

Scaled-dot Product Attention

Attention in Transformer

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Self Attention

Key concept used in Transformer

Self Attention

Layer Type	Complexity per Layer	Sequential Operations	Maximum Path Length
Self-Attention	$O(n^2 \cdot d)$	$O(1)$	$O(1)$
Recurrent	$O(n \cdot d^2)$	$O(n)$	$O(n)$
Convolutional	$O(k \cdot n \cdot d^2)$	$O(1)$	$O(\log_k(n))$
Self-Attention (restricted)	$O(r \cdot n \cdot d)$	$O(1)$	$O(n/r)$

Scaled-dot Product Attention

Model Architecture

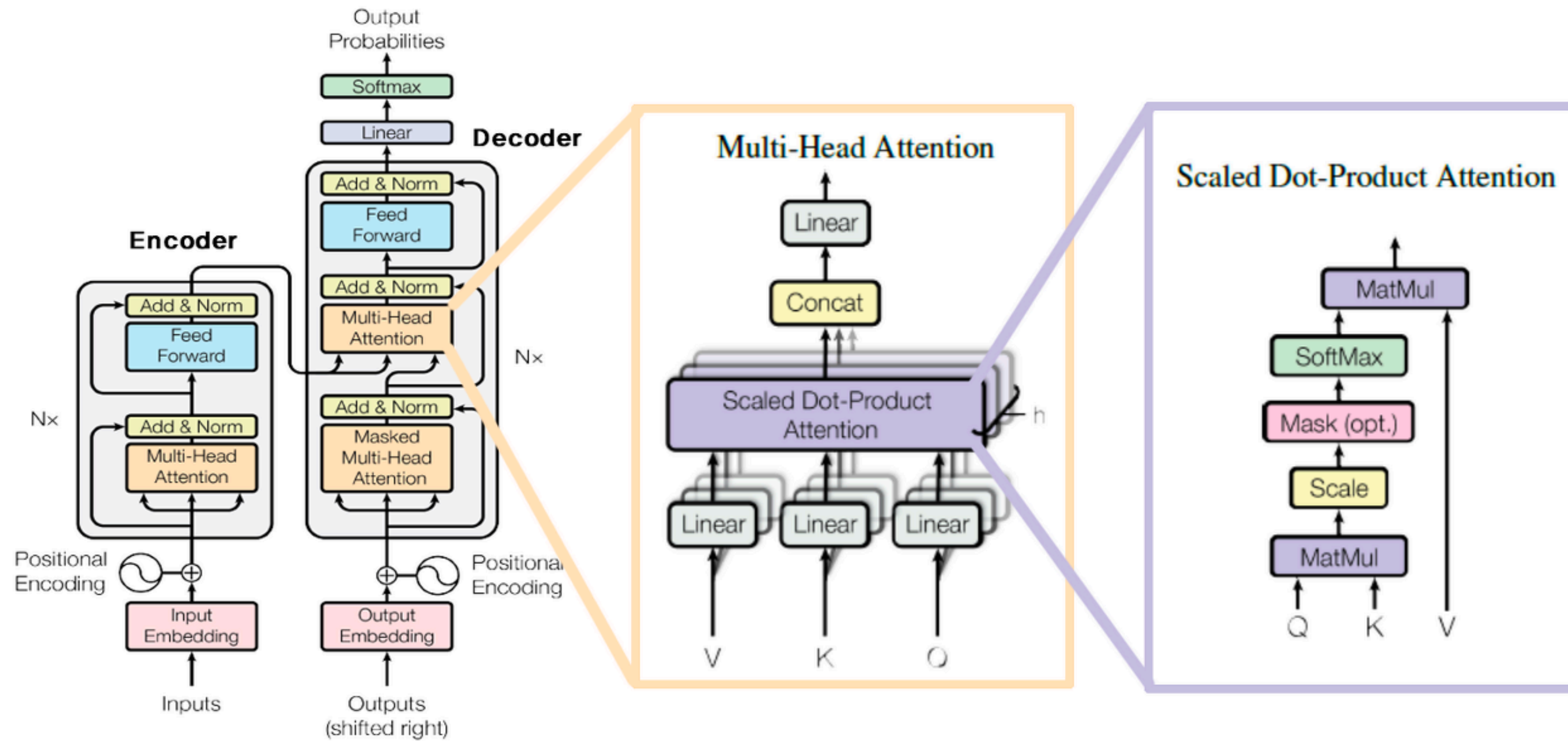
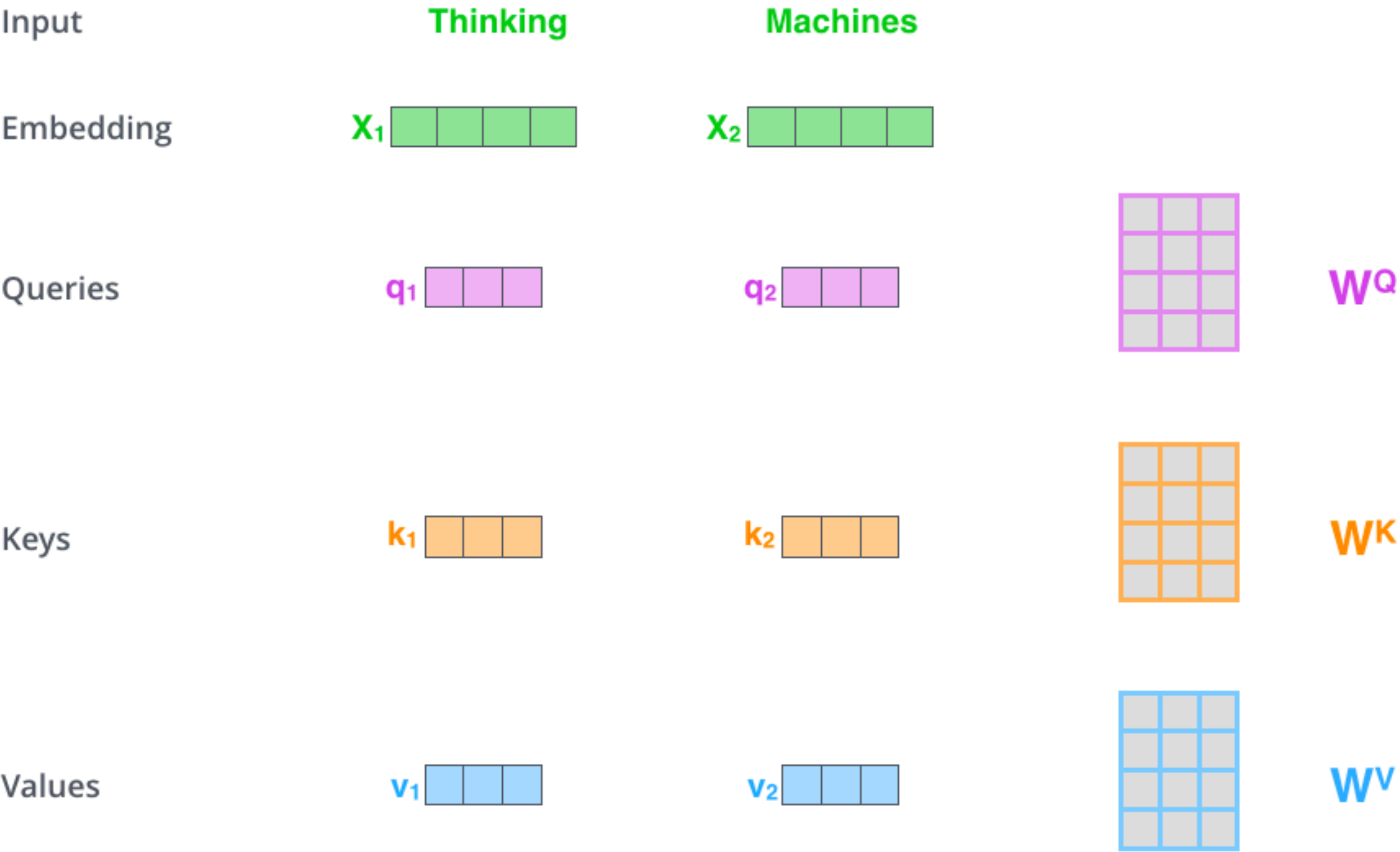


Figure 1: The Transformer - model architecture.

