Topic Models

HSS 510 / DS 518: NLP for HSS

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Agenda

Things to be covered

- What is topic modeling
- Latent Dirichlet Allocation
- Extensions
 - Correlated Topic Model
 - Structural Topic Model
- Model selection and interpretation
- Summary

What is Topic Model

Multi-membership, unsupervised algorithms to discover topics

- Unsupervised learning (no manual labeling of topics)
- Documents can contain multiple topics (←→ clustering algorithms)
- Two main usages: exploration or measurement

What is Topic Model

Topic: what is being talked about/written about

- Topic models assume an intuitive and abstract notion of a topic
- Unclear what topic actually means in theoretical terms
- "The meaning of a topic in an LDA topic model must be assessed empirically instead and defined against the background of substantive theoretical concepts, such as political issues or frames" (Maier et al. 2018)

What is Topic Model

LDA and its extensions

- Latent Dirichlet Allocation (LDA) is one fundamental approach (Blei et al., 2003)
- Alternative approaches
 - Correlated Topic Model (CTM)
 - Structural Topic Model (STM)
 - Clustering of transformer-based embeddings (Week 12)

Topic Model in Context

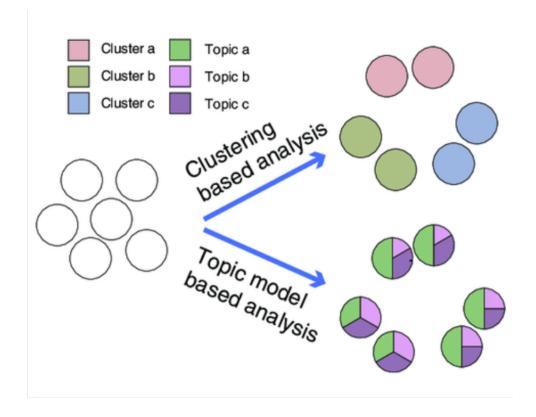
Supervised vs. Unsupervised

	Supervised	Unsupervised
Objective	Trained on a labeled data to learn a mapping from input to output	Find patterns or structures within data without labels
Outcome	Pre-defined categories	Not quite pre-defined
Model evaluation	Explicit metrics such as accuracy, precision, recall, or MSE	Can involve qualitative assessment
Examples	Classification/regression for texts	Topic models

Topic Model in Context

Clustering algorithms vs. Topic models

- Clustering (e.g., K-means)
 assumes that each document
 belongs to one cluster
- But documents often discuss multiple ideas
- Many topic models allow for mixed-membership
- Click for figure source



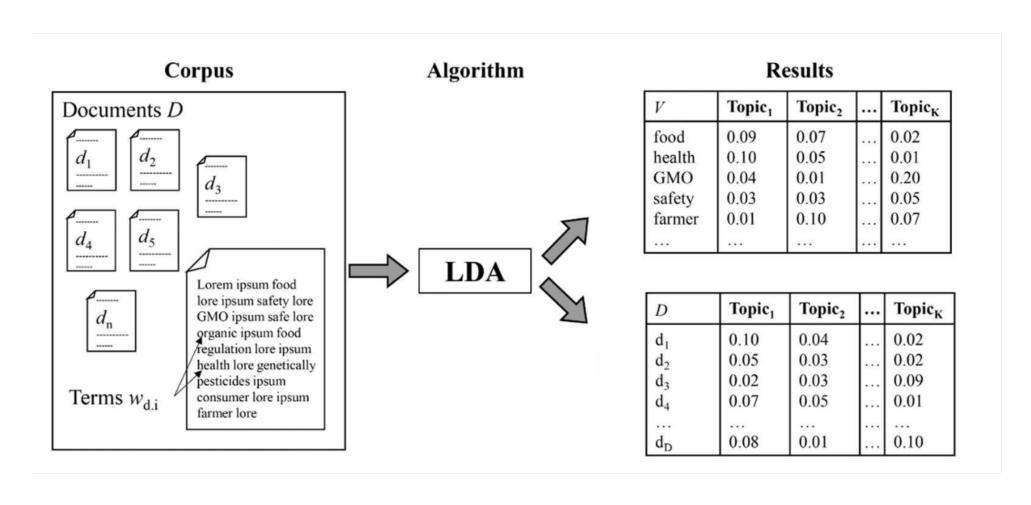
Latent Dirichlet Allocation (LDA)

