

1.

$$l = 1000\text{m}$$

$$T_{\text{winter}} = 0.00^\circ\text{C}$$

$$T_{\text{summer}} = 40.0^\circ\text{C}$$

$$\alpha_{\text{steel}} = 10.5 \times 10^{-6} \text{ K}^{-1}$$

$$\Delta L = \alpha l_0 \Delta T$$

$$\Delta L = (10.5 \times 10^{-6} \text{ K}^{-1})(1000\text{m})(40.0^\circ\text{C} - 0.00^\circ\text{C})$$

$$\boxed{\Delta L = 0.42\text{m}}$$

2.

$$\alpha_{\text{aluminum}} = 24 \times 10^{-6} \text{ K}^{-1}$$

$$T_0 = 15^\circ\text{C}$$

$$l_0 = 62.1\text{m}$$

$$T_1 = 200^\circ\text{C}$$

$$\Delta L = \alpha l_0 \Delta T$$

$$\Delta L = (24 \times 10^{-6} \text{ K}^{-1})(62.1\text{m})(200^\circ\text{C} - 15^\circ\text{C})$$

$$\Delta L = 0.276\text{m} = \boxed{27.6\text{cm}}$$

3.

$$l_{\text{brass}} = 40.1 \text{ cm} = 0.401 \text{ m}$$

$$l_{\text{aluminum}} = 79.3 \text{ cm} = 0.793 \text{ m}$$

$$T_0 = 0^\circ \text{C}$$

$$d = 0.60 \text{ cm} = 0.0060 \text{ m}$$

$$\alpha_{\text{brass}} = 2.0 \times 10^{-5} \text{ K}^{-1}$$

$$\alpha_{\text{aluminum}} = 2.4 \times 10^{-5} \text{ K}^{-1}$$

$$\Delta L_{\text{brass}} + \Delta L_{\text{aluminum}} = d$$

$$\alpha_{\text{brass}} l_{\text{brass}} \Delta T + \alpha_{\text{alum}} l_{\text{alum}} \Delta T = d$$

$$\Delta T = \frac{d}{\alpha_{\text{brass}} l_{\text{brass}} + \alpha_{\text{alum}} l_{\text{alum}}}$$

$$\Delta T = \frac{0.0060 \text{ m}}{(2.0 \times 10^{-5} \text{ K}^{-1})(0.401 \text{ m}) + (2.4 \times 10^{-5} \text{ K}^{-1})(0.793 \text{ m})}$$

$$\Delta T = 221.795^\circ \text{C} \approx 220^\circ \text{C}$$

4.

$$m = 199.0 \text{ g} = 0.199 \text{ kg}$$

$$Q = 16.0 \text{ J}$$

$$\Delta T = 10.0^\circ \text{C}$$

$$c = ?$$

$$Q = mc\Delta T$$

$$c = \frac{Q}{m\Delta T}$$

$$c = \frac{16.0 \text{ J}}{(0.199 \text{ kg})(10.0^\circ \text{C})}$$

$$c = 8.04 \text{ J kg}^{-1} \text{ } ^\circ \text{C}^{-1}$$

5.

$$m = 905 \text{ g} = 0.905 \text{ kg}$$

$$v_0 = 1629 \text{ m/s}$$

$$\Delta T = ?$$

$$c = 472 \text{ J kg}^{-1} \text{ } ^\circ \text{K}^{-1}$$

$$KE = Q$$

$$\frac{1}{2}mv^2 = mc\Delta T$$

$$\Delta T = \frac{v^2}{2c}$$

$$\Delta T = \frac{(1629 \text{ m/s})^2}{2(472 \text{ J kg}^{-1} \text{ } ^\circ \text{K}^{-1})}$$

$$\Delta T = 2811.06^\circ \text{C} \approx 2810^\circ \text{C}$$

6.

