

1 Remember

- $\overline{E} = \overline{E}(r, t) \rightarrow$ Electric field intensity .
 - $\overline{D} = \epsilon \overline{E}$ Electric flux intensity .
 - Permittivity $= \epsilon = \epsilon_0 \epsilon_r$
 - $\overline{\rho}_v$ volume charge density (C/m^3) $= \overline{\rho}_v(r, t)$
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- $\overline{H} = \overline{H}(r, t)$ Magnetic field intensity (A/m)
 - $\overline{B} = \mu \overline{H}$ Magnetic flux density
 - Permeability $= \mu = \mu_0 \mu_r$
 - $\overline{J} = \overline{J}(r, t)$ current density (A/m^2)
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- Note that all electric and magnetic quantities are functions in position and time.
- Note that electric charge is the source of electric field, while electric current is the source of magnetic field.

2 Maxwell's equations

Gauss's law :

$$\oiint \overline{D} \cdot \overline{ds} = Q_{\text{enc}} \qquad \nabla \cdot \overline{D} = \overline{\rho}_v$$

Gauss's law for magnetism :

$$\oiint \overline{B} \cdot \overline{ds} = 0 \qquad \nabla \cdot \overline{B} = 0$$

Faraday's law :

$$\text{emf} = \oint \overline{E} \cdot \overline{dl} \qquad \nabla \times \overline{E} = -\frac{\partial \overline{B}}{\partial t}$$

Ampere's law :

$$I_{\text{enc}} = \oint \overline{H} \cdot \overline{dl} \qquad \nabla \times \overline{H} = \overline{J}$$

3 Boundary conditions

For tangential components:

$$E_{t_1} = E_{t_2}$$

$$H_{t_1} = H_{t_2} \quad \text{No sheet current density } \bar{I}_{sh} = 0$$

$$(\overline{H_1} - \overline{H_2}) \times \hat{n}_{12} = \overline{J}_{sh}$$

For normal components:

$$D_{n_1} = D_{n_2}$$

$$\epsilon_1 E_{n_1} = \epsilon_2 E_{n_2}$$

$$B_{n_1} = B_{n_2}$$

$$\mu H_{n_1} = \mu H_{n_2}$$