

Testarbeit: Tunable Bandpass Filter for Embedded Devices

DSVB Part 1, HSLU-T&A, WaJ

```
close all;
clear all;
clc;
```

1. Parameter definition and verification

Primary parameters for IIR and FIR filter design:

```
f_L = 290e3;    % lower band edge frequency [Hz]
f_U = 305e3;    % upper band edge frequency [Hz]
f_S = 2e6;      % sampling frequency for digital filters [Hz]
N1 = 6;         % FIR filter order (for same # of mult as 2nd order FIR)      <<<=== To be de
N2 = 94;        % FIR filter order (for equivalent ampl. resp. as IIR filter)  <<<=== To be de
```

Secondary parameters for plotting and analysis:

```
nfp = 500;      % # of frequency points used in plotting amplitude/phase responses
```

Verify parameter values:

```
if f_U <= f_L    error('Lower band edge frequency > upper frequency'); end
if f_L < 0       error('Lower band edge frequency < 0 Hz'); end
if f_U >= f_S/2  error('Upper band edge frequency > f_S/2'); end
```

Derived parameters:

```
B = f_U - f_L;          % bandwidth of passband (frequencies above -3 dB attenuation)
f_0 = sqrt(f_L*f_U);    % center frequency of passband filter
Q = f_0/B;              % filter quality factor
om_0 = 2*pi*f_0;        % angular center frequency
f_vec = linspace(0, f_S/2, nfp); % vector of frequency points between 0 and f_S/2 for plotting
p_vec = 1i*2*pi*f_vec;   % vector of points on complex frequency axes to evaluate H(p)
A=1
```

```
A = 1
```

2. Analog Prototype Filter (Task 3a)

Define the continuous-time transfer function $H(p)$ of the analog prototype filter by explicitly constructing the numerator and denominator polynomials using vector p_vec , and subsequently element-wise division of these vectors.

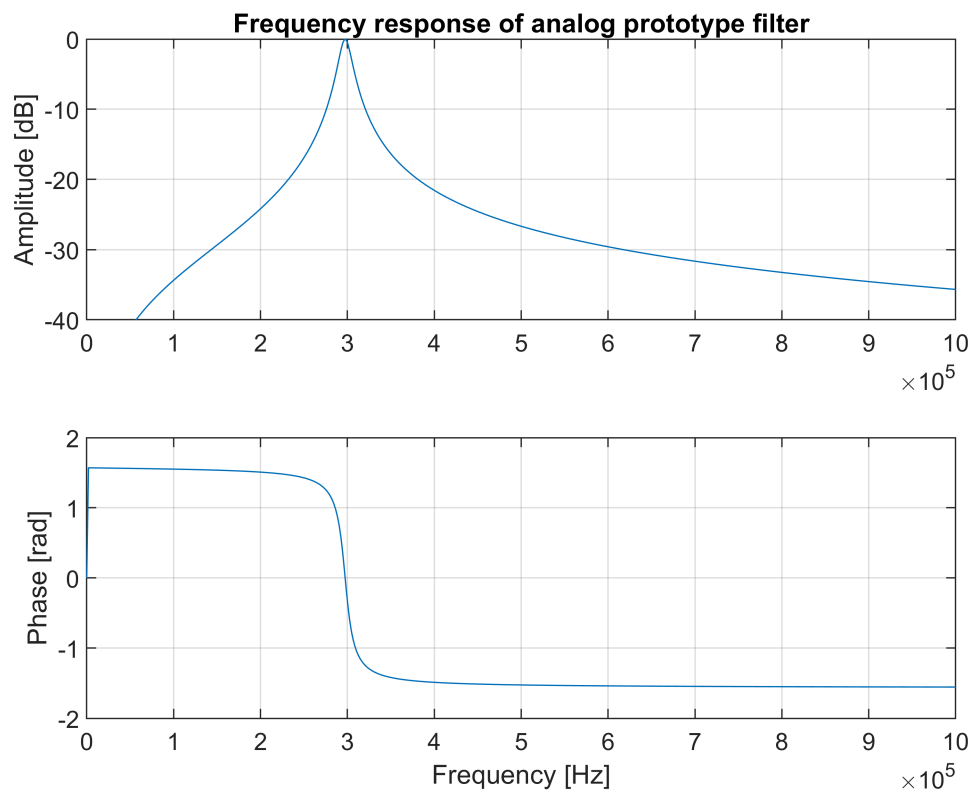
```
b_p = A.*B./(f_0.*om_0).*p_vec; % <<<<<<< ToDo
a_p = 1+B./(f_0.*om_0).*p_vec+1./om_0^2.*p_vec.^2; % <<<<<<< ToDo
H_p = b_p ./ a_p;
```

