

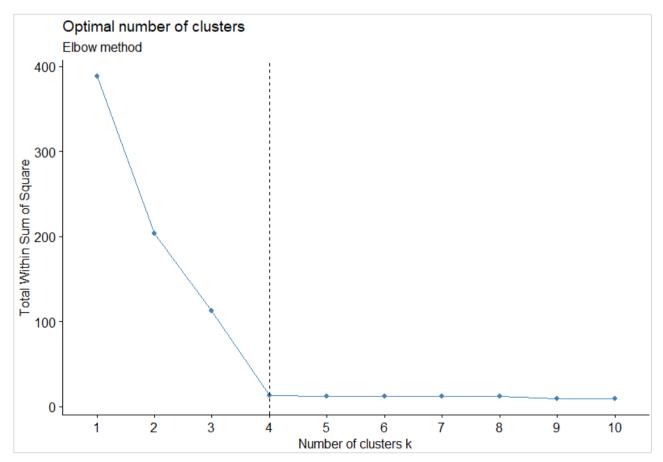
## **Pricing of First-Exposure Items**

A) In Assignment 6, you estimated the actual demand of the previously sold items. Using the estimated actual demand and the other available features in the dataset of this assignment, determine the optimal price for the first-exposure items available in the "First-exposures.csv" file. The objective of the optimization model should be to maximize the total revenue of these items and the demand should be estimated using the regression tree approach. To determine the optimal price of each item, consider {\$25.99, \$30.99, \$35.99, \$40.99} and {\$45.99, \$50,99} as the set of possible prices for items in event A and event B, respectively.

**Answer A)** From the 'Assignment6\_Data.csv' dataset, there are 1,000 obs. of 29 variables. At first, we have imported the data and then converted the categorical data into numerical data. We have used the estimated actual demand and the other available features in the dataset and have found the stockout\_time as given below:

```
> stockout_time
[1] 18 16 22 20 14 22 22 22 21 15 22 17 18 16 22 20 14 22 22 22 21 15 22 17 18 16 22 20 14 22 22 22 21 15 22 17 18 16 22 20 14 22 22 22 21 15 22 17 18 16 22 20 14 22 22 22 21 15 22 17 18 16 22 20 14 22 22 22 11 5 22 17 18 16 22 20 14 22 22 22 11 5 22 17 18 16 22 20 14 22 22 22 11 5 22 17 18 16 22 20 14 22 22 22 11 5 22 17 18 16 22 20 14 22 22 22 11 5 22 17 18 16 22 20 14 22 22 22 11 5 22 17 18 16 22 20 14 22 22 22 21 15 22 17 18 16 22 20 14 22 22 22 21 15 22 17 18 16 22 20 14 22 22 22 21 15 22 17 18 16 22 20 14 22 22 22 21 15 22 17 18 16 22 20 14 22 22 22 21 15 22 17 18 16 22 20 14 22 22 22 21 15 22 17 18 16 22 20 14 22 22 22 22 21 15 22 17 18 16 22 20 14 22 22 22 22 21 15 22 17 18 16 22 20 14 22 22 22 22 21 15 22 17 18 16 22 20 14 22 22 22 22 21 15 22 17 18 16 22 20 14 22 22 22 22 21 15 22 17 18 16 22 20 14 22 22 22 22 21 15 22 17 18 16 22 20 14 22 22 22 22 21 15 22 17 18 16 22 20 14 22 22 22 22 21 15 22 17 18 16 22 20 14 22 22 22 22 21 15 22 17 18 16 22 20 14 22 22 22 22 21 15 22 17 18 16 22 20 14 22 22 22 22 22 21 15 22 17 18 16 22 20 14 22 22 22 22 22 21 15 22 17 18 16 22 20 14 22 22 22 22 22 21 15 22 17 18 16 22 20 14 22 22 22 22 22 21 15 22 17 18 16 22 20 14 22 22 22 22 21 15 22 17 18 16 22 20 14 22 22 22 22 22 21 15 22 17 18 16 22 20 14 22 22 22 22 21 15 22 17 18 16 22 20 14 22 22 22 22 22 21 15 22 17 18 16 22 20 14 22 22 22 22 22 21 15 22 17 18 16 22 20 14 22 22 22 22 22 21 15 22 17 18 16 22 20 14 22 22 22 22 22 21 15 22 17 18 16 22 20 14 22 22 22 22 22 21 15 22 17 18 16 22 20 14 22 22 22 22 21 15 22 17 18 16 22 20 14 22 22 22 22 21 15 22 17 18 16 22 20 14 22 22 22 22 21 15 22 17 18 16 22 20 14 22 22 22 22 21 15 22 17 18 16 22 20 14 22 22 22 22 21 15 22 17 18 16 22 20 14 22 22 22 22 21 15 22 17 18 16 22 20 14 22 22 22 22 22 21 15 22 17 18 16 22 20 14 22 22 22 22 22 21 15 22 17 18 16 22 20 14 22 22 22 22 22 21 15 22 17 18 16 22 20 14 22 22 22 22 22 21 15 22 17 18 16 22 20 14 22 22 22 22 22 21 15 22 17 18 16 22 20 14 22 22 22 22 22 21 15 22 22 22 22 21 15 22 17 18 16 22 20 14 22 22 22 22 2
```

