Amsterdam University of Applied Sciences

Quantum Talent and Learning Center Intro to Quantum Computing Workshop

Available Time: 30 minutes

 $Permitted \ Materials: \ Simple \ calculator, \ graphic \ and \ advanced \ calculators \ are \ not \\ permitted$

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Name: Student number:

Generic guidelines:

- 1. Have fun!
- 2. If you need questions, please ask your teacher in the room or in the chat.
- 3. We trust you won't look up the answers online :D

NB. This is an individual exam.

Good luck!

Question 1 Find the complex transpose of the following matrices:

$$\begin{pmatrix} 1 & 2 & -3 \\ 4i & -5i & 6 \\ 7 & 8 & 9i \end{pmatrix} \tag{1}$$

$$\begin{pmatrix} 3+1i & 2-2i & 1+3i \\ 4-2i & 5+1i & 6-3i \\ 7+1i & 8-2i & 9+3i \end{pmatrix}$$

$$(2)$$

- 1. $|\psi\rangle = |0\rangle$.
- 2. $|\psi\rangle = |1\rangle$.
- 3. $|\psi\rangle = |0\rangle + |1\rangle$.
- 4. $|\psi\rangle = \frac{1}{\sqrt{2}}[|0\rangle |1\rangle].$
- 5. $|\psi\rangle = \frac{1}{\sqrt{2}}[|0\rangle + i|1\rangle].$

- $1. \ \begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix}.$
- $2. \ \binom{i}{0} \ i.$
- $3. \begin{pmatrix} 1 & 0 \\ 0 & -1 \end{pmatrix}.$
- $4. \ \begin{pmatrix} 1 & 0 \\ 0 & i \end{pmatrix}.$
- $5. \ \begin{pmatrix} 1 & 0 \\ 0 & \frac{i}{\sqrt{2}} \end{pmatrix}.$

Question 4 Let's find the state of the qubit after applying the Hadamard gate as shown in the figure.

The Hadamard gate is defined as:

$$H = \frac{1}{\sqrt{2}} \begin{pmatrix} 1 & 1\\ 1 & -1 \end{pmatrix} \tag{3}$$

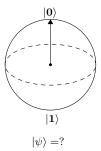
$$q_0$$
 H

First, apply the Hadamard gate to the qubit state $|\psi\rangle = |0\rangle$ and determine the new state of the qubit.

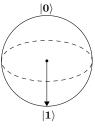
Second, apply the Hadamard gate to the qubit state $|\psi\rangle=|1\rangle$ and determine the new state of the qubit.

Third, what is the probability of measuring the qubit in the state $|0\rangle$ after applying the Hadamard gate to the qubit state $|\psi\rangle = |1\rangle$?

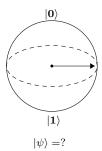
Question 5 Let's find the corresponding quantum state to a given Bloch sphere representation. Write below each Bloch sphere representation the corresponding quantum state in the computational basis. Assume the x-axis is horizontal, the z-axis is vertical, and the y-axis is perpendicular to the paper.

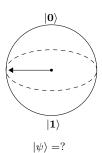






 $|\psi\rangle = ?$





Question 6 Let's emulate together a quantum circuit of two qubits and entangle them.
We initialize both qubits in state $ 0\rangle$ and two classical bits in the given quantum circuit. What will be the total initial state of the two qubits?
q_0 ———
q_1 ———
c_0
c_1
Answer is: $ q_0q_1\rangle =$
Apply a Hadamard gate to the first qubit. First, draw it in the quantum circuit given below and write the new state of the two qubits.
Second, apply a CNOT gate to the two qubits. First, draw it in the quantum circuit given above and write the new state of the two qubits.
Make your drawing here:
q_0 ————————————————————————————————————
q_1 ————————————————————————————————————
c_0
c_1
<u> </u>

How does the state of the two qubits change after applying the Hadamard and CNO gates?	Τ
Given the final state of the two qubits, how do you see the entanglement?	

<i>End</i>	of Examination ———
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