

B.TECH-CSE Assignment-2
Semester-I(Odd),Session:2025-26
BCS-303:Discrete structure and Theory of Logic

Unit-2 Unit-Name: Functions and Boolean algebra	Course Outcome: CO2 – Apply fundamental concepts of functions and Boolean algebra for solving the problems of logical abilities.
Date of Distribution:	Faculty Name: Mr. Anil Gupta

Sr.	MANDATORY QUESTIONS	BL
1	Let $f: R \rightarrow R, g: R \rightarrow R, f: R \rightarrow R$ where R is the set of real numbers be given $f(x) = x^2 - 2$ by $f(x) =$ And $g(x) = x+4$. find fog and gof.	3
2	Consider the function $f: \{1,2,3,4,5,6\} \rightarrow \{a,b,c,d\}$ given by $f = \begin{pmatrix} 1 & 2 & 3 & 4 & 5 & 6 \\ a & a & b & b & b & c \end{pmatrix}$ Find $f(\{1,2,3\})$, $f^{-1}(\{a,b\})$, and $f^{-1}(d)$	2
3	Let f and g be functions from R to R defined by $f(x) = ax+b$, $g(x) = 1-x+x^2$. If $(gof) = 9x^2-9x+3$, determine a,b.	3
4	Let $f(x)=x+2$, $g(x) = x-2$, $h(x) = 3x$ find i) fog ii) fogoh.	3
5	Define function. Explain different types of functions with suitable example.	2
6	If $f: A \rightarrow B$, $g: B \rightarrow C$ are invertible functions, then show that $gof: A \rightarrow C$ is invertible and $(gof)^{-1} = f^{-1} \circ g^{-1}$	3
7	Find the value of k, such that $f \circ g = g \circ f$ (i) $f(x) = 3x + 2$, $g(x) = 6x - k$ (ii) $f(x) = 2x - k$, $g(x) = 4x + 5$	3
8	Prove the following laws:- (i) $(a * b)' = (a' + b')$ (ii) $(a + b)' = (a' * b')$	4
9	Using Boolean identities, reduce the given Boolean expression: $F(X, Y, Z) = X'Y + YZ' + YZ + XY'Z'$.	4
10	What is the simplified sum of product form for the Boolean expression: $(A + B' + C')(A + B' + C)(A + B + C')$	4
11	Reduce the following Boolean expression: $F(P, Q, R) = (P+Q)(P+R)$	3

12	Minimize the following Boolean function by using k-map $F(A, B, C, D) = \Sigma m(0, 1, 2, 5, 7, 8, 9, 10, 13, 15)$	4
13	Minimize the following Boolean function by using k-map $F(A, B, C) = \Sigma m(0, 1, 6, 7) + \Sigma d(3, 5)$	4
14	Prove the following (i) $a + a = a$ (ii) $a * a = a$	3
15	Simplify: $F = A.B.C + \bar{A} + A.\bar{B}.C$	3
16	If $f(x) = 2x$ and $g(x) = x+1$, then find $(f \circ g)(x)$ if $x = 1$.	2
SUPPLEMENTARY QUESTIONS		
1	If $f: \mathbb{Q} \rightarrow \mathbb{Q}$ is given by $f(x) = x^2$, then find $f^{-1}(16)$.	4
2	Consider the function $f: \mathbb{R} \rightarrow \mathbb{R}$ defined by $f(x) = 2x+5$, another function $g(x) = (x-5)/2$ Prove that g is inverse of f .	4

REFERENCES

TEXTBOOKS:

Authors	Book Title	Publisher/Press	Edition & Year of Publication
B. Kolman, R. C. Busby, and S. C. Ross	Discrete Mathematical Structures	5/e, Prentice Hall	2004.
E. R. Scheinerman,	Discrete Mathematics,	Brooks/Cole	2000.
Lipschutz, Seymour	Discrete Mathematics	McGraw Hill.	2015

ONLINE/DIGITAL REFERENCES: