the new columns)
>>> titanic = titanic.drop('pclass', 'name', 'sex')
>>> titanic.show(2)
+-----+
|survived| age|sibsp|parch|fare|sex_binary|pclass_onehot| features|
+----+
                1|
                      0|7.25|
                                 0.01
                                       (3,[],[])|(8,[4,5...]
       0|22.0|
       1|38.0|
                      0|71.3|
                                 1.0| (3,[1],...|[0.0,1....|
               1|
+----+
# split into train/test sets (75/25)
>>> train, test = titanic.randomSplit([0.75, 0.25], seed=11)
# initialize logistic regression
>>> from pyspark.ml.classification import LogisticRegression
>>> lr = LogisticRegression(labelCol='survived', featuresCol='features')
```

```
# run a train-validation-split to fit best elastic net param
# ParamGridBuilder constructs a grid of parameters to search over.
>>> from pyspark.ml.tuning import ParamGridBuilder, TrainValidationSplit
>>> from pyspark.ml.evaluation import MulticlassClassificationEvaluator as MCE
>>> paramGrid = ParamGridBuilder()\
                   .addGrid(lr.elasticNetParam, [0, 0.5, 1]).build()
# TrainValidationSplit will try all combinations and determine best model using
# the evaluator (see also CrossValidator)
>>> tvs = TrainValidationSplit(estimator=lr,
                              estimatorParamMaps=paramGrid,
                              evaluator=MCE(labelCol='survived'),
                              trainRatio=0.75,
. . .
                              seed=11)
# we train the classifier by fitting our tvs object to the training data
>>> clf = tvs.fit(train)
# use the best fit model to evaluate the test data
>>> results = clf.bestModel.evaluate(test)
>>> results.predictions.select(['survived', 'prediction']).show(5)
+----+
|survived|prediction|
+----+
      0|
               1.01
       0|
               1.0
               1.01
      01
       0|
               1.0
       0|
                0.01
+----+
# performance information is stored in various attributes of "results"
>>> results.accuracy
0.7527272727272727
>>> results.weightedRecall
0.7527272727272727
>>> results.weightedPrecision
0.751035147726004
# many classifiers do not have this object-oriented interface (yet)
# it isn't much more effort to generate the same statistics for a \hookleftarrow
   DecisionTreeClassifier, for example
>>> dt_clf = dt_tvs.fit(train) # same process, except for a different paramGrid
# generate predictions - this returns a new DataFrame
>>> preds = clf.bestModel.transform(test)
>>> preds.select('survived', 'probability', 'prediction').show(5)
+----+
```

```
|survived|probability|prediction|
+-----+
| 0| [1.0,0.0]| 0.0|
| 0| [1.0,0.0]| 0.0|
| 0| [1.0,0.0]| 0.0|
| 0| [0.0,1.0]| 1.0|
+----+

# initialize evaluator object
>>> dt_eval = MCE(labelCol='survived')
>>> dt_eval.evaluate(preds, {dt_eval.metricName: 'accuracy'})
0.8433179723502304
```

Below is a broad overview of the pyspark.ml ecosystem. It should help give you a starting point when looking for a specific functionality.

PySpark ML Module	Module Purpose
pyspark.ml.feature	provides functions to transform data into feature vectors
pyspark.ml.tuning	grid search, cross validation, and train/validation split functions
pyspark.ml.evaluation	tools to compute prediction metrics (accuracy, f1, etc.)
pyspark.ml.classification	classification models (logistic regression, SVM, etc.)
pyspark.ml.clustering	clustering models (k-means, Gaussian mixture, etc.)
pyspark.ml.regression	regression models (linear regression, decision tree regressor, etc.)

Problem 5. Write a function with keyword argument filename='titanic.csv'. Load the file into a PySpark DataFrame, and use the pyspark.ml package to train a classifier that outperforms the logistic regression each of the three metrics from the example above (accuracy, weightedRecall, weightedPrecision).

Some of Spark's available classifiers are listed below. For complete documentation, visit https://spark.apache.org/docs/latest/api/python/pyspark.ml.html.