Plot magnitude and phase response of the analog prototype filter in figure #1.

```

figure('name','figure 1')
subplot(2,1,1)
plot(f_vec,20*log10(abs(H_p)));
title('Frequency response of analog prototype filter')
ylabel('Amplitude [dB]')
axis([0 f_S/2 -40 0])
grid on;
subplot(2,1,2)
plot(f_vec,angle(H_p))
axis([0 f_S/2 -2 2])
grid on;
ylabel('Phase [rad]')
xlabel('Frequency [Hz]')

```



3. IIR Bandpass Filter (Task 3b)

Get the IIR filter coefficients using the bilinear transform of the analog prototype filter without and with prewarping.

```

[b_iir_nopw,a_iir_nopw,K_iir_nopw] = bp_iir_bilin(f_L, f_U, f_S, 'no prewarp');
[b_iir_pw,a_iir_pw,K_iir_pw]       = bp_iir_bilin(f_L, f_U, f_S, 'prewarp');

```

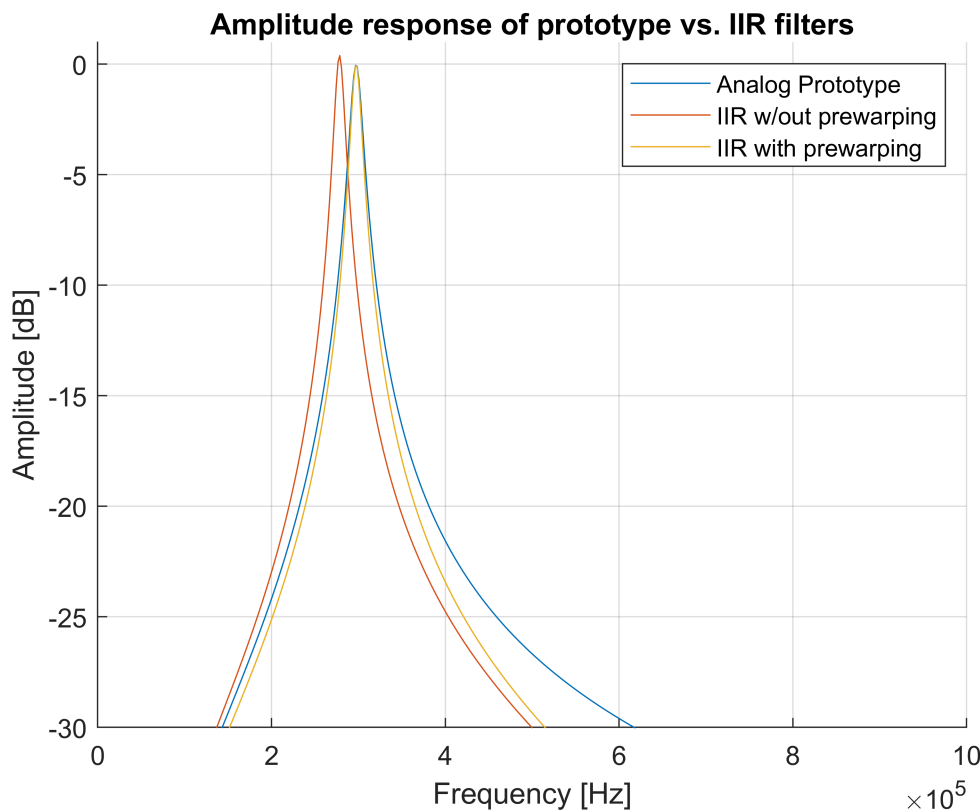
Compute the frequency response of the two IIR filters at the same frequency points used for computing the frequency response of the analog prototype filter.

```
[H_iir_nopw] =freqz(K_iir_pw.*b_iir_nopw,a_iir_nopw,2*pi*f_vec/f_S); % <<<<<<< ToDo
[H_iir_pw]   =freqz(K_iir_pw.*b_iir_pw,a_iir_pw,2*pi*f_vec/f_S) ; % <<<<<<< ToDo
```

