Data Normalization

Roberto Souza Assistant Professor Electrical and Computer Engineering Schulich School of Engineering

January 2022



Outline

Learning Goals

Data Normalization Strategies

Summary



Learning Goals

• Learn the importance of data normalization

Learn about the commonly used normalization strategies

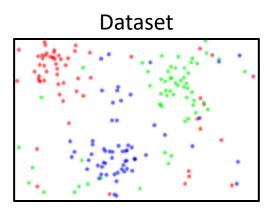


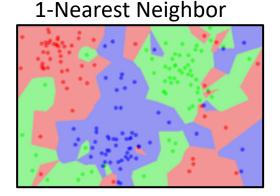
Data Normalization

 Reduce the influence of the different feature's scales (e.g., distance-based model where features have very different scales)

Improves model training

 Need to be mindful of your data scale and your network output activation scale





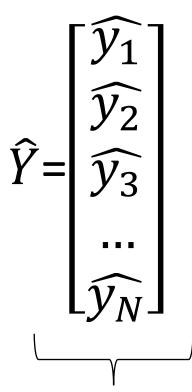


Notation

$$X = \begin{bmatrix} x_{11} & x_{12} & \dots & x_{1M} \\ x_{21} & x_{22} & \dots & x_{2M} \\ x_{31} & x_{32} & \dots & x_{3M} \\ \dots & \dots & \dots & \dots \\ x_{N1} & x_{N2} & \dots & x_{NM} \end{bmatrix}$$

$$Y = \begin{bmatrix} y_1 \\ y_2 \\ y_3 \\ \dots \\ y_5 \end{bmatrix}$$

True Labels



Predicted Labels



Notation

Notation	Meaning	Notation	Meaning	Notation	Meaning
X	Dataset	Υ	Labels of dataset	Ŷ	Predicted labels of dataset
X_{train}	Train set	Y_{train}	Labels of train set	$\widehat{Y_{train}}$	Predicted labels of train set
X _{val}	Validation set	Y _{val}	Labels of validation set	$\widehat{Y_{val}}$	Predicted labels of validation set
X_{test}	Test set	Y _{test}	Test set	$\widehat{Y_{test}}$	Predicted labels of test set



Notation

Notation	Meaning
X[i,:]	Sample i
X[:,j]	Feature j
X[i,j]	Feature j of sample i



Feature-wise Normalization



Min-max Normalization

$$X_{train}[:,i] = \frac{X_{train}[:,i] - \min(X_{train}[:,i])}{\max(X_{train}[:,i]) - \min(X_{train}[:,i])}$$

$$X_{val}[:,i] = \frac{X_{val}[:,i] - \min(X_{train}[:,i])}{\max(X_{train}[:,i]) - \min(X_{train}[:,i])}$$

$$X_{test}[:,i] = \frac{X_{test}[:,i] - \min(X_{train}[:,i])}{\max(X_{train}[:,i]) - \min(X_{train}[:,i])}$$



Standardization

$$X_{train}[:,i] = \frac{X_{train}[:,i] - \text{mean}(X_{train}[:,i])}{std(X_{train}[:,i])}$$

$$X_{val}[:,i] = \frac{X_{val}[:,i] - \text{mean}(X_{train}[:,i])}{std(X_{train}[:,i])}$$

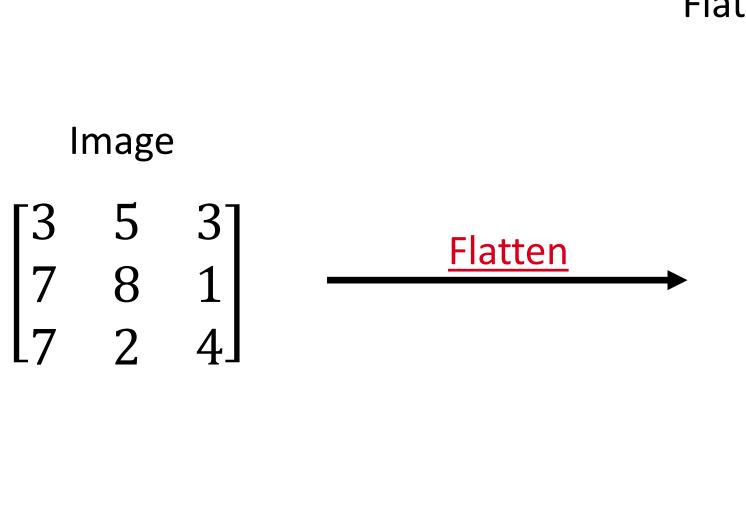
$$X_{test}[:,i] = \frac{X_{test}[:,i] - \text{mean}(X_{train}[:,i])}{\text{std}(X_{train}[:,i])}$$



Sample-wise Normalization



When working with locally correlated data...



Flattened Image

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Min-max Normalization (statistics of the training set)

$$X_{train} = \frac{X_{train} - \min(X_{train})}{\max(X_{train}) - \min(X_{train})}$$

$$X_{val} = \frac{X_{val} - \min(X_{train})}{\max(X_{train}) - \min(X_{train})}$$

$$X_{test} = \frac{X_{test} - \min(X_{train})}{\max(X_{train}) - \min(X_{train})}$$



Standardization (statistics of the training set)

$$X_{train} = \frac{X_{train} - \text{mean}(X_{train})}{std(X_{train})}$$

$$X_{val} = \frac{X_{val} - \text{mean}(X_{train})}{std(X_{train})}$$

$$X_{test} = \frac{X_{test} - \text{mean}(X_{train})}{\text{std}(X_{train})}$$



Sample-wise Normalization (statistics of the sample)

Min-max:

$$X[i,:] = \frac{X[i,:] - \min(X[i,:])}{\max(X[i,:]) - \min(X[i,:])}$$

Standardization:

$$X[i,:] = \frac{X[i,:] - \operatorname{mean}(X[i,:])}{\operatorname{std}(X[i,:])}$$



Other Normalization Strategies

- Batch Normalization
- Layer Normalization
- Output normalization

https://keras.io/api/layers/normalization_layers/



Summary

- Normalization is an essential step for properly training neural networks, special when you have features with different scales
- Three main types of normalization:
 - Feature-wise normalization based on the statistics of the feature in the training set
 - Sample-wise normalization based on the statistics of all features in the training set
 - Sample-wise normalization based on the statistics of the sample
- There is not one definite normalization method.



Thanks!

