

The grand potential of the order 3

$$\begin{aligned}
\Omega_3 = & \\
& -\frac{1}{2}\{1, 2|V|3, 4\}\{3, 4|V|1, 6\}\{5, 6|V|5, 2\}f_5^- \left( \begin{array}{c} \frac{+f_1^- f_2^- f_4^+ - f_2^- f_3^- f_4^- + f_1^- f_2^- f_3^-}{(-E_1 - E_2 + E_3 + E_4)(-E_2 + E_6)} \\ \frac{+f_3^- f_4^- f_1^+}{(-E_3 - E_4 + E_1 + E_2)(-E_3 - E_4 + E_1 + E_6)} \\ \frac{+f_3^- f_4^- f_6^- - f_1^- f_3^- f_6^- - f_1^- f_6^- f_4^+}{(-E_6 + E_2)(-E_3 - E_4 + E_1 + E_6)} \end{array} \right) \\
& +\frac{1}{24}\{1, 2|V|3, 4\}\{3, 4|V|5, 6\}\{5, 6|V|1, 2\} \left( \begin{array}{c} \frac{+f_1^- f_2^- f_3^- f_6^+ + f_1^- f_2^- f_5^- f_4^+ + f_1^- f_2^- f_4^+ f_6^+ + f_1^- f_2^- f_3^- f_5^-}{(-E_1 - E_2 + E_3 + E_4)(-E_1 - E_2 + E_5 + E_6)} \\ \frac{+f_3^- f_4^- f_5^- f_2^+ + f_1^- f_3^- f_4^- f_5^- + f_3^- f_4^- f_2^+ f_6^+ + f_1^- f_3^- f_4^- f_6^+}{(-E_3 - E_4 + E_1 + E_2)(-E_3 - E_4 + E_5 + E_6)} \\ \frac{+f_1^- f_3^- f_5^- f_6^- + f_3^- f_5^- f_6^- f_2^+ + f_5^- f_6^- f_2^+ f_4^+ + f_1^- f_5^- f_6^- f_4^+}{(-E_5 - E_6 + E_1 + E_2)(-E_5 - E_6 + E_3 + E_4)} \end{array} \right) \\
& +\frac{1}{3}\{1, 2|V|1, 4\}\{3, 4|V|3, 6\}\{5, 6|V|5, 2\}f_1^- f_3^- f_5^- \left( \begin{array}{c} \frac{+f_2^-}{(-E_2 + E_4)(-E_2 + E_6)} \\ \frac{+f_4^-}{(-E_4 + E_2)(-E_4 + E_6)} \\ \frac{+f_6^-}{(-E_6 + E_2)(-E_6 + E_4)} \end{array} \right) \\
& +\frac{1}{2}\{1, 2|V|1, 4\}\{3, 4|V|5, 2\}\{5, 6|V|3, 6\}f_1^- f_6^- \left( \frac{+f_2^- f_3^- + f_4^- f_5^- - f_3^- f_4^- - f_2^- f_5^-}{(-E_2 + E_4)(-E_3 + E_5)} \right) \\
& +\frac{1}{6}\{1, 2|V|3, 6\}\{3, 4|V|5, 2\}\{5, 6|V|1, 4\} \left( \begin{array}{c} \frac{+f_2^- f_3^- f_5^- f_6^- - f_1^- f_2^- f_5^- f_3^+ + f_1^- f_2^- f_3^- f_4^- - f_3^- f_4^- f_6^- f_2^+}{(-E_2 - E_5 + E_3 + E_4)(-E_3 - E_6 + E_1 + E_2)} \\ \frac{+f_2^- f_5^- f_6^- f_4^+ - f_1^- f_2^- f_4^- f_5^- + f_1^- f_3^- f_4^- f_5^+ - f_5^- f_4^- f_5^- f_6^-}{(-E_2 - E_5 + E_3 + E_4)(-E_5 - E_6 + E_1 + E_4)} \\ \frac{+f_1^- f_2^- f_5^- f_6^- + f_1^- f_3^- f_4^- f_6^- - f_3^- f_5^- f_6^- f_1^+ - f_1^- f_2^- f_4^- f_6^+}{(-E_1 - E_2 + E_3 + E_6)(-E_5 - E_6 + E_1 + E_4)} \end{array} \right)
\end{aligned}$$