Plot magnitude response of analog prototype filter, and two IIR filters designed with and without frequency prewarping in figure #2.

```
figure('name','figure 2')

% <<<<<<< ToDo
hold on
plot(f_vec,20*log10(abs(H_p)));
plot(f_vec,20*log10(abs(H_iir_nopw)));
plot(f_vec,20*log10(abs(H_iir_pw)));
hold off
axis([0 f_S/2 -30 1])
grid on;
ylabel('Amplitude [dB]')
xlabel('Frequency [Hz]')
title('Amplitude response of prototype vs. IIR filters')
legend('Analog Prototype','IIR w/out prewarping','IIR with prewarping','Location','NorthEast')
```



4. FIR Bandpass Filter (Task 3c)

Get the FIR filter coefficients using the window design method with a rectangular window and two different filter order:

```
b_fir_rect_N1=bp_fir_win(f_L, f_U, N1, f_S, '');%
```

```
b_fir_rect_N2=bp_fir_win(f_L, f_U, N2, f_S, '');%
```

Compute the frequency response of the two FIR filters at the same frequency points used for computing the frequency response of the IIR filters.

```
[H_fir_rect_N1] = freqz(b_fir_rect_N1,1,2*pi*f_vec/f_S);
% [H_fir_rect_N1] = freqz(b_fir_rect_N1,1,500);
% [H_fir_rect_N2] = freqz(b_fir_rect_N2,1,500);
[H_fir_rect_N2] = freqz(b_fir_rect_N2,1,2*pi*f_vec/f_S);
```

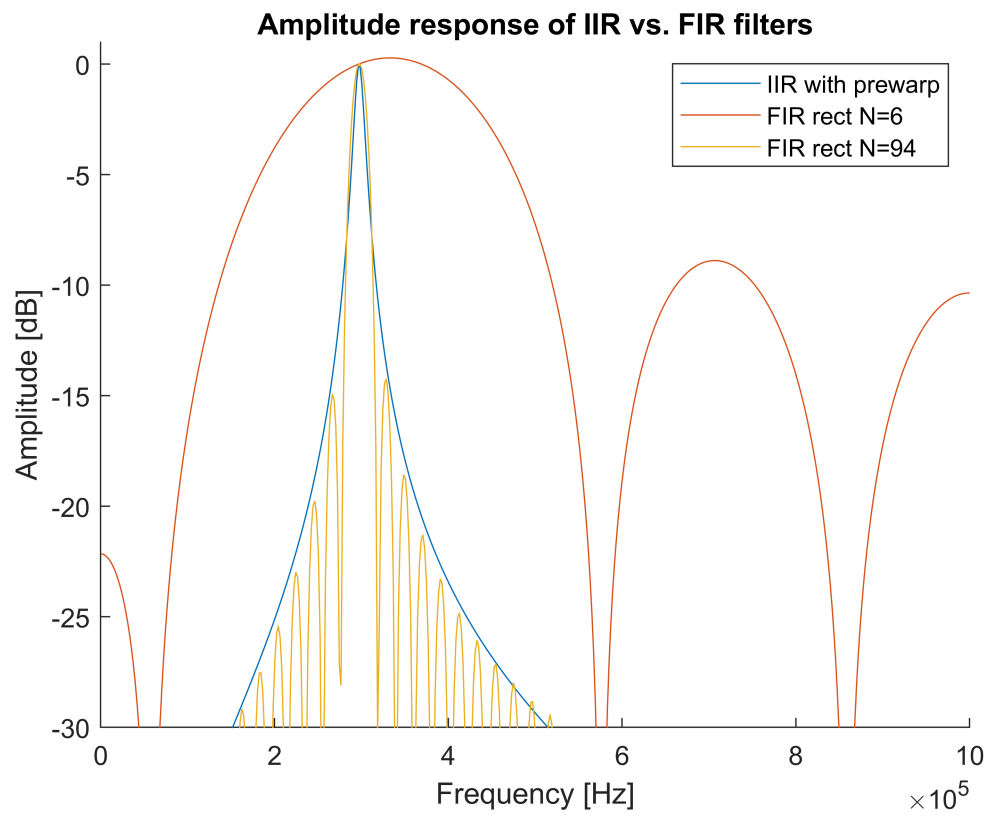
Scale the frequency response such that the gain is 1 at the passband center frequency f_0 . For this, first get gain of the current frequency response at the center frequency, and then divide the frequency response by this value.

```
% G1_f_0_custom = abs(H_fir_rect_N1(ceil(length(H_fir_rect_N1)/2)));
G1_f_0 = abs(H_fir_rect_N1(round(nfp*2*f_0/f_S)));
H_fir_rect_N1 = H_fir_rect_N1/G1_f_0;
% G2_f_0_custom = abs(H_fir_rect_N2(ceil(length(H_fir_rect_N2)/2)));
G2_f_0 = abs(H_fir_rect_N2(round(nfp*2*f_0/f_S)));
H_fir_rect_N2 = H_fir_rect_N2/G2_f_0;
```