$$T_{\text{melt}} = 20^{\circ}\text{C}$$

$$L_f = 3.9 \times 10^4 \text{ J kg}^{-1}$$

$$T_{\text{boil}} = 150^{\circ}\text{C}$$

$$L_v = 7.8 \times 10^4 \text{ J kg}^{-1}$$

$$c_{\text{solid}} = 600 \text{ J kg}^{-1} \text{ K}^{-1}$$

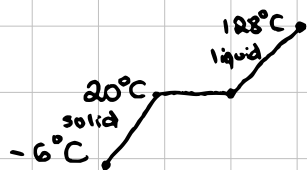
$$c_{\text{liquid}} = 1000 \text{ J kg}^{-1} \text{ K}^{-1}$$

$$c_{\text{gas}} = 400 \text{ J kg}^{-1} \text{ K}^{-1}$$

$$m = 3.80 \text{ kg}$$

$$T_o = -6^{\circ}\text{C}$$

$$T_i = 128^{\circ}\text{C}$$



$$Q_o + Q_1 + Q_2 = Q_{\text{Total}}$$

$$m(c_{\text{solid}} \Delta T_{o,1} + L_f + c_{\text{liquid}} \Delta T_{1,2}) = Q_{\text{total}}$$

$$Q_{\text{total}} = (3.80 \text{ kg}) [(600 \text{ J kg}^{-1} \text{ K}^{-1})(20^{\circ}\text{C} - (-6^{\circ}\text{C})) + 3.9 \times 10^4 \text{ J kg}^{-1} + (1000 \text{ J kg}^{-1} \text{ K}^{-1})(128^{\circ}\text{C} - 20^{\circ}\text{C})]$$

$$Q_{\text{total}} = 617880 \text{ J} = 6.179 \times 10^5 \text{ J}$$

$$= 617.88 \text{ kJ} \approx 620 \text{ kJ}$$

7.

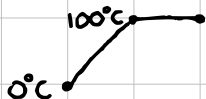
$$m = 2.0 \text{ g}$$

$$T_o = 0.00^\circ\text{C}$$

$$c = 1.0 \text{ cal g}^{-1} \text{K}^{-1}$$

$$L_f = 80 \text{ cal g}^{-1}$$

$$L_v = 539 \text{ cal g}^{-1}$$



$$Q_{\text{total}} = Q_o + Q_i$$

$$Q_{\text{total}} = m(c\Delta T_{i,o} + L_v)$$

$$Q_{\text{total}} = (2.0 \text{ g})[(1.0 \text{ cal g}^{-1} \text{K}^{-1})(100.0^\circ\text{C} - 0.0^\circ\text{C}) + 539 \text{ cal g}^{-1}]$$

$$Q_{\text{total}} = 1278 \text{ cal} \approx 1300 \text{ cal}$$

8.

$$m_{\text{water}} = 330 \text{ g} = 0.330 \text{ kg}$$

$$T_{\text{water}_0} = 45^\circ \text{C}$$

$$m_{\text{container}} = 855 \text{ g} = 0.855 \text{ kg}$$

$$T_{\text{container}_0} = 10^\circ \text{C}$$

$$C_{\text{water}} = 4190 \text{ J kg}^{-1} \text{ K}^{-1}$$

$$C_{\text{aluminium}} = 900 \text{ J kg}^{-1} \text{ K}^{-1}$$

$$T_i = ?$$

$$Q_o + Q_i = 0$$

$$m_w C_w (T_i - T_{\text{water}_0}) + m_c C_{\text{alum}} (T_i - T_{c_0}) = 0$$

$$T_i (m_w C_w + m_c C_{\text{alum}}) = m_w C_w T_{w_0} + m_c C_a T_{c_0}$$

$$T_i = \frac{m_w C_w T_{w_0} + m_c C_a T_{c_0}}{m_w C_w + m_c C_{\text{alum}}}$$

$$T_i = \frac{(0.330 \text{ kg})(4190 \text{ J kg}^{-1} \text{ K}^{-1})(45^\circ \text{C}) + (0.855 \text{ kg})(900 \text{ J kg}^{-1} \text{ K}^{-1})(10^\circ \text{C})}{(0.330 \text{ kg})(4190 \text{ J kg}^{-1} \text{ K}^{-1}) + (0.855 \text{ kg})(900 \text{ J kg}^{-1} \text{ K}^{-1})}$$

$$T_i = 32.4861^\circ \text{C} \approx 32.0^\circ \text{C}$$

9.

