

B. TECH – CS
Assignment - 1
Semester-3rd Session: 2025-26 (ODD)
BCS-303: Discrete structures and Theory of Logic

Unit-1 Set Theory, Relations , POSET & Lattices	Course Outcome: CO1 – Acquire Knowledge of sets and relations for solving the problems of POSET and lattices.
Date of Distribution:	Faculty Name: Mr. Anil Gupta

Sr.	MANDATORY QUESTIONS	BL
1	Describe the following in set builder form: <ul style="list-style-type: none"> $A = \{-4, -3, -2, -1, 0, 1, 2, 3\}$ $B = \{1, 8, 27, 64\}$ 	
2	Show that we can have $A \cap B = A \cap C$ without $B = C$.	
3	State the formula of Distributive laws and De- Morgan's Law.	
4	Let $A = \{1, 2, 3, 4\}$ and $R = \{(1, 1), (1, 2), (2, 1), (2, 2), (3, 3), (3, 4), (4, 3), (4, 4)\}$. Determine whether the relation is reflexive, irreflexive, symmetric, asymmetric, antisymmetric or transitive.	
5	Let $R = \{(1, 2), (2, 3), (3, 1)\}$ and $A = \{1, 2, 3\}$ then find the reflexive, symmetric and transitive closure.	
6	Write the Step wise Procedure of Hasse diagram and draw the hasse diagram of following: <ul style="list-style-type: none"> $[D_{16}, /]$ $(\{2, 3, 5, 30, 60, 120, 180, 360\}, /)$ $(\{1, 2, 3, 4, 6, 9\}, /)$ 	
7	Let $A = \{a, b\}$ $R = \{(a, a), (b, a), (b, b)\}$ $S = \{(a, b), (b, a), (b, b)\}$ Then, verify $(SOR)^{-1} = R^{-1} \circ S^{-1}$	
8	Let $A = \{x: x \text{ is a prime number less than } 10\}$ and $B = \{x: x \in \mathbb{N}, x \text{ is a factor of } 8\}$. Find $A \cup B$.	
9	Show that $D_{36} = \{1, 2, 3, 4, 6, 9, 12, 18, 36\}$ denote the set of divisors of 36 ordered of divisibility then $(D_{36}, 'I')$ is lattice.	
10	Justify that for any set A, B and C: i. $(A - (A \cap B)) = A - B$ ii. $(A - (B \cap C)) = (A - B) \cup (A - C)$	
11	Find the numbers between 1 to 500 that are not divisible by any of the integers 2 or 3 or 5 or 7.	
12	Express power set of each of these sets. $\{\emptyset, \{\emptyset\}\}$ $\{a, \{a\}\}$	
13	If $f: R \rightarrow R$, $g: R \rightarrow R$ and $h: R \rightarrow R$ defined by $f(x) = 3x^2 + 2$, $g(x) = 7x - 5$ and $h(x) = 1/x$. Compute the following composition functions i. $(f \circ g \circ h)(x)$	

	ii. $(gog)(x)$ iii. $(goh)(x)$ iv. $(hogof)(x)$	
14	Prove that $A \times (B \cap C) = (A \times B) \cap (A \times C)$.	
15	Determine whether the following Hasse diagram represent a lattice or not. 	
16	Distinguish between Bounded lattice and Complement lattice? Example with an example.	
SUPPLEMENTARY QUESTIONS		
1	Show that $D_{36} = \{1, 2, 3, 4, 6, 9, 12, 18, 36\}$ denote the set of divisors of 36 ordered of divisibility then $(D_{36}, '1')$ is lattice.	
2	Identify whether the each of the following relations defined on the set $X = \{1, 2, 3, 4\}$ are reflexive, symmetric, transitive and/or antisymmetric? $R_1 = \{ (1,1), (1,2), (2,1) \}$ (ii) $R_2 = \{ (1,1), (1,2), (1,4), (2,1), (2,2), (3,3), (4,1), (4,4) \}$ $R_3 = \{ (2,1), (3,1), (3,2), (4,1), (4,2), (4,3) \}$	

REFERENCES

TEXT BOOKS:				
Ref. [ID]	Authors	Book Title	Publisher/Press	Edition & Year of Publication
[T1]	B. Kolman, R.C. Busby, and S.C. Ross	Discrete Mathematical Structures	5/e, Prentice Hall	2004.
[T2]	E.R. Scheinerman,	Discrete Mathematics,	Brooks/Cole	2000.
Ref. [ID]	Authors	Book Title	Publisher/Press	Edition & Year of Publication
[R1]	Lipschutz, Seymour	Discrete Mathematics",	McGraw Hill.	2015
[R2]	J.P. Chauhan	"Discrete Structures & Graph Theory	Krishna's Education	2007
ONLINE/DIGITAL REFERENCES:				