

Homework 5 - 2D Motion

Corey Mostero - 2566652

4 April 2023

Contents

1	Book	2
1.1	3.38	2
1.2	3.41	3
1.3	3.42	4
1.4	3.43	5
2	Lab Manual	5
2.1	473	5
2.2	475	7
2.3	477	8
2.4	670	8
2.5	672	8
2.6	676	8
2.7	678	8

1 Book

1.1 3.38

$$\Delta x_{B,A} = 1500 \text{ m} = 1.5 \text{ km}$$

$$v_{\frac{b}{w}} = 4.00 \text{ km h}^{-1}$$

$$v_{\frac{p}{w}} = 4.00 \text{ km h}^{-1}$$

$$a = 0$$

$$v_w = 2.80 \text{ km h}^{-1}$$

$$\Delta x = v_f t_{b_0} - \frac{1}{2} a t_{b_0}^2$$

$$1.5 \text{ km} = (4.00 \text{ km h}^{-1} + 2.80 \text{ km h}^{-1})t - \frac{1}{2}(0)t^2$$

$$t_{b_0} = 0.221 \text{ h}$$

$$\Delta x = v_f t_{b_1} - \frac{1}{2} a t_{b_1}^2$$

$$1.5 \text{ km} = (4.00 \text{ km h}^{-1} - 2.80 \text{ km h}^{-1})t - \frac{1}{2}(0)t^2$$

$$t_{b_1} = 1.25 \text{ h}$$

$$t_b = 0.221 \text{ h} + 1.25 \text{ h}$$

$$t_b = 1.471 \text{ h}$$

$$2\Delta x = v_f t_{p_1} - \frac{1}{2} a t_{p_1}^2$$

$$2(1.5 \text{ km}) = (4.00 \text{ km h}^{-1}) t_{p_1} - \frac{1}{2} (0) t_{p_1}^2$$

$$t_p = 0.75 \text{ h}$$

$t_b = 1.471 \text{ h}, t_p = 0.75 \text{ h}$

1.2 3.41

$$\Delta x_r = 500 \text{ m}$$

$$v_{w/e} = 0\hat{x} + 2.0 \text{ m s}^{-1}\hat{y}$$

$$v_{b/r} = 4.2 \text{ m s}^{-1}\hat{x} + 0\hat{y}$$

$$v_{b/e} = 4.2 \text{ m s}^{-1}\hat{x} + 2.0 \text{ m s}^{-1}\hat{y}$$

(a)

$$v_{b/e} = \sqrt{(v_{r_x} + v_{b_x})^2 + (v_{r_y} + v_{b_y})^2}$$

$$= \sqrt{(0 + 4.2 \text{ m s}^{-1})^2 + (2.0 \text{ m s}^{-1} + 0)^2}$$

$$v_{b/e} = 4.652 \text{ m s}^{-1}$$

$$\tan(\theta) = \frac{v_{b/e_y}}{v_{b/e_x}}$$

$$\theta = \arctan\left(\frac{v_{b/e_y}}{v_{b/e_x}}\right)$$

$$\theta = \arctan\left(\frac{2.0 \text{ m s}^{-1}}{4.2 \text{ m s}^{-1}}\right)$$

$$\theta = 25.46^\circ$$

$v_{b/e} = 4.652 \text{ m s}^{-1}, \theta = 25.46^\circ \text{ S of E}$

(b)

$$\Delta x_r = v_{b/e_x} t - \frac{1}{2} a t^2$$

$$500 \text{ m} = (4.2 \text{ m s}^{-1}) t - \frac{1}{2} (0) t^2$$

$$t = 119.0 \text{ s}$$

$t = 119.0 \text{ s}$

(c)

$$y_0 = 0$$

$$\Delta y = v_{b/e_y} t - \frac{1}{2} a t^2$$

$$y_1 - 0 = (2.0 \text{ m s}^{-1})(119.0 \text{ s}) - \frac{1}{2}(0)(119.0 \text{ s})$$

$$y_1 = 238.0 \text{ m}$$

$$\boxed{\Delta y = 238.0 \text{ m}}$$

1.3 3.42

(a)

$$\sin(\theta) = \frac{v_{w/e}}{v_{b/w}}$$

$$\theta = \arcsin\left(\frac{v_{w/e}}{v_{b/w}}\right)$$

$$\theta = \arcsin\left(\frac{2.0 \text{ m s}^{-1}}{4.2 \text{ m s}^{-1}}\right)$$

$$\theta = 28.44^\circ \text{ N of E}$$

$$\boxed{\theta = 28.44^\circ \text{ N of E}}$$

(b)

$$v_{b/e} = \sqrt{(v_{b/w_x} + v_{w/e_x})^2 + (v_{b/w_y} + v_{w/e_y})^2}$$

$$v_{b/e} = \sqrt{((4.2 \text{ m s}^{-1}) \cos(28.44^\circ) + 0)^2 + ((4.2 \text{ m s}^{-1}) \sin(28.44^\circ) + 2.0 \text{ m s}^{-1})^2}$$

$$v_{b/e} = 3.693 \text{ m s}^{-1}$$

$$\boxed{v_{b/e} = 3.693 \text{ m s}^{-1}}$$

(c)

$$\Delta x_r = v_{b/e} t - \frac{1}{2} a t^2$$

$$500 \text{ m} = (3.693 \text{ m s}^{-1})t - \frac{1}{2}(0)t^2$$

$$t = 135.4 \text{ s}$$

$$\boxed{t = 135.4 \text{ s}}$$

1.4 3.43

(a)

$$v_{w/e} = (0)\hat{x} + (80.0 \text{ km h}^{-1})\hat{y}$$

$$v_{a/w} = 320.0 \text{ km h}^{-1}$$

$$\sin(\theta) = \frac{v_{w/e,y}}{v_{a/w}}$$

$$\theta = \arcsin\left(\frac{80.0 \text{ km h}^{-1}}{320.0 \text{ km h}^{-1}}\right)$$

$$\theta = 14.48^\circ \text{ N of W}$$

$$\boxed{\theta = 14.48^\circ \text{ N of W}}$$

(b)

$$\cos(\theta) = \frac{v_{a/e}}{v_{a/w}}$$

$$v_{a/e} = (v_{a/w}) \cos(\theta)$$

$$v_{a/e} = (320.0 \text{ km h}^{-1}) \cos(14.48^\circ)$$

$$v_{a/e} = 309.8 \text{ km h}^{-1}$$

$$\boxed{v_{a/e} = 309.8 \text{ km h}^{-1}}$$

2 Lab Manual

2.1 473

$$v_{r/b} = v$$

$$d_A = d$$

$$v_{A/r} = c$$

$$a_A = 0$$

$$d_B = d$$

$$v_{B/r} = c$$

$$a_B = 0$$

(a) First find t_A . Subscripts 0, 1 denote the first and second trip (0-indexed).

$$\Delta x_0 = v_{A/r} t_0 + \frac{1}{2} a_A t_0^2$$

$$d_A = (c - v) t_0 + \frac{1}{2} (0) t_0^2$$

$$t_0 = \frac{d_A}{c - v}$$

$$\begin{aligned}\Delta x_0 &= v_{A/r} t_0 + \frac{1}{2} a_A t_0^2 \\ d_A &= (c+v) t_1 + \frac{1}{2} (0) t_1^2 \\ t_1 &= \frac{d_A}{c+v}\end{aligned}$$

$$\begin{aligned}t_A &= t_0 + t_1 \\ t_A &= \frac{d_A}{c-v} + \frac{d_A}{c+v} \\ t_A &= d_A \left(\frac{1}{c(1-\frac{v}{c})} + \frac{1}{c(1+\frac{v}{c})} \right) \\ t_A &= \frac{d_A}{c} \left(\frac{1}{1-\frac{v}{c}} + \frac{1}{1+\frac{v}{c}} \right) \\ t_A &= \frac{d_A}{c} \left(\frac{1+\frac{v}{c}}{(1-\frac{v}{c})(1+\frac{v}{c})} + \frac{1-\frac{v}{c}}{(1+\frac{v}{c})(1-\frac{v}{c})} \right) \\ t_A &= \frac{2\frac{d_A}{c}}{-\left(\frac{v}{c}\right)\left(\frac{v}{c}\right) + \frac{v}{c} - \frac{v}{c} + 1} \\ t_A &= \frac{2\frac{d_A}{c}}{1 - \left(\frac{v}{c}\right)^2}\end{aligned}$$

$$\boxed{t_A = \frac{2\frac{d}{c}}{1 - \left(\frac{v}{c}\right)^2}}$$

Find t_B . Subscripts 0, 1 denote the first and second trip (0-indexed).

