

# Homework 10 Rotations

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6 June 2023

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## 1 Book

### 1.1 10.22

$$\begin{aligned}
 r &= 8.00 \text{ cm} \\
 m &= 0.180 \text{ kg} \\
 v_0 &= 0 \\
 \Delta y &= 75.0 \text{ cm} \\
 I &= mr^2
 \end{aligned}$$

(a)

$$\begin{aligned}E_{K_0} + E_{P_0} &= E_{K_1} + E_{P_1} \\0 + mgh &= \frac{1}{2}I_{cm}\omega^2 + \frac{1}{2}mr^2\omega^2 + 0 \\mgh &= \omega^2 \left( \frac{1}{2}(mr^2) + \frac{1}{2}mr^2 \right) \\\omega &= \frac{\sqrt{gh}}{r} \\\omega &= \frac{\sqrt{(10.0 \text{ m s}^{-2})(0.75 \text{ m})}}{0.08 \text{ m}} \\\omega &= 34.2 \text{ rad s}^{-1}\end{aligned}$$

(b)

$$\begin{aligned}E_{k_0} + E_{p_0} &= E_{k_1} + E_{p_1} \\0 + mgh &= \frac{1}{2}I_{cm}\omega^2 + \frac{1}{2}mv_{cm}^2 + 0 \\mgh &= \frac{1}{2}(mr^2) \left( \frac{v_{cm}}{r} \right)^2 + \frac{1}{2}mv_{cm}^2 \\v &= \sqrt{gh} \\v &= \sqrt{(10.0 \text{ m s}^{-2})(0.75 \text{ m})} \\v &= 2.74 \text{ m s}^{-1}\end{aligned}$$

## 1.2 10.26

$$I_{cm} = \frac{2}{5}mr^2$$

(a) Velocity for the first half of the bowl:

$$\begin{aligned}E_{K_0} + E_{P_0} &= E_{K_1} + E_{P_1} \\0 + mgh &= \frac{1}{2}I_{cm}\omega^2 + \frac{1}{2}mv_{cm}^2 + 0 \\mgh &= \frac{1}{2} \left( \frac{2}{5}mr^2 \right) \left( \frac{v_{cm}^2}{r^2} \right) + \frac{1}{2}mv_{cm}^2 \\v_{cm} &= \sqrt{\frac{10gh}{7}}\end{aligned}$$

Since the ball only slides and doesn't rotate, the kinetic energy it experi-

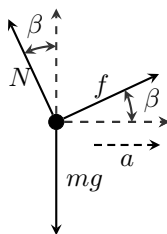
ences it purely linear velocity and *not* angular.

$$\begin{aligned}
 E_{K_0} + E_{P_0} &= E_{K_1} + E_{P_1} \\
 \frac{1}{2}mv_{cm}^2 + 0 &= 0 + mgh_1 \\
 \left(\sqrt{\frac{10gh_0}{7}}\right)^2 &= 2gh_1 \\
 h_1 &= \frac{5}{7}h_0
 \end{aligned}$$

The ball reaches only  $\frac{5}{7}$  of the height of the side of the bowl.

### 1.3 10.30

(a) Free-body diagram:



The angular velocity of the bowling ball is clockwise  $\odot$  which the friction has to oppose resulting in the friction going upwards (up the incline).

(b)

**1.4 10.79**

**1.5 9.30**

**1.6 9.49**

**1.7 9.79**

**1.8 9.86**

## **2 Lab Manual**

**2.1 1170**

**2.2 1173**

**2.3 1175**

**2.4 1177**

**2.5 1181**

**2.6 1283**

**2.7 1284**

## **3 Problem C: Spherical Symmetry Problem**

Starting with  $I = \int r^2 dm$ , calculate the moment of inertial for an axis of rotation that goes through the center of a sphere with uniform mass density  $\rho$ , and radius  $R$ . As discussed in class, you may treat this problem like the integration of a series of concentric spherical shells with thickness  $dr$ .