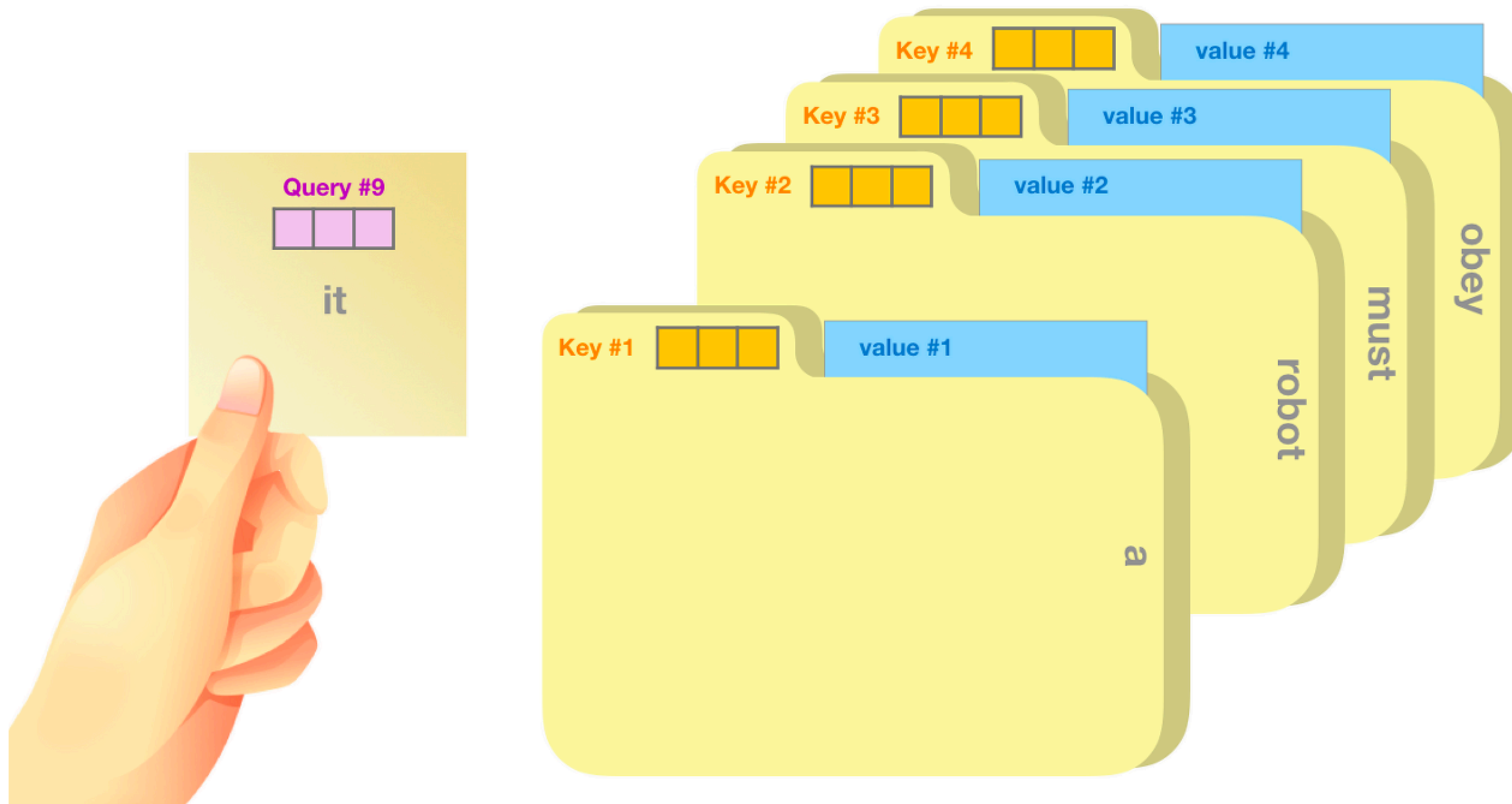
Scaled-dot Product Attention

Step by Step