$$T_{\text{melt}} = -10^\circ\text{C}$$

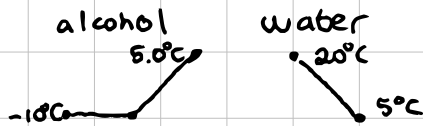
$$m_{\text{frozen}} = 200\text{g} = 0.200\text{kg}$$

$$T_{\text{frozen}_0} = -10^\circ\text{C}$$

$$m_{\text{water}} = 300\text{g} = 0.300\text{kg}$$

$$T_{\text{water}_0} = 20.0^\circ\text{C}$$

$$T_i = 5.0^\circ\text{C}$$



$$m_f = 0.200\text{kg}$$

$$m'_w = 0.500\text{kg}$$

$$T'_{w_0} = 20^\circ\text{C}$$

$$T'_i = 10^\circ\text{C}$$

$$Q_0' + Q_1' = Q_2'$$

$$m_f L_f + m_f c \Delta T_{i,f_0} = m'_w c_w \Delta T'_{i,w_0}$$

$$c = \frac{m'_w c_w \Delta T'_{i,w_0} - m_f L_f}{m_f \Delta T_{i,f_0}}$$

$$Q_0 + Q_1 = Q_2$$

$$m_f L_f + m_f c \Delta T_{i,f_0} = m_w c_w \Delta T_{i,w_0}$$

$$m_f L_f + m_f \Delta T_{i,f_0} \left[\frac{m'_w c_w \Delta T'_{i,w_0} - m_f L_f}{m_f \Delta T_{i,f_0}} \right] = m_w c_w \Delta T_{i,w_0}$$

$$L_f \left[m_f - \frac{m_f \Delta T_{i,f_0}}{\Delta T_{i,f_0}} \right] = c_w \left[m_w \Delta T_{i,w_0} - \frac{m'_w \Delta T'_{i,w_0} \Delta T_{i,f_0}}{\Delta T_{i,f_0}} \right]$$

$$L_f = c_w \left[\frac{m_w \Delta T_{i,w_0} - m'_w \Delta T'_{i,w_0} \Delta T_{i,f_0}}{\Delta T_{i,f_0}} \right] \left[\frac{\Delta T_{i,f_0}}{m_f (\Delta T'_{i,f_0} - \Delta T_{i,f_0})} \right]$$

$$L_f = (4190\text{J kg}^{-1}\text{K}^{-1}) \left[\frac{(0.300\text{kg})(5^\circ\text{C} - 20^\circ\text{C}) - (0.500\text{kg})(10^\circ\text{C} - 20^\circ\text{C})(5^\circ\text{C} - (-10^\circ\text{C}))}{(10^\circ\text{C} - (-10^\circ\text{C}))} \right]$$

$$\left[\frac{10^\circ\text{C} - (-10^\circ\text{C})}{(0.200\text{kg})[(10^\circ\text{C} - (-10^\circ\text{C})) - (5^\circ\text{C} - (-10^\circ\text{C}))]} \right]$$

$$L_f = 62850\text{J kg}^{-1} = 6.29 \times 10^4\text{J kg}^{-1} \approx 6.3 \times 10^4\text{J kg}^{-1}$$

10.

$$m_{\text{tea}} = 1.8 \text{ kg}$$

$$T_{\text{tea}_0} = 80^\circ\text{C}$$

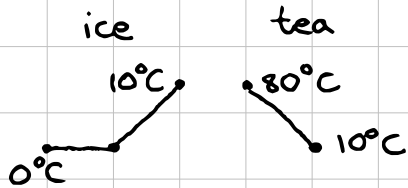
$$m_{\text{ice}} = ?$$

$$T_{\text{ice}_0} = 0.00^\circ\text{C}$$

$$T_f = 10^\circ\text{C}$$

$$L_f = 334 \text{ kJ kg}^{-1} = 334000 \text{ J kg}^{-1}$$

$$c_{\text{tea}} = 4190 \text{ J kg}^{-1} \text{ K}^{-1}$$



$$Q_{\text{water, ice}} + Q_{f, \text{ice}_0} = -Q_{f, \text{tea}_0}$$

$$m_{\text{ice}} L_f + m_{\text{ice}} c_{\text{water}} \Delta T_{f, \text{ice}_0} = -m_{\text{tea}} c_{\text{tea}} \Delta T_{f, \text{tea}_0}$$

$$m_{\text{ice}} = \frac{-m_{\text{tea}} c_{\text{tea}} \Delta T_{f, \text{tea}_0}}{L_f + c_{\text{water}} (T_f - T_{\text{ice}_0})}$$

$$m_{\text{ice}} = \frac{-(1.8 \text{ kg})(4190 \text{ J kg}^{-1} \text{ K}^{-1})[10^\circ\text{C} - 80^\circ\text{C}]}{334000 \text{ J kg}^{-1} + (4190 \text{ J kg}^{-1} \text{ K}^{-1})[10^\circ\text{C} - 0^\circ\text{C}]}$$

$$m_{\text{ice}} = 1.40 \text{ kg}$$