

1. Some definition

- Direct-permission is a permission that user has directly
- Indirect-permission is a permission that user has because he manages other user who has this permission
- Full-permissions of user is all of direct-permissions and indirect-permissions
- Direct-staff of user is staff that user manages directly

2. Algorithm

- **Step 1: Read number of users, permissions from buffer and assign for each user**
 - Read number of users: N
 - Read permissions for CEO from input buffer, add permissions to CEO. The permissions are direct-permissions of CEO
 - Read N lines from input buffer, for X-th line:
 - ✓ Add permissions to user X. The permissions are direct-permissions of user X
- **Step 2: Read and assign manager, staffs for each user**
 - Read N lines from input buffer, for X-th line:
 - ✓ If data is string **CEO**:
 - ❖ Set -1 for CEO's manager
 - ❖ Add user X to list direct-staffs of CEO
 - ✓ If data is number, assume Y, Y is manager of user X
 - ❖ Set Y for user X's manger
 - ❖ Add user XX to list direct-staffs of user Y
- **Step 3: Add full permissions (direct-permissions and indirect-permissions) for each user, using Depth First Search (DFS) algorithm, beginning from CEO.**
 - Add full-permissions (direct-permissions + indirect permissions) for all users using DFS.
- **Step 4: Write output result to writer buffer for Question 1**
 - Get full-permissions from user to write
- **Step 5: Process command and update permissions for user.**
 - Read remain lines from input buffer, for each line:
 - ✓ if data is string of format **ADD X Y**:
 - Add direct-permission Y to user X
 - Add indirect-permission Y to all user X's managers (using DFS)
 - ✓ if data is string of format **QUERY X**:
 - Print permissions of user X to output buffer
 - ✓ if data is string of format **REMOVE X Y**
 - Remove a direct-permission Y from user X
 - Remove indirect-permission Y from all user X's managers (using DFS)

3. Complexity of algorithm

- Time complexity
 - $O(N * K)$

- Space complexity
 - $O(N \cdot K)$