Used to identify the latent topic structure within a corpus

- A seminal model and one of the most widely used model
- A generative model: assumes that documents are created through a hidden process
 - "Latent": the topic structure is hidden, inferred from the data
 - "Dirichlet": Dirichlet distributions as part of the generative process
- In LDA (and similar approaches)
 - BoW (Bag of Words) assumption is used
 - "Documents" are seen as "distributions over topics"
 - "Topics" are seen as "distributions over words"

Latent Dirichlet Allocation (LDA)

The framework of LDA (adaped from Maier et al. 2018)



LDA: Key Distributions

Multinomial distribution

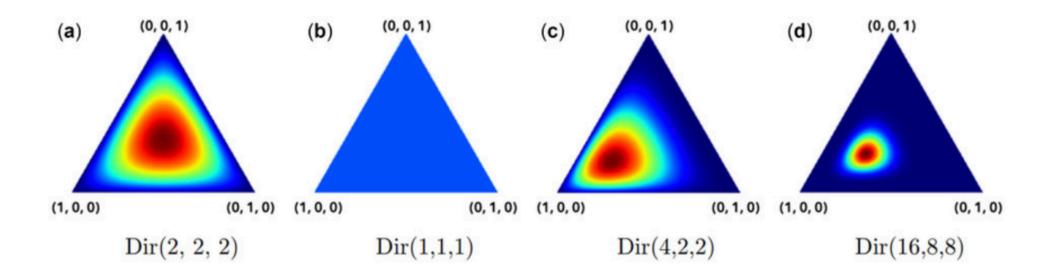
- Generalization of binomial distribution (e.g., flipping a coin)
- Probabilities of multiple outcomes (not just two)
- E.g., rolling a (6-sided) dice
 - Each side (from 1 to 6): discrete outcome
 - The probabilities sum up to 1 $(\frac{1}{6} + ... + \frac{1}{6} = 1)$
- E.g., allocating a pie to one of 3 people
 - Each person: discrete outcome
 - The probabilities sum up to 1 $(\frac{1}{4} + \frac{1}{4} + \frac{1}{2} = 1)$

LDA: Key Distributions

Dirichlet distribution

- Provides a way to randomly generate multinomial distributions
- The pie split example
 - Imagine if you did not decide ahead of time exactly how to slice the pie
 - Instead, we specify a random process to decide how likely each person gets the pie
 - Equal chances among the three people, or perhaps it's more likely that one person gets it than the others
 - E.g., [0, 0, 1], [1/3, 1/3, 1/3], [1/2, 1/4, 1/4], etc.

LDA: Key Distributions



Consider a corpus of D documents, each with N_d words, and assume there are K topics

- Assume a statistical model that generated our documents, then estimate the model and recover latent (unobserved) topics
- Each document is seen as a multinomial distribution over topics
- Each topic is seen as a multinomial distribution over words
- E.g., a stylized corpus with D = 5, N = 8 per document (and also 8 unique words in the corpus in total), and K = 3

E.g.,
$$D = 5$$
, $N = 8$, $K = 3$

- θ_d ~ Dir(α): for each d, its **topic distribution** is drawn from a Dirichlet distribution (e.g., θ_1 = [0.1, 0.7, 0.2])
- β_k ~ Dir(η): for each k, its **word distribution** is drawn from another Dirichlet distribution (e.g., β_2 = [0, 0, 0.2, 0.1, 0, 0, 0.3, 0.4])
- For *n*th word in document *d*:
 - $z_{d,n}$ ~ Multinomial(θ_d): draw a topic (z)
 - $w_{d,n}$ ~ Multinomial($\beta_{z_{d,n}}$): draw a word from the selected topic (w)

