Outliers in Time Series

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Outlier Models

- ARIMA(p, d, q) process

$$X_t = \frac{\theta(B)}{\alpha(B)\phi(B)} Z_t$$

- Roots of $\theta(B), \phi(B)$ outside unit circle
- $\alpha(B) = (1 - B)^d$
- $Z_t \sim_{iid}$ Normal$(0, \sigma^2)$

Outlier Models

- Observed series

$$X_t^* = X_t + \text{ outlier effect}$$

- Four models for outlier effect:
  - Additive outlier (AO)
  - Level shift (LS)
  - Temporary change (TC)
  - Innovational outlier (IO)

Slide with R Code and Output

```r
summary(cars)
```

```
##      speed           dist       
##  Min.   : 4.0   Min.   :  2.00  
##  1st Qu.:12.0   1st Qu.: 26.00  
##  Median :15.0   Median : 36.00  
##  Mean   :15.4   Mean   : 42.98  
##  3rd Qu.:19.0   3rd Qu.: 56.00  
##  Max.   :25.0   Max.   :120.00  
```

Slide with Plot