

Problem A.2:

$$x_3(t): T_0 = 40 \rightarrow \omega_0 = \frac{2\pi}{40} = \frac{\pi}{20}$$

$$x_3(t) = \sum_{n=-\infty}^{\infty} D_n e^{j \frac{n\pi}{20} t}$$

$$D_n = \frac{1}{40} \int_{T_0} x_3(t) e^{-j \frac{n\pi}{20} t} dt$$

$$D_n = \frac{10}{40} \int_{-5}^5 e^{-j \frac{n\pi}{20} t} dt = \frac{1}{4} \int_{-5}^5 e^{-j \frac{n\pi}{20} t} dt$$

$$= \left[\frac{1}{4} \left(\frac{-20}{jn\pi} \right) e^{-j \frac{n\pi}{20} t} \right]_{t=-5}^5 = \left[\frac{-5}{jn\pi} e^{-j \frac{n\pi}{20} t} \right]_{t=-5}^5$$

$$= \frac{-5}{jn\pi} e^{-j \frac{n\pi}{4}} + \frac{5}{jn\pi} e^{j \frac{n\pi}{4}} = \frac{10}{n\pi} \left[\frac{e^{j \frac{n\pi}{4}}}{j2} - \frac{e^{-j \frac{n\pi}{4}}}{j2} \right]$$

$$\boxed{D_n = \frac{10 \sin\left(\frac{\pi}{4} n\right)}{n\pi}}$$