

$$L_1: \begin{cases} x = 1+t \\ y = 1-t \\ z = 2t \end{cases}$$

$$L_2: \begin{cases} x = 2-t \\ y = t \\ z = 2 \end{cases}$$

$$\vec{u}_1 = \langle 1, -1, 2 \rangle$$

$$\vec{u}_2 = \langle -1, 1, 0 \rangle$$

$$\vec{n} = \vec{u}_1 \times \vec{u}_2 = \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ 1 & -1 & 2 \\ -1 & 1 & 0 \end{vmatrix} = \langle -2, -2, 0 \rangle$$

$$\begin{array}{l|l} -2(x-1) - 2(y-1) = 0 & -2(x-2) - 2(y-0) = 0 \\ -2x+2-2y+2=0 & -2x+4-2y=0 \\ 2x+2y=4 & 2x+2y=4 \\ \underline{x+y=2} & \underline{x+y=2} \end{array}$$

$$x(1-1+2i) + y(4-1-4i) = 3+10i$$

$$2ix + 3y - 4iy = 3+10i$$

$$3y + i(2x-4y) = 3+10i$$

$$3y = 3$$

$$2x-4y = 10$$

$$y = 1$$

$$2x-4 = 10$$

$$2x = 14$$

$$x = 7$$

$$x+y = 7+1 = 8$$

$$(x+iy) - 8 = i(7-2z)$$

$$x+iy - 8 = 7i - 2i(x-iy)$$

$$x-8+iy = 7i - 2ix - 2y$$

$$x-8+iy = -2y + i(7-2x)$$

$$7-2x = y$$

$$x-8 = -2y$$

$$2x+y = 7$$

$$x+2y = 8$$

$$2x+y = 7$$

$$2x+4y = 16$$

$$-3y = -9$$

$$y = 3$$

$$x = \frac{7-y}{2}$$

$$= \frac{4}{2}$$

$$x = 2$$

$$|z| = \sqrt{x^2+y^2}$$

$$= \sqrt{4+9}$$

$$= \sqrt{13}$$

$$2 - 2t + 2(3t) - (1+t) = 7$$

$$2 - 2t + 6t - 1 - t = 7$$

$$1 + 3t = 7$$

$$t = 2$$

$$x = 2 - 2t = 2 - 4 = -2$$

$$y = 3t = 6$$

$$z = 1 + t = 3$$

$$(a, b, c) = -2, 6, 3$$

$$a + b + c = -2 + 6 + 3$$

$$= 7$$

$$\vec{a} \cdot \vec{b} = \|\vec{a}\| \|\vec{b}\| \cos \theta$$

$$2 + 2 = \sqrt{6} \sqrt{x^2 + 1} \frac{1}{\sqrt{2}}$$

$$2 + x = \sqrt{3(x^2 + 1)}$$

$$x^2 + 4 + 4x = 3x^2 + 3$$

$$0 = 2x^2 - 4x - 1$$

$$2x^2 - 4x - 1 = 0$$

$$x = \frac{4 \pm \sqrt{16 - 4(2)(-1)}}{4}$$

$$= \frac{4 \pm \sqrt{16 + 8}}{4}$$

$$= 1 + \frac{\sqrt{6}}{2}$$

$$\det A = x(-3+x) = 0$$

$$x(x-3) = 0$$

$$x = 0 \quad \text{or} \quad x = 3$$

$$\therefore \text{Sum} = 3$$

$$\vec{a} \cdot \vec{b} = \sqrt{15}$$

$$\vec{a} \times \vec{b} = \langle -2, 0, 1 \rangle$$

$$\vec{a} \cdot \vec{b} = \|\vec{a}\| \|\vec{b}\| \cos \theta$$

$$\vec{a} \times \vec{b} = \|\vec{a}\| \|\vec{b}\| \sin \theta$$

$$\sin \theta = \frac{\|\vec{a} \times \vec{b}\|}{\|\vec{a}\| \|\vec{b}\|}$$

$$\cos \theta = \frac{\vec{a} \cdot \vec{b}}{\|\vec{a}\| \|\vec{b}\|}$$

$$\tan \theta = \frac{\|\vec{a} \times \vec{b}\|}{\|\vec{a}\| \|\vec{b}\|} \times \frac{\cancel{\|\vec{a}\| \|\vec{b}\|}}{\vec{a} \cdot \vec{b}}$$

$$\sin / \cos = \tan$$

$$= \frac{\sqrt{4+1}}{\sqrt{15}}$$

$$= \frac{\sqrt{5}}{\sqrt{15}}$$

$$= \frac{1}{\sqrt{3}}$$

$$\theta = \tan^{-1}\left(\frac{1}{\sqrt{3}}\right)$$

$$= \pi/6$$