In summary, the joint probability is the following

- $\theta_d \sim \text{Dir}(\alpha)$ for $d \in \{1, ..., D\}$
- $\beta_k \sim \text{Dir}(\eta)$ for $k \in \{1, ..., K\}$
- $z_{d,n}$ ~ Multinomial(θ_d)
- $w_{d,n}$ ~ Multinomial($\beta_{z_{d,n}}$)

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p(\beta_{1:K}, \theta_{1:D}, z_{1:D}, w_{1:D})
= \prod_{i=1}^{K} p(\beta_i) \prod_{d=1}^{D} p(\theta_d)
\left( \prod_{n=1}^{N} p(z_{d,n} | \theta_d) p(w_{d,n} | \beta_{1:K}, z_{d,n}) \right)
```

Figure 4. The graphical model for latent Dirichlet allocation. Each node is a random variable and is labeled according to its role in the generative process (see Figure 1). The hidden nodes—the topic proportions, assignments, and topics—are unshaded. The observed nodes—the words of the documents—are shaded. The rectangles are "plate" notation, which denotes replication. The N plate denotes the collection words within documents; the D plate denotes the collection of documents within the collection.

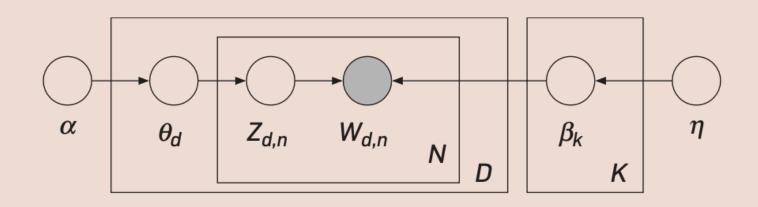


Figure 1. The intuitions behind latent Dirichlet allocation. We assume that some number of "topics," which are distributions over words, exist for the whole collection (far left). Each document is assumed to be generated as follows. First choose a distribution over the topics (the histogram at right); then, for each word, choose a topic assignment (the colored coins) and choose the word from the corresponding topic. The topics and topic assignments in this figure are illustrative—they are not fit from real data. See Figure 2 for topics fit from data.

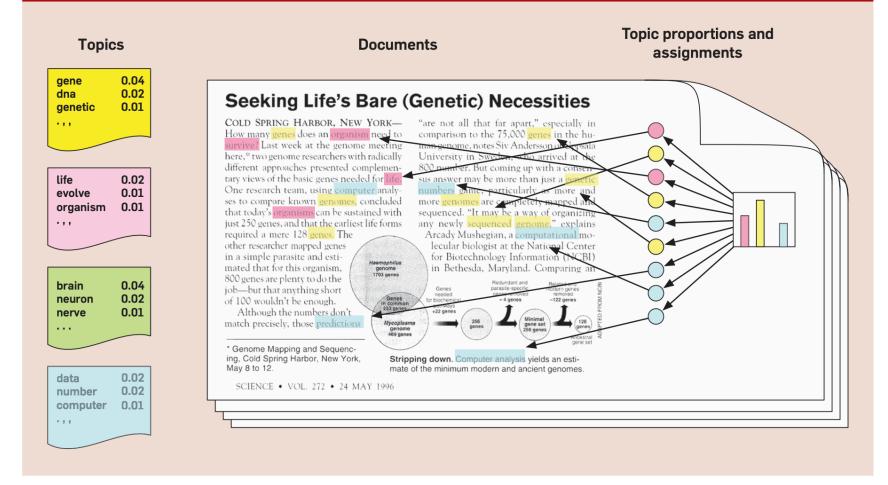
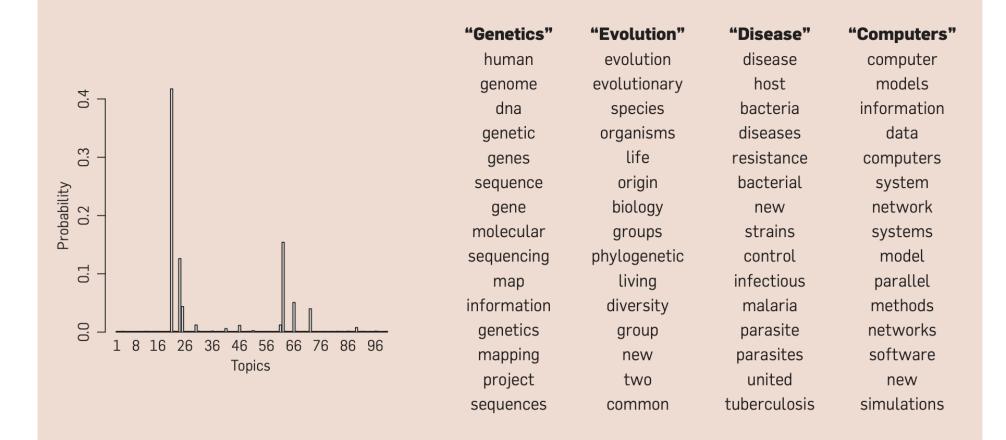


Figure 2. Real inference with LDA. We fit a 100-topic LDA model to 17,000 articles from the journal *Science*. At left are the inferred topic proportions for the example article in Figure 1. At right are the top 15 most frequent words from the most frequent topics found in this article.



