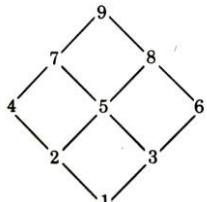


**B. TECH – CS**  
**Assignment - 1**  
**Semester-3<sup>rd</sup> Session: 2025-26 (ODD)**  
**BCS-303: Discrete structures and Theory of Logic**

<b>Unit-1</b> <b>Set Theory, Relations , POSET &amp; Lattices</b>	<b>Course Outcome: CO1 – Acquire Knowledge of sets and relations for solving the problems of POSET and lattices.</b>
<b>Date of Distribution:</b>	<b>Faculty Name: Mr. Anil Gupta</b>

Sr.	<b>MANDATORY QUESTIONS</b>	BL
1	Describe the following in set builder form: <ul style="list-style-type: none"> <li>• <math>A = \{-4, -3, -2, -1, 0, 1, 2, 3\}</math></li> <li>• <math>B = \{1, 8, 27, 64\}</math></li> </ul>	
2	Show that we can have $A \cap B = A \cap C$ without $B = C$ .	
3	State the formula of Distributive laws and De- Morgan's Law.	
4	Let $A = \{1, 2, 3, 4\}$ and $R = \{(1,1), (1,2), (2,1), (2,2), (3,3), (3,4), (4,3), (4,4)\}$ . Determine whether the relation is reflexive, irreflexive, symmetric, asymmetric, antisymmetric or transitive.	
5	Let $R = \{(1,2), (2,3), (3,1)\}$ and $A = \{1, 2, 3\}$ then find the reflexive, symmetric and transitive closure.	
6	Write the Step wise Procedure of Hasse diagram and draw the hasse diagram of following: <ul style="list-style-type: none"> <li>• <math>[D_{16}, /]</math></li> <li>• <math>(\{2, 3, 5, 30, 60, 120, 180, 360\}, /)</math></li> <li>• <math>(\{1, 2, 3, 4, 6, 9\}, /)</math></li> </ul>	
7	Let $A = \{a, b\}$ $R = \{(a,a), (b,a), (b,b)\}$ $S = \{(a,b), (b,a), (b,b)\}$ Then, verify $(SOR)^{-1} = R^{-1} \circ S^{-1}$	
8	Let $A = \{x : x \text{ is a prime number less than } 10\}$ and $B = \{x : x \in \mathbb{N}, x \text{ is a factor of } 8\}$ . Find $A \cup B$ .	
9	Show that $D_{36} = \{1, 2, 3, 4, 6, 9, 12, 18, 36\}$ denote the set of divisors of 36 ordered of divisibility then $(D_{36}, ' ')$ is lattice.	
10	Justify that for any set A, B and C: i. $(A - (A \cap B)) = A - B$ ii. $(A - (B \cap C)) = (A - B) \cup (A - C)$	
11	Find the numbers between 1 to 500 that are not divisible by any of the integers 2 or 3 or 5 or 7.	
12	Express power set of each of these sets. $\{\emptyset, \{\emptyset\}\}$ $\{a, \{a\}\}$	
13	If $f : R \rightarrow R$ , $g : R \rightarrow R$ and $h : R \rightarrow R$ defined by $f(x) = 3x^2 + 2$ , $g(x) = 7x - 5$ and $h(x) = 1/x$ . Compute the following composition functions i. $(fogoh)(x)$	

	ii. $(gog)(x)$ iii. $(goh)(x)$ iv. $(hogof)(x)$	
14	Prove that $A \times (B \cap C) = (A \times B) \cap (A \times C)$ .	
15	Determine whether the following Hasse diagram represent a lattice or not.  	
16	Distinguish between Bounded lattice and Complement lattice? Example with an example.	

#### SUPPLEMENTARY QUESTIONS

1	Show that $D_{36} = \{1, 2, 3, 4, 6, 9, 12, 18, 36\}$ denote the set of divisors of 36 ordered of divisibility then $(D_{36}, '1')$ is lattice.	
2	Identify whether the each of the following relations defined on the set $X = \{1,2,3,4\}$ are reflexive, symmetric, transitive and/or antisymmetric?  $R_1 = \{(1,1), (1,2), (2,1)\}$ (ii) $R_2 = \{(1,1), (1,2), (1,4), (2,1), (2,2), (3,3), (4,1), (4,4)\}$ $R_3 = \{(2,1), (3,1), (3,2), (4,1), (4,2), (4,3)\}$	

#### REFERENCES

TEXT BOOKS:				
Ref. [ID]	Authors	Book Title	Publisher/Press	Edition & Year of Publication
[T1]	B. Kolman, R.C. Busby, and S.C. Ross	Discrete Mathematical Structures	5/e, Prentice Hall	2004.
[T2]	E.R.Scheinerman,	Discrete Mathematics,	Brooks/Cole	2000.
Ref. [ID]	Authors	Book Title	Publisher/Press	Edition & Year of Publication
[R1]	Liptschutz, Seymour	Discrete Mathematics”,	McGraw Hill.	2015
[R2]	J.P.Chauhan	“Discrete Structures & Graph Theory	Krishna’s Education	2007

**ONLINE/DIGITAL REFERENCES:**