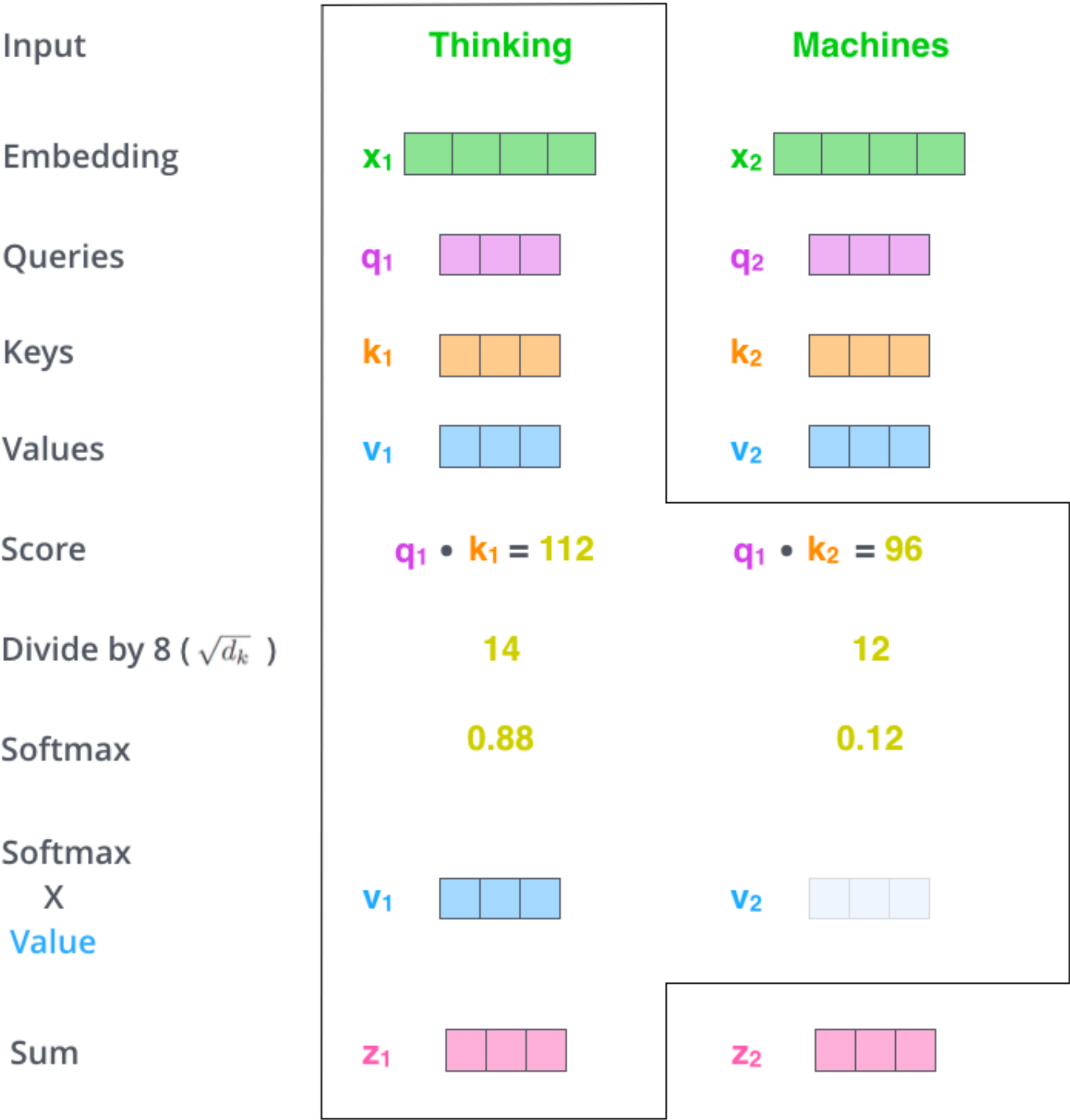
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Step by Step