```
# from pyspark.ml.classification import LinearSVC
# DecisionTreeClassifier
# GBTClassifier
# MultilayerPerceptronClassifier
# NaiveBayes
# RandomForestClassifier
```

Use randomSplit([0.75, 0.25], seed=11) to split your data into train and test sets before fitting the model. Return the accuracy, weightedRecall, and weightedPrecision for your model, in the given order as a tuple.

Hint: to calculate the accuracy of a classifer in PySpark, use accuracy = MCE(labelCol = 'survived', metricName = 'accuracy').evaluate(predictions).

Additional Material

Further DataFrame Operations

There are a few other functions built directly on top of DataFrames to further analysis. Additionally, the pyspark.sql.functions module expands the available functions significantly.⁴

```
# some immediately accessible functions
# covariance between pclass and fare
>>> titanic.cov('pclass', 'fare')
-22.86289824115662
# summary of statistics for selected columns
>>> titanic.select("pclass", "age", "fare")\
... .summary().show()
pclass
                               agel
+----+
         887|
| count|
                               887|
  mean | 2.305524239007892 | 29.471443066501564 | 32.305420253026846 |
| stddev|0.8366620036697728|14.121908405492908| 49.78204096767521|
                         20.0|
                  1|
                                          7.925|
                  2|
   25% |
                             28.0|
 50%|
                 31
                                         14.4542
  75%|
                  3|
                             38.0|
                                           31.275
                  3|
                             80.0|
| max|
                                         512.3292
+----+
# additional functions from the functions module
>>> from pyspark.sql import functions as sqlf
# finding the mean of a column without grouping requires sqlf.avg()
# alias(new_name) allows us to rename the column on the fly
>>> titanic.select(sqlf.avg("age").alias("Average Age")).show()
+----+
| Average Age|
+----+
|29.471443066516347|
+----+
# use .agg([dict]) on GroupedData to specify [multiple] aggregate
# functions, including those from pyspark.sql.functions
>>> titanic.groupBy('pclass')\
     .agg({'fare': 'var_samp', 'age': 'stddev'})\
       .show(3)
+----+
|pclass| var_samp(fare)| stddev(age)|
+----+
```

 $^{^4} https://spark.apache.org/docs/latest/api/python/pyspark.sql.html \\$

```
| 1| 6143.483042924841|14.183632587264817|
| 3|139.64879027298073|12.095083834183779|
| 2|180.02658999396826|13.756191206499766|
+----+

# perform multiple aggregate actions on the same column
>>> titanic.groupBy('pclass')\
... agg(sqlf.sum('fare'), sqlf.stddev('fare'))\
... show()
+----+
|pclass| sum(fare)| stddev_samp(fare)|
+----+
| 1|18177.412506103516| 78.38037409278448|
| 3| 6675.653553009033| 11.81730892686574|
| 2|3801.8417053222656|13.417398778972332|
+-----+
```

pyspark.sql.functions	Operation
ceil(col)	computes the ceiling of each element in col
floor(col)	computes the floor of each element in col
min(col), max(col)	returns the minimum/maximum value of col
mean(col)	returns the average of the values of col
stddev(col)	returns the unbiased sample standard deviation of col
<pre>var_samp(col)</pre>	returns the unbiased variance of the values in col
rand(seed=None)	generates a random column with i.i.d. samples from $[0,1]$
randn(seed=None)	generates a random column with i.i.d. samples from the
	standard normal distribution
exp(col)	computes the exponential of col
log(arg1, arg2=None)	returns arg1-based logarithm of arg2; if there is only one
	argument, then it returns the natural logarithm
cos(col), sin(col), etc.	computes the given trigonometric or inverse trigonometric
	(asin(col), etc.) function of col