

Homework 10 Rotations

Corey Mostero - 2566652

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Contents

1	Book	2
1.1	10.22	2
1.2	10.26	3
1.3	10.30	4
1.4	10.79	5
1.5	9.30	5
1.6	9.49	5
1.7	9.79	5
1.8	9.86	5
2	Lab Manual	5
2.1	1170	5
2.2	1173	5
2.3	1175	5
2.4	1177	5
2.5	1181	5
2.6	1283	5
2.7	1284	5
3	Problem C: Spherical Symmetry Problem	5

1 Book

1.1 10.22

$$r = 8.00 \text{ cm}$$

$$m = 0.180 \text{ kg}$$

$$v_0 = 0$$

$$\Delta y = 75.0 \text{ cm}$$

$$I = mr^2$$

(a)

$$\begin{aligned}E_{K_0} + E_{P_0} &= E_{K_1} + E_{P_1} \\0 + mgh &= \frac{1}{2}I_{cm}\omega^2 + \frac{1}{2}mr^2\omega^2 + 0 \\mgh &= \omega^2 \left(\frac{1}{2}(mr^2) + \frac{1}{2}mr^2 \right) \\\omega &= \frac{\sqrt{gh}}{r} \\\omega &= \frac{\sqrt{(10.0 \text{ m s}^{-2})(0.75 \text{ m})}}{0.08 \text{ m}} \\\omega &= 34.2 \text{ rad s}^{-1}\end{aligned}$$

(b)

$$\begin{aligned}E_{k_0} + E_{p_0} &= E_{k_1} + E_{p_1} \\0 + mgh &= \frac{1}{2}I_{cm}\omega^2 + \frac{1}{2}mv_{cm}^2 + 0 \\mgh &= \frac{1}{2}(mr^2) \left(\frac{v_{cm}}{r} \right)^2 + \frac{1}{2}mv_{cm}^2 \\v &= \sqrt{gh} \\v &= \sqrt{(10.0 \text{ m s}^{-2})(0.75 \text{ m})} \\v &= 2.74 \text{ m s}^{-1}\end{aligned}$$

1.2 10.26

$$I_{cm} = \frac{2}{5}mr^2$$

(a) Velocity for the first half of the bowl:

$$\begin{aligned}E_{K_0} + E_{P_0} &= E_{K_1} + E_{P_1} \\0 + mgh &= \frac{1}{2}I_{cm}\omega^2 + \frac{1}{2}mv_{cm}^2 + 0 \\mgh &= \frac{1}{2} \left(\frac{2}{5}mr^2 \right) \left(\frac{v_{cm}^2}{r^2} \right) + \frac{1}{2}mv_{cm}^2 \\v_{cm} &= \sqrt{\frac{10gh}{7}}\end{aligned}$$

Since the ball only slides and doesn't rotate, the kinetic energy it experi-

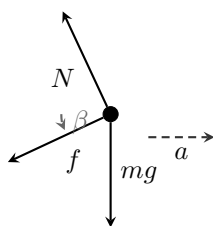
ences it purely linear velocity and *not* angular.

$$\begin{aligned}
 E_{K_0} + E_{P_0} &= E_{K_1} + E_{P_1} \\
 \frac{1}{2}mv_{cm}^2 + 0 &= 0 + mgh_1 \\
 \left(\sqrt{\frac{10gh_0}{7}}\right)^2 &= 2gh_1 \\
 h_1 &= \frac{5}{7}h_0
 \end{aligned}$$

The ball reaches only $\frac{5}{7}$ of the height of the side of the bowl.

1.3 10.30

(a) Free-body diagram:



1.4 10.79

1.5 9.30

1.6 9.49

1.7 9.79

1.8 9.86

2 Lab Manual

2.1 1170

2.2 1173

2.3 1175

2.4 1177

2.5 1181

2.6 1283

2.7 1284

3 Problem C: Spherical Symmetry Problem

Starting with $I = \int r^2 dm$, calculate the moment of inertial for an axis of rotation that goes through the center of a sphere with uniform mass density ρ , and radius R . As discussed in class, you may treat this problem like the integration of a series of concentric spherical shells with thickness dr .