Plot magnitude response of the IIR filter obtained with prewarping together with the two FIR filters designed with the windowing methods and two different filter orders in figure #3.

```
figure('name','figure 3')
hold on
plot(f_vec,20*log10(abs(H_iir_pw)));
plot(f_vec,20*log10(abs(H_fir_rect_N1)));
plot(f_vec,20*log10(abs(H_fir_rect_N2)));
hold off

axis([0 f_S/2 -30 1])
ylabel('Amplitude [dB]')
xlabel('Frequency [Hz]')
title('Amplitude response of IIR vs. FIR filters')
legend('IIR with prewarp', ['FIR rect N=' num2str(N1)], ['FIR rect N=' num2str(N2)], 'Location', 'N')
```



Notes:

$$\begin{aligned}
 p &= v \cdot \frac{z-1}{z+1}, \quad v = \frac{\frac{2\pi f}{T_s}}{\sqrt{\frac{2\pi f}{T_s}^2 + 1}} \\
 \mu &= \frac{\beta}{f_o \cdot \omega_o} \\
) &= A \cdot \frac{\mu \cdot v \cdot \frac{z-1}{z+1}}{1 + \mu \cdot v \cdot \frac{z-1}{z+1} + \frac{1}{\omega_o^2} \cdot v^2 \cdot \frac{(z-1)^2}{(z+1)^2}} \cdot \frac{(z+1)^2}{(z+1)^2} \\
 &= A \cdot \frac{\mu \cdot v \cdot (z-1)(z+1)}{(z+1)^2 + \mu \cdot v \cdot (z-1)(z+1) + \frac{1}{\omega_o^2} v^2 (z-1)^2} \\
 &= \frac{A_{\mu v} (z^2 - 1)}{z^2 + 2z + 1 + \mu v (z^2 - 1) + \frac{1}{\omega_o^2} v^2 (z^2 - 2z + 1)} \\
 &= \frac{z^2 A_{\mu v} - A_{\mu v}}{z^2 + 2z + 1 + \cancel{z^2 A_{\mu v}} - \mu v + \frac{1}{\omega_o^2} v^2 z^2 - \frac{1}{\omega_o^2} v^2 2z + \frac{1}{\omega_o^2} v^2} \cdot z^{-2} \\
 A_{\mu v} &= A_{\mu v} z^{-2} \\
 1 + \cancel{2z^{-1}} + \cancel{2z^{-2}} + \mu v - \mu v z^{-2} + \frac{1}{\omega_o^2} v^2 - \frac{1}{\omega_o^2} v^2 2z^{-1} + \frac{1}{\omega_o^2} v^2 z^{-2}
 \end{aligned}$$

$$\begin{aligned}
 &= A_{\mu v} \cdot \frac{b_0 b_2}{(1 - z^{-2})} \\
 &= A_{\mu v} \cdot \frac{\underbrace{uv+1}_{a_0} + \underbrace{\frac{1}{\omega_o^2} v^2}_{2 \cdot a_1} + \underbrace{\frac{-1}{z} \left(1 - \frac{1}{\omega_o^2} v^2\right)}_{2 \cdot a_1}}{(1 - z^{-2})} \\
 &\quad \text{oben \& unten} \cdot 1 \\
 &= \frac{A_{\mu v}}{1 + \frac{1}{\omega_o^2} v^2 \cdot \mu v} \cdot \frac{b_0 b_2}{1 + \frac{1}{\omega_o^2} v^2} \\
 &\quad \underbrace{\hspace{1cm}}_{a_0} \quad \underbrace{\hspace{1cm}}_{a_1}
 \end{aligned}$$