LDA: Estimation

E.g., with D = 1000, |V| = 10000, and K = 3

• LDA estimates θ (distributions over topics) and β (distributions over vocabulary)

$$\theta = \underbrace{\begin{pmatrix} \theta_{1,1} & \theta_{1,2} & \theta_{1,3} \\ \theta_{2,1} & \theta_{2,2} & \theta_{2,3} \\ \dots & \dots & \dots \\ \theta_{1000,1} & \theta_{1000,2} & \theta_{1000,3} \end{pmatrix}}_{1000 \times 3} = \underbrace{\begin{pmatrix} 0.7 & 0.2 & 0.1 \\ 0.3 & 0.1 & 0.6 \\ \dots & \dots & \dots \\ 0.1 & 0.8 & 0.1 \end{pmatrix}}_{1000 \times 3}$$

$$\beta = \underbrace{\begin{pmatrix} \beta_{1,1} & \beta_{1,2} & \dots & \beta_{1,10000} \\ \beta_{2,1} & \beta_{2,2} & \dots & \beta_{2,10000} \\ \beta_{3,1} & \beta_{3,2} & \dots & \beta_{3,10000} \end{pmatrix}}_{3 \times 10000} = \underbrace{\begin{pmatrix} 0.04 & 0.01 & \dots & 0.0001 \\ 0.00002 & 0.001 & \dots & 0.05 \\ 0.00001 & 0.03 & \dots & 0.0001 \end{pmatrix}}_{3 \times 10000}$$

LDA: Estimation

Estimation

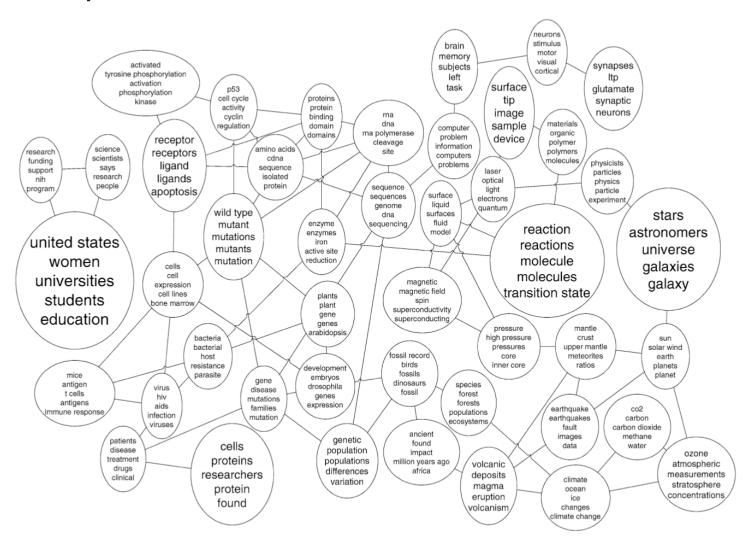
- Done in a Bayesian framework
- Estimation methods (see Blei (2012) for more discussions)
 - Gibbs sampling methods
 - Variational approximations

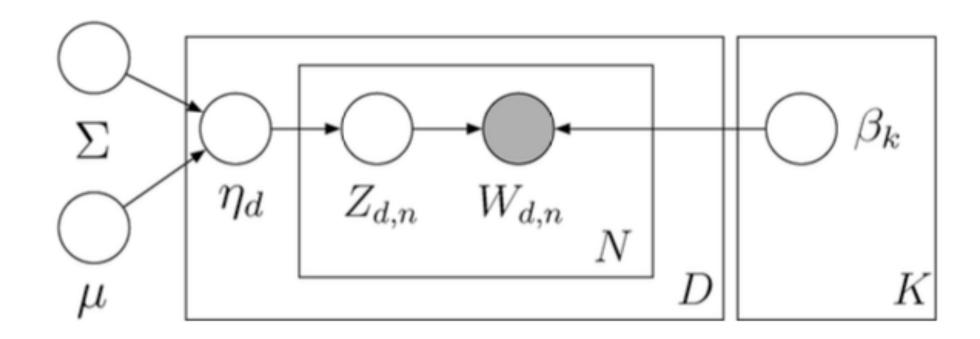
Model Selection

Determining hyperparameters: K (and α , η)

- *K*: based on a combination of quantitative metrics and human judgement
- The Dirichlet priors; α (the topic distribution prior) and η (the word distribution prior)
 - Often set symmetric (e.g., [0.1, 0.1, 0.1] for K = 3)
 - Typically both are set at 0.1 or 0.01 (the smaller, the fewer topics/words dominate the document/topic) but this can be tuned and affect model performance
 - See Maier et al. (2018) for more discussions

- Blei and Lafferty (2005) and (2007)
- A limitation of LDA is the inability to model topic correlation