$$\begin{aligned}v_{B/r}^2 - v_{r/b}^2 &= v_{B/b}^2 \\ v_{B/b} &= \sqrt{c^2 - v^2}\end{aligned}$$

$$\begin{aligned}2\Delta x &= v_{B/b} t_B + \frac{1}{2} a_B t_B^2 \\ 2d_B &= \left(\sqrt{c^2 - v^2} \right) t_B + \frac{1}{2} (0) t_B^2 \\ t_B &= \frac{2d_B}{\sqrt{c^2 \left(1 - \frac{v^2}{c^2} \right)}} \\ t_B &= \frac{2d_B}{c \sqrt{1 - \frac{v^2}{c^2}}} \\ t_B &= \frac{2\frac{d_B}{c}}{\sqrt{1 - \left(\frac{v}{c}\right)^2}}\end{aligned}$$

$$t_B = \frac{2\frac{d}{c}}{\sqrt{1 - \left(\frac{v}{c}\right)^2}}$$

- (b) Utilize the negative binomial series $(x+1)^{-n} = 1 - nx + \frac{1}{2}n(n+1)x^2 - \dots$ as the prompt states that $\frac{v}{c} < 1$.

$$\begin{aligned} t_A - t_B &\approx \frac{v^2 d}{c^3} \\ 2\frac{d}{c} \left(1 - \left(\frac{v}{c}\right)^2\right)^{-1} - 2\frac{d}{c} \left(1 - \left(\frac{v}{c}\right)^2\right)^{-1/2} &\approx \frac{v^2 d}{c^3} \\ 2\frac{d}{c} \left(\left(1 + \left(\frac{v}{c}\right)^2\right) - \left(1 + \frac{1}{2}\left(\frac{v}{c}\right)^2\right)\right) &\approx \frac{v^2 d}{c^3} \\ \frac{v^2 d}{c^3} &\approx \frac{v^2 d}{c^3} \end{aligned}$$

$$t_A - t_B \approx \frac{v^2 d}{c^3}$$

2.2 475

(a)

$$\begin{aligned} v_{p/e} &= (8 \text{ mi h}^{-1} \sin(\theta))\hat{x} + (8 \text{ mi h}^{-1} \cos(\theta))\hat{y} \\ v_{w/e} &= (0)\hat{x} + (20 \text{ mi h}^{-1})\hat{y} \end{aligned}$$

$$\begin{aligned} \sin(\theta) &= \frac{v_{p/e}}{v_{w/e}} \\ \theta &= \arcsin\left(\frac{v_{p/e}}{v_{w/e}}\right) \\ \theta &= \arcsin\left(\frac{8 \text{ mi h}^{-1}}{20 \text{ mi h}^{-1}}\right) \\ \theta &= 23.58^\circ \end{aligned}$$

$$\theta = 23.58^\circ$$

(a)

$$\begin{aligned} \text{distance} &= D \\ \frac{dV}{dx} &= v_{r/g} \cdot A \\ \text{wetness} &= \frac{dV}{dx} t \end{aligned}$$

$$\text{wetness} = (v_{r/g} \cdot A)t$$

$$t = \frac{\Delta D}{v_{r/g}}$$

$$\text{wetness} = (v_{r/g} \cdot A) \left(\frac{D}{v_{r/g}} \right)$$

$$\text{wetness} = AD$$

$\text{wetness} = AD$

In the end, the angle that the rain hits the engineer ends up having no effect whether they are running or walking. More specifically, when the engineer walks, the value of theta is closer to 90° meaning the rainfall per distance $\frac{dV}{dx}$ is of smaller volume. As the engineer runs faster, more rainfall will hit the engineer, though the speed at which they're traveling makes the total volume of rain hit the same (given adequate/perfectly consistent variables).

2.3 477

2.4 670

2.5 672

2.6 676

2.7 678