Scaled-dot Product Attention

Step by Step



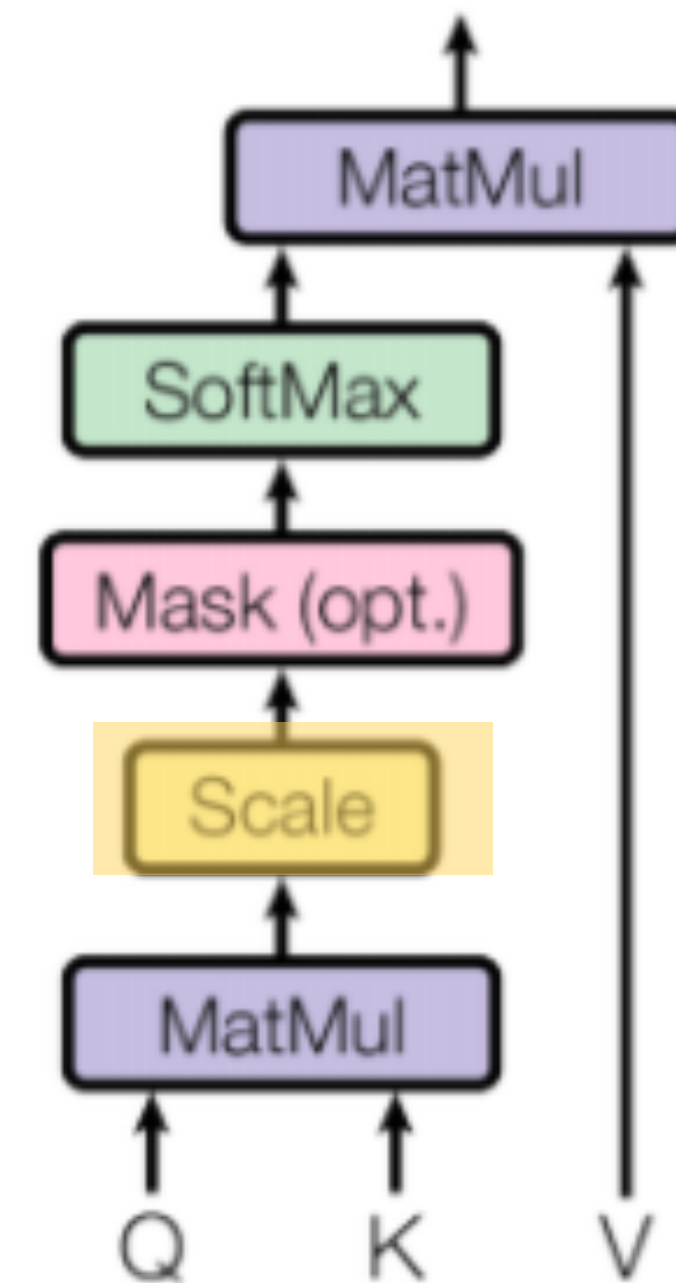
Scaled-dot Product Attention

How it works?

$$\text{Attention}(Q, K, V) = \text{softmax}\left(\frac{QK}{\sqrt{d_k}}\right)V$$

$$Q = XW_q, V = XW_k, V = XW_v \quad W_q, W_k, W_v \in \mathbb{R}^{d \times d_k}$$

Scaled Dot-Product Attention



Scaled-dot Product Attention

Step by Step

$$\text{softmax}\left(\frac{\begin{matrix} \text{Q} \\ \begin{array}{|c|c|c|} \hline & & \\ \hline & & \\ \hline \end{array} \end{matrix} \times \begin{matrix} \text{K}^T \\ \begin{array}{|c|c|} \hline & \\ \hline & \\ \hline & \\ \hline \end{array} \end{matrix}\right) \begin{matrix} \text{V} \\ \begin{array}{|c|c|c|} \hline & & \\ \hline & & \\ \hline \end{array} \end{matrix}$$

=

$$\begin{matrix} \text{Z} \\ \begin{array}{|c|c|c|} \hline & & \\ \hline & & \\ \hline \end{array} \end{matrix}$$

References

- <https://welcome-to-dewy-world.tistory.com/108>
- <https://towardsdatascience.com/illustrated-self-attention-2d627e33b20a>
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- “Attention is all you need”
Vaswani, A., Shazeer, N., Parmar, N., Uszkoreit, J., Jones, L., Gomez, A. N., Kaiser, Ł. & Polosukhin, I.
(2017). Attention is all you need. *Advances in Neural Information Processing Systems* (p./pp. 5998--6008), .

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