- "A document about genetics is more likely to also be about disease than X-ray astronomy" (Blei and Lafferty (2007))
- CTM, which relies on logistic normal distribution, allows for modeling correlations between topics through a covariance matrix
- The authors report that this can lead to a better model fit (what the model fit means will be discussed soon)





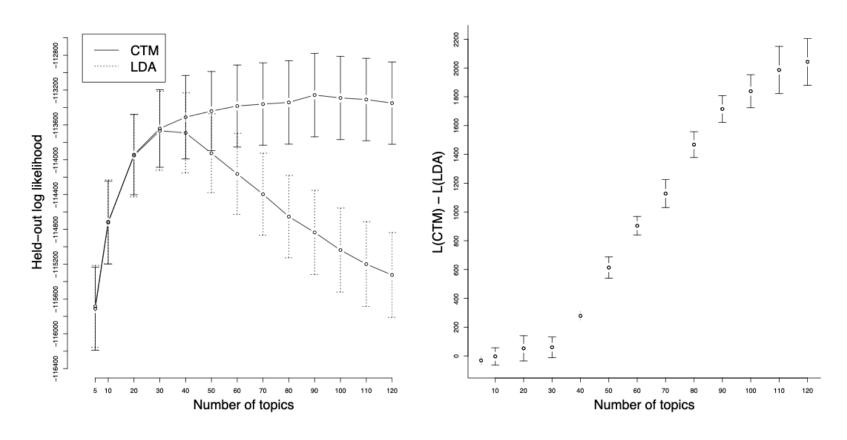
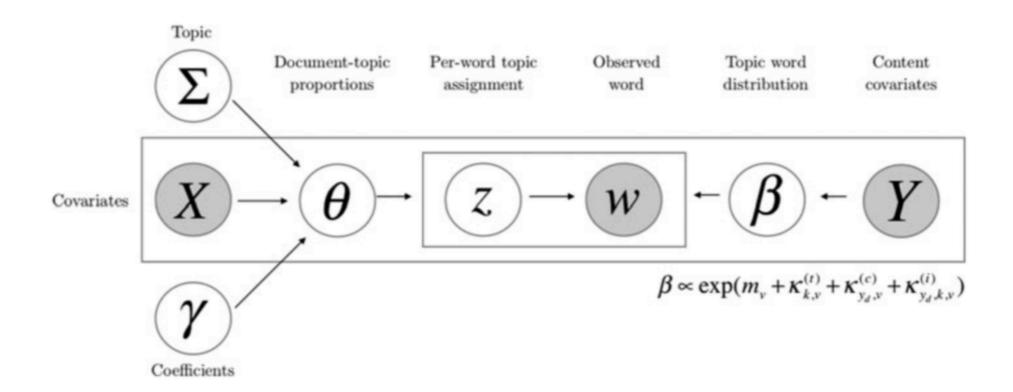


Figure 3: (L) The average held-out probability; CTM supports more topics than LDA. See figure at right for the standard error of the difference. (R) The log odds ratio of the held-out probability. Positive numbers indicate a better fit by the correlated topic model.

- Roberts et al. (2013) and Roberts et al. (2014)
- Key motivation: short documents do not provide the opportunity to observe the correlations between words—key information used to estimate topics
- "Structure": how document-level covariates drives topics
 - E.g., group, time, etc.
- Covariates can be modeled to estimate a) topic prevalence and b)
 topic content
- Without any covariates, the model reduces to CTM

- Topic prevalence
 - Documents which have similar covariates will tend to talk about the same topics
 - Topic proportions within documents can vary through covariates
 - E.g., social media posts by Republican politicians might have different topic proportions than those posted by Democrats

- Topic content
 - Word proportions within topics can vary through covariates
 - Documents which have similar covariates will tend to talk about topics in a similar way
 - E.g. when talking about a health care topic, Republican politicians might use different words than Democrats



Model Selection and Interpretation

Quantitative + qualitative approaches

- Quantitative
 - Held-out likelihood: for some unseen documents, how likely would the model have generated/predicted these documents?