We have applied the 'Elbow Method' to find and plot the optimal number of clusters as shown below:



*Figure 01:* Number of clusters using K-Means



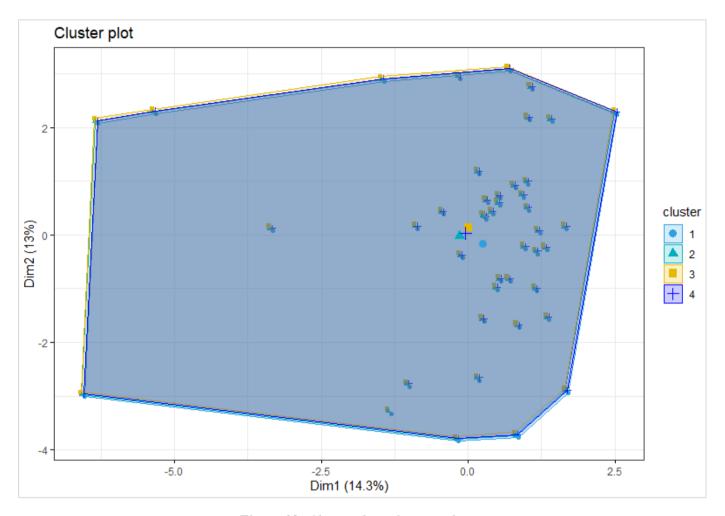


Figure 02: Cluster plots of not\_stockouts

Then we have generated the output of the 'Stockouts' and 'Not\_Stockouts' in CSV format and this has been submitted with this assignment. The clusters center output is given below:

```
clusters$center
  Dep_category Part_of_day
                                    hour.1
                                                hour.2
                                                             hour.3
                                                                          hour.4
                                                                                        hour.5
                                                                                                     hour.6
                                                                                                                  hour.7
                                                                                                                               hour.8
1
                              0 0.2568421 0.1385167 0.07392344 0.06622010 0.05440191 0.04344498 0.04043062 0.03856459 0.02287081
                              1 0.2557769 0.1375697 0.06832669 0.07083665 0.05430279 0.04462151 0.03924303 0.03984064 0.02382470 1 0.2668902 0.1382927 0.07347561 0.06951220 0.05378049 0.04256098 0.04134146 0.04140244 0.02560976
2
3
               0
4
               0
                              0 0.2622378 0.1329371 0.07146853 0.07405594 0.05041958 0.04020979 0.04020979 0.04069930 0.02692308
      hour.10
                   hour.11
                                hour.12
                                             hour.13
                                                          hour.14
                                                                         hour.15
                                                                                      hour.16
                                                                                                    hour.17
                                                                                                                   hour.18
                                                                                                                                 hour.19
1 0.02727273 0.02588517 0.02368421 0.02100478 0.01363636 0.008995215 0.01105263 0.006889952 0.004928230 0.004114833
2 0.02685259 0.02601594 0.02179283 0.02043825 0.01310757 0.009681275 0.01258964 0.007370518 0.004780876 0.004501992 3 0.02603659 0.02554878 0.02128049 0.02134146 0.01207317 0.008475610 0.01085366 0.005670732 0.003475610 0.002743902
4 0.02615385 0.02650350 0.02181818 0.02041958 0.01188811 0.009720280 0.00965035 0.007832168 0.004055944 0.004195804
       hour. 20
                     hour.21
                                   hour.22
                                                  hour.23
                                                                hour.24
1 0.005358852 0.008373206 0.006985646 0.004784689 0.006076555
2 0.005896414 0.008286853 0.008007968 0.004223108 0.006653386
3 0.004451220 0.006646341 0.006341463 0.003353659 0.006585366
4 0.006293706 0.008251748 0.007132867 0.004405594 0.006503497
```



We have used the ANOVA method in regression tree approach, thus getting the output as shown below: The output of the regression tree is as following:

```
> regression_tree
n= 1000
node), split, n, deviance, yval
        « denotes terminal node
 1) root 1000 1522537.000 90.34239
    2) Price>=59.95 609 535513.500
                                             80.24741
      4) Branded< 0.5 139 39087.820 67.05189
      5) Branded>=0.5 470 465064.900
   10) Price>=164.9 78 24983.970 69.52
11) Price< 164.9 392 420078.000 87.0
3) Price< 59.95 391 828296.600 106.06580
6) Num_Branded_Events12< 7.5 371 51283
                                                  69.52501 *
                                                  87.05997
                                                  512832.500 102.82610
       12) Num_Branded_Events12< 0.5 107
                                                    128193.000
                                                                    88.99956
          24) Brand_MSRP_Index>=0.575 84
                                                     33364.150
                                                                   80.28134
          25) Brand_MSRP_Index< 0.575 23
                                                     65126.470 120.84000
             50) ConcurrentEvents>=2.5 11
51) ConcurrentEvents< 2.5 12
                                                      5819.847
                                                                  81.16605
                                                     26120.970 157.20780
      13) Num_Branded_Events12>=0.5 264 355893.300 108.43(7) Num_Branded_Events12>=7.5 20 239340.300 166.16150
                                                    355893.300 108.43000
       14) Event_Length< 2.5 12
                                           9724.686 108.80040
       15) Event_Length>=2.5 8 130906.800 252.20310 *
```