 - Evaluation of predictive power (≠ coherent topics)
 - For how they differ, see Chang et al.(2009) and/or this video)
 - Semantic coherence: how likely do the most common words for a topic co-occur in the same documents?
 - Exclusivity: do words with high probability in one topic have low probabilities in others?

Model Selection and Interpretation

Quantitative + qualitative approaches

- Qualitative
 - Careful reading of exemplar texts
 - Select a small subset of the documents with the highest proportion of the document assigned to the particular category under consideration
 - Read those documents to assess their common facets and interrogate whether a particular organization makes sense
 - Examine words that are indicative of a particular topic
 - The most straightforward method for obtaining these words is to select the highest probability words in each topic

Model Selection and Interpretation

Quantitative + qualitative approaches

- No quantitative metric can replace human judgement
- "The most effective method for assessing model fit is to carefully read documents that are closely associated with particular topics to verify that the semantic concept covered by the topic is reflected in the text." (Roberts et al. 2016)

Summary

- Topic models help us explore or explicitly measure the thematic structure of a large collection of documents
- Select an algorithm that suits your goal
- Experiment with hyper-parameters, including the number of topics
- Quantitative measures for model selection is useful
- Manual reading plays a crucial role in model selection and labeling

Guided Coding

- LDA basics: LDA with SOTU address data in R
- LDA and BERTopic (Week 12): LDA/BERTopic on Stack Overflow data in Python
- Materials for STM
 - Official documentation of stm package
 - Short demonstration
 - Tutorial with Facebook posts data