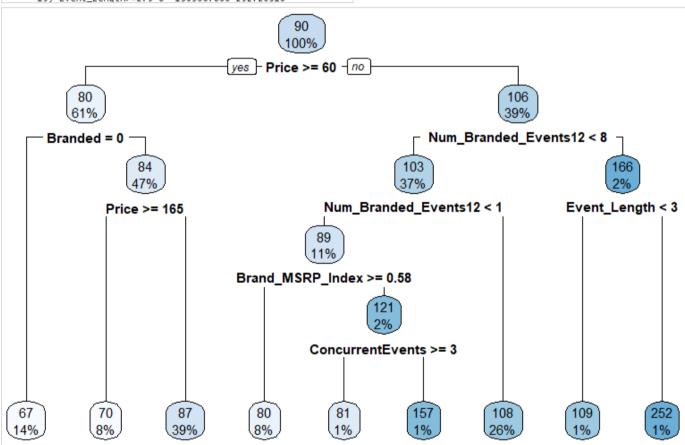


Figure 03: Output using the ANOVA method using regression tree approach



For Event A – we have put the set of possible prices for items and thus found the optimal prices, which has shown below:

```
> D1
 [1] 108.43004 108.43004 157.20781 87.05997 87.05997 87.05997 87.05997 87.05997 87.05997 87.05997 87.05997
[12] 87.05997
> Final_solutions
      [,1] [,2] [,3] [,4] [,5] [,6] [,7] [,8] [,9] [,10] [,11] [,12]
               0
                    0
                          0
                               1
                                     0
                                          0
                                               0
                                                            0
                                                                  0
                                                                        0
 [2,]
[3,]
         0
                    0
                          0
                               1
                                     0
                                          0
                                               0
                                                     1
                                                            0
                                                                  0
                                                                        0
         0
                          0
                                     0
                                          0
                                               0
                                                     1
                                                                  0
                                                                        0
 [4,]
                          0
                               0
                                                     1
                                                                        0
               0
                    1
                                     1
                                          0
 [5,]
         0
               0
                          0
                               0
                                     0
                                                     1
                                                                  0
                                                                        0
 [6,]
[7,]
         0
               0
                          0
                                     0
                                          0
                                               0
                                                     0
                                                            0
                                                                  0
                                                                        1
                    1
                               1
         0
               0
                          0
                               0
                                     0
                                                     0
                                                                  0
                                                                        0
                                          0
                                               1
                                                            1
                    1
 [8,]
[9,]
         0
               0
                                     0
                                               0
                    1
                          0
                               0
                                                     0
                                                            0
                                                                  0
                                                                        1
                                          1
         0
               0
                    1
                          0
                               0
                                     0
                                          0
                                               1
                                                     0
                                                            0
                                                                  0
                                                                        1
         0
               0
                    0
[10,]
                          1
                               0
                                     0
                                          0
                                                     0
                                                            0
                                                                  0
                                                                        1
> Final_objectives.
[1] 7343.474 7885.624 10183.286 10618.586 11053.886 11489.186 11924.486 12359.786 12795.086 10705.765
  Final_solutions_A[match(max(Final_objectives_A),Final_objectives_A),]
[1] 0 0 1 0 0 0 0 1 0 0 0 1
```

For Event B – we have put the set of possible prices for items and thus found the optimal prices, which has shown below:

```
> D2
[1] 108.43004 108.43004 87.05997 87.05997
> Final_solutions_B
     [,1] [,2] [,3] [,4]
       1 0
[1,]
                  1
                       0
[2,]
[3,]
        0
                       0
             1
                  1
        0
                  0
             1
                       1
> Final_objectives_B
[1] 8990.586 9532.736 9968.036
Final_solutions_B[match(max(Final_objectives_B),Final_objectives_B),]
[1] 0 1 0 1
```



## Bibliographic Reference:

Creed J. (2016) *Optimal Pricing and Predicting Demand* Retrieved from https://rpubs.com/jcreed/opplastersand

Monroe J. T. (2021) *Business Analytics with R* Retrieved from https://bookdown.org/jeffreytmonroe/business\_analytics\_with\_r7/marketing.html

Laurinec P. August 22, 2017 *Using regression trees for forecasting double-seasonal time series with trend in R* Retrieved from https://petolau.github.io/Regression-trees-for-forecasting-time-series-in-R